PRINCIPLES OF POLYMERIZATION

FOURTH EDITION

GEORGE ODIAN
PRINCIPLES OF POLYMERIZATION

Fourth Edition

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CONTENTS

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INDEX
This book describes the physical and organic chemistry of the reactions by which polymer molecules are synthesized. The sequence I have followed is to introduce the reader to the characteristics which distinguish polymers from their much smaller sized homologs (Chap. 1) and then proceed to a detailed consideration of the three types of polymerization reactions—step, chain, and ring-opening polymerizations (Chaps. 2–5, 7). Polymerization reactions are characterized as to their kinetic and thermodynamic features, their scope and utility for the synthesis of different types of polymer structures, and the process conditions which are used to carry them out. Polymer chemistry has advanced to the point where it is often possible to tailor-make a variety of different types of polymers with specified molecular weights and structures. Emphasis is placed throughout the text on understanding the reaction parameters which are important in controlling polymerization rates, polymer molecular weight, and structural features such as branching and crosslinking. It has been my intention to give the reader an appreciation of the versatility which is inherent in polymerization processes and which is available to the synthetic polymer chemist.

The versatility of polymerization resides not only in the different types of reactants which can be polymerized but also in the variations allowed by copolymerization and stereoselective polymerization. Chain copolymerization is the most important kind of copolymerization and is considered separately in Chap. 6. Other copolymerizations are discussed in the appropriate chapters. Chapter 8 describes the stereochemistry of polymerization with emphasis on the synthesis of polymers with stereoregular structures by the appropriate choice of initiators and polymerization conditions. In the last chapter, there is a discussion of the reactions of polymers that are useful for modifying or synthesizing new polymer structures and the use of polymeric reagents, substrates, and catalysts. The literature has been covered through early 2003.

It is intended that this text be useful to chemists with no background in polymers as well as the experienced polymer chemist. The text can serve as a self-educating introduction to polymer synthesis for the former. Each topic is presented with minimal assumptions.
regarding the reader’s background, except for undergraduate organic and physical chemistry. Additionally, it is intended that the book will serve as a classroom text. With the appropriate selection of materials, the text can be used at either the undergraduate or graduate level. Each chapter contains a selection of problems. A solutions manual for the problems is available directly from the author.

Many colleagues have been helpful in completing this new edition. I am especially indebted to Chong Cheng, Krzysztof Matyjaszewski, and Stephen A. Miller who graciously gave their time to read and comment on portions of the text. Their suggestions for improvements and corrections were most useful. I also thank the many colleagues who generously responded to my inquiries for their advice on various topics: Helmut G. Alt, Jose M. Asua, Lisa S. Baugh, Sabine Beuermann, Vincenzo Busico, Luigi Cavallo, John Chadwick, Geoff Coates, Scott Collins, James V. Crivello, Michael F. Cunningham, Thomas P. Davis, Pieter J. Dijkstra, Rudolf Faust, Hanns Fischer, Michel Fontanille, Robert Gilbert, Alexei Gridnev, Richard A. Gross, Robert H. Grubbs, Howard Haubenstock, Jorge Herrera-Ordonez, Walter Hertler, Hans Heuts, Henry Hsieh, Aubrey Jenkins, Jaroslav Kahovec, Mikiharu Kamachi, Walter Kaminsky, Hans Kricheldorf, Morton Litt, Roberto Olayo, Patrick Lacroix-Desmazes, W. V. Metanomski, Michael J. Monteiro, Timothy E. Patten, Stanislaw Penczek, Peter Plesch, Jorge Puig, Roderic P. Quirk, Anthony K. Rappe, Luigi Resconi, Ezio Rizzardo, Greg Russell, Erling Rytter, Richard R. Schrock, Donald Tomalia, Brigitte Voit, Kenneth Wagener, Robert M. Waymouth, Owen W. Webster, Yen Wei, David G. Westmoreland, Edward S. Wilks, Bernard Witholt, Nan-loh Yang, Masahiro Yasuda, and Adolfo Zambelli. Their helpful and insightful comments enriched and improved the text.

I welcome comments from readers, including notice of typographical, factual, and other errors.

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George Odi

PREFACE

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INTRODUCTION

Polymers are macromolecules built up by the linking together of large numbers of much smaller molecules. The small molecules that combine with each other to form polymer molecules are termed monomers, and the reactions by which they combine are termed polymerizations. There may be hundreds, thousands, tens of thousands, or more monomer molecules linked together in a polymer molecule. When one speaks of polymers, one is concerned with materials whose molecular weights may reach into the hundreds of thousands or millions.

1-1 TYPES OF POLYMERS AND POLYMERIZATIONS

There has been and still is considerable confusion concerning the classification of polymers. This is especially the case for the beginning student who must appreciate that there is no single generally accepted classification that is unambiguous. During the development of polymer science, two types of classifications have come into use. One classification is based on polymer structure and divides polymers into condensation and addition polymers. The other classification is based on polymerization mechanism and divides polymerizations into step and chain polymerizations. Confusion arises because the two classifications are often used interchangeably without careful thought. The terms condensation and step are often used synonymously, as are the terms addition and chain. Although these terms may often be used synonymously because most condensation polymers are produced by step polymerizations and most addition polymers are produced by chain polymerizations, this is not always the case. The condensation–addition classification is based on the composition or structure of polymers. The step–chain classification is based on the mechanisms of the polymerization processes.
Polymers were originally classified by Carothers [1929] into condensation and addition polymers on the basis of the compositional difference between the polymer and the monomer(s) from which it was synthesized. Condensation polymers were those polymers that were formed from polyfunctional monomers by the various condensation reactions of organic chemistry with the elimination of some small molecule such as water. An example of such a condensation polymer is the polyamides formed from diamines and diacids with the elimination of water according to

\[ nH_2N-R-NH_2 + nHO_2C-R'-CO_2H \rightarrow H\left\{NH-R-NHCO-R'-CO\right\}_nOH + (2n-1)H_2O \quad (1-1) \]

where R and R’ are aliphatic or aromatic groupings. The unit in parentheses in the polyamide formula repeats itself many times in the polymer chain and its termed the *repeating unit*. The elemental composition of the repeating unit differs from that of the two monomers by the elements of water. The polyamide synthesized from hexamethylene diamine, R = (CH₂)₆, and adipic acid, R’ = (CH₂)₄, is the extensively used fiber and plastic known commonly as nylon 6/6 or poly(hexamethylene adipamide). Other examples of condensation polymers are the polyesters formed from diacids and diols with the elimination of water and the polycarbonates from the reaction of an aromatic dihydroxy reactant and phosgene with the elimination of hydrogen chloride:

\[ nHO-R-OH + nHO_2C-R'-CO_2H \rightarrow H\left\{O-R-O-CO-R'-CO\right\}_nOH + (2n-1)H_2O \quad (1-2) \]

The common condensation polymers and the reactions by which they are formed are shown in Table 1-1. It should be noted from Table 1-1 that for many of the condensation polymers there are different combinations of reactants that can be employed for their synthesis. Thus polyamides can be synthesized by the reactions of diamines with diacids or diacyl chlorides and by the self-condensation of amino acids. Similarly, polyesters can be synthesized from diols by esterification with diacids or ester interchange with diesters.

Some naturally occurring polymers such as cellulose, starch, wool, and silk are classified as condensation polymers, since one can postulate their synthesis from certain hypothetical reactants by the elimination of water. Thus cellulose can be thought of as the polyether formed by the dehydration of glucose. Carothers included such polymers by defining condensation polymers as those in which the formula of the repeating unit lacks certain atoms that are present in the monomer(s) from which it is formed or to which it may be degraded. In this
<table>
<thead>
<tr>
<th>Type</th>
<th>Characteristic Linkage</th>
<th>Polymerization Reaction</th>
</tr>
</thead>
<tbody>
<tr>
<td>Polyamide</td>
<td>−NH–CO–</td>
<td>$\text{H}_2\text{N}–\text{R}–\text{NH}_2 + \text{HO}_2\text{C}–\text{R}'–\text{CO}_2\text{H} \rightarrow \text{H}{\text{NH}–\text{R}–\text{NHCO}–\text{R}'–\text{CO}}_n\text{OH} + \text{H}_2\text{O}$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$\text{H}_2\text{N}–\text{R}–\text{NH}_2 + \text{ClCO}–\text{R}'–\text{COCl} \rightarrow \text{H}{\text{NH}–\text{R}–\text{NHCO}–\text{R}'–\text{CO}}_n\text{Cl} + \text{HCl}$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$\text{H}_2\text{N}–\text{R}–\text{CO}_2\text{H} \rightarrow \text{H}{\text{NH}–\text{R}–\text{CO}}_n\text{OH} + \text{H}_2\text{O}$</td>
</tr>
<tr>
<td>Protein, wool, silk</td>
<td>−NH–CO–</td>
<td>Naturally occurring polypeptide polymers; degradable to mixtures of different amino acids.</td>
</tr>
<tr>
<td>Polyester</td>
<td>−CO–O–</td>
<td>$\text{HO}–\text{R}–\text{OH} + \text{HO}_2\text{C}–\text{R}'–\text{CO}_2\text{H} \rightarrow \text{H}{\text{O}–\text{R}–\text{OCO}–\text{R}'–\text{CO}}_n\text{OH} + \text{H}_2\text{O}$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$\text{HO}–\text{R}–\text{OH} + \text{R''O}_2\text{C}–\text{R''–CO}_2\text{R''} \rightarrow \text{H}{\text{O}–\text{R}–\text{OCO}–\text{R}'–\text{CO}}_n\text{OH} + \text{R''OH}$</td>
</tr>
<tr>
<td>Polyurethane</td>
<td>−O–CO–NH–</td>
<td>$\text{HO}–\text{R}–\text{OH} + \text{OCN}–\text{R}'–\text{NCO} \rightarrow \text{H}{\text{O}–\text{R}–\text{OCO}–\text{NH}–\text{R}'–\text{NH–CO}}_n$</td>
</tr>
<tr>
<td>Polysiloxane</td>
<td>−Si–O–</td>
<td>$\text{Cl–SiR}_2–\text{Cl} \xrightarrow{\text{H}_2\text{O}} \text{HO}–\text{SiR}_2–\text{OH} \rightarrow \text{H}{\text{O}–\text{SiR}_2}_n\text{OH} + \text{H}_2\text{O}$</td>
</tr>
<tr>
<td>Phenol–formaldehyde</td>
<td>−Ar–CH₂–</td>
<td>$\text{H}_2\text{N}–\text{CO}–\text{NH}_2 + \text{CH}_2\text{O} \rightarrow \text{H}{\text{HN}–\text{CO}–\text{NH}–\text{CH}_2}_n + \text{H}_2\text{O}$</td>
</tr>
<tr>
<td>Urea–formaldehyde</td>
<td>−NH–CH₂–</td>
<td>$\text{H}_2\text{N}–\text{CO}–\text{NH}_2 + \text{CH}_2\text{O} \rightarrow \text{H}{\text{HN}–\text{CO}–\text{NH}–\text{CH}_2}_n + \text{H}_2\text{O}$</td>
</tr>
<tr>
<td>Melamine–formaldehyde</td>
<td>−NH–CH₂–</td>
<td>$\text{H}_2\text{N}–\text{C}–\text{N}–\text{C}–\text{NH}_2 + \text{CH}_2\text{O} \rightarrow \text{H}{\text{HN}–\text{C}–\text{N}–\text{C}–\text{NH}–\text{CH}_2}_n + \text{H}_2\text{O}$</td>
</tr>
<tr>
<td>Polysulfide</td>
<td>−Sₙ–</td>
<td>$\text{Cl–R–Cl} + \text{Na}_2\text{S}_m \rightarrow \text{S}_m\text{–R}_n + \text{NaCl}$</td>
</tr>
<tr>
<td>Polyacetal</td>
<td>−O–CH–O–ᵣ</td>
<td>$\text{R}–\text{CHO} + \text{HO}–\text{R}’–\text{OH} \rightarrow \text{H}{\text{O}–\text{R}’–\text{OCH}R}_n + \text{H}_2\text{O}$</td>
</tr>
</tbody>
</table>
sense cellulose is considered a condensation polymer, since its hydrolysis yields glucose, which contains the repeating unit of cellulose plus the elements of water

\[
\begin{align*}
\text{Cellulose} & \quad \text{Glucose} \\
\left[ \begin{array}{c}
\text{CH}_2\text{OH} \\
\text{OH} \\
\text{CH} \\
\text{CH} \\
\text{CH}_2\text{OH}
\end{array} \right] \quad & \quad \left[ \begin{array}{c}
\text{CH}_2\text{OH} \\
\text{CH} \\
\text{CH} \\
\text{OH} \\
\text{OH}
\end{array} \right] + (n-1)\text{H}_2\text{O} \\
\text{CH}_2\text{OH} \quad & \quad \text{nHO-Ch} \quad \text{CH}_2\text{OH}
\end{align*}
\]

Addition polymers were classified by Carothers as those formed from nonomers without the loss of a small molecule. Unlike condensation polymers, the repeating unit of an addition polymer has the same composition as the monomer. The major addition polymers are those formed by polymerization of monomers containing the carbon–carbon double bond. Such monomers will be referred to as vinyl monomers throughout this text. (The term vinyl, strictly speaking, refers to a \( \text{CH}_2=\text{CH}^− \) group attached to some substituent. Our use of the term vinyl monomer is broader—it applies to all monomers containing a carbon–carbon double bond, including monomers such as methyl methacrylate, vinylidene chloride, and 2-butene as well as vinyl chloride and styrene. The term substituted ethylenes will also be used interchangeably with the term vinyl monomers.) Vinyl monomers can be made to react with themselves to form polymers by conversion of their double bonds into saturated linkages, for example

\[
n\text{CH}_2=\text{CHY} \quad \rightarrow \quad \left\{ \text{CH}_2=\text{CHY} \right\}_n
\]

where \( Y \) can be any substituent group such as hydrogen, alkyl, aryl, nitrile, ester, acid, ketone, ether, and halogen. Table 1-2 shows many of the common addition polymers and the monomers from which they are produced.

The development of polymer science with the study of new polymerization processes and polymers showed that the original classification by Carothers was not entirely adequate and left much to be desired. Thus, for example, consider the polyurethanes, which are formed by the reaction of diols with diisocyanates without the elimination of any small molecule:

\[
n\text{HO-R-}\text{OH} + n\text{OCN-R′-NCO} \quad \rightarrow \quad \text{HO}\left\{ \text{R-OCONH-R′-NHCO-O} \right\}_{(n-1)}\text{R-OCONH-R′-NCO}
\]

Using Carothers’ original classification, one would classify the polyurethanes as addition polymers, since the polymer has the same elemental composition as the sum of the monomers. However, the polyurethanes are structurally much more similar to the condensation polymers than to the addition polymers. The urethane linkage (−NH−CO−O−) has much in common with the ester (−CO−O−) and amide (−NH−CO−) linkages.

To avoid the obviously incorrect classification of polyurethanes as well as of some other polymers as addition polymers, polymers have also been classified from a consideration of the chemical structure of the groups present in the polymer chains. Condensation polymers have been defined as those polymers whose repeating units are joined together by functional
Thus the structure of condensation polymers has been defined by

$$\text{R} \longrightarrow \text{Z} \longrightarrow \text{R} \longrightarrow \text{Z} \longrightarrow \text{R} \longrightarrow \text{Z}$$

where R is an aliphatic or aromatic grouping and Z is a functional unit such as $-\text{OCO}-$, $-\text{NHCO}-$, $-\text{S}-$, $-\text{OCONH}-$, $-\text{O}-$, $-\text{OCOO}-$, and $-\text{SO}_2-$. Addition polymers, on the other hand, do not contain such functional groups as part of the polymer chain. Such groups may, however, be present in addition polymers as pendant substituents hanging off the polymer chain. According to this classification, the polyurethanes are readily and more correctly classified as condensation polymers.

### TABLE 1-2 Typical Addition Polymers

<table>
<thead>
<tr>
<th>Polymer</th>
<th>Monomer</th>
<th>Repeating Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Polyethylene</td>
<td>$\text{CH}_2\equiv\text{CH}_2$</td>
<td>$\text{CH}_2\equiv\text{CH}_2$</td>
</tr>
<tr>
<td>Polyisobutylene</td>
<td>$\text{CH}_2\equiv\text{C} - \text{CH}_3$</td>
<td>$\text{CH}_2\equiv\text{C} - \text{CH}_3$</td>
</tr>
<tr>
<td>Polyacrylonitrile</td>
<td>$\text{CH}_2\equiv\text{CH} - \text{CN}$</td>
<td>$\text{CH}_2\equiv\text{CH} - \text{CN}$</td>
</tr>
<tr>
<td>Poly(vinyl chloride)</td>
<td>$\text{CH}_2\equiv\text{CH} - \text{Cl}$</td>
<td>$\text{CH}_2\equiv\text{CH} - \text{Cl}$</td>
</tr>
<tr>
<td>Polystyrene</td>
<td>$\text{CH}_2\equiv\text{CH} - \phi$</td>
<td>$\text{CH}_2\equiv\text{CH} - \phi$</td>
</tr>
<tr>
<td>Poly(methyl methacrylate)</td>
<td>$\text{CH}_2\equiv\text{C} - \text{CO}_2\text{CH}_3$</td>
<td>$\text{CH}_2\equiv\text{C} - \text{CO}_2\text{CH}_3$</td>
</tr>
<tr>
<td>Poly(vinyl acetate)</td>
<td>$\text{CH}_2\equiv\text{CH} - \text{OCOCH}_3$</td>
<td>$\text{CH}_2\equiv\text{CH} - \text{OCOCH}_3$</td>
</tr>
<tr>
<td>Poly(vinylidene chloride)</td>
<td>$\text{CH}_2\equiv\text{C} - \text{Cl}$</td>
<td>$\text{CH}_2\equiv\text{C} - \text{Cl}$</td>
</tr>
<tr>
<td>Polytetrafluoroethylene</td>
<td>$\text{C} - \text{F} - \text{F}$</td>
<td>$\text{C} - \text{F} - \text{F}$</td>
</tr>
<tr>
<td>Polyisoprene (natural rubber)</td>
<td>$\text{CH}_2\equiv\text{C} - \text{CH} = \text{CH}_2 - \text{CH}_3$</td>
<td>$\text{CH}_2\equiv\text{C} - \text{CH} = \text{CH}_2 - \text{CH}_3$</td>
</tr>
</tbody>
</table>
It should not be taken for granted that all polymers that are defined as condensation polymers by Carothers’ classification will also be so defined by a consideration of the polymer chain structure. Some condensation polymers do not contain functional groups such as ester or amide in the polymer chain. An example is the phenol–formaldehyde polymers produced by the reaction of phenol (or substituted phenols) with formaldehyde

\[
\begin{align*}
\text{OH} \quad n & \quad + \quad n\text{CH}_2\text{O} \quad \rightarrow \quad \text{OH} \quad \left[ \text{CH}_2\text{OH} \quad \left( n-1 \right) \right] \quad + \quad (n-1)\text{H}_2\text{O} \\
\end{align*}
\]

These polymers do not contain a functional group within the polymer chain but are classified as condensation polymers, since water is split out during the polymerization process. Another example is poly(\(p\)-xylene), which is produced by the oxidative coupling (dehydrogenation) of \(p\)-xylene:

\[
\begin{align*}
\text{CH}_3 \quad n & \quad \text{-} \quad \text{CH}_3 \quad \rightarrow \quad \text{H} \quad \left[ \text{CH}_2 \quad \left( n \right) \right] \quad + \quad (n-1)\text{H}_2 \\
\end{align*}
\]

In summary, a polymer is classified as a condensation polymer if its synthesis involves the elimination of small molecules, or it contains functional groups as part of the polymer chain, or its repeating unit lacks certain atoms that are present in the (hypothetical) monomer to which it can be degraded. If a polymer does not fulfill any of these requirements, it is classified as an addition polymer.

1-1b Polymerization Mechanism

In addition to the structural and compositional differences between polymers, Flory [1953] stressed the very significant difference in the mechanism by which polymer molecules are built up. Although Flory continued to use the terms condensation and addition in his discussions of polymerization mechanism, the more recent terminology classifies polymerizations into step and chain polymerizations.

Chain and step polymerizations differ in several features, but the most important difference is in the identities of the species that can react with each other. Another difference is the manner in which polymer molecular size depends on the extent of conversion.

Step polymerizations proceed by the stepwise reaction between the functional groups of reactants as in reactions such as those described by Eqs. 1-1 through 1-3 and Eqs. 1-6 through 1-8. The size of the polymer molecules increases at a relatively slow pace in such polymerizations. One proceeds from monomer to dimer, trimer, tetramer, pentamer, and so on.

- Monomer + monomer → dimer
- Dimer + monomer → trimer
- Dimer + dimer → tetramer
- Trimer + monomer → tetramer
- Trimer + dimer → pentamer
- Trimer + trimer → hexamer
Tetramer monomer pentamer+
Tetramer dimer hexamer+
Tetramer trimer heptamer+
Tetramer tetramer octamer+
etc.
until eventually large-sized polymer molecules have been formed. The characteristic of step polymerization that distinguishes it from chain polymerization is that reaction occurs between any of the different-sized species present in the reaction system.

The situation is quite different in chain polymerization where an initiator is used to produce an initiator species $R^*$ with a reactive center. The reactive center may be either a free radical, cation, or anion. Polymerization occurs by the propagation of the reactive center by the successive additions of large numbers of monomer molecules in a chain reaction. The distinguishing characteristic of chain polymerization is that polymer growth takes place by monomer reacting only with the reactive center. Monomer does not react with monomer and the different-sized species such as dimer, trimer, tetramer, and $n$-mer do not react with each other. By far the most common example of chain polymerization is that of vinyl monomers. The process can be depicted as

$$
R^* \xrightarrow{\text{CH}_2=\text{CH}_Y} R-\text{CH}_2=\text{C}^* \xrightarrow{\text{CH}_2=\text{CH}_Y} R-\text{CH}_2=\text{CH}_2=\text{C}^* \xrightarrow{\text{CH}_2=\text{CH}_Y} \ldots
$$

Each monomer molecule that adds to a reactive center regenerates the reactive center. Polymer growth proceeds by the successive additions of hundreds or thousands or more monomer molecules. The growth of the polymer chain ceases when the reactive center is destroyed by one or more of a number of possible termination reactions.

The typical step and chain polymerizations differ significantly in the relationship between polymer molecular weight and the percent conversion of monomer. Thus if we start out step and chain polymerizations side by side, we may observe a variety of situations with regard to their relative rates of polymerization. However, the molecular weights of the polymers produced at any time after the start of the reactions will always be very characteristically different for the two polymerizations. If the two polymerizations are stopped at 0.1% conversion, 1% conversion, 10% conversion, 40% conversion, 90% conversion, and so on, one will always observe the same behavior. The chain polymerization will show the presence of high-molecular-weight polymer molecules at all percents of conversion. There are no intermediate-sized molecules in the reaction mixture—only monomer, high-polymer, and initiator species. The only change that occurs with conversion (i.e., reaction time) is the continuous increase in the number of polymer molecules (Fig. 1-1a). On the other hand, high-molecular-weight polymer is obtained in step polymerizations only near the very end of the reaction (>98% conversion) (Fig. 1-1b). Thus both polymer size and the amount of polymer are dependent on conversion in step polymerization.

The classification of polymers according to polymerization mechanism, like that by structure and composition, is not without its ambiguities. Certain polymerizations show a linear increase of molecular weight with conversion (Fig. 1-1c) when the polymerization
mechanism departs from the normal chain pathway. This is observed in certain chain poly-
merizations, which involve a fast initiation process coupled with the absence of reactions that
terminate the propagating reactive centers. Biological syntheses of proteins also show the
behavior described by Fig. 1-1c because the various monomer molecules are directed to react
in a very specific manner by an enzymatically controlled process.

Fig. 1-1 Variation of molecular weight with conversion; (a) chain polymerization; (b) step polymeriza-
tion; (c) nonterminating chain polymerization and protein synthesis.
The ring-opening polymerizations of cyclic monomers such as propylene oxide

\[ n\text{CH}_3\text{CH}–\text{CH}_2\text{O} \rightarrow \bigg[\text{CH}_2–\text{CH}–\text{O} \bigg]_n \]  

(1-10)

or ε-caprolactam

\[ n\text{CH}_2\text{CH}_2\text{NH}–\text{CO} \rightarrow \bigg[\text{NHCH}_2\text{CH}_2\text{CH}_2\text{CH}_2\text{CO} \bigg]_n \]  

(1-11)

usually proceed by the chain polymerization mechanism, but the dependence of polymer molecular weight on conversion almost never follows the behavior in Fig. 1-1a. Ring-opening polymerizations often follow the behavior in Fig. 1-1c.

The International Union of Pure and Applied Chemistry [IUPAC, 1994] suggested the term polycondensation instead of step polymerization, but polycondensation is a narrower term than step polymerization since it implies that the reactions are limited to condensations—reactions in which small molecules such as water are expelled during polymerization. The term step polymerization encompasses not only condensations but also polymerizations in which no small molecules are expelled. An example of the latter is the reaction of diols and disocyanates to yield polyurethanes (Eq. 1-6). The formation of polyurethanes follows the same reaction characteristics as the formation of polyesters, polyamides, and other polymerizations in which small molecules are expelled.

Ring-opening polymerizations point out very clearly that one must distinguish between the classification of the polymerization mechanism and that of the polymer structure. The two classifications cannot always be used interchangeably. Polymers such as the polyethers and polyamides produced in Eqs. 1-10 and 1-11, as well as those from other cyclic monomers, must be separately classified as to polymerization mechanism and polymer structure. These polymers are structurally classified as condensation polymers, since they contain functional groups (e.g., ether, amide) in the polymer chain. They, like the polyurethanes, are not classified as addition polymers by the use of Carothers’ original classification. The situation is even more complicated for a polymer such as that obtained from ε-caprolactam. The exact same polymer can be obtained by the step polymerization of the linear monomer ε-aminocaproic acid. It should suffice at this point to stress that the terms condensation and step polymer or polymerization are not synonymous nor are the terms addition and chain polymer or polymerization, even though these terms are often used interchangeably. The classification of polymers based only on polymer structure or only on polymerization mechanism is often an oversimplification that leads to ambiguity and error. Both structure and mechanism are usually needed in order to clearly classify a polymer.

1-2 NOMENCLATURE OF POLYMERS

Polymer nomenclature leaves much to be desired. A standard nomenclature system based on chemical structure as is used for small inorganic and organic compounds is most desired.
Unfortunately, the naming of polymers has not proceeded in a systematic manner until relatively late in the development of polymer science. It is not at all unusual for a polymer to have several names because of the use of different nomenclature systems. The nomenclature systems that have been used are based on either the structure of the polymer or the source of the polymer [i.e., the monomer(s) used in its synthesis] or trade names. Not only have there been several different nomenclature systems, but their application has not always been rigorous. An important step toward standardization was initiated in the 1970s by the International Union of Pure and Applied Chemistry.

1-2a Nomenclature Based on Source

The most simple and commonly used nomenclature system is probably that based on the source of the polymer. This system is applicable primarily to polymers synthesized from a single monomer as in addition and ring-opening polymerizations. Such polymers are named by adding the name of the monomer onto the prefix “poly” without a space or hyphen. Thus the polymers from ethylene and acetaldehyde are named polyethylene and polyacetaldehyde, respectively. When the monomer has a substituted parent name or a multiworded name or an abnormally long name, parentheses are placed around its name following the prefix “poly.” The polymers from 3-methyl-1-pentene, vinyl chloride, propylene oxide, chlorotrifluoroethylene, and ε-caprolactam are named poly(3-methyl-1-pentene), poly(vinyl chloride), poly(propylene oxide), poly(chlorotrifluoroethylene), and poly(ε-caprolactam), respectively. Other examples are listed in Table 1-2. The parentheses are frequently omitted in common usage when naming polymers. Although this will often not present a problem, it is incorrect and in some cases the omission can lead to uncertainty as to the structure of the polymer named. Thus the use of polyethylene oxide instead of poly(ethylene oxide) can be ambiguous in denoting one of the following possible structures:

\[
\begin{align*}
\text{II} & \quad \left(\text{CH}_2\text{CH}_2\right)_n \quad \text{O} \quad \left(\text{CH}_2\text{CH}_2\right)_n \\
\text{III} & \quad \left(\text{CH}_2\text{CH}_3\right)_n \quad \text{O}
\end{align*}
\]

instead of the polymer, \(\left(\text{CH}_2\text{CH}_2\right)_n \quad \text{O} \), from ethylene oxide.

Some polymers are named as being derived from hypothetical monomers. Thus poly (vinyl alcohol) is actually produced by the hydrolysis of poly(vinyl acetate)

\[
\begin{align*}
\text{CH}_3\text{COO} \\
\text{CH}_2\text{CH}_3 + n\text{H}_2\text{O} \rightarrow \quad \text{HO} \\
\text{CH}_2\text{CH}_3 + n\text{CH}_3\text{COOH}
\end{align*}
\]

It is, however, named as a product of the hypothetical monomer vinyl alcohol (which in reality exists exclusively as the tautomer–acetaldehyde).

Condensation polymers synthesized from single reactants are named in a similar manner. Examples are the polyamides and polyesters produced from amino acids and hydroxy acids, respectively. Thus, the polymer from 6-aminocaproic acid is named poly(6-aminocaproic acid)
It should be noted that there is an ambiguity here in that poly(6-aminocaproic acid) and poly(ε-caprolactam) are one and the same polymer. The same polymer is produced from two different monomers—a not uncommonly encountered situation.

1-2b Nomenclature Based on Structure (Non-IUPAC)

A number of the more common condensation polymers synthesized from two different monomers have been named by a semisystematic, structure-based nomenclature system other than the more recent IUPAC system. The name of the polymer is obtained by following the prefix poly without a space or hyphen with parentheses enclosing the name of the structural grouping attached to the parent compound. The parent compound is the particular member of the class of the polymer—the particular ester, amide, urethane, and so on. Thus the polymer from hexamethylene diamine and sebacic acid is considered as the substituted amide derivative of the compound sebacic acid, HO₂C(CH₂)₈CO₂H, and is named poly(hexamethylene sebacamide). Poly(ethylene terephthalate) is the polymer from ethylene glycol and terephthalic acid, p-HO₂C-C₆H₄-CO₂H. The polymer from trimethylene glycol and ethylene diisocyanate is poly(trimethylene ethylene–urethane)

\[
\left[\text{HN}-(\text{CH₂})₆-\text{NHCO}-(\text{CH₂})₈-\text{CO}\right]_n
\]

Poly(hexamethylene sebacamide)

\[
\left[\text{O} - \text{CH₂CH₂} - \text{OCO} - \text{O} - \text{CO}\right]_n
\]

Poly(ethylene terephthalate)

\[
\left[\text{O} - \text{CH₂CH₂CH₂} - \text{OCONH} - \text{CH₂CH₂} - \text{NHCO}\right]_n
\]

Poly(trimethylene ethyleneurethane)

A suggestion was made to name condensation polymers synthesized from two different monomers by following the prefix poly with parentheses enclosing the names of the two reactants, with the names of the reactants separated by the term -co-. Thus, the polymer in Eq. 1-7 would be named poly(phenol-co-formaldehyde). This suggestion did not gain acceptance.

1-2c IUPAC Structure-Based Nomenclature System

The inadequacy of the preceding nomenclature systems was apparent as the polymer structures being synthesized became increasingly complex. The IUPAC rules allow one to name
single-strand organic polymers in a systematic manner based on polymer structure (IUPAC, 1991, 1994, 2002, in press; Panico et al., 1993; Wilks, 2000). Single-strand organic polymers have any pair of adjacent repeat units interconnected through only one atom. All the polymers discussed to this point and the large majority of polymers to be considered in this text are single-strand polymers. Double-strand polymers have uninterrupted sequences of rings. A ladder polymer is a double-strand polymer in which adjacent rings have two or more atoms in common, for example, structure VII. Some aspects of double-strand polymers are considered in Secs. 2-14a and 2-17d.

VII

The basis of IUPAC polymer nomenclature system is the selection of a preferred constitutional repeating unit (abbreviated as CRU). The CRU is also referred to as the structural repeating unit. The CRU is the smallest possible repeating unit of the polymer. It is a bivalent unit for a single-strand polymer. The name of the polymer is the name of the CRU in parentheses or brackets prefixed by poly. The CRU is synonymous with the repeating unit defined in Sec. 1-1a except when the repeating unit consists of two symmetric halves, as in the polymers \(-\text{CH}_2\text{CH}_2\) and \(-\text{CF}_2\text{CF}_2\). The CRU is CH\(_2\) and CF\(_2\), respectively, for polyethylene and polytetrafluoroethylene, while the repeating unit is CH\(_2\)CH\(_2\) and CF\(_2\)CF\(_2\), respectively.

The constitutional repeating unit is named as much as possible according to the IUPAC nomenclature rules for small organic compounds. The IUPAC rules for naming single-strand polymers dictate the choice of a single CRU so as to yield a unique name, by specifying both the seniority among the atoms or subunits making up the CRU and the direction to proceed along the polymer chain to the end of the CRU. A CRU is composed of two or more subunits when it cannot be named as a single unit. The following is a summary of the most important of the IUPAC rules for naming single-stand organic polymers:

1. The name of a polymer is the prefix poly followed in parentheses or brackets by the name of the CRU. The CRU is named by naming its subunits. Subunits are defined as the largest subunits that can be named by the IUPAC rules for small organic compounds.

2. The CRU is written from left to right beginning with the subunit of highest seniority and proceeding in the direction involving the shortest route to the subunit next in seniority.

3. The seniority of different types of subunits is heterocyclic rings > heteroatoms or acyclic subunits containing heteroatoms > carbocyclic rings > acyclic subunits containing only carbon. The presence of various types of atoms, groups of atoms, or rings that are not part of the main polymer chain but are substituents on the CRU do not affect this order of seniority.

4. For heterocyclic rings the seniority is a ring system having nitrogen in the ring > a ring system having a heteroatom other than nitrogen in the order of seniority defined by rule 5 below > a ring system having the greatest number of heteroatoms > a ring system having the largest individual ring > a ring system having the greatest variety of heteroatoms > a ring system having the greatest number of heteroatoms highest in the order given in rule 5.

5. For heteroatom(s) or acyclic subunits containing heteroatom(s), the order of decreasing priority is O, S, Se, Te, N, P, As, Sb, Bi, Si, Ge, Sn, Pb, B, Hg. (Any heteroatom
has higher seniority than carbon—rule 3.) The seniority of other heteroatoms within this order is determined from their positions in the periodic table.

6. For carbocyclic rings the seniority is a ring system having the greatest number of rings > the ring system having the largest individual ring > the ring system having the greatest number of atoms common to its rings.

7. For a given carbocyclic or heterocyclic ring system: (a) when rings differ only in degree of unsaturation, seniority increases with degree of unsaturation; (b) for the same ring system, seniority is higher for the ring system having the lowest location number (referred to as locant), which designates the first point of difference for ring junctions.

8. These orders of seniority are superseded by the requirement of minimizing the number of free valences in the CRU, that is, the CRU should be a bivalent unit wherever possible.

9. Where there is a choice subunits should be oriented so that the lowest locant results for substituents.

Let us illustrate some of these rules by naming a few polymers. For the polymer

\[ \text{CHCH}_2\text{OCHCH}_2\text{OCHCH}_2\text{OCHCH}_2\text{O} \]

the possible CRUs are

\[ \text{IX} \quad \text{X} \quad \text{XI} \]

\[ \text{XII} \quad \text{XIII} \quad \text{XIV} \]

Note that CRUs XII–XIV are simply the reverse of CRUs IX–XI. Application of the nomenclature rules dictates the choice of only one of these as the CRU. That oxygen has higher seniority than carbon (rule 5) eliminates all except XI and XII as the CRU. Application of rule 8 results in XI as the CRU and the name poly[oxy(1-fluoroethylene)]. Choosing XII as the CRU would result in the name poly[oxy(2-fluoroethylene)], which gives the higher locant for the fluorine substituent. The name poly[oxy(fluoromethylenemethylene)] is incorrect because it does not define the largest possible subunit (which is CHFCH₂ vs. CHF plus CH₂).

Rule 7 specifies \(-\text{CH}==\text{CH}−\) as the correct CRU in preference to \(=\text{CH}−\text{CH}=\), since the former is bivalent, while the latter is tetravalent. The polymer \((=\text{CH}−\text{CH}=)_n\) is poly(ethene-1,2-diyl).

The higher seniority of heterocyclic rings over carbocyclic rings (rule 3) and the higher seniority with higher unsaturation for cyclic subunits (rule 7a) yield the CRU XV with the name poly(pyridine-2,4-diyl-1,4-phenylenecyclohexane-1,4-diyl).

\[ \text{XV} \]
The higher seniority of cyclic subunits over acyclic subunits (rule 3) and the higher seniority of a subunit with lower locant(s) relative to the same subunit with higher locant(s) (rule 7b) yield the CRU XVI with the name poly(cyclohexane-1,3-diylcyclohexane-1,4-diyl-1-methylpropane-1,3-diyl). Note that all acyclic subunits except CH$_2$ and CH$_2$CH$_2$ are named as alkane-$\alpha$, $\omega$-diyl. CH$_2$ and CH$_2$CH$_2$ subunits are named methylene and ethylene, respectively.

![Graph](XVI)

In the IUPAC system locants are placed immediately before the part of the name to which they apply; for instance subunits such as pyridine-2,4-diyl and 1-methylpropane-1,3-diyl. One of the few exceptions is the phenylene subunit, for example, 1,4-phenylene in XV. The IUPAC nomenclature system is always evolving and some of the details (e.g., the names of some subunits) have changed in recent years. One should use caution when using less recent nomenclature references than those listed in this text.

The IUPAC nomenclature system recognizes that most of the common (commercial) polymers have source-based or semisystematic names that are well established by usage. IUPAC does not intend that such names be supplanted by the IUPAC names but anticipates that such names will be kept to a minimum. The IUPAC system is generally used for all except the common polymers. The IUPAC names for various of the common polymers are indicated below the more established source or semisystematic name in the following:

- $\left\{\text{CH}_2\text{CH}_2\right\}_n$ Polyethylene or polyethene
  Polymethylene
- $\left\{\text{CHCH}_2\right\}_n$ Polypropylene or polypropene
  Poly(1-methylethylene)
- $\left\{\text{CHCH}_2\right\}_n$ Polystyrene
  Poly(1-phenylethylene)
- $\left\{\text{CHCH}_2\right\}_n$ Poly(methyl acrylate)
  Poly[1-(methoxycarbonyl)ethylene]
- $\left\{\text{OCH}_2\right\}_n$ Polyformaldehyde
  Poly(oxymethylene)
- $\left\{\text{OCH}_2\right\}_n$ Poly(phenylene oxide)
  Poly(oxy-1,4-phenylene)
\[ \text{NH(CH}_2\text{)}_6\text{NHCO(CH}_2\text{)}_4\text{CO}_n \]

XXIII

Poly(hexamethylene adipamide)
Poly(iminohexanedioyliminohexane-1,6-diyl)

\[ \text{NHCO(CH}_2\text{)}_5\text{O}_n \]

XXIV

Poly(\(\varepsilon\)-caprolactam) or poly(\(\varepsilon\)-aminocaproic acid) depending on the source of polymer

Poly[imino(1-oxohexane-1,6-diyl)]

\[ \text{OCH}_2\text{CH}_2\text{O} - \text{CO} - \text{COOCH}_2\text{CH}_2\text{O}_n \]

XXV

Poly(ethylene terephthalate)
Poly(oxyethyleneoxyterephthaloyl)

The IUPAC nomenclature will be used in this book with some exceptions. One exception is the use of well-established, non-IUPAC names for most of the commonly encountered polymers of commercial importance. Another exception will be in not following rule 2 for writing the constitutional repeating unit (although the correct IUPAC name will be employed). Using the IUPAC choice of the CRU leads in some cases to structures that are longer and appear more complicated. Thus the IUPAC structure for the polymer in Eq. 1-3 is

\[ \text{Cl} - \text{CO} - \text{O} - \text{R} - \text{O} - \text{CO} - \text{O} - \text{R}_n \]

XXVI

which is clearly not as simple as

\[ \text{H} - \text{O} - \text{R} - \text{O} - \text{CO} - \text{Cl}_n \]

XXVII

although both XXVI and XXVII denote the exact same structure. This type of problem arises only with certain polymers and then only when the drawn structure is to include the ends of the polymer chain instead of simply the repeating unit or the CRU. The CRU will also generally not be used in equations such as Eq. 1-9. The polymerization mechanism in such reactions involves the propagating center on the substituted carbon atom of the monomer. Using

\[ R - \text{CH}_2 - \text{C} - \text{CH}_2 - \text{C} - \text{Y}_m \]

termination

\[ \overset{\text{H}}{\text{C} - \text{CH}_2}_n \]

(1-14)
the CRU would yield Eq. 1-14 in place of Eq. 1-9, which appears unbalanced and confusing, at least to the beginning student, compared to

\[
\begin{align*}
\text{CH}_2\text{C} & \quad \text{H} \\
\quad & \quad \text{Y} \\
\quad \quad & \quad \quad m \\
\text{CH}_2\text{C}^* & \quad \text{H} \\
\quad & \quad \text{Y} \\
\quad \quad & \quad \quad n
\end{align*}
\]

Equation 1-9 has the repeating unit written the same way on both sides, while Eq. 1-14 has the repeating unit reversed on the right side relative to what it is on the left side.

Before proceeding one needs to mention Chemical Abstracts (CA), a journal published by the American Chemical Society, that abstracts the world’s chemical literature and has developed its own nomenclature rules. The CA rules are generally very close to the IUPAC rules, but there are some differences. Most of the differences are not important at the level of the discussions in this book. One difference that needs to be mentioned is the placement of locants. CA does not place locants immediately before the part of the name to which they apply. Thus, the CA name for the first subunit in XV is 2,4-pyridinediyl instead of pyridine-2,4-diyl. The difference between IUPAC and CA is also seen in the placement of locants in naming vinyl monomers such as CH_2=CHCH_2CH_3. The IUPAC name is but-1-ene; the CA name is 1-butene. Most chemists tend to follow the CA placement of locants for small molecules. This text will generally follow the IUPAC rule for locants for CRU subunits, but the CA rule for monomers.

1-2d Trade Names and Nonnames

Special terminology based on trade names has been employed for some polymers. Although trade names should be avoided, one must be familiar with those that are firmly established and commonly used. An example of trade-name nomenclature is the use of the name nylon for the polyamides from unsubstituted, nonbranched aliphatic monomers. Two numbers are added onto the word “nylon” with the first number indicating the number of methylene groups in the diamine portion of the polyamide and the second number the number of carbon atoms in the diacyl portion. Thus poly(hexamethylene adipamide) and poly(hexamethylene sebacamide) are nylon 6,6 and nylon 6,10, respectively. Variants of these names are frequently employed. The literature contains such variations of nylon 6,6 as nylon 66, 66 nylon, nylon 6/6, 6,6 nylon, and 6-6 nylon. Polyamides from single monomers are denoted by a single number to denote the number of carbon atoms in the repeating unit. Poly(ɛ-caprolactam) or poly(6-aminocaproic acid) is nylon 6.

In far too many instances trade-name polymer nomenclature conveys very little meaning regarding the structure of a polymer. Many condensation polymers, in fact, seem not to have names. Thus the polymer obtained by the step polymerization of formaldehyde and phenol is variously referred to as a phenol–formaldehyde polymer, phenol–formaldehyde resin, phenolic, phenolic resin, and phenoplast. Polymers of formaldehyde or other aldehydes with urea or melamine are generally referred to as amino resins or aminoplasts without any more specific names. It is often extremely difficult to determine which aldehyde and which amino monomers have been used to synthesize a particular polymer being referred to as an amino resin. More specific nomenclature, if it can be called that, is afforded by indicating the two reactants as in names such as urea–formaldehyde resin or melamine–formaldehyde resin.

A similar situation exists with the naming of many other polymers. Thus the polymer XXVII is usually referred to as “the polycarbonate from bisphenol A” or polycarbonate. The
1-3 LINEAR, BRANCHED, AND CROSSLINKED POLYMERS

Polymers can be classified as linear, branched, or crosslinked polymers depending on their structure. In the previous discussion on the different types of polymers and polymerizations we have considered only those polymers in which the monomer molecules have been linked together in one continuous length to form the polymer molecule. Such polymers are termed
linear polymers. Under certain reaction conditions or with certain kinds of monomers the polymers can be quite different.

Branched polymers, polymers with more than two chain ends per molecule, can form in both step and chain polymerizations. Branched polymer molecules are those in which there are side branches of linked monomer molecules protruding from various central branch points along the main polymer chain. The difference between the shapes of linear and branched polymer molecules can be seen from the structural representations in Fig. 1-2. The branch points are indicated by heavy dots. The illustrations show that there are several different kinds of branched polymers. The branched polymer can be comblike in structure with either long (A) or short (B) branches. When there is extensive branching, the polymer can have a dendritic structure in which there are branches protruding from other branches, that is, branched branches (C). The presence of branching in a polymer usually has a large effect on many important polymer properties. The most significant property change brought about by branching is the decrease in crystallinity. Branched polymers do not pack as easily into a crystal lattice as do linear polymers.

It is important to point out that the term branched polymer does not refer to linear polymers containing side groups that are part of the monomer structure. Only those polymers that contain side branches composed of complete monomer units are termed branched polymers. Thus polystyrene XXVIII is classified as a linear polymer, and not as a branched polymer, because the phenyl groups are part of the monomer unit and are not considered as branches. Branched polystyrene would be the polymer XXIX in which one has one or more polystyrene branches protruding from the main linear polystyrene chain.
When polymers are produced in which the polymer molecules are linked to each other at points other than their ends, the polymers are said to be crosslinked (Fig. 1-2). Crosslinking can be made to occur during the polymerization process by the use of appropriate monomers. It can also be brought about after the polymerization by various chemical reactions. The crosslinks between polymer chains can be of different lengths depending on the crosslinking method and the specific conditions employed. One can also vary the number of crosslinks so as to obtain lightly or highly crosslinked polymers. When the number of crosslinks is sufficiently high, a three-dimensional or space network polymer is produced in which all the polymer chains in a sample have been linked together to form one giant molecule. Light crosslinking is used to impart good recovery (elastic) properties to polymers to be used as rubbers. High degrees of crosslinking are used to impart high rigidity and dimensional stability (under conditions of heat and stress) to polymers such as the phenol-formaldehyde and urea–formaldehyde polymers.

1-4 MOLECULAR WEIGHT

The molecular weight of a polymer is of prime importance in the polymer’s synthesis and application. Chemists usually use the term molecular weight to describe the size of a molecule. The more accurate term is molar mass, usually in units of g mol⁻¹. The term molecular weight is the ratio of the average mass per formula unit of a substance to \( \frac{1}{12} \)th of the mass of an atom of \( ^{12}\text{C} \) and is dimensionless (IUPAC, 1991, in press). This text will use molecular weight throughout irrespective of the units, because molecular weight is the more familiar term for most chemists.

The interesting and useful mechanical properties that are uniquely associated with polymeric materials are a consequence of their high molecular weight. Most important mechanical properties depend on and vary considerably with molecular weight as seen in Fig. 1-3. There is a minimum polymer molecular weight (A), usually a thousand or so, to produce any significant mechanical strength at all. Above A, strength increases rapidly with molecular weight until a critical point (B) is reached. Mechanical strength increases more slowly above B and eventually reaches a limiting value (C). The critical point B generally corresponds to the minimum molecular weight for a polymer to begin to exhibit sufficient strength to be useful. Most practical applications of polymers require higher molecular weights to obtain higher strengths. The minimum useful molecular weight (B), usually in the range 5000–10,000, differs for different polymers. The plot in Fig. 1-3 generally shifts to the right as the magnitude of the intermolecular forces decreases. Polymer chains with stronger

![Fig. 1-3 Dependence of mechanical strength on polymer molecular weight.](image-url)
intermolecular forces, for example, polyamides and polyesters, develop sufficient strength to be useful at lower molecular weights than polymers having weaker intermolecular forces, for example, polyethylene.

Properties other than strength also show a significant dependence on molecular weight. However, most properties show different quantitative dependencies on molecular weight. Different polymer properties usually reach their optimum values at different molecular weights. Further, a few properties may increase with molecular weight to a maximum value and then decrease with further increase in molecular weight. An example is the ability to process polymers into useful articles and forms (e.g., film, sheet, pipe, fiber). Processability begins to decrease past some molecular weight as the viscosity becomes too high and melt flow too difficult. Thus the practical aspect of a polymerization requires one to carry out the process to obtain a compromise molecular weight—a molecular weight sufficiently high to obtain the required strength for a particular application without overly sacrificing other properties. Synthesizing the highest possible molecular weight is not necessarily the objective of a typical polymerization. Instead, one often aims to obtain a high but specified, compromise molecular weight. The utility of a polymerization is greatly reduced unless the process can be carried out to yield the specified molecular weight. The control of molecular weight is essential for the practical application of a polymerization process.

When one speaks of the molecular weight of a polymer, one means something quite different from that which applies to small-sized compounds. Polymers differ from the small-sized compounds in that they are polydisperse or heterogeneous in molecular weight. Even if a polymer is synthesized free from contaminants and impurities, it is still not a pure substance in the usually accepted sense. Polymers, in their purest form, are mixtures of molecules of different molecular weight. The reason for the polydispersity of polymers lies in the statistical variations present in the polymerization processes. When one discusses the molecular weight of a polymer, one is actually involved with its average molecular weight. Both the average molecular weight and the exact distribution of different molecular weights within a polymer are required in order to fully characterize it. The control of molecular weight and molecular weight distribution (MWD) is often used to obtain and improve certain desired physical properties in a polymer product.

Various methods based on solution properties are used to determine the average molecular weight of a polymer sample. These include methods based on colligative properties, light scattering, and viscosity [Heimenz, 1984; Morawetz, 1975; Slade, 1998; Sperling, 2001]. The various methods do not yield the same average molecular weight. Different average molecular weights are obtained because the properties being measured are biased differently toward the different-sized polymer molecules in a polymer sample. Some methods are biased toward the larger-sized polymer molecules, while other methods are biased toward the smaller-sized molecules. The result is that the average molecular weights obtained are correspondingly biased toward the larger- or smaller-sized molecules. The following average molecular weights are determined:

1. The number-average molecular weight $M_n$ is determined by experimental methods that count the number of polymer molecules in a sample of the polymer. The methods for measuring $M_n$ are those that measure the colligative properties of solutions—vapor pressure lowering (vapor pressure osmometry), freezing point depression (cryoscopy), boiling point elevation (ebulliometry), and osmotic pressure (membrane osmometry). The colligative properties are the same for small and large molecules when comparing solutions at the same molal (or mole fraction) concentration. For example, a 1-molal solution of a polymer of molecular weight $10^5$ has the same vapor pressure, freezing point, boiling point, and osmotic
pressure as a 1-molal solution of a polymer of molecular weight $10^3$ or a 1-molal solution of a small molecule such as hexane. $\overline{M}_n$ is defined as the total weight $w$ of all the molecules in a polymer sample divided by the total number of moles present. Thus the number-average molecular weight is

$$\overline{M}_n = \frac{w}{\sum N_x} = \frac{\sum N_x M_x}{\sum N_x}$$

(1-15)

where the summations are over all the different sizes of polymer molecules from $x = 1$ to $x = \infty$ and $N_x$ is the number of moles whose weight is $M_x$. Equation 1-15 can also be written as

$$\overline{M}_n = \sum N_x M_x$$

(1-16)

where $N_x$ is the mole fraction (or the number-fraction) of molecules of size $M_x$. The most common methods for measuring $\overline{M}_n$ are membrane osmometry and vapor pressure osmometry since reasonably reliable commercial instruments are available for those methods. Vapor pressure osmometry, which measures vapor pressure indirectly by measuring the change in temperature of a polymer solution on dilution by solvent vapor, is generally useful for polymers with $\overline{M}_n$ below 10,000–15,000. Above that molecular weight limit, the quantity being measured becomes too small to detect by the available instruments. Membrane osmometry is limited to polymers with $\overline{M}_n$ above about 20,000–30,000 and below 500,000. The lower limit is a consequence of the partial permeability of available membranes to smaller-sized polymer molecules. Above molecular weights of 500,000, the osmotic pressure of a polymer solution becomes too small to measure accurately. End-group analysis is also useful for measurements of $\overline{M}_n$ for certain polymers. For example, the carboxyl end groups of a polyester can be analyzed by titration with base and carbon–carbon double bond end groups can be analyzed by $^1$H NMR. Accurate end-group analysis becomes difficult for polymers with $\overline{M}_n$ values above 20,000–30,000.

2. Light scattering by polymer solutions, unlike coligative properties, is greater for larger-sized molecules than for smaller-sized molecules. The average molecular weight obtained from light-scattering measurements is the weight-average molecular weight $\overline{M}_w$ defined as

$$\overline{M}_w = \sum w_x M_x$$

(1-17)

where $w_x$ is the weight fraction of molecules whose weight is $M_x$. $\overline{M}_w$ can also be defined as

$$\overline{M}_w = \frac{\sum c_x M_x}{\sum c_x} = \frac{\sum N_x M_x^2}{\sum N_x M_x}$$

(1-18)

where $c_x$ is the weight concentration of $M_x$ molecules, $c$ is the total weight concentration of all the polymer molecules, and the following relationships hold:

$$w_x = \frac{c_x}{c}$$

(1-19)

$$c_x = N_x M_x$$

(1-20)

$$c = \sum c_x = \sum N_x M_x$$

(1-21)
Since the amount of light scattered by a polymer solution increases with molecular weight, this method becomes more accurate for higher polymer molecular weights. There is no upper limit to the molecular weight that can be accurately measured except the limit imposed by insolubility of the polymer. The lower limit of $M_w$ by the light scattering method is close to 5000–10,000. Below this molecular weight, the amount of scattered light is too small to measure accurately.

3. Solution viscosity is also useful for molecular-weight measurements. Viscosity, like light scattering, is greater for the larger-sized polymer molecules than for smaller ones. However, solution viscosity does not measure $M_w$ since the exact dependence of solution viscosity on molecular weight is not exactly the same as light scattering. Solution viscosity measures the viscosity-average molecular weight $M_v$, defined by

$$
M_v = \left[ \sum w_i M_i^a \right]^{1/a} = \left[ \frac{\sum N_i M_i^{a+1}}{\sum N_i M_i^a} \right]^{1/a}
$$

where $a$ is a constant. The viscosity- and weight-average molecular weights are equal when $a$ is unity. $M_v$ is less than $M_w$ for most polymers, since $a$ is usually in the range 0.5–0.9. However, $M_v$ is much closer to $M_w$ than $M_n$, usually within 20% of $M_w$. The value of $a$ is dependent on the hydrodynamic volume of the polymer, the effective volume of the solvated polymer molecule in solution, and varies with polymer, solvent, and temperature.

More than one average molecular weight is required to reasonably characterize a polymer sample. There is no such need for a monodisperse product (i.e., one composed of molecules whose molecular weights are all the same) for which all three average molecular weights are the same. The situation is quite different for a polydisperse polymer where all three molecular weights are different if the constant $a$ in Eq. 1-22 is less than unity, as is the usual case. A careful consideration of Eqs. 1-15 through 1-22 shows that the number-, viscosity-, and weight-average molecular weights, in that order, are increasingly biased toward the higher-molecular-weight fractions in a polymer sample. For a polydisperse polymer

$$
M_w > M_v > M_n
$$

with the differences between the various average molecular weights increasing as the molecular-weight distribution broadens. A typical polymer sample will have the molecular-weight distribution shown in Fig. 1-4. The approximate positions of the different average molecular weights are indicated on this distribution curve.

For most practical purposes, one usually characterizes the molecular weight of a polymer sample by measuring $M_n$ and either $M_w$ or $M_v$. $M_v$ is commonly used as a close approximation of $M_w$, since the two are usually quite close (within 10–20%). Thus in most instances, one is concerned with the $M_n$ and $M_w$ of a polymer sample. The former is biased toward the lower-molecular-weight fractions, while the latter is biased toward the higher-molecular-weight fractions. The ratio of the two average molecular weights $M_w/M_n$ depends on the breadth of the distribution curve (Fig. 1-4) and is often useful as a measure of the polydispersity in a polymer. The value of $M_w/M_n$ would be unity for a perfectly monodisperse polymer. The ratio is greater than unity for all actual polymers and increases with increasing polydispersity.

The characterization of a polymer by $M_n$ alone, without regard to the polydispersity, can be extremely misleading, since most polymer properties such as strength and melt viscosity are determined primarily by the size of the molecules that make up the bulk of the sample by weight. Polymer properties are much more dependent on the larger-sized molecules in a
sample than on the smaller ones. Thus, for example, consider a hypothetical mixture containing 95% by weight of molecules of molecular weight 10,000, and 5% of molecules of molecular weight 100. (The low-molecular-weight fraction might be monomer, a low-molecular-weight polymer, or simply some impurity.) The $M_n$ and $M_w$ are calculated from Eqs. 1-15 and 1-17 as 1680 and 9505, respectively. The use of the $M_n$ value of 1680 gives an inaccurate indication of the properties of this polymer. The properties of the polymer are determined primarily by the 10,000-molecular-weight molecules that make up 95% of the weight of the mixture. The weight-average molecular weight is a much better indicator of the properties to be expected in a polymer. the utility of $M_n$ resides primarily in its use to obtain an indication of polydispersity in a sample by measuring the ratio $M_w/M_n$.

In addition to the different average molecular weights of a polymer sample, it is frequently desirable and necessary to know the exact distribution of molecular weights. As indicated previously, there is usually a molecular weight range for which any given polymer property will be optimum for a particular application. The polymer sample containing the greatest percentage of polymer molecules of that size is the one that will have the optimum value of the desired property. Since samples with the same average molecular weight may possess different molecular weight distributions, information regarding the distribution allows the proper choice of a polymer for optimum performance. Various methods have been used in the past to determine the molecular weight distribution of a polymer sample, including fractional extraction and fractional precipitation. These methods are laborious and determinations of molecular weight distributions were not routinely performed. However, the development of size exclusion chromatography (SEC), also referred to as gel permeation chromatography (GPC) and the availability of automated commercial instruments have changed the situation. Molecular-weight distributions are now routinely performed in most laboratories using SEC.

Size exclusion chromatography involves the permeation of a polymer solution through a column packed with microporous beads of crosslinked polystyrene [Potschka and Dublin, 1996; Yau et al., 1979]. The packing contains beads of different-sized pore diameters. Molecules pass through the column by a combination of transport into and through the beads and through the interstitial volume (the volume between beads). Molecules that penetrate the beads are slowed down more in moving through the column than molecules that do not penetrate the beads; in other words, transport through the interstitial volume is faster than through

---

Fig. 1-4 Distribution of molecular weights in a typical polymer sample.
the pores. The smaller-sized polymer molecules penetrate all the beads in the column since
their molecular size (actually their hydrodynamic volume) is smaller than the pore size of
the beads with the smallest-sized pores. A larger-sized polymer molecule does not penetrate
all the beads since its molecular size is larger than the pore size of some of the beads. The larger
the polymer molecular weight, the fewer beads that are penetrated and the greater is the
extent of transport through the interstitial volume. The time for passage of polymer mole-
cules through the column decreases with increasing molecular weight. The use of an appro-
riate detector (refractive index, viscosity, light scattering) measures the amount of polymer
passing through the column as a function of time. This information and a calibration of
the column with standard polymer samples of known molecular weight allow one to obtain
the molecular weight distribution in the form of a plot such as that in Fig. 1-4. Not only does
SEC yield the molecular weight distribution, but $M_n$ and $M_w$ (and also $M_v$ if $a$ is known) are
also calculated automatically. SEC is now the method of choice for measurement of $M_n$ and
$M_w$ since the SEC instrument is far easier to use compared to methods such as osmometry
and light scattering.

1-5 PHYSICAL STATE

1-5a Crystalline and Amorphous Behavior

Solid polymers differ from ordinary, low-molecular-weight compounds in the nature of their
physical state or morphology. Most polymers show simultaneously the characteristics of both
crystalline and amorphous solids [Keller et al., 1995; Mark et al., 1993; Porter and Wang,
1995; Sperling, 2001; Woodward, 1989; Wunderlich, 1973]. X-Ray and electron diffraction
patterns often show the sharp features typical of three-dimensionally ordered crystalline
solids as well as the diffuse, unordered features characteristic of amorphous solids. (Amor-
phous solids have sometimes been referred to as highly viscous liquids.) The terms crystal-
line and amorphous are used to indicate the ordered and unordered polymer regions,
respectively. Different polymers show different degrees of crystalline behavior. The known
polymers constitute a spectrum of materials from those that are completely amorphous to
others that possess low to moderate to high crystallinity. The term semicrystalline is used
to refer to polymers that are partially crystalline. Completely crystalline polymers are rarely
encountered.

The exact nature of polymer crystallinity has been the subject of considerable contro-
versy. The fringed-micelle theory, developed in the 1930s, considers polymers to consist
of small-sized, ordered crystalline regions—termed crystallites—imbedded in an unordered,
amorphous polymer matrix. Polymer molecules are considered to pass through several dif-
f erent crystalline regions with crystallites being formed when extended-chain segments from
different polymer chains are precisely aligned together and undergo crystallization. Each
polymer chain can contribute ordered segments to several crystallites. The segments of the
chain in between the crystallites make up the unordered amorphous matrix. This concept of
polymer crystallinity is shown in Fig. 1-5.

The folded-chain lamella theory arose in the last 1950s when polymer single crystals in
the form of thin platelets termed lamella, measuring about 10,000 Å × 100 Å, were grown
from polymer solutions. Contrary to previous expectations, X-ray diffraction patterns showed
the polymer chain axes to be parallel to the smaller dimension of the platelet. Since polymer
molecules are much longer than 100 Å, the polymer molecules are presumed to fold back and
forth on themselves in an accordionlike manner in the process of crystallization. Chain
folding was unexpected, since the most thermodynamically stable crystal is the one involving completely extended chains. The latter is kinetically difficult to achieve and chain folding is apparently the system’s compromise for achieving a highly stable crystal structure under normal crystallization conditions. Two models of chain folding can be visualized. Chain folding is regular and sharp with a uniform fold period in the adjacent-reentry model (Fig. 1-6). In the nonadjacent-reentry or switchboard model (Fig. 1-7) molecules wander through the non-regular surface of a lamella before reentering the lamella or a neighboring lamella. In the chain-folded lamella picture of polymer crystallinity less than 100% crystallinity is attributed to defects in the chain-folding process. The defects may be imperfect folds, irregularities in packing, chain entanglements, loose chain ends, dislocations, occluded impurities, or numerous other imperfections. The adjacent reentry and switchboard models differ in the details of

Fig. 1-5 Fringed-micelle model of polymer crystallinity.

Fig. 1-6 Adjacent reentry model of single crystal.
what constitutes the chain-folding defects. The switchboard model indicates that most defects are at the crystal surfaces, while the adjacent-reentry model indicates that defects are located as much within the crystal as at the crystal surfaces.

Folded-chain lamella represent the morphology not only for single crystals grown from solution but also polymers crystallized from the melt—which is how almost all commercial and other synthetic polymers are obtained. Melt-crystallized polymers have the most prominent structural feature of polymer crystals—the chains are oriented perpendicular to the lamella face so that chain folding must occur. Chain folding is maximum for polymers crystallized slowly near the crystalline melting temperature. Fast cooling (quenching) gives a more chaotic crystallization with less chain folding. Melt crystallization often develops as a spherical or spherulitic growth as seen under the microscope. Nucleation of crystal growth occurs at various nuclei and crystal growth proceeds in a radical fashion from each nucleus until the growth fronts from neighboring structures impinge on each other. These spherical structures, termed spherulites, completely fill the volume of a crystallized polymer sample. Spherulites have different sizes and degrees of perfection depending on the specific polymer and crystallization conditions.

A spherulite is a complex, polycrystalline structure (Fig. 1-8). The nucleus for spherulitic growth is the single crystal in which a multilayered stack is formed, and each lamella extends to form a lamellar fibril. The flat ribbonlike lamellar fibrils diverge, twist, and branch as they grow outward from the nucleus. Growth occurs by chain folding with the polymer chain axes being perpendicular to the length of the lamellar fibril. The strength of polymers indicates that more than van der Waals forces hold lamellae together. There are interlamellar or intercrystalline fibrils (also termed tie molecules) between the lamellar fibrils within a spherulite and between fibrils of different spherulites. Some polymer molecules simultaneously participate in the growth of two or more adjacent lamellae and provide molecular links that reinforce the crystalline structure. The chain axes of tie molecules lie parallel to the long axes of the link—each link between lamellae is an extended-chain type of single crystal. The tie molecules are the main component of the modern picture of polymer crystallinity, which is a carryover from the fringed-micelle theory. The amorphous content of a semicrystalline, melt-crystallized polymer sample consists of the defects in the chain-folding structure, tie molecules, and the material that is either, because of entanglements, not included in the growing lamellar fibril or is rejected from it owing to its unacceptable nature; low-molecular-weight chains and nonregular polymer chain segments, for example, are excluded.

Some natural polymers such as cotton, silk, and cellulose have the extended-chain morphology, but their morphologies are determined by enzymatically controlled synthesis and crystallization processes. Extended-chain morphology is obtained in some synthetic
polymers under certain circumstances. These include crystallization from the melt (or annealing for long time periods) under pressure or other applied stress and crystallization of polymers from the liquid crystalline state. The former has been observed with several polymers, including polyethylene and polytetrafluoroethylene. The latter is observed with polymers containing stiff or rigid-rod chains, such as poly(p-phenylene terephthalamide) (Sec. 2-8f). Extended-chain morphology is also obtained in certain polymerizations involving conversion of crystalline monomer to crystalline polymer, for example, polymerization of diacetylenes (Sec. 3-16c).

A variety of techniques have been used to determine the extent of crystallinity in a polymer, including X-ray diffraction, density, IR, NMR, and heat of fusion [Sperling, 2001; Wunderlich, 1973]. X-ray diffraction is the most direct method but requires the somewhat difficult separation of the crystalline and amorphous scattering envelopes. The other methods are indirect methods but are easier to use since one need not be an expert in the field as with X-ray diffraction. Heat of fusion is probably the most often used method since reliable thermal analysis instruments are commercially available and easy to use [Bershtein and Egorov, 1994; Wendlandt, 1986]. The difficulty in using thermal analysis (differential scanning calorimetry and differential thermal analysis) or any of the indirect methods is the uncertainty in the values of the quantity measured (e.g., the heat of fusion per gram of sample or density) for 0 and 100% crystalline samples since such samples seldom exist. The best technique is to calibrate the method with samples whose crystallinites have been determined by X-ray diffraction.

1-5b Determinants of Polymer Crystallinity

Regardless of the precise picture of order and disorder in polymers, the prime consideration that should be emphasized is that polymers have a tendency to crystallize. The extent of this crystallization tendency plays a most significant role in the practical ways in which polymers are used. This is a consequence of the large effect of crystallinity on the thermal, mechanical,
and other important properties of polymers. Different polymers have different properties and are synthesized and used differently because of varying degrees of crystallinity. The extent of crystallinity developed in a polymer sample is a consequence of both thermodynamic and kinetic factors. In this discussion we will note the general tendency to crystallize under moderate crystallization conditions (that is, conditions that exclude extremes of time, temperature, and pressure). Thermodynamically crystallizable polymers generally must crystallize at reasonable rates if crystallinity is to be employed from a practical viewpoint. The extent to which a polymer crystallizes depends on whether its structure is conducive to packing into the crystalline state and on the magnitude of the secondary attractive forces of the polymer chains. Packing is facilitated for polymer chains that have structural regularity, compactness, streamlining, and some degree of flexibility. The stronger the secondary attractive forces, the greater will be the driving force for the ordering and crystallization of polymer chains.

Some polymers are highly crystalline primarily because their structure is conducive to packing, while others are crystalline primarily because of strong secondary attractive forces. For still other polymers both factors may be favorable for crystallization. Polyethylene, for example, has essentially the best structure in terms of its ability to pack into the crystalline state. Its very simple and perfectly regular structure allows chains to pack tightly and without any restrictions as to which segment of one chain need line up next to which other segment of the same chain or of another chain. The flexibility of the polyethylene chains is also conducive to crystallization in that the conformations required for packing can be easily achieved. Even though its secondary attractive forces are small, polyethylene crystallizes easily and to a high degree because of its simple and regular structure.

Polymers other than polyethylene have less simple and regular chains. Poly(ε-caprolactam) can be considered as a modified polyethylene chain containing the amide group in between every five methylenes. Poly(ε-caprolactam) and other polyamides are highly crystalline polymers. The amide group is a polar one and leads to much larger secondary attractive forces in polyamides (due to hydrogen bonding) compared to polyethylene; this is most favorable for crystallization. However, the polyamide chains are not as simple as those of polyethylene and packing requires that chain segments be brought together so that the amide groups are aligned. This restriction leads to a somewhat lessened degree of crystallization in polyamides than expected, based only on a consideration of the high secondary attractive forces. Crystallinity in a polymer such as a polyamide can be significantly increased by mechanically stretching it to facilitate the ordering and alignment of polymer chains.

Polymers such as polystyrene, poly(vinyl chloride), and poly(methyl methacrylate) show very poor crystallization tendencies. Loss of structural simplicity (compared to polyethylene) results in a marked decrease in the tendency toward crystallization. Fluorocarbon polymers such as poly(vinyl fluoride), poly(vinylidene fluoride), and polytetrafluoroethylene are exceptions. These polymers show considerable crystallinity since the small size of fluorine does not preclude packing into a crystal lattice. Crystallization is also aided by the high secondary attractive forces. High secondary attractive forces coupled with symmetry account for the presence of significant crystallinity in poly(vinylidene chloride). Symmetry alone without significant polarity, as in polyisobutylene, is insufficient for the development of crystallinity. (The effect of stereoregularity of polymer structure on crystallinity is postponed to Sec. 8-2a.)

Polymers with rigid, cyclic structures in the polymer chain, as in cellulose and poly(ethylene terephthalate), are difficult to crystallize. Moderate crystallization does occur in these cases, as a result of the polar polymer chains. Additional crystallization can be induced by mechanical stretching. Cellulose is interesting in that native cellulose in the form of cotton is much more crystalline than cellulose that is obtained by precipitation of cellulose from...
solution (Sec. 9-3a). The biosynthesis of cotton proceeds with an enzymatic ordering of the polymer chains in spite of the rigid polymer chains. Excess chain rigidity in polymers due to extensive crosslinking, as in phenol–formaldehyde and urea–formaldehyde polymers, completely prevents crystallization.

Chain flexibility also affects the ability of a polymer to crystallize. Excessive flexibility in a polymer chain as in polysiloxanes and natural rubber leads to an inability of the chains to pack. The chain conformations required for packing cannot be maintained because of the high flexibility of the chains. The flexibility in the cases of the polysiloxanes and natural rubber is due to the bulky Si—O and cis-olefin groups, respectively. Such polymers remain as almost completely amorphous materials, which, however, show the important property of elastic behavior.

1-5c Thermal Transitions

Polymeric materials are characterized by two major types of transition temperatures—the crystalline melting temperature $T_m$ and the glass transition temperature $T_g$. The crystalline melting temperature is the melting temperature of the crystalline domains of a polymer sample. The glass transition temperature is the temperature at which the amorphous domains of a polymer take on the characteristic properties of the glassy state—brittleness, stiffness, and rigidity. The difference between the two thermal transitions can be understood more clearly by considering the changes that occur in a liquid polymer as it is cooled. The translational, rotational, and vibrational energies of the polymer molecules decrease on cooling. When the total energies of the molecules have fallen to the point where the translational and rotational energies are essentially zero, crystallization is possible. If certain symmetry requirements are met, the molecules are able to pack into an ordered, lattice arrangement and crystallization occurs. The temperature at which this occurs is $T_m$. However, not all polymers meet the necessary symmetry requirements for crystallization. If the symmetry requirements are not met, crystallization does not take place, but the energies of the molecules continue to decrease as the temperature decreases. A temperature is finally reached—the $T_g$—at which long-range motions of the polymer chains stop. Long-range motion, also referred to as segmental motion, refers to the motion of a segment of a polymer chain by the concerted rotation of bonds at the ends of the segment. [Bond rotations about side chains, e.g., the C—CH$_3$ and C—COOCH$_3$ bonds in poly(methyl methacrylate), do not cease at $T_g$.]

Whether a polymer sample exhibits both thermal transitions or only one depends on its morphology. Completely amorphous polymers show only a $T_g$. A completely crystalline polymer shows only a $T_m$. Semicrystalline polymers exhibit both the crystalline melting and glass transition temperatures. Changes in properties such as specific volume and heat capacity occur as a polymer undergoes each of the thermal transitions. Figure 1-9 shows the changes in specific volume with temperature for completely amorphous and completely crystalline polymers (the solid lined plots). $T_m$ is a first-order transition with a discontinuous change in the specific volume at the transition temperature. $T_g$ is a second-order transition involving only a change in the temperature coefficient of the specific volume. (A plot of the temperature coefficient of the specific volume versus temperature shows a discontinuity.) The corresponding plot for a semicrystalline polymer consists of the plot for the crystalline polymer plus the dotted portion corresponding to the glass transition. A variety of methods have been used to determine $T_g$ and $T_m$, including dilatometry (specific volume), thermal analysis, dynamic mechanical behavior, dielectric loss, and broad-line NMR. The most commonly used method is differential scanning calorimetry (DSC). DSC reflects the change in heat capacity of a sample as a function of temperature by measuring the heat flow required to
maintain a zero temperature differential between an inert reference material and the polymer sample.

The melting of a polymer takes place over a wider temperature range than that observed for small organic molecules such as benzoic acid, due to the presence of different-sized crystalline regions and the more complicated process for melting of large molecules. $T_m$, generally reported as the temperature for the onset of melting, is determined as the intersection from extrapolation of the two linear regions of Fig. 1-9 (before and after the onset). $T_g$ also occurs over a wide temperature range and is determined by extrapolation of the two linear regions, before and after $T_g$. The glass transition is a less well understood process than melting. There are indications that it is at least partially a kinetic phenomenon. The experimentally determined value of $T_g$ varies significantly with the timescale of the measurement. Faster cooling rates result in higher $T_g$ values. Further, significant densification still takes place below $T_g$ with the amount dependent on the cooling rate. Perhaps the best visualization of $T_g$ involves the existence of a modest range of temperatures at which there is cessation of segmental motion for polymer chain segments of different lengths (~5–20 chain atoms).

Some polymers undergo other thermal transitions in addition to $T_g$ and $T_m$. These include crystal–crystal transitions (i.e., transition from one crystalline form to another and crystalline-liquid crystal transitions.

The values of $T_g$ and $T_m$ for a polymer affect its mechanical properties at any particular temperature and determine the temperature range in which that polymer can be employed. The $T_g$ and $T_m$ values for some of the common polymers are shown in Table 1–3 [Brandrup et al., 1999; Mark, 1999]. (These are the values at 1 atm pressure.) Consider the manner in
which $T_g$ and $T_m$ vary from one polymer to another. One can discuss the two transitions simultaneously since both are affected similarly by considerations of polymer structure. Polymers with low $T_g$ values usually have low $T_m$ values; high $T_g$ and high $T_m$ values are usually found together. Polymer chains that do not easily undergo bond rotation so as to pass through the glass transition would also be expected to melt with difficulty. This is reasonable, since similar considerations of polymer structure are operating in both instances.

The two thermal transitions are generally affected in the same manner by the molecular symmetry, structural rigidity, and secondary attractive forces of polymer chains [Billmeyer, 1984; Mark et al., 1993; Sperling, 2001]. High secondary forces (due to high polarity or hydrogen bonding) lead to strong crystalline forces requiring high temperatures for melting. High secondary attractive forces also decrease the mobility of amorphous polymer chains, leading to

<table>
<thead>
<tr>
<th>Polymer</th>
<th>Repeating Unit</th>
<th>$T_g$ (°C)</th>
<th>$T_m$ (°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Polydimethylsiloxane</td>
<td>$-\text{OSi(CH}_3\text{)}_2-$</td>
<td>-127</td>
<td>-40</td>
</tr>
<tr>
<td>Polyethylene</td>
<td>$-\text{CH}_2\text{CH}_2-$</td>
<td>-125</td>
<td>137</td>
</tr>
<tr>
<td>Polyoxymethylene</td>
<td>$-\text{CH}_2\text{O}-$</td>
<td>-83</td>
<td>181</td>
</tr>
<tr>
<td>Natural rubber (polysoprene)</td>
<td>$-\text{CH}_2\text{C(}\text{CH}_3\text{)}=\text{CHCH}_2-$</td>
<td>-73</td>
<td>28</td>
</tr>
<tr>
<td>Polyisobutylene</td>
<td>$-\text{CH}_2\text{C(}\text{CH}_3\text{)}_2-$</td>
<td>-73</td>
<td>44</td>
</tr>
<tr>
<td>Poly(ethylene oxide)</td>
<td>$-\text{CH}_2\text{CH}_2\text{O}-$</td>
<td>-53</td>
<td>66</td>
</tr>
<tr>
<td>Poly(vinylidene fluoride)</td>
<td>$-\text{CH}_2\text{CF}_2-$</td>
<td>-40</td>
<td>185</td>
</tr>
<tr>
<td>Polypropene</td>
<td>$-\text{CH}_2\text{CH(}\text{CH}_3\text{)}-$</td>
<td>-1</td>
<td>176</td>
</tr>
<tr>
<td>Poly(vinyl fluoride)</td>
<td>$-\text{CH}_2\text{CHF}-$</td>
<td>41</td>
<td>200</td>
</tr>
<tr>
<td>Poly(vinylidene chloride)</td>
<td>$=\text{CH}_2\text{CCl}_2-$</td>
<td>-18</td>
<td>200</td>
</tr>
<tr>
<td>Poly(vinyl acetate)</td>
<td>$-\text{CH}_2\text{CH(OCOCH}_3\text{)}-$</td>
<td>32</td>
<td></td>
</tr>
<tr>
<td>Poly(chlorotrifluoroethylene)</td>
<td>$-\text{CF}_2\text{CFCI}-$</td>
<td></td>
<td>220</td>
</tr>
<tr>
<td>Poly(ε-caprolactam)</td>
<td>$-\text{(CH}_3\text{)}_3\text{CONH}-$</td>
<td>40</td>
<td>223</td>
</tr>
<tr>
<td>Poly(hexamethylene adipamide)</td>
<td>$=\text{NH(CH}_2\text{)}_6\text{NHCO(CH}_2\text{)}_4\text{CO}-$</td>
<td>50</td>
<td>265</td>
</tr>
<tr>
<td>Poly(ethylene terephthalate)</td>
<td>$-\text{OCH}_2\text{CH}_2\text{OCO}$</td>
<td>61</td>
<td>270</td>
</tr>
<tr>
<td>Poly(vinyl chloride)</td>
<td>$-\text{CH}_2\text{CHCl}-$</td>
<td>81</td>
<td>273</td>
</tr>
<tr>
<td>Polystyrene</td>
<td>$-\text{CH}_2\text{CHβ}-$</td>
<td>100</td>
<td>250</td>
</tr>
<tr>
<td>Poly(methyl methacrylate)</td>
<td>$-\text{CH}_2\text{C(}\text{CH}_3\text{)}(\text{CO}_2\text{CH}_3\text{)}-$</td>
<td>105</td>
<td>220</td>
</tr>
<tr>
<td>Cellulose triacetate</td>
<td>$\text{CH}_2\text{OAc}$</td>
<td></td>
<td>306</td>
</tr>
<tr>
<td>Polytetrafluoroethylene</td>
<td>$-\text{CF}_2\text{CF}_2-$</td>
<td>117</td>
<td>327</td>
</tr>
</tbody>
</table>

aData from Brandrup et al. [1999].
high $T_g$. Decreased mobility of polymer chains, increased chain rigidity, and high $T_g$ are found where the chains are substituted with several substituents as in poly(methyl methacrylate) and polytetrafluoroethylene or with bulky substituents as in polystyrene. The $T_m$ values of crystalline polymers produced from such rigid chains would also be high. The effects of substituents are not always easy to understand. A comparison of poly(propene), poly(vinyl chloride), and poly(vinyl fluoride) with polyisobutylene, poly(vinylidene chloride), and poly(vinylidene fluoride), respectively, shows the polymers from 1,1-disubstituted ethylenes have lower $T_g$ and $T_m$ values than do those from the monosubstituted ethylenes. One might have predicted the opposite result because of the greater polarity and molecular symmetry of the polymers from 1,1-disubstituted ethylenes. Apparently, the presence of two side groups instead of one separates polymer chains from each other and results in more flexible polymer chains. Thus, the effects of substituents on $T_g$ and $T_m$ depend on their number and identity.

The rigidity of polymer chains is especially high when there are cyclic structures in the main polymer chains. Polymers such as cellulose have high $T_g$ and $T_m$ values. On the other hand, the highly flexible polysiloxane chain (a consequence of the large size of Si) results in very low values of $T_g$ and $T_m$.

Although $T_g$ and $T_m$ depend similarly on molecular structure, the variations in the two transition temperature do not always quantitative parallel each other. Table 1-3 shows the various polymers listed in order of increasing $T_g$ values. The $T_m$ values are seen to generally increase in the same order, but there are many polymers whose $T_m$ values do not follow in the same exact order. Molecular symmetry, chain rigidity, and secondary forces do not affect $T_g$ and $T_m$ in the same quantitative manner. Thus polyethylene and polyoxyethylene have low $T_g$ values because of their highly flexible chains; however, their simple and regular structures yield tightly packed crystal structures with high $T_m$ values. An empirical consideration of ratio $T_g/T_m$ (Kelvin temperatures) for various polymers aids this discussion. The $T_g/T_m$ ratio is approximately 1/2 for symmetric polymers [e.g., poly(vinylidene chloride)], but the ratio is closer to 3/4 for unsymmetric polymers (e.g., poly[vinyl chloride]). This result indicates that $T_m$ is more dependent on molecular symmetry, while $T_g$ is more dependent on secondary forces and chain flexibility.

It should be evident that some of the factors that decrease the crystallization tendency of a polymer also lead to increased values of $T_m$ (and also $T_g$). The reason for this is that the extent of crystallinity developed in a polymer is both kinetically and thermodynamically controlled, while the melting temperature is only thermodynamically controlled. Polymers with rigid chains are difficult or slow to crystallize, but the portion that does crystallize will have a high melting temperature. (The extent of crystallinity can be significantly increased in such polymers by mechanical stretching to align and crystallize the polymer chains.) Thus compare the differences between polyethylene and poly(hexamethylene adipamide). Polyethylene tends to crystallize easier and faster than the polyamide because of its simple and highly regular structure and is usually obtained with greater degrees of crystallinity. On the other hand, the $T_m$ of the polyamide is much higher (by ~130°C) than that of polyethylene because of the much greater secondary forces.

1-6 APPLICATIONS OF POLYMERS

1-6a Mechanical Properties

Many polymer properties such as solvent, chemical, and electrical resistance and gas permeability are important in determining the use of a specific polymer in a specific application. However, the prime consideration in determining the general utility of a polymer is its
mechanical behavior, that is, its deformation and flow characteristics under stress. The mechanical behavior of a polymer can be characterized by its stress–strain properties [Billmeyer, 1984; Nielsen and Landel, 1994]. This often involves observing the behavior of a polymer as one applies tension stress to it in order to elongate (strain) it to the point where it ruptures (pulls apart). The results are usually shown as a plot of the stress versus elongation (strain). The stress is usually expressed in newtons per square centimeter (N cm$^{-2}$) or megapascals (MPa) where 1 MPa = 100 N cm$^{-2}$. The strain is the fractional increase in the length of the polymer sample (i.e., $\Delta L/L$, where $L$ is the original, unstretched sample length). The strain can also be expressed as the percent elongation, $\Delta L/L \times 100\%$. Although N cm$^{-2}$ is the SI unit for stress, psi (pounds per square inch) is found extensively in the literature. The conversion factor is 1 N cm$^{-2}$ = 1.450 psi. SI units will be used throughout this text with other commonly used units also indicated.

Several stress–strain plots are shown in Fig. 1-10. Four important quantities characterize the stress–strain behavior of a polymer:

1. **Modulus.** The resistance to deformation as measured by the initial stress divided by $\Delta L/L$.

Fig. 1-10 Stress–strain plots for a typical elastomer, flexible plastic, rigid plastic, and fiber.
2. **Ultimate Strength or Tensile Strength.** The stress required to rupture the sample.

3. **Ultimate Elongation.** The extent of elongation at the point where the sample ruptures.

4. **Elastic Elongation.** The elasticity as measured by the extent of reversible elongation.

Polymers vary widely in their mechanical behavior depending on the degree of crystallinity, degree of crosslinking, and the values of $T_g$ and $T_m$. High strength and low extensibility are obtained in polymers by having various combinations of high degrees of crystallinity or crosslinking or rigid chains (characterized by high $T_g$). High extensibility and low strength in polymers are synonymous with low degrees of crystallinity and crosslinking and low $T_g$ values. The temperature limits of utility of a polymer are governed by its $T_g$ and/or $T_m$. Strength is lost at or near $T_g$ for an amorphous polymer and at or near $T_m$ for a crystalline polymer.

An almost infinite variety of polymeric materials can be produced. The polymer scientist must have an awareness of the properties desired in the final polymer in order to make a decision about the polymer to be synthesized. Different polymers are synthesized to yield various mechanical behaviors by the appropriate combinations of crystallinity, crosslinking, $T_g$, and $T_m$. Depending on the particular combination, a specific polymer will be used as a fiber, flexible plastic, rigid plastic, or elastomer (rubber). Commonly encountered articles that typify these uses of polymers are clothing and rope (fiber), packaging films and seat covers (flexible plastic), eyeglass lenses and housings for appliances (rigid plastic), and rubber bands and tires (elastomer). Table 1-4 shows the uses of many of the common polymers. Some polymers are used in more than one category because certain mechanical properties can be manipulated by appropriate chemical or physical means, such as by altering the crystallinity or adding plasticizers (Sec. 3-14c-1) or copolymerization (Sec. 3-14b, Chap. 6). Some polymers are used as both plastics and fibers, other as both elastomers and plastics.

### Table 1-4 Use of Polymers

<table>
<thead>
<tr>
<th>Elastomers</th>
<th>Plastics</th>
<th>Fibers</th>
</tr>
</thead>
<tbody>
<tr>
<td>Polyisoprene</td>
<td>Polyethylene</td>
<td></td>
</tr>
<tr>
<td>Polyisobutylene</td>
<td>Polytetrafluoroethylene</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Poly(methyl methacrylate)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Phenol–formaldehyde</td>
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</tr>
<tr>
<td></td>
<td>Urea–formaldehyde</td>
<td></td>
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<tr>
<td></td>
<td>Melamine–formaldehyde</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Polystyrene</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Poly(vinyl chloride)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Polyurethane</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Polysiloxane</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Polyanilide</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Polyacrylonitrile</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Polyethylene</td>
<td></td>
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<td></td>
<td>Polyethylene</td>
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<td>Polyethylene</td>
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<tr>
<td></td>
<td>Polyethylene</td>
<td></td>
</tr>
</tbody>
</table>

An almost infinite variety of polymeric materials can be produced. The polymer scientist must have an awareness of the properties desired in the final polymer in order to make a decision about the polymer to be synthesized. Different polymers are synthesized to yield various mechanical behaviors by the appropriate combinations of crystallinity, crosslinking, $T_g$, and $T_m$. Depending on the particular combination, a specific polymer will be used as a fiber, flexible plastic, rigid plastic, or elastomer (rubber). Commonly encountered articles that typify these uses of polymers are clothing and rope (fiber), packaging films and seat covers (flexible plastic), eyeglass lenses and housings for appliances (rigid plastic), and rubber bands and tires (elastomer). Table 1-4 shows the uses of many of the common polymers. Some polymers are used in more than one category because certain mechanical properties can be manipulated by appropriate chemical or physical means, such as by altering the crystallinity or adding plasticizers (Sec. 3-14c-1) or copolymerization (Sec. 3-14b, Chap. 6). Some polymers are used as both plastics and fibers, other as both elastomers and plastics.
The differences between fibers, plastics, and elastomers can be seen in the stress–strain plots in Fig.1-10. The modulus of a polymer is the initial slope of such a plot; the tensile strength and ultimate elongation are the highest stress and elongation values, respectively. Elastomers are the group of polymers that can easily undergo very large, reversible elongations (≤ 500–1000%) at relatively low stresses. This requires that the polymer be completely (or almost completely) amorphous with a low glass transition temperature and low secondary forces so as to obtain high polymer chain mobility. Some degree of crosslinking is needed so that the deformation is rapidly and completely reversible (elastic). The initial modulus of an elastomer should be very low (<100 N cm⁻²), but this should increase fairly rapidly with increasing elongation; otherwise, it would have no overall strength and resistance to rupture at low strains. Most elastomers obtain the needed strength via crosslinking and the incorporation of reinforcing inorganic fillers (e.g., carbon black, silica). Some elastomers undergo a small amount of crystallization during elongation, especially at very high elongations, and this acts as an additional strengthening mechanism. The $T_m$ of the crystalline regions must be below or not significantly above the use temperature of the elastomer in order that the crystals melt and deformation be reversible when the stress is removed. Polyisoprene (natural rubber) is a typical elastomer—it is amorphous, is easily crosslinked, has a low $T_g$ (−73°C), and has a low $T_m$ (28°C). Crosslinked (moderately) polyisoprene has a modulus that is initially less than 70 N cm⁻²; however, its strength increases to about 1500 N cm⁻² at 400% elongation and about 2000 N cm⁻² at 500% elongation. Its elongation is reversible over the whole elongation range, that is, up to just prior to the rupture point. The extent of crosslinking and the resulting strength and elongation characteristics of an elastomer cover a considerable range depending on the specific end use. The use of an elastomer to produce an automobile tire requires much more crosslinking and reinforcing fillers than does the elastomer used for producing rubber bands. The former application requires a stronger rubber with less tendency to elongate than the latter application. Extensive crosslinking of a rubber converts the polymer to a rigid plastic.

Fibers are polymers that have very high resistance to deformation—they undergo only low elongations (<10–50%) and have very high moduli (>35,000 N cm⁻²) and tensile strengths (>35,000 N cm⁻²). A polymer must be very highly crystalline and contain polar chains with strong secondary forces in order to be useful as a fiber. Mechanical stretching is used to impart very high crystallinity to a fiber. The crystalline melting temperature of a fiber must be above 200°C so that it will maintain its physical integrity during the use temperatures encountered in cleaning and ironing. However, $T_m$ should not be excessively high—not higher than 300°C—otherwise, fabrication of the fiber by melt spinning may not be possible. The polymer should be soluble in solvents used for solution spinning of the fiber but not in dry-cleaning solvents. The glass transition temperature should have an intermediate value; too high a $T_g$ interferes with the stretching operation as well as with ironing, while too low a $T_g$ would not allow crease retention in fabrics. Poly(hexamethylene adipamide) is a typical fiber. It is stretched to high crystallinity, and its amide groups yield very strong secondary forces due to hydrogen bonding; the result is very high tensile strength (70,000 N cm⁻²), very high modulus (500,000 N cm⁻²), and low elongation (<20%). The $T_m$ and $T_g$ have optimal values of 265 and 50°C, respectively. [The use of polypropene as a fiber is an exception to the generalization that polar polymers are required for fiber applications. The polypropene used as a fiber has a highly stereoregular structure and can be mechanically stretched to yield a highly oriented polymer with the strength characteristics required of a fiber (see Sec. 8-11d).]
Plastics represent a large group of polymers that have a wide range of mechanical behaviors in between those of the elastomers and fibers. There are two types of plastics—flexible plastics and rigid plastics. The flexible plastics possess moderate to high degrees of crystallinity and a wide range of $T_m$ and $T_g$ values. They have moderate to high moduli ($15,000–350,000 \text{ N cm}^{-2}$), tensile strengths ($1500–7000 \text{ N cm}^{-2}$), and ultimate elongations (20–800%). The more typical members of this subgroup have moduli and tensile strengths in the low ends of the indicated ranges with elongations in the high end. Thus polyethylene is a typical flexible plastic with a tensile strength of 2500 N cm$^{-2}$, a modulus of 20,000 N cm$^{-2}$, and an ultimate elongation of 500%. Other flexible plastics include polypropene and poly(hexamethylene adipamide). Poly(hexamethylene adipamide) is used as both a fiber and a flexible plastic. It is a plastic when it has moderate crystallinity, while stretching converts it into a fiber. Many flexible plastics undergo large ultimate elongations—some as large as those of elastomers. However, they differ from elastomers in that only a small portion (approximately <20%) of the ultimate elongation is reversible. The elongation of a plastic past the reversible region results in its permanent deformation, that is, the plastic will retain its elongated shape when the stress is removed.

The rigid plastics are quite different from the flexible plastics. The rigid plastics are characterized by high rigidity and high resistance to deformation. They have high moduli (70,000–350,000 N cm$^{-2}$) and moderate to high tensile strengths (3000–8500 N cm$^{-2}$), but more significantly, they undergo very small elongations (<0.5–3%) before rupturing. The polymers in this category are amorphous polymers with very rigid chains. The high chain rigidity is achieved in some cases by extensive crosslinking, for example, phenol–formaldehyde, urea–formaldehyde, and melamine–formaldehyde polymers. In other polymers the high rigidity is due to bulky side groups on the polymer chains resulting in high $T_g$ values, for example, polystyrene ($T_g = 100\degree C$) and poly(methyl methacrylate) ($T_g = 105\degree C$).

**REFERENCES**


**PROBLEMS**

1-1 Show by equations the overall chemical reactions involved in the synthesis of polymers from

a. CH$_2$=CH$\rightarrow$CO$_2$H

b. O

c. H$_2$N$\rightarrow$(CH$_2$)$_5$NH$_2$ + ClCO$\rightarrow$(CH$_2$)$_5$COCl

d. HO$\rightarrow$(CH$_2$)$_5$CO$_2$H

e. CH$_3$\[NCO \rightarrow \text{NCO} + \text{HO-CH$_2$CH$_2$-OH}

f. CH$_2$=CH$\rightarrow$F

1-2 What is the structure of the repeating unit in each of the polymers in Problem 1-1? Can any other monomer(s) be used to obtain the same polymer structure for any of these polymer?

1-3 Classify the polymers as to whether they are condensation or addition polymers. Classify the polymerizations as to whether they are step, chain, or ring-opening polymerizations.

1-4 How would you experimentally determine whether the polymerization of an unknown monomer X was proceeding by a step or a chain mechanism?

1-5 Name each of the polymers in Problem 1-1 by the IUPAC system. Indicate alternate names where applicable based on the polymer source, non-IUPAC structure system, or trade names.

1-6 Name each of the following polymers by the IUPAC system

a. \(\left\{\text{OCH}\right\}_n\)

\[\text{CH}_2\text{COOCH}_3\]
A sample of polystyrene is composed of a series of fractions of different-sized molecules:

<table>
<thead>
<tr>
<th>Fraction</th>
<th>Weight Fraction</th>
<th>Molecular Weight</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>0.10</td>
<td>12,000</td>
</tr>
<tr>
<td>B</td>
<td>0.19</td>
<td>21,000</td>
</tr>
<tr>
<td>C</td>
<td>0.24</td>
<td>35,000</td>
</tr>
<tr>
<td>D</td>
<td>0.18</td>
<td>49,000</td>
</tr>
<tr>
<td>E</td>
<td>0.11</td>
<td>73,000</td>
</tr>
<tr>
<td>F</td>
<td>0.08</td>
<td>102,000</td>
</tr>
<tr>
<td>G</td>
<td>0.06</td>
<td>122,000</td>
</tr>
<tr>
<td>H</td>
<td>0.04</td>
<td>146,000</td>
</tr>
</tbody>
</table>

Calculate the number-average and weight-average molecular weights of this polymer sample. Draw a molecular weight distribution curve analogous to Fig. 1-4.

1-8 Indicate how the extent of polymer crystallinity is affected by chemical structure.

1-9 Define $T_m$ and $T_g$ and indicate how they are affected by chemical structure.

1-10 Describe the differences in the properties and uses of flexible plastics, rigid plastics, fibers, and elastomers. What types of chemical structures are typical of each?
CHAPTER 2

STEP POLYMERIZATION

Many of the common condensation polymers are listed in Table 1-1. In all instances the polymerization reactions shown are those proceeding by the step polymerization mechanism. This chapter will consider the characteristics of step polymerization in detail. The synthesis of condensation polymers by ring-opening polymerization will be subsequently treated in Chap. 7. A number of different chemical reactions may be used to synthesize polymeric materials by step polymerization. These include esterification, amidation, the formation of urethanes, aromatic substitution, and others. Polymerization usually proceeds by the reactions between two different functional groups, for example, hydroxyl and carboxyl groups, or isocyanate and hydroxyl groups.

All step polymerizations fall into two groups depending on the type of monomer(s) employed. The first involves two different bifunctional and/or polyfunctional monomers in which each monomer possesses only one type of functional group. (A polyfunctional monomer is a monomer with more than one functional group per molecule. A bifunctional monomer is one with two functional groups per molecule.) The second involves a single monomer containing both types of functional groups. The synthesis of polyamides illustrates both groups of polymerization reactions. Thus polyamides can be obtained from the reaction of diamines with diacids

\[
\begin{align*}
nH_2N-R-NH_2 + nHOOCC-R'-CO_2H & \rightarrow \\
H \rightarrow N\rightarrow H-NHCO-R'-CO \rightarrow \underbrace{\text{OH}}_{n} + (2n-1)H_2O
\end{align*}
\]

(2-1a)

or from the reaction of amino acids with themselves:

\[
\begin{align*}
nH_2N-R-CO_2H & \rightarrow \\
H \rightarrow N\rightarrow H-R-CO \rightarrow \underbrace{\text{OH}}_{n} + (n-1)H_2O
\end{align*}
\]

(2-1b)
The two groups of reactions can be represented in a general manner by the equations

\[ nA-A + nB-B \rightarrow \underbrace{A-AB-B}_{n} \] \hspace{2cm} (2-2)

\[ nA-B \rightarrow \underbrace{A-B}_{n} \] \hspace{2cm} (2-3)

where A and B are the two different types of functional groups. The characteristics of these two polymerization reactions are very similar. The successful synthesis of high polymers (i.e., polymer of sufficiently high molecular weight to be useful from the practical viewpoint) using any step polymerization reaction generally is more difficult than the corresponding small molecule reaction, since high polymers can be achieved only at very high conversions (>98–99%). A conversion of 90%, which would be considered excellent for the synthesis of ethyl acetate or methyl benzamide, is a disaster for the synthesis of the corresponding polyester or polyamide. The need for very high conversions to synthesize high polymer places several stringent requirements on any reaction to be used for polymerization—a favorable equilibrium and the absence of cyclization and other side reactions. These stringent requirements are met by a relatively small fraction of the reactions familiar to and used by chemists to synthesize small molecules. An additional requirement for achieving high molecular weights is the need for the A and B functional groups to be be present at very close to stoichiometric amounts.

### 2-1 Reactivity of Functional Groups

#### 2-1a Basis for Analysis of Polymerization Kinetics

The kinetics of polymerization are of prime interest from two viewpoints. The practical synthesis of high polymers requires a knowledge of the kinetics of the polymerization reaction. From the theoretical viewpoint the significant differences between step and chain polymerizations reside in large part in their respective kinetic features.

Step polymerization proceeds by a relatively slow increase in molecular weight of the polymer. Consider the synthesis of a polyester from a diol and a diacid. The first step is the reaction of the diol and diacid monomers to form dimer:

\[ \text{HO-}R\text{-OH} + \text{HO}_2\text{C-}R'-\text{CO}_2\text{H} \rightarrow \text{HO-}R\text{-OCO-}R'-\text{CO}_2\text{H} + \text{H}_2\text{O} \] \hspace{2cm} (2-4)

The dimer then forms trimer by reaction with diol monomer

\[ \text{HO-}R\text{-OCO-}R'-\text{CO}_2\text{H} + \text{HO-}R\text{-OH} \rightarrow \text{HO-}R\text{-OCO-}R'-\text{CO}_2\text{H} + \text{H}_2\text{O} \] \hspace{2cm} (2-5)

and also with diacid monomer:

\[ \text{HO-}R\text{-OCO-}R'-\text{CO}_2\text{H} + \text{HO}_2\text{C-}R'-\text{CO}_2\text{H} \rightarrow \text{HO}_2\text{C-}R'-\text{COO-}R\text{-OCO-}R'-\text{CO}_2\text{H} + \text{H}_2\text{O} \] \hspace{2cm} (2-6)

Dimer reacts with itself to form tetramer:

\[ 2\text{HO-}R\text{-OCO-}R'-\text{CO}_2\text{H} \rightarrow \text{HO-}R\text{-OCO-}R'-\text{COO-}R\text{-OCO-}R'-\text{CO}_2\text{H} + \text{H}_2\text{O} \] \hspace{2cm} (2-7)
The tetramer and trimer proceed to react with themselves, with each other, and with monomer and dimer. The polymerization proceeds in this stepwise manner with the molecular weight of the polymer continuously increasing with time (conversion). Step polymerizations are characterized by the disappearance of monomer early in the reaction far before the production of any polymer of sufficiently high molecular weight (approximately $>5000$–$10,000$) to be of practical utility. Thus for most step polymerizations there is less than 1% of the original monomer remaining at a point where the average polymer chain contains only $\sim10$ monomer units. As will be seen in Chap. 3, the situation is quite different in the case of chain polymerization.

The rate of a step polymerization is, therefore, the sum of the rates of reaction between molecules of various sizes, that is, the sum of the rates for reactions such as

\[
\text{Monomer} + \text{monomer} \rightarrow \text{dimer} \\
\text{Dimer} + \text{monomer} \rightarrow \text{trimer} \\
\text{Dimer} + \text{dimer} \rightarrow \text{tetramer} \\
\text{Trimer} + \text{monomer} \rightarrow \text{tetramer} \\
\text{Trimer} + \text{dimer} \rightarrow \text{pentamer} \\
\text{Trimer} + \text{trimer} \rightarrow \text{hexamer} \\
\text{Tetramer} + \text{monomer} \rightarrow \text{pentamer} \\
\text{Tetramer} + \text{dimer} \rightarrow \text{hexamer} \\
\text{Tetramer} + \text{trimer} \rightarrow \text{heptamer} \\
\text{Tetramer} + \text{tetrimer} \rightarrow \text{octamer} \\
\text{Pentamer} + \text{trimer} \rightarrow \text{octamer} \\
\text{Pentamer} + \text{tetrimer} \rightarrow \text{nonamer}
\]

which can be expressed as the general reaction

\[
\text{n-mer} + \text{m-mer} \rightarrow (\text{n + m})\text{-mer}
\]

The reaction mixture at any instance consists of various-sized diol, diacid, and hydroxy acid molecules. Any HO-containing molecule can react with any COOH-containing molecule. This is a general characteristic of step polymerization.

The kinetics of such a situation with innumerable separate reactions would normally be difficult to analyze. However, kinetic analysis is greatly simplified if one assumes that the reactivities of both functional groups of a bifunctional monomer (e.g., both hydroxyls of a diol) are the same, the reactivity of one functional group of a bifunctional reactant is the same irrespective of whether the other functional group has reacted, and the reactivity of a functional group is independent of the size of the molecule to which it is attached (i.e., independent of the values of $n$ and $m$). These simplifying assumptions, often referred to as the concept of equal reactivity of functional groups, make the kinetics of step polymerization identical to those for the analogous small molecule reaction. As will be seen shortly, the kinetics of a polyesterification, for example, become essentially the same as that for the esterification of acetic acid with ethanol.

### 2-1b Experimental Evidence

These simplifying assumptions are justified on the basis that many step polymerizations have reaction rate constants that are independent of the reaction time or polymer molecular
weight. It is, however, useful to examine in more detail the experimental and theoretical justifications for these assumptions. Studies of the reactions of certain nonpolymeric molecules are especially useful for understanding polymerization kinetics [Flory, 1953]. The independence of the reactivity of a functional group on molecular size can be observed from the reaction rates in a homologous series of compounds differing from each other only in molecular weight. Consider, for example, the rate constant data in the first column in Table 2-1 for the esterification of a series of homologous carboxylic acids [Bhide and Sudborough, 1925]:

\[
H(CH_2)_xCO_2H + CH_3CH_2OH + HCl \rightarrow H(CH_2)_xCO_2CH_3 + H_2O
\]

(2-9)

It is evident that, although there is a decrease in reactivity with increased molecular size, the effect is significant only at a very small size. The reaction rate constant very quickly reaches a limiting value at \(x = 3\), which remains constant and independent of molecular size. Analogous results are found for the polyesterification of sebacoyl chloride with \(\alpha,\omega\)-alkane diols [Ueberreiter and Engel, 1977]:

\[
HO(CH_2)_xOH + ClOC(CH_2)_nCOCl \rightarrow HCl \rightarrow O(CH_2)_xOOC(CH_2)_nCO
\]

(2-10)

The rate constant for esterification is independent of \(x\) for the compounds studied (Table 2-2). Examples of similar behavior can be found for other reactions [Rand et al., 1965]. The results for sebacoyl chloride offer direct evidence of the concept of functional group reactivity being independent of molecular size, since the rate constant is independent of \(n\) as well as \(x\).

The independence of functional group reactivity of molecular size is contrary to the general impression that was widely held in the early years of polymer science. There was a general misconception of decreased reactivity with increased molecular size. This was due

<table>
<thead>
<tr>
<th>Molecular Size ((x))</th>
<th>(k \times 10^4) for</th>
<th>(k \times 10^4) for</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(H(CH_2)_xCO_2H)</td>
<td>((CH_2)_x(CO_2H)_2)</td>
</tr>
<tr>
<td>1</td>
<td>22.1</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>15.3</td>
<td>6.0</td>
</tr>
<tr>
<td>3</td>
<td>7.5</td>
<td>8.7</td>
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<td>7.8</td>
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<td>7.3</td>
</tr>
<tr>
<td>8</td>
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<tr>
<td>9</td>
<td>7.4</td>
<td></td>
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<tr>
<td>11</td>
<td>7.6</td>
<td></td>
</tr>
<tr>
<td>13</td>
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<td></td>
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<tr>
<td>15</td>
<td>7.7</td>
<td></td>
</tr>
<tr>
<td>17</td>
<td>7.7</td>
<td></td>
</tr>
</tbody>
</table>

*Rate constants are in units of L mol\(^{-1}\) s\(^{-1}\).

Data from Bhide and Sudborough [1925].
in large part to the fact that reactions with the larger-sized species were often attempted without adjusting concentrations so as to have equivalent concentrations of the reacting functional groups. In many instances the low or difficult solubility of the higher-molecular-weight reactants in a homologous series was responsible for the observed, apparent low reactivity. These effects are still pitfalls to be avoided.

2-1c Theoretical Considerations

There is theoretical justification for the independence of the reactivity of a functional group of molecular size [Rabinowitch, 1937]. The common misconception regarding the alleged low reactivity of groups attached to large molecules comes from the lower diffusion rates of the latter. However, the observed reactivity of a functional group is dependent on the collision frequency of the group, not on the diffusion rate of the whole molecule. The collision frequency is the number of collisions one functional group makes with other functional groups per unit of time. A terminal functional group attached to a growing polymer has a much greater mobility than would be expected from the mobility of the polymer molecule as a whole. The functional group has appreciable mobility due to the conformational rearrangements that occur in nearby segments of the polymer chain. The collision rate of such a functional group with neighboring groups will be about the same as for small molecules.

The lowered mobility of the polymer molecule as a whole alters the time distribution of collisions. A lower diffusion rate means that any two functional groups will undergo more total collisions before diffusing apart. Thus in any particular time interval (which is long compared to the interval required for diffusion of a group from one collision partner to the next) the number of partners with which a functional group undergoes collisions is less for a group attached to a polymer chain than for one attached to a small molecule. But, most significantly, their overall collision frequencies are the same in the two cases. If the diffusion of a functional group from one collision partner to the next were too slow to maintain the concentration of the reactive pairs of functional groups at equilibrium, one would observe decreased reactivity for the functional group. The opposite is the case, since reaction between two functional groups in a step polymerization occurs only about once in every $10^{13}$ collisions [Flory, 1953]. During the time interval required for this many collisions, sufficient diffusion of the molecule and of the functional group occurs to maintain the equilibrium concentration of collision pairs of functional groups. The net result of these

<table>
<thead>
<tr>
<th>Molecular Size ($x$)</th>
<th>$k \times 10^3$ for HO(CH$_2$)$_x$OH</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>0.60</td>
</tr>
<tr>
<td>6</td>
<td>0.63</td>
</tr>
<tr>
<td>7</td>
<td>0.65</td>
</tr>
<tr>
<td>8</td>
<td>0.62</td>
</tr>
<tr>
<td>9</td>
<td>0.65</td>
</tr>
<tr>
<td>10</td>
<td>0.62</td>
</tr>
</tbody>
</table>

$^a$ Rate constants are in units of L mol$^{-1}$ s$^{-1}$.

$^b$ Data from Ueberreiter and Engel [1977].
considerations is that the reactivity of a functional group will be independent of the size of the molecule to which it is attached. Exceptions to this occur when the reactivities of the groups are very high and/or the molecular weights of the polymer are very high. The polymerization becomes diffusion-controlled in these cases because mobility is too low to allow maintenance of the equilibrium concentration of reactive pairs and of their collision frequencies.

2-1d Equivalence of Groups in Bifunctional Reactants

The equivalence of the reactivities of the two functional groups in bifunctional reactants has also been demonstrated in many systems. The second column in Table 2-1 shows data for the esterification of a homologous series of dibasic acids:

\[
\begin{align*}
\text{H}_2\text{C}-(\text{CH}_2)_x\text{CO}_2\text{H} + 2\text{C}_2\text{H}_5\text{OH} & \rightarrow \\
\text{C}_2\text{H}_4\text{O}_2\text{C}-(\text{CH}_2)_x\text{CO}_2\text{C}_2\text{H}_5 + 2\text{H}_2\text{O}
\end{align*}
\]

The rate constants tabulated are the averages of those for the two carboxyl groups in each dibasic acid. The rate constants for the two carboxyls were the same within experimental error. Further, a very important observation is that the reactivity of one of the functional groups is not dependent on whether the other has reacted. As in the case of the monocarboxylic acids, the reactivity of the carboxyl group quickly reaches a limiting value. Similar results were observed for the polyesterification of sebacoyl chloride (Table 2-2).

It should not be concluded that the reactivity of a functional group is not altered by the presence of a second group. The data show that at small values of \(x\) up to 4 or 5, there is an effect of the second group. In most instances the effect disappears fairly rapidly with increasing molecular size as the two functional groups become isolated from each other. Thus the rate constant for the esterification of the dibasic acid with \(x = 6\) is the same as that for the monobasic acids. It might appear at first glance that polymerizations involving bifunctional reagents with low \(x\) values would present a problem. However, the difference in reactivities of the functional groups of a bifunctional reagent compared to the functional group in a monofunctional reagent is not an important consideration in handling the kinetics of step polymerization. The most significant considerations are that the reactivity of a functional group in a bifunctional monomer is not altered by the reaction of the other group, and that the reactivities of the two functional groups are the same and do not change during the course of the polymerization.

2-2 KINETICS OF STEP POLYMERIZATION

Consider the polyesterification of a diacid and a diol to illustrate the general form of the kinetics of a typical step polymerization. Simple esterification is a well-known acid-catalyzed reaction and polyesterification follows the same course [Otton and Ratton, 1988; Vancso-Szmercsanyi and Makay-Bodi, 1969]. The reaction involves protonation of the carboxylic acid,

\[
\begin{align*}
\text{O} & \quad \text{C}^-\text{OH} + \text{HA} \xrightarrow{k_1} \text{C}^-\text{OH}(A^-) \\
& \quad \text{HA} \xrightarrow{k_2} \text{C}^-\text{OH} + \\
\end{align*}
\]

(2-12)
followed by reaction of the protonated species I with the alcohol to yield the ester

\[
\begin{align*}
\text{OH} & \quad \text{C}^- \text{OH} + \text{OH} \quad (A^-) \quad \xrightleftharpoons{\kappa_3} \quad \text{OH} \quad \text{C}^- \text{OH} + \text{OH} \quad (A^-) \\
\text{OH} & \quad \text{C}^- \text{OH} \quad \xrightarrow{\kappa_4} \quad \text{OH} \\
\end{align*}
\]

(2-13)

\[
\begin{align*}
\text{OH} & \quad \text{C}^- \text{OH} \quad \xrightleftharpoons{\kappa_5} \quad \text{O} \quad \text{C}^- \text{O}\text{OH} + \text{H}_2\text{O} + \text{HA} \\
\text{OH} & \quad \text{C}^- \text{OH} \quad (A^-) \\
\end{align*}
\]

(2-14)

In the above equations \(~\) and \(~\) are used to indicate all acid or alcohol species in the reaction mixture (i.e., monomer, dimer, trimer, \ldots, \textit{n}-mer). Species I and II are shown in the form of their associated ion pairs since polymerization often takes place in organic media of low polarity. (\(A^-\)) is the negative counterion derived from the acid HA. Polyesterifications, like many other step polymerizations, are equilibrium reactions. However, from the practical viewpoint of obtaining high yields of high-molecular-weight product such polymerizations are run in a manner so as to continuously shift the equilibrium in the direction of the polymer. In the case of a polyesterification this is easily accomplished by removal of the water that is a by-product of the reaction species II (Eq. 2-14). Under these conditions the kinetics of polymerization can be handled by considering the reactions in Eqs. 2-13 and 2-14 to be irreversible. (A consideration of the kinetics of a reversible step polymerization is given in Sec. 2-4c.)

The rate of a step polymerization is conveniently expressed in terms of the concentrations of the reacting functional groups. Thus the polyesterification can be experimentally followed by titrating for the unreacted carboxyl groups with a base. The \textit{rate of polymerization} \(R_p\) can then be expressed as the \textit{rate of disappearance of carboxyl groups} \(-d[\text{COOH}]/dt\). For the usual polyesterification, the polymerization rate is synonymous with the rate of formation of species II; that is, \(k_4\) is vanishingly small (since the reaction is run under conditions that drive Eqs. 2-13 and 2-14 to the right), and \(k_1, k_2,\) and \(k_5\) are large compared to \(k_3\).

An expression for the reaction rate can be obtained following the general procedures for handling a reaction scheme with the characteristics described [Moore and Pearson, 1981]. The rate of polymerization is given by

\[
R = \frac{-d[\text{COOH}]}{dt} = k_3[\text{C} (\text{OH})_2][\text{OH}] \\
\]

(2-15)

where \([\text{COOH}], [\text{OH}],\) and \([\text{C}(\text{OH})_2]\) represent the concentrations of carboxyl, hydroxyl, and protonated carboxyl (I) groups, respectively. The concentration terms are in units of moles of the particular functional group per liter of solution.

Equation 2-15 is inconvenient in that the concentration of protonated carboxylic groups is not easily determined experimentally. One can obtain a more convenient expression for \(R_p\) by substituting for \(\text{C}(\text{OH})_2\) from the equilibrium expression

\[
K = \frac{k_1}{k_2} = \frac{[\text{C} (\text{OH})_2]}{[\text{COOH}][\text{HA}]} \\
\]

(2-16)
for the protonation reaction (Eq. 2-12). Combination of Eqs. 2-15 and 2-16 yields

$$\frac{-d[\text{COOH}]}{dt} = k_3 K [\text{COOH}][\text{OH}][\text{HA}]$$

(2-17)

Two quite different kinetic situations arise from Eq. 2-17 depending on the identity of HA, that is, on whether a strong acid such as sulfuric acid or p-toluenesulfonic acid is added as an external catalyst.

### 2-2a Self-Catalyzed Polymerization

In the absence of an externally added strong acid the diacid monomer acts as its own catalyst for the esterification reaction. For this case [HA] is replaced by [COOH] and Eq. 2-17 can be written in the usual form [Flory, 1953]

$$\frac{-d[\text{COOH}]}{dt} = k [\text{COOH}]^2 [\text{OH}]$$

(2-18)

where $K$ and $k_3$ have been combined into the experimentally determined rate constant $k$. Equation 2-18 shows the important characteristic of the self-catalyzed polymerization—the reaction is third-order overall with a second-order dependence on the carboxyl concentration. The second-order dependence on the carboxyl concentration is comprised of two first-order dependencies—one for the carboxyl as the reactant and one as the catalyst.

For most polymerizations the concentrations of the two functional groups are very nearly stoichiometric, and Eq. 2-18 can be written as

$$\frac{-d[M]}{dt} = k[M]^3$$

(2-19a)

or

$$\frac{-d[M]}{[M]^3} = k \, dt$$

(2-19b)

where $[M]$ is the concentration of hydroxyl groups or carboxyl groups. Integration of Eq. 2-19b yields

$$2kt = \frac{1}{[M]^2} - \frac{1}{[M]^2_0}$$

(2-20)

where $[M]_0$ is the initial (at $t = 0$) concentration of hydroxyl or carboxyl groups. It is convenient at this point to write Eq. 2-20 in terms of the extent or fraction of reaction $p$ defined as the fraction of the hydroxyl or carboxyl functional groups that has reacted at time $t$. $p$ is also referred to as the extent or fraction of conversion. (The value of $p$ is calculated from a determination of the amount of unreacted carboxyl groups.) The concentration $[M]$ at time $t$ of either hydroxyl or carboxyl groups is then given by

$$[M] = [M]_0 - [M]_0 p = [M]_0 (1 - p)$$

(2-21)
Combination of Eqs. 2-20 and 2-21 yields

\[
\frac{1}{(1-p)^2} = 2|M_0|^2 kt + 1
\]  

(2-22)

### 2-2a-1 Experimental Observations

Equation 2-22 indicates that a plot of \(1/(1-p)^2\) versus \(t\) should be linear. This behavior has been generally observed in polyesterifications. Figure 2-1 shows the results for the polymerization of diethylene glycol, \((\text{HOCH}_2\text{CH}_2)_2\text{O}\), and adipic acid [Flory, 1939; Solomon, 1967, 1972]. The results are typical of the behavior observed for polyesterifications. Although various authors agree on the experimental data, there has been considerable disagreement on the interpretation of the results. At first glance the plot does not appear to exactly follow the relationship. The experimental points deviate from the third-order plot in the initial region below 80% conversion and in the later stages above 93% conversion. These deviations led various workers [Amass, 1979; Fradet and Marechal, 1982a,b; Solomon, 1967, 1972] to suggest alternate kinetic expressions based on either 1- or \(\frac{3}{2}\)-order dependencies of

![Fig. 2-1 Third-order plot of the self-catalyzed polyesterification of adipic acid with diethylene glycol at 166°C. After Solomon [1967] by permission of Marcel Dekker, New York) from the data of Flory [1939] (by permission of American Chemical Society, Washington, DC).](image-url)
the reaction rate on the carboxyl concentration, that is, 2- and $2\frac{1}{2}$-order dependencies according to

$$\frac{-d[\text{COOH}]}{dt} = k[\text{COOH}][\text{OH}] \quad (2-23a)$$

and

$$\frac{-d[\text{COOH}]}{dt} = k[\text{COOH}]^{3/2}[\text{OH}] \quad (2-23b)$$

However, a critical evaluation shows that both kinetic possibilities leave much to be desired. The experimental rate data fits Eq. 2-23a well only in the region between 50 and 86% conversion with an excessively poor fit above 86% conversion. On the other hand, a plot according to Eq. 2-23b fits reasonably well up to about 80% conversion but deviates badly above that point. Neither of the two alternate kinetic plots comes close to being as useful as the third-order plot in Fig. 2-1. The third-order plot fits the experimental data much better than does either of the others at the higher conversions. The fit of the data to the third-order plot is reasonably good over a much greater range of the higher conversion region. The region of high conversion is of prime importance, since, as will be shown in Sec. 2-2a-3, high-molecular-weight polymer is obtained only at high conversions. From the practical viewpoint, the low conversion region of the kinetic plot is of little significance.

### 2-2a-2 Reasons for Nonlinearity in Third-Order Plot

The failure to fit the data over the complete conversion range from 0 to 100% to a third-order plot has sometimes been ascribed to failure of the assumption of equal functional group reactivity, but this is an invalid conclusion. The nonlinearities are not inherent characteristics of the polymerization reaction. Similar nonlinearities have been observed for nonpolymerization esterification reactions such as esterifications of lauryl alcohol with lauric or adipic acid and diethylene glycol with caproic acid [Flory, 1939; Fradet and Marechal, 1982b].

#### 2-2a-2-a Low-Conversion Region

Flory attributed the nonlinearity in the low conversion region to the large changes that take place in the reaction medium. The solvent for the reaction changes from an initial mixture of carboxylic acid and alcohol to an ester. There is a large decrease in the polarity of the reaction system as the polar alcohol and acid groups are replaced by the less polar ester groups with the simultaneous removal of water. This effect may exert itself in two ways—a change in the reaction rate constant or order of reaction. Either possibility is compatible with the experimental observations. The low conversion region of the third-order plot in Fig. 2-1 is approximately linear but with a smaller slope (rate constant) than in the region of higher conversion. The direction of this change corresponds to that expected for a reaction involving a charged substrate (protonated carboxyl) and neutral nucleophile (alcohol). The reaction rate constant increases with decreased solvent polarity since the transition state is less charged than the reactants [Ritchie, 1990]. It has also been suggested that extensive association of both the diol and diacid reactants in the low conversion region lowers the reaction rate by effectively decreasing the concentrations of the reactive species, that is, free, unassociated OH and COOH groups [Ueberreiter and Hager, 1979].

The low conversion region fits an overall $2\frac{1}{2}$ reaction order better than it does 3-order. A change from $2\frac{1}{2}$ to 3-order as the reaction medium becomes less polar is compatible with a
change from specific acid (i.e., H\(^+\)) catalysis to general-acid catalysis. The proton concentration is relatively high and [H\(^+\)] is a more effective catalyst than the unionized carboxylic acid in the polar, low conversion region. HA in Eqs. 2-12, 2-16, and 2-17 is replaced by H\(^+\). The reaction rate becomes first-order each in carboxyl and hydroxyl groups and H\(^+\). The proton concentration is given by

\[ [H^+] = (K_{HA}[HA])^{1/2} \]  

(2-24)

where \(K_{HA}\) is the ionization constant for the carboxylic acid. Combination of Eqs. 2-17 and 2-24 yields

\[ \frac{-d[COOH]}{dt} = k_3KK_{HA}^{1/2}[COOH]^{3/2}[OH] \]  

(2-25)

for the polymerization rate. The reaction medium becomes less polar after the low-conversion (>80%) region and the major catalyst in the reaction system is the unionized carboxylic acid—the reaction is second-order in carboxylic acid and third-order overall (Eqs. 2-18 and 2-19).

Another problem is the very high concentrations of reactants present in the low-conversion region. The correct derivation of any rate expression such as Eqs. 2-20 and 2-22 requires the use of activities instead of concentrations. The use of concentrations instead of activities assumes a direct proportionality between concentration and activity. This assumption is usually valid at the dilute and moderate concentrations where kinetic studies on small molecules are typically performed. However, the assumption often fails at high concentrations and those are the reaction conditions for the typical step polymerization that proceeds with neat reactants. A related problem is that neither concentration nor activity may be the appropriate measure of the ability of the reaction system to donate a proton to the carboxyl group. The acidity function \(h_0\) is often the more appropriate measure of acidity for nonaqueous systems or systems containing high acid concentrations [Ritchie, 1990]. Unfortunately, the appropriate \(h_0\) values are not available for polymerization systems.

Yet another possibility for the nonlinearity in the low conversion region is the decrease in the volume of the reaction mixture with conversion due to loss of one of the products of reaction (water in the case of esterification). This presents no problem if concentration is plotted against time as in Eq. 2-20. However, a plot of \(1/(1-p)^2\) against time (Eq. 2-22) has an inherent error since the formulation of Eq. 2-21 assumes a constant reaction volume (and mass) [Szabo-Rethy, 1971]. Elias [1985] derived the kinetics of step polymerization with correction for loss of water, but the results have not been tested. It is unclear whether this effect alone can account for the nonlinearity in the low conversion region of esterification and polyesterification.

2-2a-2-b High-Conversion Region. The nonlinearity observed in the third-order plot in the final stages of the polyesterification (Fig. 2-1) is probably not due to any of the above mentioned reasons, since the reaction system is fairly dilute and of relatively low polarity. Further, it would be difficult to conjecture that the factors responsible for nonlinearity at low conversions are present at high conversion but absent in between. It is more likely that other factors are responsible for the nonlinear region above 93% conversion.

Polyesterifications, like many step polymerizations, are carried out at moderate to high temperatures not only to achieve fast reaction rates but also to aid in removal of the small molecule by-product (often H\(_2\)O). The polymerization is an equilibrium reaction and the
equilibrium must be displaced to the right (toward the polymer) to achieve high conversions (synonymous with high molecular weights). Partial vacuum (often coupled with purging of the reaction system by nitrogen gas) is usually also employed to drive the system toward high molecular weight. Under these conditions small amounts of one or the other or both reactants may be lost by degradation or volatilization. In the case of polyestherification, small degradative losses might arise from dehydration of the diol, decarboxylation of the diacid, or other side reactions (Sec. 2-8d). Although such losses may not be important initially, they can become very significant during the later stages of reaction. Thus a loss of only 0.3% of one reactant can lead to an error of almost 5% in the concentration of that reactant at 93% conversion. Kinetic studies on esterification and polyestherification have been performed under conditions which minimized the loss of reactants by volatilization or side reactions [Hamann et al., 1968]. An ester or polyester was synthesized in a first stage, purified, and then used as the solvent for a second-stage esterification or polyestherification. The initial reactant concentrations of the second-stage reactions corresponded to 80% conversion relative to the situation if the first-stage reaction had not been stopped but with an important difference—the reactant concentrations are accurately known. The second-stage reaction showed third-order behavior up to past 98–99% conversion (higher conversions were not studied). This compares with the loss of linearity in the third-order plot at about 93% conversion if the first-stage reactions were carried out without interruption.

Another possible reason for the observed nonlinearity is an increase in the rate of the reverse reaction. The polyestherification reaction (as well as many other step polymerizations) is an equilibrium reaction. It often becomes progressively more difficult to displace the equilibrium to the right (toward the polymer) as the conversion increases. This is due in large part to the greatly increased viscosity of the reaction medium at high conversions. The viscosity in the adipic acid–diethylene glycol polymerization increases from 0.015 to 0.30 poise during the course of the reaction [Flory, 1939]. This large viscosity increase decreases the efficiency of water removal and may lead to the observed decrease in the reaction rate with increasing conversion. High viscosity in the high-conversion region may also lead to failure of the assumption of equal reactivity of functional groups—specifically to a decrease in functional group reactivity at very large molecular size if there is too large a decrease in molecular mobility.

2-2a-3 Molecular Weight of Polymer

The molecular weight of a polymer is of prime concern from the practical viewpoint, for unless a polymer is of sufficiently high molecular weight (approximately >5000–10,000) it will not have the desirable strength characteristics. It is therefore important to consider the change in polymer molecular weight with reaction time. For the case of stoichiometric amounts of diol and diacid, the number of unreacted carboxyl groups \( N \) is equal to the total number of molecules present in the system at some time \( t \). This is so because each molecule larger than a monomer will on the average have a hydroxyl at one end and a carboxyl at the other end, while each diacid monomer molecule contains two carboxyls and each diol monomer contains no carboxyls.

The residue from each diol and each diacid (separately, not together) in the polymer chain is termed a structural unit (or a monomer unit). The repeating unit of the chain consists of two structural units, one each of the diol and diacid. The total number of structural units in any particular system equals the total number of bifunctional monomers initially present. The number-average degree of polymerization \( \bar{X}_n \) is defined as the average number of structural units per polymer chain. (The symbols \( P \) and \( DP \) are also employed to signify
the number-average degree of polymerization. $X_n$ is simply given as the total number of monomer molecules initially present divided by the total number of molecules present at time $t$:

$$X_n = \frac{N_0}{N} = \frac{[M]_0}{[M]}$$

(2-26)

Combining Eqs. 2-21 and 2-26, one obtains

$$X_n = \frac{1}{(1 - p)}$$

(2-27)

This equation relating the degree of polymerization to the extent of reaction was originally set forth by Carothers [1936] and is often referred to as the Carothers equation.

The number-average molecular weight $M_n$, defined as the total weight of a polymer sample divided by the total number of moles in it (Eqs. 1-15 and 1-16), is given by

$$M_n = M_o X_n + M_{eg} = \frac{M_o}{(1 - p)} + M_{eg}$$

(2-28)

where $M_o$ is the mean of the molecular weights of the two structural units, and $M_{eg}$ is the molecular weight of the end groups. For the polyesterification of adipic acid, HO$_2$C(CH$_2$)$_4$CO$_2$H, and ethylene glycol, HOCH$_2$CH$_2$OH, the repeating unit is

$$\text{—OCH₂CH₂OCO(CH₂)₄CO—}$$

III

and one half of its weight or 86 is the value of $M_o$. The end groups are H$^-$ and —OH and $M_{eg}$ is 18. For even a modest molecular weight polymer the contribution of $M_{eg}$ to $M_n$ is negligibly small, and Eq. 2-28 becomes

$$M_n = M_o X_n = \frac{M_o}{(1 - p)}$$

(2-29)

Combination of Eqs. 2-22 and 2-27 yields

$$\bar{X}_n^2 = 1 + 2[M]_0^2 kt$$

(2-30)

Since the reaction time and degree of polymerization appear as the first and second powers, respectively, the polymer molecular weight will increase very slowly with reaction time except in the early stages of the reaction. This means that very long reaction times are needed to obtain a high-molecular-weight polymer product. The right-hand ordinate of Fig. 2-1 shows the variation of $X_n$ with $t$. The slow increase of the molecular weight of the polymer with time is clearly apparent. The rate of increase of $X_n$ with time decreases as the reaction proceeds. The production of high polymers requires reaction times that are too long from the practical viewpoint.

2-2b  External Catalysis of Polymerization

The slow increase in molecular weight was mistakenly thought originally to be due to the low reactivity of functional groups attached to large molecules. It is, however, simply a
consequence of the third-order kinetics of the direct polycondensation reaction. The realization of this kinetic situation led to the achievement of high-molecular-weight products in reasonable reaction times by employing small amounts of externally added strong acids (such as sulfuric acid or p-toluenesulfonic acid) as catalysts. Under these conditions, $[HA]$ in Eq. 2-17 is the concentration of the catalyst. Since this remains constant throughout the course of the polymerization, Eq. 2-17 can be written as

$$\frac{-d[M]}{dt} = k'[M]^2$$

(2-31)

where the various constant terms in Eq. 2-17 have been collected into the experimentally determinable rate constant $k'$. Equation 2-31 applies to reactions between stoichiometric concentrations of the diol and diacid.

Integration of Eq. 2-31 yields

$$k't = \frac{1}{[M]} - \frac{1}{[M]_0}$$

(2-32)

Combining Eqs. 2-32 and 2-21 yields the dependence of the degree of polymerization on reaction time as

$$[M]_0k't = \frac{1}{(1-p)} - 1$$

(2-33a)

or

$$\bar{X}_n = 1 + [M]_0k't$$

(2-33b)

Data for the polymerization of diethylene glycol with adipic acid catalyzed by p-toluenesulfonic acid are shown in Fig. 2-2. The plot follows Eq. 2-33 with the degree of polymerization increasing linearly with reaction time. The much greater rate of increase of $\bar{X}_n$ with reaction time in the catalyzed polycondensation (Fig. 2-2) relative to the uncatalyzed reaction (Fig. 2-1) is a general and most significant phenomenon. The polycondensation becomes a much more economically feasible reaction when it is catalyzed by an external acid. The self-catalyzed polymerization is not a useful reaction from the practical viewpoint of producing high polymers in reasonable reaction times.

Equations 2-27 and 2-33 and Fig. 2-2 describe the much greater difficulty of performing a successful polymerization compared to the analogous small-molecule reaction (such as the synthesis of ethyl acetate from acetic acid and ethanol). Consider the case where one needs to produce a polymer with a degree of polymerization of 100, which is achieved only at 99% reaction. Running the polymerization to a lower conversion such as 98%, an excellent conversion for a small-molecule synthesis, results in no polymer of the desired molecular weight. Further, one must almost double the reaction time (from ~450 min to 850 min in Fig. 2-2) to achieve 99% reaction and the desired polymer molecular weight. For the small molecule reaction one would not expend that additional time to achieve only an additional 1% conversion. For the polymerization one has no choice other than to go to 99% conversion.

The nonlinearity in the initial region of Fig. 2-2 is, like that in Fig. 2-1, a characteristic of esterifications in general and not of the polymerization reaction. The general linearity of the plot in the higher conversion region is a strong confirmation of the concept of functional group reactivity independent of molecular size. Figure 2-2 shows that the polyesterification
continues its second-order behavior at least up to a degree of polymerization of 90 correspond-
ing to a molecular weight of \( \sim 10,000 \). There is no change in the reactivities of the
hydroxyl and carboxyl groups in spite of the large increase in molecular size (and the accom-
panying large viscosity increase of the medium). Similar results have been observed in many
other polymerizations. Data on the degradation of polymers also show the same effect. Thus
in the acid hydrolysis of cellulose there is no effect of molecular size on hydrolytic reactivity
up to a degree of polymerization of 1500 (molecular weight 250,000) [Flory, 1953]. The
concept of functional group reactivity independent of molecular size has been highly success-
ful in allowing the kinetic analysis of a wide range of polymerizations and reactions of
polymers. Its validity, however, may not always be quite rigorous at very low or very high
conversions.

2-2c Step Polymerizations Other than Polyesterification:
Catalyzed versus Uncatalyzed

The kinetics of step polymerizations other than polyesterification follow easily from those
considered for the latter. The number of different general kinetic schemes encountered in
actual polymerization situations is rather small. Polymerizations by reactions between the
A and B functional groups of appropriate monomers proceed by one of the following situations [Saunders and Dobinson, 1976]:

1. Some polymerizations, such as the formation of polyamides, proceed at reasonable rates as uncatalyzed reactions.
2. Other polymerizations such as those of urea, melamine, or phenol with formaldehyde (see Table 1-1) require an externally added acid or base catalyst to achieve the desired rates of reaction.
3. A few polymerizations can be reasonably employed either in a catalyzed or an uncatalyzed process. Polyurethane formation is an example of this type of behavior. The reaction between diols and diisocyanates is subject to base catalysis. However, the polymerization is often carried out as an uncatalyzed reaction to avoid various undesirable side reactions.

Regardless of the situation into which a particular polymerization falls, the observed overall kinetic features will be the same. The polymerization rates will be dependent on both the A and B groups. For the usual case where one has stoichiometric amounts of the two functional groups, the kinetics will be governed by Eq. 2-30 or 2-33. The observed kinetics will also be the same whether the polymerization is carried by the reaction of A–A and B–B monomers or by the self-reaction of an A—B monomer.

The derivation (Sec. 2-2b) of the kinetics of catalyzed polyesterification assumes that the catalyzed reaction is much faster than the uncatalyzed reaction, that is, \( k' \gg k \). This assumption is usually valid and therefore one can ignore the contribution by the uncatalyzed polyesterification to the total polymerization rate. For example, \( k' \) is close to two orders of magnitude larger than \( k \) for a typical polyesterification. For the atypical situation where \( k \) is not negligible relative to \( k' \), the kinetic expression for \([M]\) or \(X_n\) as a function of reaction time must be derived [Hamann et al., 1968] starting with a statement of the polymerization rate as the sum of the rates of the catalyzed and uncatalyzed polymerizations:

\[
-\frac{d[M]}{dt} = k[M]^3 + k'[M]^2
\] (2-34)

Integration of Eq. 2-34 yields

\[
k't = \frac{k}{k'} \ln \left[ \frac{[M]_0(k[M]_0 + k')}{(k[M]_0 + k')[M]_0} + \frac{1}{[M]} - \frac{1}{[M]_0} \right] \] (2-35)

The natural log term on the right side of Eq. 2-35 is the contribution of the uncatalyzed reaction. Its relative importance increases as \( k/k' \) increases. (When \( k/k' \) is very small, Eq. 2-35 converts to Eq. 2-32.)

2-2d Nonequivalence of Functional Groups in Polyfunctional Reagents

2-2d-1 Examples of Nonequivalence

There are instances where some or all parts of the concept of equal reactivity of functional groups are invalid [Kronstadt et al., 1978; Lovering and Laidler, 1962]. The assumption of equal reactivities of all functional groups in a polyfunctional monomer may often be incorrect. The same is true for the assumption that the reactivity of a functional group is
independent of whether the other functional groups in the monomer have reacted. Neither of these assumptions is valid for 2,4-tolylene diisocyanate (IV)

\[
\text{IV}
\]

which is one of diisocyanate monomers used in the synthesis of polyurethanes [Caraculacu and Coseri, 2001].

Urethane formation can be depicted as occurring by the sequence

\[
\begin{align*}
\text{R-N=CO}^- + \text{B} & \rightarrow \text{R-N=C-B}^+ \\
\text{R-NH-COOR}' & \rightarrow \text{R-NH-C-B}^+ \\
& \downarrow \text{ROH} \\
& \text{R}^+ \text{OH}
\end{align*}
\]

where B: is a base catalyst (e.g., a tertiary amine). The reaction involves a rate-determining nucleophilic attack by the alcohol on the electrophilic carbon-nitrogen linkage of the isocyanate. This is substantiated by the observation that the reactivity of the isocyanate group increases with the electron-pulling ability of the substituent attached to it [Kaplan, 1961].

In 2,4-tolylene diisocyanate several factors cause the reactivities of the two functional groups to differ. These can be discussed by considering the data in Table 2-3 on the reactivities of various isocyanate groups compared to that in phenyl isocyanate toward reaction with

<table>
<thead>
<tr>
<th>Isocyanate Reactant</th>
<th>Rate Constants $^b$</th>
<th>$k_1$</th>
<th>$k_2$</th>
<th>$k_1/k_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Monoisocyanate</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Phenyl isocyanate</td>
<td></td>
<td>0.406</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$p$-Tolyl isocyanate</td>
<td></td>
<td>0.210</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$o$-Tolyl isocyanate</td>
<td></td>
<td>0.0655</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Diisocyanates</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$m$-Phenylene diisocyanate</td>
<td></td>
<td>4.34</td>
<td>0.517</td>
<td>8.39</td>
</tr>
<tr>
<td>$p$-Phenylene diisocyanate</td>
<td></td>
<td>3.15</td>
<td>0.343</td>
<td>9.18</td>
</tr>
<tr>
<td>2,6-Tolylene diisocyanate</td>
<td></td>
<td>0.884</td>
<td>0.143</td>
<td>6.18</td>
</tr>
<tr>
<td>2,4-Tolylene diisocyanate</td>
<td></td>
<td>1.98</td>
<td>0.166</td>
<td>11.9</td>
</tr>
</tbody>
</table>

$^a$ Data from Brock [1959].

$^b$ Rate constants are in units of L mol$^{-1}$ s$^{-1}$. 

KINETICS OF STEP POLYMERIZATION 55
n-butanol at 39.7°C in toluene solution with triethylamine as the catalyst [Brock, 1959, 1961]. It is clear that a methyl substituent deactivates the isocyanate group by decreasing its electronegativity; the effect is greater when the substituent is at the nearby ortho position. For the diisocyanates in Table 2-3 \( k_1 \) is the rate constant for the more reactive isocyanate group, while \( k_2 \) is the rate constant for the reaction of the less reactive isocyanate group after the more reactive one has been converted to a urethane group. One isocyanate group activates the other by electron withdrawal, as shown by the increased reactivity in the diisocyanates relative to the monoisocyanates. However, once the first isocyanate group has reacted the reactivity of the second group decreases, since the urethane group is a much weaker electron-pulling substituent than the isocyanate group. For 2,4-tolylene diisocyanate analysis of the experimental data at low conversion shows the para isocyanate group at be 2.7 times as reactive as the ortho groups. However, the effective difference in reactivity of the two functional groups is much greater \( (k_1/k_2 = 11.9) \), since the reactivity of the ortho group drops an additional factor of approximately 4 after reaction of the para isocyanate group.

The reactivity differences of the two functional groups in 2,4-tolylene diisocyanate result from its unsymmetric and aromatic structure. The environments (steric and electrostatic) of the two isocyanate groups are different to begin with, and the effect of reaction of one group is efficiently transmitted through the conjugated \( \pi \)-electron system of the aromatic ring. These differences disappear for a reactant such as 1,4-cyclohexylene diisocyanate, which is symmetric to begin with and possesses no aromatic system to transmit the effect of the reacted isocyanate group to the unreacted group.

The change in reactivity of one functional group upon reaction of the other has been noted in several systems as a difference in the reactivity of monomer compared to the other-sized species, although all other species from dimer on up had the same reactivity [Hodkin, 1976; Yu et al., 1986]. This behavior usually occurs with monomers having two functional groups in close proximity and where polymerization involves a significant change in the electron-donating or electron-withdrawing ability of the functional group. Thus the reactivity of the hydroxyl group in ethylene glycol (V) toward esterification is considerably higher than the hydroxyl of a half-esterified glycol (VI) [Yamanis and Adelman, 1976]. The nucleophilicity

\[
\text{HO} - \text{CH}_2\text{CH}_2\text{OH} \quad \text{HO} - \text{CH}_2\text{CH}_2\text{OCO} - \text{R} - \text{OCO} \quad \text{V} \quad \text{VI}
\]

of a hydroxyl group is enhanced more by an adjacent hydroxyl relative to an adjacent ester group. Similarly, in the polymerization of sodium \( p \)-fluorothiophenoxide (an A—B reactant), nucleophilic substitution at the aromatic C—F bond occurs faster at fluorophenyl end groups of a growing polymer compared to monomer [Lenz et al., 1962]. The electron-donating effect of the para \( S^- \) group in the monomer decreases the electron deficiency of the para carbon more than does a \( \sigma S \) group in species larger than monomer.

Polymerization of terephthalic acid with 4,6-diamino-1,3-benzenediol via oxazole formation (Eq. 2-219) proceeds with a sharp and continuous decrease in reaction rate with increasing polymer molecular weight [Cotts and Berry, 1981]. Reaction becomes progressively more diffusion-controlled with increasing molecular size due to the increasing rigid-rod structure of the growing polymer.

Trifunctional monomers constitute an important class of monomers. One often encounters such reactants in which the various functional groups have different reactivities. Thus, the polyestefication of glycerol (VII) with phthalic anhydride proceeds with incomplete
utilization of the hydroxyl groups [Kienle et al., 1939]. This has been attributed to the lowered reactivity of the secondary hydroxyl group compared to the two primary hydroxyls.

2-2d-2 Kinetics

Kinetic analysis of a step polymerization becomes complicated when all functional groups in a reactant do not have the same reactivity. Consider the polymerization of $A - A$ with $B - B'$ where the reactivities of the two functional groups in the $B - B'$ reactant are initially of different reactivities and, further, the reactivities of $B$ and $B'$ each change on reaction of the other group. Even if the reactivities of the two functional groups in the $A - A$ reactant are the same and independent of whether either group has reacted, the polymerization still involves four different rate constants. Any specific-sized polymer species larger than dimer is formed by two simultaneous routes. For example, the trimer $A - AB - B'A - A$ is formed by

$$B - B' \xrightarrow{k_2} B - B'A - A$$  \hspace{1cm} (2-37a)

$$A - A \xrightarrow{k_1} A - A$$  \hspace{1cm} (2-37b)

$$A - AB - B' \xrightarrow{k_3} A - AB - B'A - A$$ \hspace{1cm} (2-37c)

$$A - AB - B' \xrightarrow{k_4} A - B'A - A$$ \hspace{1cm} (2-37d)

The two routes (one is Eqs. 2-37b and 2-37c; the other is Eqs. 2-37a and 2-37d) together constitute a complex reaction system that consists simultaneously of competitive, consecutive and competitive, parallel reactions.

Obtaining an expression for the concentration of $A$ (or $B$ or $B'$) groups or the extent of conversion or $X_n$ as a function of reaction time becomes more difficult than for the case where the equal reactivity postulate holds, that is, where $k_1 = k_2 = k_3 = k_4$. As a general approach, one writes an expression for the total rate of disappearance of $A$ groups in terms of the rates of the four reactions 2-37a, b, c, and d and then integrates that expression to find the time-dependent change in $[A]$. The difficulty arises because the differential equations that must be integrated are not linear equations and do not have exact solutions except in very particular cases. Numerical methods are then needed to obtain an approximate solution.

2-2d-2-a Polymerization of $A - A$ with $B - B'$. The kinetics of the reaction system described in Eq. 2-37 is relatively difficult to treat because there are four different rate constants. Special (and simpler) cases involving only two rate constants can be more easily treated. One such case is where the two functional groups $B$ and $B'$ have different reactivities but
their individual reactivities are decoupled in that neither the reactivity of \( B \) nor of \( B' \) changes on reaction of the other group:

\[
\begin{align*}
  k_1 & \neq k_2 \\
k_1 & = k_4 \\
k_2 & = k_3
\end{align*}
\]  

(2-38a)

(2-38b)

(2-38c)

The reaction system converts from one (Eq. 2-37), that is, from the kinetic viewpoint, simultaneously competitive, consecutive (series) and competitive, simultaneous (parallel) to one (Eq. 2-38) that is only competitive, simultaneous. The polymerization consists of the \( B \) and \( B' \) functional groups reacting independently with \( A \) groups. The rates of disappearance of \( A \), \( B \), and \( B' \) functional groups are given by

\[
\begin{align*}
  -\frac{d[B]}{dt} & = k_1 [A][B] \\
  -\frac{d[B']}{dt} & = k_2 [A][B'] \\
  -\frac{d[A]}{dt} & = k_1 [A][B] + k_2 [A][B']
\end{align*}
\]  

(2-39)

(2-40)

(2-41)

The polymerization rate is synonymous with the rate of disappearance of \( A \) groups (or the sum of the rates of disappearance of \( B \) and \( B' \) groups).

In the typical polymerization one has equimolar concentrations of the \( A-A \) and \( B-B' \) reactants at the start of polymerization. The initial concentrations of \( A \), \( B \), and \( B' \) groups are

\[
[A]_0 = 2[B]_0 = 2[B']_0
\]  

(2-42)

and the relationship between the concentrations of \( A \), \( B \), and \( B' \) at any time during polymerization is

\[
[A] = [B] + [B']
\]  

(2-43)

Combination of Eqs. 2-41 and 2-43 yields the polymerization rate as

\[
-\frac{d[A]}{dt} = (k_1 - k_2)[A][B] + k_2[A]^2
\]  

(2-44)

Introduction of the dimensionless variables \( \alpha \), \( \beta \), \( \gamma \), and \( \tau \) and the parameter \( s \) defined by

\[
\begin{align*}
  \alpha & = \frac{[A]}{[A]_0} \\
  \beta & = \frac{[B]}{[B]_0} \\
  \gamma & = \frac{[B']}{[B']_0} \\
  \tau & = \frac{[B]_0 k_2 t}{k_1} \\
  s & = \frac{k_2}{k_1}
\end{align*}
\]  

(2-45a)

(2-45b)

(2-45c)

(2-45d)

(2-45e)
simplifies the mathematical solution of Eq. 2-44. \(a, b,\) and \(g\) are the fractions of A, B, and B' groups, respectively, which remain unreacted at any time. \(\tau\) is dimensionless time and \(s\) is the ratio of two rate constants. It is then possible to solve the coupled system of Eqs. 2-39 through 2-44 to give

\[
\tau = \int_{0}^{1} \frac{s d\beta}{\beta^2 [1 + \beta^{(s-1)}]} \tag{2-46}
\]

\[
\gamma = \beta^s \tag{2-47}
\]

where

\[
\alpha = \frac{\beta + \gamma}{2} = \frac{\beta + \beta^s}{2} \tag{2-48}
\]

The integral in Eq. 2-46 yields simple integrals for \(s\) values of 0, 1, and \(\infty\). The dependencies of \(\alpha, \beta,\) and \(\gamma\) on \(\tau\) in these instances are

1. For \(s = 1\), that is, \(k_2 = k_1\),

\[
\beta = \frac{1}{1 + 2\tau} = \gamma = \alpha \tag{2-49}
\]

2. For \(s = 0\), that is, \(k_1 \gg k_2\), where \(k_1\) has some value and \(k_2 \rightarrow 0\): B' groups do not react (\(\gamma = 1\)) and

\[
\ln \left( \frac{1 + \beta}{2\beta} \right) = \tau \tag{2-50a}
\]

\[
\alpha = \frac{1 + \beta}{2} \tag{2-50b}
\]

3. For \(s = \infty\), that is, \(k_2 \gg k_1\), where \(k_2\) has some value and \(k_1 \rightarrow 0\): B groups do not react (\(\beta = 1\)) and

\[
\ln \left( \frac{1 + \gamma}{2\gamma} \right) = \tau \tag{2-51a}
\]

\[
\alpha = \frac{1 + \gamma}{2} \tag{2-51b}
\]

For almost all other values of \(s\) the integral in Eq. 2-46 must be numerically evaluated. The results of such calculations are presented in graphical form in Figs. 2-3 and 2-4 as plots of \(\alpha, \beta,\) and \(\gamma\) versus log \(\tau\) for \(s\) values of 1 and larger [Ozizmir and Odian, 1980]. There is no need for plots for \(s < 1\), since the B and B' groups have interchangeable roles due to the symmetry of the reaction system. \(\alpha\) at any time is exactly the same for \(s = z\) or \(s = 1/z\), where \(z\) is any number. The only difference for an \(s\) value of \(z\) or \(1/z\) is whether it is the B or B' type of group, which reacts rapidly while the other reacts slowly. Figure 2-3 gives \(\beta\) and \(\gamma\) as a function of \(\tau\). When \(s = 1\) both \(\beta\) and \(\gamma\) decay at the same rate according to Eq. 2-49. As \(s\) increases the \(\beta\) plots move sharply above the plot for \(s = 1\) since B groups react more slowly with A. Although \(k_2\) is fixed, increasing values of \(s\) help move the \(\gamma\) plots gradually below the plot for \(s = 1\), since B groups reacting more slowly with A leaves comparably more \([A]\) for
B groups to react with. As $s \to \infty$ the condition is reached in which $[B]$ remains constant at $\frac{1}{2}[B]_0$ during the complete decay of $B_0$ according to Eq. 2-51b.

Figure 2-4 shows the decay in $\alpha$ and the corresponding increase in $X_n$ with $\tau$ (since $X_n = 1/\alpha$). It becomes progressively more difficult to achieve high degrees of polymerization in reasonable times for reaction systems of $s > 1$. At sufficiently large $s$ (small $k_1$) the
reaction time to obtain high polymer ($\bar{X}_n > 50–100$) becomes impractical. The extreme situation occurs at $s \rightarrow \infty$ ($k_1 \rightarrow 0$), where the maximum degree of polymerization is 2. Reaction systems with very small $k_1$ values must be avoided in order to achieve high degrees of polymerization. The desirable system from the viewpoint of polymerization rate and $\bar{X}_n$ is that with $s = 1$. (The exception to this generalization is for systems of $s > 1$ where both $k_1$ and $k_2$ are large.)

The $A-A$ plus $B-B'$ system with $k_1 \neq k_4$ and $k_2 \neq k_3$ has been treated in a similar manner [Ozizmir and Odian, 1981]. The parameters $\alpha$, $\beta$, $\gamma$, and $s$ as defined by Eqs. 2-45a, 2-45b, 2-45c, and 2-45e are retained in the treatment. $\tau$ is redefined as

$$\tau = (k_1 + k_2)[B]_0 t$$ (2-52)

and the parameters $u_1$ and $u_2$

$$u_1 = \frac{k_4}{k_1}$$ (2-53)

$$u_2 = \frac{k_3}{k_2}$$ (2-54)

are introduced to describe the changes in the rate constants for the B and B' functional groups. The results are shown in Fig. 2-5 as a plot of $\alpha$ and the degree of polymerization versus $\tau$ for a range of values of $s$, $u_1$, and $u_2$. For the case where the two functional groups B and B' have the same initial reactivity ($s = 1$) (plots 1–3), the polymerization rate decreases if the reactivity of either B or B' decreases on reaction of the other group (i.e., if $u_1 < 1$ or $u_2 < 1$). The polymerization rate increases if the reactivity of either B or B' increases on reaction of the other group ($u_1 > 1$ or $u_2 > 1$). The effects reinforce each other.

![Fig. 2-5](image)

**Fig. 2-5**  Decay in $\alpha$ and increase in degree of polymerization of $A-A$ with $B-B'$ for $k_1 \neq k_4$ and $k_2 \neq k_3$. Values of $s$, $\mu_1$, $\mu_2$ are 1, 1, 1 (plot 1); 1, 0.2, 0.2 (plot 2); 1, 5, 5 (plot 3); 5, 1, 1 (plot 4); 5, 0.2, 1 (plot 5); 5, 5, 1 (plot 6). After Ozizmir and Odian [1980] (by permission of Wiley-Interscience, New York).
when both \( u_1 \) and \( u_2 \) change in the same direction, but tend to cancel each other when \( u_1 \) and \( u_2 \) change in opposite directions. When the B and B' groups have different initial reactivities, for example, \( s = 5 \) (B' five times more reactive than B), the polymerization rate is decreased (compare plots 1 and 4) unless compensated for by an increase in the reactivity of B on reaction of B' (\( u_1 > 1 \)). There is an increase in polymerization rate when the increased reactivity of B is large (compare plots 4 and 6). The polymerization rate becomes more depressed when B groups decrease in reactivity on reaction of B' (\( u_1 < 1 \)) (compare plots 4 and 5).

2-2d-2-b Variation of Rate Constant with Size. The usual kinetic analysis of step polymerization, including that described for the A–A plus B–B' system, assumes the rate constants are independent of molecular size. The effect of a rate constant dependence on molecular size has been analyzed for A–B or A–A plus B–B polymerizations where a functional group on a monomer molecule has a different reactivity from the same group in species

![Figure 2-6](image-url)  

**Fig. 2-6** Variation of degree of polymerization with time when monomer has a different reactivity from large-sized species. Values of \( u \) are noted for each plot; the plots for \( u = 25 \) and 100 are indistinguishable from each other. After Gupta et al. [1979a,b] (by permission of Pergamon Press, London and Elsevier, Oxford).
larger than monomer (i.e., for dimer and larger) [Goel et al., 1977; Gupta et al., 1979a,b]. The following terms are defined:

\[ u = \frac{k_m}{k_p} \]  
\[ \tau = [A]_0 k_p t \]  

where \( k_m \) is the rate constant for A and B groups that are part of monomer molecules and \( k_p \) is the corresponding rate constant for A and B groups that are part of all species larger than monomer.

Figure 2-6 shows the results plotted as the polymer degree of polymerization versus \( \tau \) for various values of \( u \). The mathematical solution of this case shows that the initial limiting slope (at \( \tau \to 0 \)) is \( u/2 \) while the final limiting slope (at large values of \( \tau \)) is \( 1/2 \) independent of the value of \( u \). Most of these features are evident in Fig. 2-6. Dimer is produced more rapidly when monomer is more reactive than the larger-sized species (that is, the larger the value of \( u \)). There is a subsequent slower rate of increase in \( X_n \) with the limiting slope of \( 1/2 \) being reached more rapidly for larger \( u \) values. The initial rate of increase of \( X_n \) is slower for \( u < 1 \) (monomer less reactive than larger sized species), and it takes longer to reach the limiting slope of \( 1/2 \). More significantly, it takes much longer reaction times to reach a particular degree of polymerization when \( u < 1 \). This is a kinetic characteristic of consecutive (series) reaction systems—the overall rate of production of the final product (high polymer) is faster when the initial reaction (reaction of monomer) is faster and the later reaction (reaction of dimer and larger sized species) is slow than vice versa. The trends described in this section would also apply (qualitatively at least) for the case where \( k \) is a continuously varying function of molecular size. If \( k \) increases with molecular size, the situation is qualitatively analogous to the above system for \( u < 1 \). The situation is analogous to \( u > 1 \) when \( k \) decreases with molecular size.

2-3 ACCESSIBILITY OF FUNCTIONAL GROUPS

In order for a polymerization to yield high polymers the polymer must not precipitate from the reaction mixture before the desired molecular weight is reached. Premature precipitation effectively removes the growing polymer molecules from the reaction; further growth is prevented because the polymer's functional end groups are no longer accessible to each other. The effect can be seen in Table 2-4 for the polymerization of bis(4-isocyanatophenyl)methane with ethylene glycol [Lyman, 1960]:

\[ \text{HO-CH}_2\text{CH}_2\text{-OH} + \text{OCN-CH}_2\text{-CH}_2\text{-NCO} \rightarrow \]

\[ \left[ \text{O-CH}_2\text{CH}_2\text{-OCO-NH-CH}_2\text{-NH-OCO-CH}_2\text{-NH-NH}_2 \right]_n \]  

The inherent viscosity \( \eta_{inh} \) is a measure of the polymer molecular weight. Larger values of \( \eta_{inh} \) indicate higher molecular weights. Early precipitation of the polyurethane occurs in
xylene and chlorobenzene and limits the polymerization to a low molecular weight. Higher molecular weights are obtained when the solvent for the reaction becomes a better solvent for the polymer. The highest polymer molecular weight is obtained in DMSO (dimethylsulfoxide), a highly polar aprotic solvent, in which the polyurethane is completely soluble during the entire course of the polymerization.

Figure 2-7 shows similar behavior for the polymerization between terephthaloyl chloride and trans-2,5-dimethylpiperazine in mixtures of chloroform with carbon tetrachloride or

<table>
<thead>
<tr>
<th>Solvent</th>
<th>$\eta_{inh}$</th>
<th>Solubility of Polymer</th>
</tr>
</thead>
<tbody>
<tr>
<td>Xylene</td>
<td>0.06</td>
<td>Precipitates at once</td>
</tr>
<tr>
<td>Chlorobenzene</td>
<td>0.17</td>
<td>Precipitates at once</td>
</tr>
<tr>
<td>Nitrobenzene</td>
<td>0.36</td>
<td>Precipitates after $\frac{1}{2}$ h</td>
</tr>
<tr>
<td>Dimethyl sulfoxide</td>
<td>0.69</td>
<td>Polymer is soluble</td>
</tr>
</tbody>
</table>

aData from Lyman [1960].
bPolymerization temperature: 115°C.
cMeasured in dimethylformamide at room temperature.

Fig. 2-7  Polymerization of terephthaloyl chloride and trans-2,5-dimethylpiperazine in mixed solvents. After Morgan [1963, 1965] (by permission of Wiley-Interscience, New York).
n-hexane [Morgan, 1963, 1965]. Chloroform is a good solvent for the polymer, while carbon tetrachloride and n-hexane are poor solvents. The inherent viscosity of the polymer (measured at 30°C in m-cresol) increases as the reaction mixture contains a larger proportion of chloroform. The better the reaction medium as a solvent for the polymer the longer the polymer stays in solution and the larger the polymer molecular weight. With a solvent medium that is a poor solvent for polymer, the molecular weight is limited by precipitation. Other examples of this behavior are described in Secs. 2-8c and 2-14.

In addition to the effect of a solvent on the course of a polymerization because the solvent is a poor or good solvent for the polymer, solvents affect polymerization rates and molecular weights due to preferential solvation or other specific interactions with either the reactants or transition state of the reaction or both. The direction of the solvation effect is generally the same in polymerization as in the corresponding small molecule reaction and will not be considered in detail. Thus polar solvents enhance the rate of a polymerization with a transition state more polar than the reactants. Polar solvents are not desirable for reactions involving transition states that are less polar than the reactants. The course of a polymerization can be dramatically affected by specific interactions of a solvent with the functional groups of a reactant. The reactivity of a functional group can be altered by specific interaction with solvent. Thus solvents markedly affect the polymer molecular weight in the polymerization of adipic acid and hexamethylene diamine with certain ketone solvents yielding the highest molecular weights [Ogata, 1973]. The molecular weight enhancement by ketones has been ascribed to an enhancement of the diamine nucleophilicity due possibly to a polar interaction between ketone and amine. Alternately, the intermediate formation of an imine may be responsible, since imines can be formed from the diamine and ketone. The imine would be expected to be more reactive than the amine toward the carboxylic acid.

### 2-4 EQUILIBRIUM CONSIDERATIONS

#### 2-4a Closed System

Many, if not most, step polymerizations involve equilibrium reactions, and it becomes important to analyze how the equilibrium affects the extent of conversion and, more importantly, the polymer molecular weight. A polymerization in which the monomer(s) and polymer are in equilibrium is referred to as an equilibrium polymerization or reversible polymerization. A first consideration is whether an equilibrium polymerization will yield high-molecular-weight polymer if carried out in a closed system. By a closed system is meant one where none of the products of the forward reaction are removed. Nothing is done to push or drive the equilibrium point for the reaction system toward the polymer side. Under these conditions the concentrations of products (polymer and usually a small molecule such as water) build up until the rate of the reverse reaction becomes equal to the polymerization rate. The reverse reaction is referred to generally as a depolymerization reaction; other terms such as hydrolysis or glycolysis may be used as applicable in specific systems. The polymer molecular weight is determined by the extent to which the forward reaction has proceeded when equilibrium is established.

Consider an external acid-catalyzed polyesterification

\[
\begin{align*}
\text{COOH} + \text{OH} & \rightleftharpoons \text{CO} - \text{O} - \text{H} + \text{H}_2\text{O} \\
\end{align*}
\]  

(2-58)
in which the initial hydroxyl group and carboxyl group concentrations are both $[M]_0$. The concentration of ester groups $[\text{COO}]$ at equilibrium is $p_e [M]_0$, where $p_e$ is the extent of reaction at equilibrium. $p_e [M]$ also represents $[\text{H}_2\text{O}]$ at equilibrium. The concentrations of hydroxyl and carboxyl groups at equilibrium are each $( [M]_0 - p_e [M]_0 )$. The equilibrium constant for the polymerization is given by

$$K = \frac{[\text{COO}][\text{H}_2\text{O}]}{[\text{COOH}][\text{OH}]} = \frac{(p_e [M]_0)^2}{([M]_0 - p_e [M]_0)^2} \quad (2-59)$$

which simplifies to

$$K = \frac{p_e^2}{(1 - p_e)^2} \quad (2-60)$$

Solving for $p_e$ yields

$$p_e = \frac{K^{1/2}}{1 + K^{1/2}} \quad (2-61)$$

Equation 2-61 yields the extent of conversion as a function of the equilibrium constant. To obtain an expression for the degree of polymerization as a function of $K$, Eq. 2-61 is combined with Eq. 2-27 to yield

$$\bar{X}_n = 1 + K^{1/2} \quad (2-62)$$

Table 2-5 shows $p_e$ and $\bar{X}_n$ values calculated for various $K$ values. These calculations clearly indicate the limitation imposed by equilibrium on the synthesis of even a modest molecular weight polymer. A degree of polymerization of 100 (corresponding to a molecular weight of approximately $10^4$ in most systems) can be obtained in a closed system only if the equilibrium constant is almost $10^4$. The higher molecular weights that are typically required for practical applications would require even larger equilibrium constants. A consideration of the equilibrium constants for various step polymerizations or the corresponding small

<table>
<thead>
<tr>
<th>Equilibrium Constant ($K$)</th>
<th>$p$</th>
<th>$\bar{X}_n$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.001</td>
<td>0.0099</td>
<td>1.01</td>
</tr>
<tr>
<td>0.01</td>
<td>0.0909</td>
<td>1.10</td>
</tr>
<tr>
<td>1</td>
<td>0.500</td>
<td>2</td>
</tr>
<tr>
<td>16</td>
<td>0.800</td>
<td>5</td>
</tr>
<tr>
<td>81</td>
<td>0.900</td>
<td>10</td>
</tr>
<tr>
<td>361</td>
<td>0.950</td>
<td>20</td>
</tr>
<tr>
<td>2,401</td>
<td>0.980</td>
<td>50</td>
</tr>
<tr>
<td>9,801</td>
<td>0.990</td>
<td>100</td>
</tr>
<tr>
<td>39,601</td>
<td>0.995</td>
<td>200</td>
</tr>
<tr>
<td>249,001</td>
<td>0.998</td>
<td>500</td>
</tr>
</tbody>
</table>
molecule reactions quickly shows that polymerizations cannot be carried out as closed systems [Allen and Patrick, 1974; Saunders and Dobinson, 1976; Zimmerman, 1988]. For example, the equilibrium constants for a polyesterification is typically no larger than 1–10, $K$ for a transesterification is in the range 0.1–1 and $K$ for polyamidation is in the range $10^2$–$10^3$. Although the equilibrium constant for a polyamidation is very high as $K$ values go, it is still too low to allow the synthesis of high-molecular-weight polymer. Further, even for what appear to be essentially irreversible polymerizations, reversal of polymerization is a potential problem if the by-product small molecule is not removed (or, alternately, the polymer is not removed).

It is worth mentioning that $K$ values reported in the literature for any specific step polymerization often differ considerably. Thus, $K$ values for the polymerization of adipic acid and hexamethylene diamine range from a low of 250 to a high of 900. There are several reasons for these differences, not the least of which is the experimental difficulty in carrying out measurements on polymerizations involving highly concentrated systems (often containing only the monomers, without any solvent) at moderately high temperatures (200–300°C). Other reasons for the variation in $K$ values are the effects of temperature and the concentration of the small molecule by-product on $K$. Most step polymerizations are exothermic and $K$ decreases with increasing temperature (see Sec. 2-8a). The common practice of extrapolating values of $K$ determined at certain temperatures to other temperatures can involve considerable error if $\Delta H$ is not accurately known. The variation of $K$ with the concentration of the small molecule by-product has been established in the polyamidation reaction but the quantitative effect has not been generally studied. The effect may be due to a change of $K$ with polarity of the reaction medium.

2-4b Open, Driven System

The inescapable conclusion is that except in a minority of systems a step polymerization must be carried out as an open, driven system. That is, we must remove at least one of the products of the forward (polymerization) reaction so as to drive the equilibrium toward high molecular weights. It is usually more convenient to remove the small molecule by-product rather than the polymer. When water is the by-product, it can be removed by a combination of temperature, reduced pressure, and purging with inert gas. Conveniently one often carries out step polymerizations at temperatures near or above the boiling point of water. This is usually done for purposes of obtaining desired reaction rates, but it has the added advantage of facilitating water removal. A small molecule by-product such as HCl can be removed in the same manner or by having a base present in the reaction system to neutralize the hydrogen chloride. Driving an equilibrium toward polymer requires considerable effort, since the water or hydrogen chloride or other small molecule must diffuse through and out of the reaction mixture. Diffusion is not so easy since the typical step polymerization system is fairly viscous at very high conversions. The polymerization can become diffusion-controlled under these conditions with the polymerization being controlled by the rate of diffusion of the small molecule by-product [Campbell et al., 1970].

The extent to which one must drive the system in the forward direction can be seen by calculating the lowering of the small molecule concentration, which is necessary to achieve a particular molecular weight. For the polyesterification (Eq. 2-58) one can rewrite Eq. 2-59 as

$$K = \frac{p[H_2O]}{[M]_0(1-p)^2}$$

(Eq. 2-63)
which is combined with Eq. 2-27 to yield

\[
K = \frac{p[H_2O]|X_n|^2}{|M|_0} \tag{2-64}
\]

and this result combined with Eq. 2-27 to give

\[
[H_2O] = \frac{K|M|_0}{X_n(X_n - 1)} \tag{2-65}
\]

Equation 2-65, which applies equally to A–B polymerizations, indicates that [H₂O] must be greatly reduced to obtain high \(X_n\) values. [H₂O] is inversely dependent on essentially the square of \(X_n\) since \((X_n - 1)\) is close to \(X_n\) for large values of \(X_n\). It is also seen that the level to which the water concentration must be lowered to achieve a particular degree of polymerization increases with increasing \(K\) and increasing initial concentration of the reactants. Table 2-6 shows the calculated [H₂O] values for selected values of \(K\) and \(X_n\) at

<table>
<thead>
<tr>
<th>(K)</th>
<th>(X_n)</th>
<th>[H₂O] (a) (mol L(^{-1}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.1</td>
<td>1.32(^b)</td>
<td>1.18(^b)</td>
</tr>
<tr>
<td></td>
<td>20</td>
<td>(1.32 \times 10^{-3})</td>
</tr>
<tr>
<td></td>
<td>50</td>
<td>(2.04 \times 10^{-4})</td>
</tr>
<tr>
<td></td>
<td>100</td>
<td>(5.05 \times 10^{-5})</td>
</tr>
<tr>
<td></td>
<td>200</td>
<td>(1.26 \times 10^{-5})</td>
</tr>
<tr>
<td></td>
<td>500</td>
<td>(2.00 \times 10^{-6})</td>
</tr>
<tr>
<td>1</td>
<td>2(^b)</td>
<td>2.50(^b)</td>
</tr>
<tr>
<td></td>
<td>20</td>
<td>(1.32 \times 10^{-2})</td>
</tr>
<tr>
<td></td>
<td>50</td>
<td>(2.04 \times 10^{-3})</td>
</tr>
<tr>
<td></td>
<td>100</td>
<td>(5.05 \times 10^{-4})</td>
</tr>
<tr>
<td></td>
<td>200</td>
<td>(1.26 \times 10^{-4})</td>
</tr>
<tr>
<td></td>
<td>500</td>
<td>(2.01 \times 10^{-5})</td>
</tr>
<tr>
<td>16</td>
<td>5(^b)</td>
<td>4.00(^b)</td>
</tr>
<tr>
<td></td>
<td>20</td>
<td>0.211</td>
</tr>
<tr>
<td></td>
<td>50</td>
<td>(3.27 \times 10^{-2})</td>
</tr>
<tr>
<td></td>
<td>100</td>
<td>(8.10 \times 10^{-3})</td>
</tr>
<tr>
<td></td>
<td>200</td>
<td>(2.01 \times 10^{-3})</td>
</tr>
<tr>
<td></td>
<td>500</td>
<td>(3.21 \times 10^{-4})</td>
</tr>
<tr>
<td>81</td>
<td>10(^b)</td>
<td>4.50(^b)</td>
</tr>
<tr>
<td></td>
<td>20</td>
<td>1.07</td>
</tr>
<tr>
<td></td>
<td>50</td>
<td>0.166</td>
</tr>
<tr>
<td></td>
<td>100</td>
<td>(4.09 \times 10^{-2})</td>
</tr>
<tr>
<td></td>
<td>200</td>
<td>(1.02 \times 10^{-2})</td>
</tr>
<tr>
<td></td>
<td>500</td>
<td>(1.63 \times 10^{-3})</td>
</tr>
<tr>
<td>361</td>
<td>20(^b)</td>
<td>4.75(^b)</td>
</tr>
<tr>
<td></td>
<td>50</td>
<td>0.735</td>
</tr>
<tr>
<td></td>
<td>100</td>
<td>0.183</td>
</tr>
<tr>
<td></td>
<td>200</td>
<td>(4.54 \times 10^{-2})</td>
</tr>
<tr>
<td></td>
<td>500</td>
<td>(7.25 \times 10^{-3})</td>
</tr>
</tbody>
</table>

\(a\) [H₂O] values are for \(|M|_0 = 5.\)

\(b\) These values are for a closed reaction system at equilibrium.
[M]₀ = 5 M. A concentration of 5 M is fairly typical of a step polymerization that is often carried out with only the reactant(s) present (without solvent). The lowering of [H₂O] to achieve a particular Xₙ is less the more favorable the equilibrium (that is, the larger the K value). Thus the synthesis of polyamides (with typical K values > 10²) is clearly easier from the equilibrium viewpoint than polyester synthesis (K ~ 0.1-1). Polyesterification requires a greater lowering of [H₂O] than does polyamidation. It should be understood that simply to lower [H₂O] as much as possible is not the desired approach. One needs to control the [H₂O] so as to obtain the desired degree of polymerization.

2-4c Kinetics of Reversible Polymerization

Although reversible or equilibrium polymerizations would almost always be carried out in an irreversible manner, it is interesting to consider the kinetics of polymerization for the case in which the reaction was allowed to proceed in a reversible manner. (The kinetics of reversible ring-opening polymerizations are discussed in Sec. 7-2b-5).

Consider the polyesterification of Eq. 2-58 under stoichiometric conditions, where k₁ and k₂ are the rate constants for the forward and back reactions. The initial carboxyl and hydroxyl group concentrations are [M]₀. The values at any time are [M], which is given by (1 - p) [M]₀. The concentrations of the products, [COO] and [H₂O], at any time are equal because of the stoichiometry and are given by p[M]₀. The polymerization rate is the difference between the rates of the forward and back reactions

$$\frac{-d[M]}{dt} = \frac{-[M]₀d(1-p)}{dt} = k₁(1-p)^2[M]₀^2 - k₂p²[M]₀^2$$

which can be simplified to

$$\frac{-dp}{dt} = [M]₀[k₁(1-p)^2 - k₂p²]$$

Integration of Eq. 2-67 [Levenspiel, 1972; Moore and Pearson, 1981] yields

$$\ln\left[\frac{p_e - p(2p_e - 1)}{p_e - p}\right] = 2k₁\left(\frac{1}{p_e - 1}\right)[M]₀t$$

Equation 2-68 can be used to calculate the extent of conversion at any time if k₁ and pₑ are known. pₑ is experimentally determined, or calculated from Eq. 2-61 if K is known. From experimental values of p as a function of time, Eq. 2-68 yields a straight line when the left side of the equation is plotted against time. The slope of the line then allows one to calculate k₁.

2-5 CYCLIZATION VERSUS LINEAR POLYMERIZATION

2-5a Possible Cyclization Reactions

The production of linear polymers by the step polymerization of polyfunctional monomers is sometimes complicated by the competitive occurrence of cyclization reactions. Ring formation is a possibility in the polymerizations of both the A—B and A—A plus B—B types.
Reactants of the A–B type such as amino or hydroxy acids may undergo intramolecular cyclization instead of linear polymerization.

\[
\begin{align*}
H_2N-\text{R- COOH} & \quad \rightarrow \quad HN-\text{R- CO} \\
\text{HO- R- COOH} & \quad \rightarrow \quad O-\text{R- CO}
\end{align*}
\]  

Reactants of the A–A (or B–B) type are not likely to undergo direct cyclization instead of linear polymerization. A groups do not react with each other and B groups do not react with each other under the conditions of step polymerization. Thus there is usually no possibility of anhydride formation from reaction of the carboxyl groups of a diacid reactant under the reaction conditions of a polyesterification. Similarly, cyclization does not occur between hydroxyl groups of a diol, amine groups of a diamine, isocyanate groups of a diisocyanate, and so on.

Once linear polymerization has reached the dimer size, intramolecular cyclization is a possibility throughout any A–B

\[
\begin{align*}
\text{H- } \text{O- RCO} \quad \text{O- COOH} & \quad \rightarrow \quad \text{H- O RCO} \quad \text{O-} \\
\text{O- RCO} & \quad \rightarrow \quad \text{O- RCO}
\end{align*}
\]  

or A–A + B–B polymerization

\[
\begin{align*}
\text{H- } \text{O- RCO} \quad \text{O- COOH} & \quad \rightarrow \quad \text{H- O RCO} \quad \text{O-} \\
\text{O- RCO} & \quad \rightarrow \quad \text{O- RCO}
\end{align*}
\]  

The extent to which cyclization occurs during polymerization depends on whether the polymerization proceeds under equilibrium control or kinetic control, the ring sizes of the possible cyclic products, and the specific reaction conditions.

2-5b Cyclization Tendency versus Ring Size

Whether cyclization is competitive with linear polymerization for a particular reactant or pair of reactants depends on thermodynamic and kinetic considerations of the size of the ring structure that may be formed. An understanding of the relative ease of cyclization or linear polymerization comes from a variety of sources. These include direct studies with various bifunctional monomers in cyclization reactions (such as those in Eqs. 2-69 through 2-72) as well as ring-opening polymerizations (Chap. 7) and data such as the heats of combustion of cyclic compounds [Carothers and Hill, 1933; Eliel, 1962; Sawada, 1976]. Consider first the thermodynamics stability of different sized ring structures. Some of the most useful data on the effect of ring size on thermodynamic stability is that on the heats of combustion of cycloalkanes (Table 2-7) (1 kJ = 0.2388 kcal). A comparison of the heats of combustion per methylene group in these ring compounds with that in an open-chain alkane yields a general measure of the thermodynamic stabilities of different-sized rings. More precisely, thermodynamic stability decreases with increasing strain in the ring structure as measured by the differences in the heats of combustion per methylene group of the cycloalkane and the \( n \)-alkane. The strain in cyclic structures is very high for the 3- and 4-membered rings, decreases sharply for 5-, 6-, and 7-membered rings, increases for 8–13-membered rings, and then decreases again for larger rings.

The strain in ring structures is of two types—\textit{angle strain} and \textit{conformational strain}. Ring structures of less than five atoms are highly strained due to the high degree of angle strain,
that is, the large distortion of their bond angles from the normal tetrahedral bond angle. Bond angle distortion is virtually absent in rings of five or more members. For rings larger than five atoms the strain due to bond angle distortion would be excessive for planar rings. For this reason rings larger than five atoms exist in more stable, nonplanar (puckered) forms. The differences in strain among rings of five members and larger are due to differences in conformational strain. The 5- and 7-membered rings are somewhat strained in comparison to the 6-membered ring because of the torsional strain arising from eclipsed conformations on adjacent atoms of the ring. Rings of 8 or more members have transannular strain arising from repulsive interactions between hydrogens or other groups which are forced to crowd positions in the interior of the ring structure. Transannular strain virtually disappears for rings larger than 13 members; the ring becomes sufficiently large to accommodate substituents without transannular repulsions.

The general order of thermodynamic stability of different-sized rings is given by $3, 4 \ll 5, 7–13 < 6, 14$ and larger. This same order of stability is generally observed for a variety of ring structures, including those containing atoms or groups other than methylene. Although data are not as extensive for ring structures such as ethers, lactones, or lactams, the general expectation is borne out. The substitution of an oxygen, carbonyl, nitrogen, or other group for methylene does not appreciably alter the bond angles in the ring structure. Replacement of a methylene group by a less bulky oxygen atom or carbonyl group may, however, slightly increase the stability of the ring structure by a decrease in the conformational strain. It has also been observed that substituents, other than hydrogen, on a ring structure generally increase its stability relative to the linear structure as repulsive interactions between substituents are less severe in the ring structure.

### TABLE 2-7 Heats of Combustion and Strains of Cycloalkanes per Methylene Group$^a$

<table>
<thead>
<tr>
<th>n (CH$_2$)$_n$</th>
<th>Heat of Combustion per Methylene Group (kJ mol$^{-1}$)</th>
<th>Strain per Methylene Group$^b$ (kJ mol$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>697.6</td>
<td>38.6</td>
</tr>
<tr>
<td>4</td>
<td>686.7</td>
<td>27.7</td>
</tr>
<tr>
<td>5</td>
<td>664.5</td>
<td>5.5</td>
</tr>
<tr>
<td>6</td>
<td>659.0</td>
<td>0.0</td>
</tr>
<tr>
<td>7</td>
<td>662.8</td>
<td>3.8</td>
</tr>
<tr>
<td>8</td>
<td>664.1</td>
<td>5.1</td>
</tr>
<tr>
<td>9</td>
<td>664.9</td>
<td>5.9</td>
</tr>
<tr>
<td>10</td>
<td>664.1</td>
<td>5.1</td>
</tr>
<tr>
<td>11</td>
<td>663.2</td>
<td>4.2</td>
</tr>
<tr>
<td>12</td>
<td>660.3</td>
<td>1.3</td>
</tr>
<tr>
<td>13</td>
<td>660.7</td>
<td>1.7</td>
</tr>
<tr>
<td>14</td>
<td>659.0</td>
<td>0.0</td>
</tr>
<tr>
<td>15</td>
<td>659.5</td>
<td>0.5</td>
</tr>
<tr>
<td>16</td>
<td>659.5</td>
<td>0.5</td>
</tr>
<tr>
<td>17</td>
<td>658.2</td>
<td>−0.8</td>
</tr>
<tr>
<td>n-Alkane</td>
<td>659.0</td>
<td>0.0</td>
</tr>
</tbody>
</table>

$^a$ Data from Eliel [1962].

$^b$ Calculated as the heat of combustion per methylene group minus the value (659.0) for the n-alkane methylene group.
In addition to thermodynamics stability kinetic feasibility is important in determining the competitive position of cyclization relative to linear polymerization. Kinetic feasibility for the cyclization reaction depends on the probability of having the functional end groups of the reactant molecules approach each other. As the potential ring size increases, the monomers which would give rise to ring structures have many conformations, very few of which involve the two ends being adjacent. The probability of ring formation decreases as the probability of the two functional groups encountering each other decreases. The effect is reflected in an increasingly unfavorable entropy of activation. Specifically, the kinetic factor becomes less favorable with increasing ring size [Jacobson and Stockmayer, 1950; Semlyen, 1996].

The overall ease of cyclization is thus dependent on the interplay of two factors: (1) the continuous decrease in kinetic feasibility with ring size, and (2) the thermodynamic stability, which varies with ring size as indicated above. From the practical viewpoint of obtaining linear polymer, ring formation in A–B polymerizations is a major problem when the monomer can form a 6-membered ring, that is, when R in Eqs. 2-69 and 2-70 contributes 4 atoms to the ring. With rare exceptions, such monomers do not undergo linear polymerization. Cyclization also predominates at the dimer stage \((n = 2\) and \(1\), respectively, in Eqs. 2-71 and 2-72) for monomers with R and \(R'\) groups containing only one carbon. The extent of cyclization for species larger than dimer (larger \(n\)) depends on the specific reaction conditions. Monomers that can cyclize to 5- and 7-membered rings undergo polymerization, but there is a significant tendency to cyclize–although much less than for monomers that cyclize to 6-membered rings.

### 2-5c Reaction Conditions

High concentrations of monomers favor linear polymerization since cyclization is a unimolecular (intramolecular) reaction, while linear polymerization is a bimolecular (intermolecular) reaction. The ratio of cyclization to linear polymerization varies inversely with the first power of monomer concentration according to

\[
\frac{\text{Cyclization}}{\text{Linear polymerization}} = \frac{k_c[M]}{k_p[M]^2} = \frac{k_c}{k_p[M]} \tag{2-73}
\]

where \(k_c\) and \(k_p\) are the rate constants for cyclization and polymerization, respectively.

There is a crossover phenomenon at \([M] = 1\ M\). From the viewpoint of monomer concentration linear polymerization is favored above 1 \(M\) with cyclization favored below 1 \(M\). The rate constants \(k_c\) and \(k_p\) are also important in determining the competition between linear polymerization and cyclization. \(k_p\) does not change as linear polymerization proceeds (the equal reactivity of functional groups assumption), but \(k_c\) decreases as the linear polymer increases in molecular weight (kinetic feasibility decreases with increasing ring size). The effects of the rate constants and \([M]\) oppose each other and the outcome will be determined by their quantitative interplay in Eq. 2-73. In general, the decrease in \(k_c\) is greater than the decrease in \([M]\) and linear polymerization is still favored over cyclization even at high conversions.

Monomer structure can affect the competition between cyclization and linear polymerization. For example, phthalic acid (ortho isomer) is more prone to cyclization than terephthalic acid (para isomer) at the very-low-molecular-weight end, for example, the dimer stage. The ortho structure makes more likely the conformations that are more favorable for cyclization. Stiff linear chains such as those formed in the reaction between an aromatic diamine and aromatic diacid chloride are much less prone to cyclization than the flexible chains formed from the corresponding aliphatic monomers.
Kricheldorf and coworkers [2001a,b,c] have stressed that step polymerizations can proceed either with kinetic control or thermodynamic control. Polymerizations under thermodynamic control proceed with an equilibrium between cyclic and linear products. Polymerizations under kinetic control proceed without an equilibrium between cyclic and linear products.

The reactions used in most industrial step polymerizations proceed under thermodynamic control, and most frequently the equilibrium favors linear polymerization over cyclization. However, the extent of cyclization, or at least the presence of cyclic products, is not necessarily zero. Although data are not available for a wide range of systems, the total cyclic content in some polymerizations (e.g., polyesterification and polyamidation) has been found to be as high as 1–3% [Goodman, 1988; Semlyen, 1986; Zimmerman, 1988]. (The cyclic content in polysiloxanes is higher; see Sec. 2-12f.) The cyclics present in these polymerizations are generally oligomers with little high-molecular-weight cyclics. Most of the cyclic oligomers are not formed by cyclization reactions between end groups of growing linear polymers (Eqs. 2-71, 2-72) [Kricheldorf and Schwarz, 2003; Kricheldorf et al., 2001a,b,c]. The cyclic oligomers are formed mostly by backbiting, which involves an intramolecular (interchange) nucleophilic substitution reaction, for example, the attack of the hydroxyl end group of a polyester chain on one of its ester carbonyl groups

\[
\text{H} \{ \text{O-RCO} \}_n \text{OH} \rightarrow \{ \text{O-RCO} \}_{m-n} + \text{H} \{ \text{O-RCO} \}_{m-n} \text{OH}
\]  

(2-74)

The presence of even small amounts of cyclic oligomers can be detrimental for the utilization of a polymer if the cyclics migrate out of the product during its use. Many commercial processes remove cyclic by extraction (e.g., with steam in polyamide production) or thermal devolatilization (polysiloxane).

Kinetic control instead of thermodynamic control occurs in reaction systems in which the small-molecule by-product does not react with linkages in the cyclic or linear products. Thus, whereas polyesterification between diacids and diols proceeds with thermodynamic control, polyestyrerization between diacyl chlorides and diols proceeds with kinetic control. The byproduct water in the former reaction is reactive with ester linkages to reverse the reaction. There is no reversal in the latter reaction because the by-product HCl is not reactive with ester linkages. The end result is that there is a continuous increase in cyclic products with increasing conversion even though the rate of cyclization decreases with polymer chain length (which increases with conversion). The cyclic products formed by reaction between end groups of linear chains are inert under the polymerization conditions. Their concentration increases whereas the concentration of linear chains decreases. A number of polymerizations systems with kinetic control have been observed [Kricheldorf et al., 2001a,b,c], almost all of which are not industrial polymerizations. However, Kricheldorf and colleagues reported the presence of considerable cyclic oligomer and polymer in commercial samples of polyethersulfones (Sec. 2-14c), and it may turn out cyclization is important in other industrial polymerizations.

The Carothers equation (Eq. 2-27) has been reformulated as

\[
\bar{X}_n = \frac{1}{1 - p[1 - (1/X^a)]}
\]

(2-75)

to include linear polymerization with varying extents of cyclization. \(X\) is a constant greater than 1 and dependent on the reactant concentration. \(a\) is the ratio of the rate of linear
polymerization to the rate of cyclization. Equation 2-75 shows that cyclization decreases \( \bar{X}_n \) from the value predicted by the Carothers equation. However, the utility of Eq. 2-75 is limited because values of \( X \) and \( a \) are unavailable. When cyclization is negligible, \( a \) is large, and Eq. 2-75 becomes the Carothers equation.

### 2-5e Other Considerations

The previous discussions have concerned rings containing C, C and O, or C and N atoms. The situation regarding the competition between cyclization and linear polymerization as a function of ring size may be altered when other atoms make up the ring structure. Thus in the case of polysiloxanes where the ring structure VIII contains alternating O and Si atoms, rings of less than eight atoms are quite strained because of the large size of the Si atom, the longer length of the Si—O bond, and the larger Si—O—Si bond angle. The optimum ring size is the 8-membered ring, although the preference is not overwhelming because of the kinetic factor. Larger-sized rings are not as favored for the reasons previously discussed.

![Diagram of VIII](image)

### 2-6 MOLECULAR WEIGHT CONTROL IN LINEAR POLYMERIZATION

#### 2-6a Need for Stoichiometric Control

There are two important aspects with regard to the control of molecular weight in polymerizations. In the synthesis of polymers, one is usually interested in obtaining a product of very specific molecular weight, since the properties of the polymer will usually be highly dependent on molecular weight. Molecular weights higher or lower than the desired weight are equally undesirable. Since the degree of polymerization is a function of reaction time, the desired molecular weight can be obtained by quenching the reaction (e.g., by cooling) at the appropriate time. However, the polymer obtained in this manner is unstable in that subsequent heating leads to changes in molecular weight because the ends of the polymer molecules contain functional groups (referred to as end groups) that can react further with each other.

This situation is avoided by adjusting the concentrations of the two monomers (e.g., diol and diacid) so that they are slightly nonstoichiometric. One of the reactants is present in slight excess. The polymerization then proceeds to a point at which one reactant is completely used up and all the chain ends possess the same functional group—the group that is in excess. Further polymerization is not possible, and the polymer is stable to subsequent molecular-weight changes. Thus the use of excess diamine in the polymerization of a diamine with a diacid (Eq. 1-1) yields a polyamide (IX) with amine end groups in the absence of any diacid for further polymerization. The use of excess diacid accomplishes the same result; the polyamide (X) in this case has carboxyl end groups which are incapable of further
reaction, since the diamine has completely reacted.

\[
\begin{align*}
\text{Excess } & \quad H_2NR-NR-NH_2 + HO_2C-R'-CO_2H \\
& \xrightarrow{\text{HR-NHCO-R'-CO}_2} \quad H \left\{ \text{NH-R-NHCO-R'-CO}_2 \right\}_n \text{NH-R-NH}_2
\end{align*}
\]

(2-76a)

IX

\[
\begin{align*}
\text{Excess } & \quad HO_2C-R'-CO_2H + H_2NR-NR-NH_2 \\
& \xrightarrow{\text{HO-C-R'-CONH-R-NH}_2} \quad HO \left\{ \text{CO-R'-CONH-R-NH}_2 \right\}_n \text{CO-R'-COOH}
\end{align*}
\]

(2-76b)

Another method of achieving the desired molecular weight is by addition of a small amount of a monofunctional monomer, a monomer with only one functional group. Acetic acid or lauric acid, for example, are often used to achieve molecular weight stabilization of polyamides. The monofunctional monomer, often referred to as a chain stopper, controls and limits the polymerization of bifunctional monomers because the growing polymer yields chain ends devoid of functional groups and therefore incapable of further reaction. Thus, the use of benzoic acid in the polyamide synthesis yields a polyamide (XI) with phenyl end groups that are unreactive toward polymerization.

\[
\begin{align*}
H_2NR-NR-NH_2 + HO_2C-R'-CO_2H + \phi\text{CO}_2H \\
\phi\text{CO} \left\{ \text{NH-R-NHCO-R'-CO}_2 \right\}_n \text{NHRNHOCO}\phi
\end{align*}
\]

(2-77)

XI

2-6b Quantitative Aspects

In order to properly control the polymer molecular weight, one must precisely adjust the stoichiometric imbalance of the bifunctional monomers or of the monofunctional monomer. If the nonstoichiometry is too large, the polymer molecular weight will be too low. It is therefore important to understand the quantitative effect of the stoichiometric imbalance of reactants on the molecular weight. This is also necessary in order to know the quantitative effect of any reactive impurities that may be present in the reaction mixture either initially or that are formed by undesirable side reactions. Impurities with A or B functional groups may drastically lower the polymer molecular weight unless one can quantitatively take their presence into account. Consider now the various different reactant systems which are employed in step polymerizations:

TYPE 1. For the polymerization of the bifunctional monomers A—A and B—B (e.g., diol and diacid or diamine and diacid) where B—B is present in excess, the numbers of A and B functional groups are given by \(N_A\) and \(N_B\), respectively. \(N_A\) and \(N_B\) are equal to twice the number of A—A and B—B molecules, respectively, that are present. \(r\), called the stoichiometric ratio or imbalance, is always defined to have a value equal to or less than unity but never greater than unit, that is, the B groups are those in excess. The total number of monomer molecules is given by \((N_A + N_B)/2\) or \(N_A(1 + 1/r)/2\).

The extent of reaction \(p\) is defined as the fraction of the limiting groups (A groups) that have reacted at a particular time. The fraction of B groups that have reacted is given by \(rp\). The fractions of unreacted A and B groups are \((1 - p)\) and \((1 - rp)\), respectively. The total numbers of unreacted A and B groups are \(N_A(1 - p)\) and \(N_B(1 - rp)\), respectively. The total number of polymer chain ends is given by the sum of the total number of unreacted
A and B groups. Since each polymer chain has two chain ends, the total number of polymer molecules is one half the total number of chain ends or $\frac{1}{2}N_A(1-p) + N_B(1-rp)$.

The number-average degree of polymerization $\bar{X}_n$ is the total number of $A-A$ and $B-B$ molecules initially present divided by the total number of polymer molecules

$$\bar{X}_n = \frac{N_A(1+1/r)/2}{N_A(1-p) + N_B(1-rp)/2} = \frac{1+r}{1+r-2rp}$$

Equation 2-78 shows the variation of $\bar{X}_n$ with the stoichiometric imbalance $r$ and the extent of reaction $p$. There are two limiting forms of this relationship. When the two bifunctional monomers are present in stoichiometric amounts ($r = 1$), Eq. 2-78 reduces to the previous discussed Carothers relationship (Eq. 2-27)

$$\bar{X}_n = \frac{1}{(1-p)}$$

On the other hand, for 100% conversion ($p = 1$), Eq. 2-78 becomes

$$\bar{X}_n = \frac{(1+r)}{(1-r)}$$

In actual practice, $p$ may approach but never becomes equal to unity.

Figure 2-8 shows plots of $\bar{X}_n$ versus the stoichiometric ratio for several values of $p$ in accordance with Eq. 2-78. The stoichiometric imbalance is expressed as both the ratio $r$ and the mole percent excess of the $B-B$ reactant over the $A-A$ reactant. The various plots show how $r$ and $p$ must be controlled so as to obtain a particular degree of polymerization. However, one does not usually have complete freedom of choice of the $r$ and $p$ values in a polymerization. Complete control of the stoichiometric ratio is not always possible, since reasons of economy and difficulties in the purification of reactants may prevent one from obtaining $r$ values very close to 1.000. Similarly, many polymerizations are carried out to less than 100% completion (i.e., to $p < 1.000$) for reasons of time and economy. The time required to achieve each of the last few percent of reaction is close to that required for the first ~97–98% of reaction. Thus a detailed consideration of Fig. 2-2 shows that the time required to go from $p = 0.97$ ($\bar{X}_n = 33.3$) to $p = 0.98$ ($\bar{X}_n = 50$) is approximately the same as that to reach $p = 0.97$ from the start of reaction.

Consider a few examples to illustrate the use of Eq. 2-78 and Fig. 2-8. For stoichiometric imbalances of 0.1 and 1 mol% ($r$ values of 1000/1001 and 100/101, respectively) at 100% reaction, the values of $\bar{X}_n$ are 2001 and 201, respectively. The degree of polymerization decreases to 96 and 66, respectively, at 99% reaction and to 49 and 40 at 98% reaction. It is clear that step polymerizations will almost always be carried out to at least 98% reaction, since a degree of polymerization of at least approximately 50–100 is usually required for a useful polymer. Higher conversions and the appropriate stoichiometric ratio are required to obtain higher degrees of polymerization. The exact combination of $p$ and $r$ values necessary to obtain any particular degree of polymerization is obtained from Fig. 2-8 and Eq. 2-78. One can also calculate the effect of losses of one reactant or both during the polymerization through volatilization, or side reactions. The precision required in the control of the stoichiometric ratio in a polymerization is easily found from Eq. 2-78. An error in the experimentally employed $r$ value yields a corresponding error in $\bar{X}_n$. The shape of the plots in Fig. 2-8 shows that the effect of an error in $r$, however, is progressively greater at higher degrees of polymerization. Progressively greater control is required to synthesize the higher-molecular-weight polymer.
MOLECULAR WEIGHT CONTROL IN LINEAR POLYMERIZATION

TYPE 2. The control of the degree of polymerization in the polymerization of an equimolar mixture \( A / C_0 / A \) and \( B / C_0 / B \) by the addition of small amounts of a monofunctional reactant, for example, \( B / C_0 / B \), has been described above. The same equations that apply to a type 1 polymerization are also applicable here, except that \( r \) must be redefined as

\[
r = \frac{N_A}{N_B + 2N_B'}
\]

where \( N_B' \) is the number of B molecules present and \( N_A = N_B \). The coefficient 2 in front of \( N_B' \) is required since one B molecule has the same quantitative effect as one excess \( B - B \)

\[\text{Fig. 2-8} \quad \text{Dependence of the number-average degree of polymerization } \overline{X}_n \text{ on the stoichiometric ratio } r \text{ for different extents of reaction } p \text{ in the polymerization of } A - A \text{ with } B - B.\]

\[\text{TYPE 2. The control of the degree of polymerization in the polymerization of an equimolar mixture } A - A \text{ and } B - B \text{ by the addition of small amounts of a monofunctional reactant, for example, } B, \text{ has been described above. The same equations that apply to a type 1 polymerization are also applicable here, except that } r \text{ must be redefined as }\]

\[
r = \frac{N_A}{N_B + 2N_B'}
\]

\[\text{where } N_B' \text{ is the number of B molecules present and } N_A = N_B. \text{ The coefficient 2 in front of } N_B' \text{ is required since one B molecule has the same quantitative effect as one excess } B - B.\]
molecule in limiting the growth of a polymer chain. Equations 2-78 to 2-80 do not apply to type 2 systems unless equimolar amounts of A—A and B—B are present. Other situations are correctly analyzed only by Eqs. 2-137 and 2-139 in Sec. 2-10a.

**TYPE 3.** Polymerizations of A—B type monomers such as hydroxy and amino acids automatically take place with internally supplied stoichiometry. For such a polymerization Eqs. 2-78 and 2-79 apply with \( r \) equal to 1. This leads to a polymer product that is subsequently unstable toward molecular weight changes because the end groups of the polymer molecules can react with each other. Molecular weight stabilization is usually accomplished by using a monofunctional B reactant. In this latter case the same equations apply with \( r \) redefined as

\[
N_A = \frac{N_A}{N_B + 2N_B'}
\]

(2-81)

where \( 2N_B' \) has the same meaning as in a type 2 polymerization, and \( N_A = N_B = \) the number of A—B molecules. (Bifunctional A—A or B—B monomers can also be employed to control molecular weight in this polymerization.)

The plots in Fig. 2-8 apply equally well to polymerizations of types 1, 2, and 3, although the scale of the \( x \) axis may be different. When the \( x \) axis is expressed as the stoichiometric ratio \( r \) the scale is exactly the same for all three types of polymerization. Different scales will be applicable when the \( x \) axis is expressed in terms of the mole percent excess of the molecular weight controlling reactant. Thus, the \( x \) axis is shown as the mole percent excess of the B—B reactant for type 1 polymerizations. For polymerizations of type 2 when \( N_A = N_B \) and those of type 3, the \( x \) axis is shown as the mole percent excess of B groups. The two \( x \) axes differ by a factor of 2 because one B—B molecule is needed to give the same effect as one B molecule. The relationship between the degree of polymerization and the stoichiometric ratio (Eqs. 2-78 through 2-81 and Fig. 2-8) has been verified in a large number of step polymerizations. Its verification and use for molecular weight control has been reviewed in several systems, including polyamides, polyesters, and polybenzimidazoles [Korshak, 1966]. The effect of excess bifunctional reactants as well as monofunctional reactants follows the expected behavior.

The discussion in this section, including the derivations of Eqs. 2-78 through 2-80 assumes that the initial stoichiometric ratio of reactants is the effective stoichiometric ratio throughout the polymerization from start to finish. However, this is seldom the case, as there may be losses of one or all reactants as polymerization proceeds. Losses are of two types. Monomer loss due to volatilization is not uncommon, since moderately high reaction temperatures are often used. For example, volatilization losses of the diamine reactant are a problem in polyamidation because of the much higher vapor pressure of diamine compared to the diacid. The extent of this loss depends on the particular diamine used, the specific reaction conditions (temperature, pressure) and whether the polymerization reactor has provision for preventing or minimizing the losses. Aside from volatilization losses, the other pathway by which reactant losses occur is by side reactions. Many polymerization systems involve reactants that can undergo some reaction(s) other than polymerization. Specific examples of such side reactions are described in Secs. 2-8, 2-12, and 2-14. Polymerization conditions usually involve a compromise between conditions that yield the highest reaction rates and those that minimize side reactions and volatilization losses. Because of the very large effect of \( r \) on polymer molecular weight, this compromise may be much closer to reaction conditions that minimize any change in \( r \). An alternate and/or simultaneous approach involves adjusting the stoichiometric imbalance by a continuous or batchwise replenishment of the
“lost” reactant. The amount of added reactant must be precisely calculated based on a chemical analysis of the \( r \) value for the reaction system as a function of conversion. Also the additional amount of the “lost” reactant must be added at the appropriate time. Premature addition or the addition of an incorrect amount results in performing the polymerization at other than the required stoichiometric ratio.

There is a reaction condition in which high polymer molecular weights have been obtained independent of the stoichiometric ratio—when one of the two monomers is only slightly soluble in the reaction mixture and is present in excess. An example is the reaction of \( \text{bis}(o\text{-aminophenol}) \) with terephthalic acid in polyphosphoric acid (Sec. 2-14h) [So, 2001]. \( \text{Bis}(o\text{-aminophenol}) \) is soluble but terephthalic acid is only slightly soluble in the reaction mixture. At any instant the polymer chain ends are those from the soluble monomer \( \text{bis}(o\text{-aminophenol}) \), but these chain ends react quickly with the small amount of dissolved terephthalic acid, and then there is reaction again with \( \text{bis}(o\text{-aminophenol}) \). Polymerization proceeds to high molecular weight because there is a continuous dissolution of terephthalic acid to maintain its saturation concentration. On the other hand, high molecular weights are not achieved when the soluble monomer is present in excess. Similar results have been reported for the polymerization of terephthalic acid with ethylene glycol, \( p\text{-dichlorobenzene} \) with sodium sulfide, and some aromatic diacid chlorides with aromatic diamines [Goodman, 1988; Liou and Hsiao, 2001a].

### 2-6c Kinetics of Nonstoichiometric Polymerization

The kinetics of polymerizations involving nonstoichiometric amounts of A and B functional groups can be handled in a straightforward manner. Consider the external acid-catalyzed A—A plus B—B polymerization with \( r < 1 \). The polymerization rate, defined as the rate of disappearance of the functional groups present in deficient amount, is given by

\[
\frac{-d[A]}{dt} = k[A][B]
\]

(2-82)

The following stoichiometry holds:

\[
[A]_0 - [A] = [B]_0 - [B]
\]

(2-83)

where \([A]_0\) and \([B]_0\) are the initial concentrations of A and B groups. Combination of Eqs. 2-82 and 2-83 followed by integration [Moore and Pearson, 1981] yields

\[
\frac{1}{[B]_0 - [A]_0} \ln \left[ \frac{[A]_0[B]}{[B]_0[A]} \right] = kt
\]

(2-84)

which is combined with \( r = \frac{[A]_0}{[B]_0} \) to give

\[
\ln \frac{[B]}{[A]} = -\ln r + [B]_0(1 - r)kt
\]

(2-85)

A plot of \( \ln \left( \frac{[B]}{[A]} \right) \) versus \( t \) is linear with a positive slope of \( [B]_0(1 - r)k \) and an intercept of \( -\ln r \).

When \( r \) is close to unity the polymerization rate is adequately described by the expressions in Secs. 2-2a and 2-2b for the case of \( r = 1 \). Only when \( r \) is considerably different from unity does it become necessary to use Eq. 2-85 or its equivalent. Most step polymerizations
are carried out with close to stoichiometric amounts of the two reacting functional groups. The main exceptions to this generalization are some of the reaction systems containing polyfunctional reactants (Secs. 2-10 and 2-12).

2-7 MOLECULAR WEIGHT DISTRIBUTION IN LINEAR POLYMERIZATION

The product of a polymerization is a mixture of polymer molecules of different molecular weights. For theoretical and practical reasons it is of interest to discuss the distribution of molecular weights in a polymerization. The molecular weight distribution (MWD) has been derived by Flory by a statistical approach based on the concept of equal reactivity of functional groups [Flory, 1953; Howard, 1961; Peebles, 1971]. The derivation that follows is essentially that of Flory and applies equally to \( A-B \) and stoichiometric \( A-A \) plus \( B-B \) types of step polymerizations.

2-7a Derivation of Size Distributions

Consider the probability of finding a polymer molecule containing \( x \) structural units. This is synonymous with the probability of finding a molecule with \( (x - 1) \) \( A \) groups reacted and one \( A \) group unreacted. The probability that an \( A \) group has reacted at time \( t \) is defined as the extent of reaction \( p \). The probability that \( (x - 1) \) \( A \) groups have reacted is the product of \( (x - 1) \) separate probabilities or \( p^{x-1} \). Since the probability of an \( A \) group being unreacted is \( (1 - p) \), the probability \( N_x \) of finding the molecule in question, with \( x \) structural units, is given by

\[
N_x = p^{x-1}(1 - p)
\]  

(2-86)

Since \( N_x \) is synonymous with the mole or number fraction of molecules in the polymer mixture that are \( x \)-mers (i.e., that contain \( x \) structural units), then

\[
N_x = Np^{x-1}(1 - p)
\]  

(2-87)

where \( N \) is the total number of polymer molecules and \( N_x \) is the number that are \( x \)-mers. If the total number of structural units present initially is \( N_0 \), then \( N = N_0(1 - p) \) and Eq. 2-87 becomes

\[
N_x = N_0(1 - p)^2p^{x-1}
\]  

(2-88)

Neglecting the weights of the end groups, the weight fraction \( w_x \) of \( x \)-mers (i.e., the weight fraction of the molecules that contains \( x \) structural units) is given by \( w_x = xN_x/N_0 \) and Eq. 2-88 becomes

\[
w_x = x(1 - p)^2p^{x-1}
\]  

(2-89)

Equations 2-86 and 2-89 give the number- and weight-distribution functions, respectively, for step polymerizations at the extent of polymerization \( p \). These distributions are usually referred to as the most probable or Flory or Flory–Schulz distributions. Plots of the two distribution functions for several values of \( p \) are shown in Figs. 2-9 and 2-10. It is seen that on a
number basis there are more monomer molecules than any polymer species regardless of the extent of reaction. Although the number of monomer molecules decreases as $p$ increases, they are still the most plentiful species. The situation is quite different for the weight distribution of molecular weights. On a weight basis, the proportion of low-molecular-weight species is very small and decreases as $p$ increases. The maxima in Fig. 2-10 occur at $x = -(1/\ln p)$, which is very near the number-average degree of polymerization given by Eq. 2-27.

The experimental determination of a molecular weight distribution is frequently obtained in an integral form in which the combined or cumulative weight fraction $I_x$ of all polymer molecules having degrees of polymerization up to and including $x$ are plotted against $x$. For this purpose it is useful to express the Flory distribution function in terms of $I_x$. This is done by summing $w_x$ values from Eq. 2-89

$$I_x = \sum w_x = (1 - p)^2 \sum x p^{x-1} \quad (2-90)$$

![Fig. 2-9](image) Number-fraction distribution curve for linear polymerization. Plot 1, $p = 0.9600$; plot 2, $p = 0.9875$; plot 3, $p = 0.9950$. After Howard [1961] (by permission of Iliffe Books, London and Elsevier, Oxford).

![Fig. 2-10](image) Weight fraction distribution plot for linear polymerization. Plot 1, $p = 0.9600$; plot 2, $p = 0.9875$; plot 3, $p = 0.9950$. After Howard [1961] (by permission of Iliffe Books, London and Elsevier, Oxford).
for all values of $x$ from 1 to $x$ to yield

$$I_x = 1 - p^x - xp^x(1 - p) \quad (2.91)$$

The limit of $I_x$ at high values of $x$ is 1 and is reached at progressively higher values of $x$ for higher conversions.

### 2-7b Breadth of Molecular Weight Distribution

The number- and weight-average degree of polymerization $X_n$ and $X_w$ can be derived from the number and weight distribution functions, respectively. The number- and weight-average molecular weights have been defined by Eqs. 1-15 and 1-17. Dividing Eq. 1-15 by the weight $M_o$ of a structural unit yields the number-average degree of polymerization as

$$X_n = \frac{\sum N_i}{\sum N_i} = \frac{\sum N_i}{N_x} \quad (2.92)$$

where the summations are over all values of $x$. Combination of Eqs. 2-86 and 2-92 gives

$$X_n = \sum x p^{x-1} (1 - p) \quad (2.93)$$

Evaluation of this summation yields

$$X_n = \frac{1}{(1 - p)} \quad (2.27)$$

which is the same result obtained earlier. Dividing Eq. 1-17 by $M_o$ yields

$$X_w = \sum w_x \quad (2.94)$$

Combination of Eqs. 2-89 and 2-94 gives

$$X_w = \sum x^2 p^{x-1} (1 - p)^2 \quad (2.95)$$

which is evaluated as

$$X_w = \frac{(1 + p)}{(1 - p)} \quad (2.96)$$

The **breadth of the molecular weight distribution** is then given by

$$\frac{X_w}{X_n} = (1 + p) \quad (2.97)$$

The ratio $X_w/X_n$ is synonymous with the ratio $M_w/M_n$ discussed in Sec. 1-4. It is a measure of the polydispersity of a polymer sample. The value of $X_w/X_n$ increases with the extent of reaction and approaches 2 in the limit of large extents of reaction. The ratio $X_w/X_n$ is also referred to as the **polydispersity index** (PDI).

The most probable distribution of Flory is generally well established, although its experimental verification has been somewhat limited. Direct evidence for the most probable
distribution requires the fractionation of polymer samples followed by molecular-weight measurements on the fractions to allow the construction of experimental plots of $N_x$, $w_x$, $I_n$ versus $x$ for comparison with the theoretical plots. The experimental difficulties involved in polymer fractionation previously limited the number of polymerizations that had been extensively studied. The availability of automated size exclusion chromatography (SEC), also referred to as gel permeation chromatography (GPC), has significantly increased the available data on molecular-weight distributions of polymers. (The availability of calibration standards for only certain polymers is a limiting factor for size exclusion chromatography. However, the combination of SEC with osmometry and light-scattering measurements of molecular weight offers a powerful combination for examining polymer size distributions.) The Flory distribution has been experimentally verified for a number of step polymerizations, including polyamides and polyesters. Less direct verification of the most probable distribution has been made in many instances by determining the ratio $X_w/X_n$. For many different step polymerizations, this ratio has been found to be close to 2 as required by Eq. 2-97.

**2-7c Interchange Reactions**

Some polymers (polyesters, polyamides, polysulfides, and others) undergo interchange reactions under appropriate conditions. Interchange involves reaction between the terminal functional group of one polymer molecule with the interunit repeating linkage of another polymer molecule, for example, between the terminal $-\text{NH}_2$ and interunit $-\text{CONH}$ groups of polyamide molecules. Two polymer chains may react to yield one shorter and one longer chain,

$$H\text{NH} - R\text{CO} - \text{OH}_n + H\text{NH} - R\text{CO} - \text{OH}_m \rightarrow H\text{NH} - R\text{CO} - \text{OH}_w + H\text{NH} - R\text{CO} - \text{OH}_z \quad (2-98)$$

If free interchange occurs, the molecular weight distribution will be the Flory distribution described by Eqs. 2-86 and 2-89. Free interchange corresponds to all interunit linkages in all polymer molecules having equal probabilities of interchange. This is analogous to the concept of functional group reactivity independent of molecular size as applied to the interchange reaction. It is apparent that the presence of interchange during a polymerization will not affect the size distribution from that expected for the random polymerization. The Flory or most probable distribution is also that expected for the random scission of the interunit linkages of polymer chains, for example, in the hydrolysis of cellulose.

**2-7d Alternate Approaches for Molecular-Weight Distribution**

A number of treatments other than that by Flory have been given for the molecular weight distributions in linear step polymerizations [Burchard, 1979; Durand and Bruneau, 1979a,b]. However, a knowledge of the average properties ($\bar{M}_n$, $\bar{M}_w$, and PDI) is often sufficient for many practical purposes. Macosko and Miller [1976] developed a useful statistical approach for obtaining the average properties without the need to calculate the molecular weight distributions. This approach will be described for a polymerization system composed of $A\rightarrow A$, $B\rightarrow B$, and $B'\rightarrow B'$ where A groups can react with B groups and with B' groups [Ozizmir and Odian, 1980]. To keep the system as simple as possible, the molecular weights of the three structural units are taken as equal (and denoted by $M_0$) and the initial system contains equimolar amounts of $B\rightarrow B$ and $B'\rightarrow B'$ monomers where the total moles of $A\rightarrow A$ is equal to the sum of $B\rightarrow B$ and $B'\rightarrow B'$. 
The expected masses of polymers which contain a randomly selected A, B, or B’ group in the system are denoted by \(w_A\), \(w_B\), and \(w_{B'}\). In order to obtain these quantities it is convenient to introduce the quantities \(w^i_A\), \(w^o_A\), \(w^i_B\), \(w^o_B\), \(w^i_{B'}\), and \(w^o_{B'}\). Here \(w^i_A\) represents the expected mass attached to a randomly selected A group in the system looking inward toward the other A group of the A–A structural unit of which it is a part and \(w^o_A\) represents the expected mass attached looking outward from the randomly selected A group as shown in XII. Similarly, \(w^i_B\), \(w^o_B\), \(w^i_{B'}\), and \(w^o_{B'}\) represent the expected inward and outward masses attached to B and B’ groups.

\[
\begin{align*}
A & \rightarrow AB \rightarrow B \\
\text{XII}
\end{align*}
\]

The following relationships hold for this system:

\[
\begin{align*}
w_A &= w^i_A + w^o_A \\
w_B &= w^i_B + w^o_B \\
w_{B'} &= w^i_{B'} + w^o_{B'} \\
w^i_A &= M_o + w^o_A \\
w^o_A &= \frac{p_A \left( \frac{p_B w^i_B}{(p_B + p_{B'})} + \frac{p_B w^i_{B'}}{(p_B + p_B')} \right)}{2} \\
w^i_B &= M_o + w^o_B \\
w^o_B &= p_B w^i_A \\
w^i_{B'} &= M_o + w^o_{B'} \\
w^o_{B'} &= p_{B'} w^i_A \\
p_A &= \frac{(p_B + p_{B'})}{2}
\end{align*}
\]

Most of these relationships are simple material balance statements. Equations 2-99 through 2-101 state that the total mass of polymer attached to an A, B, or B’ group is the sum of the inward and outward masses attached to that group. Equations 2-102, 2-104, and 2-106 state that the difference between the inward and outward masses attached to a group is \(M_o\). Equation 2-107 indicates that the polymer mass attached to a B’ group looking outward from the B’ group equals the probability of that group having reacted with an A group multiplied by the mass of polymer attached to the A group looking inward from that A group. The corresponding descriptions for \(w^o_A\) and \(w^o_B\) are Eqs. 2-103 and 2-105.

Equations 2-102 through 2-108 can be solved and their results combined with Eqs. 2-99 through 2-101 to yield

\[
\begin{align*}
w_A &= U - M_o \\
w_B &= M_o + p_B U \\
w_{B'} &= M_o + p_{B'} U
\end{align*}
\]
where

\[ U = 2w_A = \frac{2M_o + (p_B M_o + p_{B'} M_o)}{1 - (p_B^2 + p_{B'}^2)/2} \]  

(2-110)

The weight-average molecular weight, obtained by a weight averaging of \( w_A, w_B, \) and \( w_{B'} \), is given by

\[ M_w = \frac{w_A}{2} + \frac{w_B}{4} + \frac{w_{B'}}{4} \]  

(2-111)

which yields

\[ M_w = M_o \frac{(2 + p_B + p_{B'})^2}{4 \left(1 - (p_B^2 + p_{B'}^2)/2\right)} \]  

(2-112)

on substitution for \( w_A, w_B, \) and \( w_{B'} \). The number-average molecular weight, obtained by dividing the total number of moles of reactants initially present divided by the total present at any time, yields

\[ \overline{M_n} = \frac{M_n}{1 - p_A} \]  

(2-29)

It is useful to introduce the fractions of unreacted A, B, and \( B' \) functional groups

\[ \alpha = 1 - p_A \]  

(2-113a)

\[ \beta = 1 - p_B \]  

(2-113b)

\[ \gamma = 1 - p_{B'} \]  

(2-113c)

For the case where \( B \) and \( B' \) groups have the same reactivity:

\[ \gamma = \beta \]  

(2-114)

Combination of Eqs. 2-108, 2-112 through 2-114, and 2-29 yields the polydispersity index as

\[ \text{PDI} = \frac{(2 - \alpha)^3}{2 - (\beta^2 + \gamma^2)/2\alpha} \]  

(2-115)

Equation 2-115 yields PDI as a function of conversion in a straightforward manner without having to solve differential equations to obtain the number- and weight-average molecular weight distributions. One need only take a set of \( \beta \) values and then calculate the corresponding \( \gamma, \alpha, \) and PDI values from Eqs. 2-114 and 2-115. The limit of PDI at complete conversion \( (p_A = 1, \alpha = 0) \) is 2 as for the Flory distribution. The Macosko-Miller method has also been applied to other polymerizations, including the \( A/B + A'/B' \) system. In addition to being a simpler method for obtaining the average properties compared to the Flory and similar methods, it more readily allows an evaluation of the effect of various reaction parameters such as unequal group reactivity or nonstoichiometric amounts of reactants on \( \overline{M_n}, \overline{M_w}, \) and PDI (see Sec. 2-7e).
2-7e Effect of Reaction Variables on MWD

2-7e-1 Unequal Reactivity of Functional Groups

The molecular weight distribution and/or PDI has been described for several cases where the assumption of equal reactivity of functional groups is not valid. Unequal reactivity is easily handled by the Macosko–Miller method. For the A–A + B–B + B′–B′ system described in the previous section, we simply redefine the relationship between β and γ by

\[ \gamma = \beta^s \] (2-47)

(which was derived previously in Sec. 2-2d-2) where s is the ratio of rate constants for reaction of B’ and B groups [Ozizmir and Odian, 1980].

The polydispersity index increases (for conversions <100%) when the reactivities of B and B’ groups are different compared to the case where the reactivities are the same. The opposite trend is found for the A–A + B–B’ system [Gandhi and Babu, 1979, 1980]. There is a basic difference between the two- and the three-species reaction systems. In the three-species system, when B’ groups have higher reactivity than B groups, the B’–B’ monomer continues polymerization with A–A monomer, independently of the B–B monomer, to form large-sized polymer chains. In the two-species system, long chains cannot be formed without participation of B groups in the polymerization process. The extents of the broadening and narrowing effects in the two systems increase as the difference in reactivities of B and B’ become larger. The effects are significant at low conversions; for instance, PDI is 2.10 at 50% conversion for the three-species system when B’ is 20-fold more reactive than B compared to a PDI of 1.50 for the equal reactivity case. However, the PDI at complete conversion equals 2 in both the two- and three-species systems, which is the same limit as for the equal-reactivity case.

2-7e-2 Change in Reactivity on Reaction

An increase in the reactivity of one functional group in a bifunctional reactant on reaction of the other functional group results in an increase in PDI [Gandhi and Babu, 1979, 1980]. The PDI at complete conversion exceeds 2 when there is a greater than twofold increase in reactivity. PDI decreases when there is a decrease in reactivity of one functional group on reaction of the other group but the PDI at complete conversion is 2. The same trends are found but are more exaggerated when functional group reactivity varies continuously with molecular size [Gupta et al., 1979a,b; Nanda and Jain, 1968].

2-7e-3 Nonstoichiometry of Functional Groups

Using the Macosko–Miller approach for the A–A + B–B + B′–B’ system, we introduce \( r_1 \) and \( r_2 \)

\[ r_1 = \frac{[B_0]}{[A_0]} \] (2-116a)

\[ r_2 = \frac{[B'_0]}{[A_0]} \] (2-116b)

\[ p_A = r_1 p_B + r_2 p_{B'} \] (2-116c)
to describe the relative amounts and extents of reaction of the three reactant groups and reformulate Eqs. 2-103 and 2-110 as

\[ w_A^0 = (p_B r_1 w_B^0 + p_B r_2 w_B^0) \]  

\[ U = 2 w_A^0 = \frac{2M_A + (p_B r_1 M_A + p_B r_2 M_A)}{1 - (p_B^2 r_1 + p_B^2 r_2)/2} \]

The expressions for \( M_w, M_n \), and PDI are complicated but can be solved numerically [Ozizmir and Odian, 1990]. When B and B' groups together are in excess over A groups \((r_1 + r_2 > 1)\) and the reactivities of B and B' are the same \((s = 1)\), PDI is very slightly decreased at all conversions in comparison to the stoichiometric case \((r_1 + r_2 = 1)\). The final PDI is 1.98. For \( s > 1 \) (B' more reactive than B), PDI is initially decreased but increases with conversion and the final PDI is above 2. The trends are more exaggerated when B' is in excess over B and less exaggerated when B is in excess over B'. For example, for the case \( r_1 + r_2 = 1.25, s = 20 \), the final PDI is 2.63, 6.50, and 2.16, respectively, when \( r_1/r_2 \) is 1, 3, and \( \frac{1}{3} \). When A groups are in excess over B and B', PDI is very slightly decreased at all conversions in comparison to the stoichiometric case. The final PDI is 1.98 independent of \( s, r_1/r_2, \) and \( (r_1 + r_2) \).

Nonstoichiometric amounts of reactants decrease PDI at all conversions for A—A + B—B' polymerizations [Gandi and Babu, 1979, 1980]. The decrease in PDI is greater the larger the difference in the reactivities of B and B' groups when B—B' is in excess over A—A. The decrease in PDI is independent of the difference in reactivities of B and B' when A—A is in excess. The trend is the same with A—A in excess when B and B' have the same initial reactivity but the reactivity of each group changes on reaction of the other. However, a different trend is seen when B—B' is in excess. PDI increases with a limiting value at complete conversion of 2 or greater than 2 depending on whether the difference in reactivity of B and B' is less than or greater than 2.

### 2-8 PROCESS CONDITIONS

#### 2-8a Physical Nature of Polymerization Systems

Several considerations are common to all processes for step polymerizations in order to achieve high molecular weights. One needs to employ a reaction with an absence or at least a minimum of side reactions, which would limit high conversions. Polymerizations are carried out at high concentrations to minimize cyclization and maximize the reaction rate. High-purity reactants in stoichiometric or near-stoichiometric amounts are required. The molecular weight is controlled by the presence of controlled amounts of monofunctional reagents or an excess of one of the bifunctional reagents. Equilibrium considerations are also of prime importance. Since many step polymerizations are equilibrium reactions, appropriate means must be employed to displace the equilibrium in the direction of the polymer product. Distillation of water or other small molecule products from the reaction mixture by suitable reaction temperatures and reduced pressures are often employed for this purpose.

Table 2-8 shows values of some kinetic and thermodynamic characteristics of typical step polymerizations [Bekhli et al., 1967; Chelnokova et al., 1949; Fukumoto, 1956; Hamann et al., 1968; Malhotra and Avinash, 1975, 1976; Ravens and Ward, 1961; Saunders and Dobinson, 1976; Stevenson, 1969; Ueberreiter and Engel, 1977]. These data have implications on the temperature at which polymerization is carried out. Most step polymerizations
<table>
<thead>
<tr>
<th>Reactantsa</th>
<th>$T$ (°C)</th>
<th>$k 	imes 10^3$ (L mol$^{-1}$ s$^{-1}$)</th>
<th>$E_a$ (kJ mol$^{-1}$)</th>
<th>$\Delta H$ (kJ mol$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Polyester</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>HO(CH$<em>2$)$</em>{10}$OH + HOOC(CH$_2$)$_2$COOH</td>
<td>161</td>
<td>$7.5 \times 10^{-2}$</td>
<td>59.4</td>
<td></td>
</tr>
<tr>
<td>HO(CH$<em>2$)$</em>{10}$OH + HOOC(CH$_2$)$_2$COOH$^c$</td>
<td>161</td>
<td>1.6</td>
<td></td>
<td></td>
</tr>
<tr>
<td>HOCH$_2$CH$_2$OH + p-HOOC−φ−COOH</td>
<td>150</td>
<td>−</td>
<td>−10.9</td>
<td></td>
</tr>
<tr>
<td>HO(CH$_2$)$_2$OH + ClO(C(H$_2$)$_2$COCl</td>
<td>58.8</td>
<td>2.9</td>
<td>41</td>
<td></td>
</tr>
<tr>
<td>$p$-HOCH$_2$C$_6$H$_4$OCO−φ−COOCH$_2$CH$_2$OH</td>
<td>275</td>
<td>0.5</td>
<td>188</td>
<td></td>
</tr>
<tr>
<td>$p$-HOCH$_2$C$_6$H$_4$OCO−φ−COOCH$_2$CH$_2$OH$^d$</td>
<td>275</td>
<td>10</td>
<td>58.6</td>
<td></td>
</tr>
<tr>
<td>Polyamide</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>H$_2$N(CH$_2$)$_6$NH$_2$ + HOOC(CH$_2$)$_2$COOH</td>
<td>185</td>
<td>1.0</td>
<td>100.4</td>
<td></td>
</tr>
<tr>
<td>Piperazine + $p$-Cl−CO−φ−CO−Cl</td>
<td></td>
<td>$10^7 − 10^8$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>H$_2$N(CH$_2$)$_6$COOH</td>
<td>235</td>
<td></td>
<td>−24</td>
<td></td>
</tr>
<tr>
<td>Polyurethane</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$m$-OCN−φ−NCO + HOCH$_2$CH$_2$OCO(CH$_2$)$_6$COOCH$_2$CH$_2$OH</td>
<td>60</td>
<td>0.40$^e$</td>
<td>31.4</td>
<td></td>
</tr>
<tr>
<td>$p$-OCN−φ−NCO + HOCH$_2$CH$_2$OCO(CH$_2$)$_6$COOCH$_2$CH$_2$OH</td>
<td>60</td>
<td>0.23$^f$</td>
<td>35.0</td>
<td></td>
</tr>
<tr>
<td>Phenol-formaldehyde polymer</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>φ−OH + H$_2$CO$^c$</td>
<td>75</td>
<td>1.1$^g$</td>
<td>77.4</td>
<td></td>
</tr>
<tr>
<td>φ−OH + H$_2$CO$^h$</td>
<td>75</td>
<td>0.048$^g$</td>
<td>76.6</td>
<td></td>
</tr>
</tbody>
</table>

$^a$ Uncatalyzed unless otherwise noted.

$^b$ 1 cal = 4.184 J.

$^c$ Acid-catalyzed.

$^d$ Catalyzed by Sb$_2$O$_3$.

$^e$ $k_1$ value.

$^f$ $k_2$ value.

$^g$ Average $k$ for all functional groups.

$^h$ Base-catalyzed.
proceed at relatively slow rates at ordinary temperatures. High temperatures in the range of 150–200°C and higher are frequently used to obtain reasonable polymerization rates. Table 2-8 shows that the rate constants are not large even at these temperatures. Typical rate constants are of the order of $10^{-3}$ L mol$^{-1}$ s$^{-1}$. There are a few exceptions of step polymerizations with significantly larger $k$ values, for example, the polymerization reaction between acid halides and alcohols. The need to use higher temperatures can present several problems, including loss of one or the other reactant by degradation or volatilization. Oxidative degradation of polymer is also a potential problem in some cases. The use of an inert atmosphere (N$_2$, CO$_2$) can minimize oxidative degradation.

*Bulk or mass polymerizations* is the simplest process for step polymerizations, since it involves only the reactants and whatever catalyst, if any, which is required [Menikheim, 1988]. There is a minimum of potentialities for contamination, and product separation is simple. Bulk polymerization is particularly well suited for step polymerization because high-molecular-weight polymer is not produced until the very last stages of reaction. This means that the viscosity is relatively low throughout most of the course of the polymerization and mixing of the reaction mixture is not overly difficult. Thermal control is also relatively easy, since the typically reaction has both a modest activation energy $E_a$ and enthalpy of polymerization $\Delta H$. Although some step polymerizations have moderately high activation energies, for example, 100.4 kJ mol$^{-1}$ for the polymerization of sebacic acid and hexamethylene diamine (Table 2-8), the $\Delta H$ is still only modestly exothermic. The exact opposite is the case for chain polymerizations, which are generally highly exothermic with high activation energies and where the viscosity increases much more rapidly. Thermal control and mixing present much greater problems in chain polymerizations.

Bulk polymerization is widely used for step polymerizations. Many polymerizations, however, are carried out in *solution* with a solvent present to solubilize the reactants, or to allow higher reaction temperatures to be employed, or as a convenience in moderating the reaction and acting as a carrier.

### 2-8b Different Reactant Systems

For many step polymerizations there are different combinations of reactants that can be employed to produce the same type of polymer (Table 1-1). Thus the polymerization of a hydroxy acid yields a polymer very similar to (but not the same as) that obtained by reacting a diol and diacid:

$$n\text{HO} - \text{R} - \text{CO}_2\text{H} \quad \rightarrow \quad \text{H}_\text{n} \{\text{O} - \text{R} - \text{CO}_2\} \text{OH} + (n-1)\text{H}_2\text{O}$$  \hspace{1cm} (2-119)

$$n\text{HO} - \text{R} - \text{OH} + n\text{HO}_2\text{C} - \text{R} - \text{CO}_2\text{H} \quad \rightarrow \quad \text{HO}_\text{n} \{\text{R} - \text{OCO} - \text{R} - \text{COO}\} \text{H} + (2n-1)\text{H}_2\text{O}$$  \hspace{1cm} (2-120)

On the other hand, it is apparent that there are different reactant systems that can yield the exact same polymer. Thus the use of the diacid chloride or anhydride instead of the diacid in Eq. 2-120 would give exactly the same polymer product. The organic chemical aspects of the synthesis of various different polymers by different step polymerization processes have been discussed [Elias, 1984; Lenz, 1967; Morgan, 1965]. Whether one particular reaction or another is employed to produce a specific polymer depends on several factors. These include the availability, ease of purification, and properties (both chemical and physical) of the different reactants and whether one or another reaction is more devoid of destructive side reactions.
The ability to obtain high-molecular-weight polymer from a reaction depends on whether the equilibrium is favorable. If the equilibrium is unfavorable as it is in many instances, success depends on the ease with which the polymerization can be driven close to completion. The need for and the ease of obtaining and maintaining stoichiometry in a polymerization is an important consideration. The various requirements for producing a high polymer may be resolved in quite different ways for different polymers. One must completely understand each type of polymerization reaction so as to appropriately meet the stringent requirements for the synthesis of high-molecular-weight polymer. Various step polymerizations are described below and serve to illustrate how the characteristics of a polymerization reaction are controlled so as to obtain high polymer.

2-8c Interfacial Polymerization

Many of the polymers that are produced by the usual high-temperature reactions could be produced at lower temperatures by using the faster Schotten–Baumann reactions of acid chlorides. Thus polyesters and polyamides could be produced by replacing the diacid or diester reactant by the corresponding diacyl chloride

$$n\text{ClCO} \cdot \text{R} \cdot \text{COCl} + n\text{HO} \cdot \text{R}^-' \cdot \text{OH} \rightarrow \left(\text{CO} \cdot \text{R} \cdot \text{CO} \cdot \text{R}^-' \cdot \text{O}\right)_n + 2n\text{HCl}$$

(2-121)

$$n\text{ClCO} \cdot \text{R} \cdot \text{COCl} + n\text{H}_2\text{N} \cdot \text{R}^-' \cdot \text{NH}_2 \rightarrow \left(\text{CO} \cdot \text{R} \cdot \text{CONH} \cdot \text{R}^-' \cdot \text{NH}\right)_n + 2n\text{HCl}$$

(2-122)

2-8c-1 Description of Process

The rate constants for these reactions are orders of magnitude greater than those for the corresponding reactions of the diacid or diester reactants (Table 2-8). The use of such reactants in a novel low-temperature polymerization technique called interfacial polymerization has been extensively studied [Morgan and Kwolek, 1959a,b; Nikonov and Savinov, 1977]. Temperatures in the range 0–50°C are usually employed. Polymerization of two reactants is carried out at the interface between two liquid phases, each containing one of the reactants (Fig. 2-11). Polyamidation is performed at room temperature by placing an aqueous solution of the diamine on top of an organic phase containing the acid chloride. The reactants diffuse to and undergo polymerization at the interface. The polymer product precipitates and is continuously withdrawn in the form of a continuous film or filament if it has sufficient mechanical strength. Mechanically weak polymers that cannot be removed impede the transport of reactants to the reaction site and the polymerization rate decreases with time. The polymerization rate is usually diffusion-controlled, since the rates of diffusion of reactants to the interface are slower than the rate of reaction of the two functional groups. (This may not be the situation when reactions with small rate constants are employed.)

Interfacial polymerization is mechanistically different from the usual step polymerization in that the monomers diffusing to the interface will react only with polymer chain ends. The reaction rates are so high that diacid chloride and diamine monomer molecules will react with the growing polymer chain ends before they can penetrate through the polymer film to start the growth of new chains. There is thus a strong tendency to produce higher-molecular-weight polymer in the interfacial process compared to the usual processes. Also, interfacial polymerization does not require overall bulk stoichiometry of the reactants in the two phases. Stoichiometry automatically exists at the interface where polymerization proceeds. There is always a supply of both reactants at the interface due to diffusion from the
organic and aqueous phases. Furthermore, high-molecular-weight polymer is formed at the interface regardless of the overall percent conversion based on the bulk amounts of the two reactants. The overall percent conversion can be increased by employing a stirred system as a means of increasing the total area of reacting interface.

Several reaction parameters must be controlled in order for interfacial polymerization to proceed successfully. An inorganic base must be present in the aqueous phase to neutralize the by-product hydrogen chloride. If it were not neutralized the hydrogen chloride would tie up the diamine as its unreactive amine hydrochloride salt leading to greatly lowered reaction rates. The acid chloride may undergo hydrolysis to the unreactive acid at high concentrations of the inorganic base or at low polymerization rates. Hydrolysis not only decreases the polymerization rate but also greatly limits the polymer molecular weight, since it converts the diacid chloride into the diacid, which is unreactive at the temperatures employed in interfacial polymerization. The slower the polymerization rate, the greater the problem of hydrolysis as the acid chloride will have more time to diffuse through the interface and into the water layer. Thus acid hydrolysis prevents the use of the interfacial technique for the synthesis of polyesters from diols, since the reaction is relatively slow \( (k \sim 10^{-3} \text{ L mol}^{-1} \text{ s}^{-1}) \). The reaction of diacid chlorides and diamines is so fast \( (k \sim 10^4-10^5 \text{ L mol}^{-1} \text{ s}^{-1}) \) that hydrolysis is usually completely absent.

The choice of the organic solvent is very important in controlling the polymer molecular weight, since it appears that the polymerization actually occurs on the organic solvent side of the interface in most systems. The reason for this is the greater tendency of the diamine to

---

**Fig. 2-11** Interfacial polymerization; removal of polymer film from the interface. From Morgan and Kwolek [1959 a,b] (by permission of Division of Chemical Education, American Chemical Society, Washington, DC and Wiley-Interscience, New York); an original photograph, from which this figure was drawn, was kindly supplied by Dr. P. W. Morgan.
diffuse into the organic solvent compared to the diffusion of diacid chloride into the aqueous side of the interface. (For some systems, e.g., the reaction of the disodium salt of a dihydric phenol with a diacid chloride, the exact opposite is the case and polymerization occurs on the aqueous side of the interface.) An organic solvent that precipitates the high-molecular-weight polymer but not the low-molecular-weight fractions is desirable. Premature precipitation of the polymer will prevent the production of the desired high-molecular-weight product. Thus, for example, xylene and carbon tetrachloride are precipitants for all molecular weights of poly (hexamethylene sebacate), while chloroform is a precipitant only for the high-molecular-weight polymer. Interfacial polymerization with the former organic solvents would yield only low-molecular-weight polymer. The molecular weight distributions observed in interfacial polymerizations are usually quite different from the most probable distribution [Arai et al., 1985; Korshak, 1966; Morgan, 1965]. Most interfacial polymerizations yield distributions broader than the most probable distribution, but narrower distributions have also been observed. The differences are probably due to fractionation when the polymer undergoes precipitation. The effect is dependent on the organic solvent used and the solubility characteristics of the polymer.

The organic solvent can also affect the polymerization by affecting the diffusion characteristics of the reaction system. A solvent that swells the precipitated polymer is desirable to maximize the diffusion of reactants through it to the reaction site. However, the swelling should not decrease the mechanical strength of the polymer below the level that allows it to be continuously removed from the interface. It has been found that the optimum molar ratio of the two reactants in terms of producing the highest yield and/or highest molecular weight is not always 1 : 1 and often varies with the organic solvent. The lower the tendency of the water-soluble reactant to diffuse into the organic phase, the greater must be its concentration relative to the other reactant’s concentration. The optimum ratio of concentrations of the two reactants is that which results in approximately equalizing the rates of diffusion of the two reactants to the interface.

2-8c-2 Utility

The interfacial technique has several advantages. Bulk stoichiometry is not needed to produce high-molecular-weight polymers and fast reactions are used. The low temperatures allow the synthesis of polymers that may be unstable at the high temperatures required in the typical step polymerization. The interfacial technique has been extended to many different polymerizations, including the formation of polyamides, polyesters, polyurethanes, polysulfonamides, polycarbonates, and polyureas. However, there are disadvantages to the process, which have limited its commercial utility. These include the high cost of acid chloride reactants and the large amounts of solvents that must be used and recovered. Commercial utilization has been limited to some polycarbonates, aliphatic polysulfides, and aromatic polyamides.

2-8d Polyesters

Various combinations of reactant(s) and process conditions are potentially available to synthesize polyesters [Fakirov, 2002; Goodman, 1988]. Polyesters can be produced by direct esterification of a diacid with a diol (Eq. 2-120) or self-condensation of a hydroxy carboxylic acid (Eq. 2-119). Since polyesterification, like many step polymerizations, is an equilibrium reaction, water must be continuously removed to achieve high conversions and high molecular weights. Control of the reaction temperature is important to minimize side reactions such as dehydration of the diol to form diethylene glycol

\[
\text{HOCH}_2\text{CH}_2\text{OH} \quad \rightarrow \quad \text{HOCH}_2\text{CH}_2\text{OCH}_2\text{CH}_2\text{OH} + \text{H}_2\text{O}
\] (2-123)
and β-scission of the polyester to form acid and alkene end groups that subsequently react to form an anhydride plus acetaldehyde

\[
\begin{align*}
&\sim RX\text{–COOCH}_2\text{CH}_2\text{OCO} \sim RX \\
&\sim R\text{–COOH} + \text{CH}_2\text{=CH} \text{–OCO} \sim R \\
&\text{CH}_3\text{CHO} + \sim R\text{–COOCO} \sim R
\end{align*}
\]

(2-124)

Other reported side reactions include dehydration between alcohol end groups, decarboxylation of diacid monomer, dehydration between carboxyl end groups, and scission and polymerization of the alkene end groups formed in Eq. 2-124. Side reactions directly interfere with the polymerization by altering the stoichiometric ratio of the reacting functional groups, and this affects the polymer molecular weight. Additionally, side reactions can have deleterious effects on polymer properties. For example, diethylene glycol formed by dehydration of ethylene glycol (Eq. 2-123) takes part in the polymerization. For poly(ethylene terephthalate), the \(T_m\) is decreased by the introduction of diethylene glycol units in place of ethylene glycol units in the polymer chain. The presence of acetaldehyde as an impurity causes problems when poly(ethylene terephthalate) is used to produce food and beverage containers. Acetaldehyde also results in discoloration in the final polymer product, due to the formation of aldol-type by-products. The production of food-grade polymers requires the use of purer reactants than those to be used for applications in which the polymers do not contact foodstuffs.

The carboxyl functional groups for synthesizing polyesters can be supplied by using diacids, acid anhydrides, diacid chlorides, or dimethyl esters. The cost and purity of the different reactants is important as are the reaction conditions required. Direct reactions of diacids or anhydrides with diols are often avoided because of the high temperatures required to completely aliminate water. However, these reactions are used to produce low-molecular-weight and crosslinked polyesters based on phthalic and maleic anhydrides (Sec. 2-12a). Diacid chlorides have been used with dihydric phenols to produce polycarbonates (Sec. 2-8e). Ester interchange, typically using a dimethyl ester, has often been used to advantage instead of direct esterification with the diacid or anhydride because the reaction is fast and the dimethyl ester is often more easily purified and has better solubility characteristics. Various weak bases such as the oxides and acetates of manganese, antimony, and zinc are used to catalyze the polymerization [Jabarin, 1996].

The most important commercial polyester is poly(ethylene terephthalate), often referred to as PET. The IUPAC name is poly(oxyethyleneoxyterephthaloyl). Two processes are used for the synthesis of PET, one based on dimethyl terephthalate (DMT) and the other on terephthalic acid (TA). The DMT process was the first to be commercialized because DMT was available in the required purity, but TA was not. That is no longer the case, pure TA is available, and both processes are used. The DMT process is a two-stage ester interchange process between DMT and ethylene glycol. The first stage is an ester interchange to produce bis(2-hydroxyethyl)terephthalate along with small amounts of larger-sized oligomers. The reactants are heated at temperatures increasing from 150 to 210°C and the methanol is continuously distilled off.

\[
\begin{align*}
&\text{CH}_3\text{OCO} \text{–COOCH}_3 + 2\text{HOCH}_2\text{CH}_2\text{OH} \\
&\text{HOCH}_2\text{CH}_2\text{OCO} \text{–COOCH}_2\text{CH}_2\text{OH} + 2\text{CH}_3\text{OH}
\end{align*}
\]

(2-125)
In the second-stage the temperature is raised to 270–280°C and polymerization proceeds with the removal of ethylene glycol being facilitated by using a partial vacuum of 0.5–1 torr (66–133 Pa). The first stage of the polymerization is a solution polymerization. The second stage is a melt polymerization since the reaction temperature is above the crystalline melting temperature of the polymer. Figure 2-12 illustrates a commercial process for this polymerization [Ellwood, 1967].

\[
\begin{align*}
\text{HOCH}_2\text{CH}_2\text{OCO} & \text{ COOCH}_2\text{CH}_2\text{OH} \\
\text{OCH}_2\text{CH}_2\text{OCO} & \text{ COH} \text{ OCH}_2\text{CH}_2\text{OH} \\
n & (n-1)\text{HOCH}_2\text{CH}_2\text{OH} \\
\end{align*}
\]

(2-126)

The properties and usefulness of the final polymer depends on controlling its structure by appropriate control of process variables during polymerization and subsequent processing into product. Temperature control and the choice of catalysts are critical in minimizing deliterious side reactions. A dual catalyst system is used in PET synthesis. The first-stage catalyst is an acetate of manganese, zinc, calcium, cobalt, or magnesium. Antimony(III) oxide is usually added as the second-stage catalyst; it is ineffective alone for the first-stage reaction. The first-stage catalyst is often inactivated by the addition of an alkyl or aryl phosphate or phosphate.

The production of high-molecular-weight polymer requires the complete removal of ethylene glycol because of the unfavorable equilibrium that would otherwise exist. If ethylene glycol were not removed, equilibrium would be established at too low an extent of reaction (approximately \( p < 0.7 \)) and the product would be of very low molecular weight (Fig. 2-8). A unique feature of the ester interchange process is the absence of the need for stoichiometric balance of the two functional groups at the start of the polymerization. Stoichiometric balance is inherently achieved at the end of the second stage of the process. In fact, an excess of ethylene glycol is initially used to increase the rate of formation of bis(2-hydroxyethyl)terephthalate.

The TA process is a modification of the DMT process. Terephthalic acid and an excess of ethylene glycol (in the form of a paste) are used to produce the bis(2-hydroxyethyl)terephthalate, which is then polymerized as described above. The TA process has grown to exceed the DMT process.

Poly(ethylene terephthalate), known by the trade names Mylar, Dacron, and Terylene, is a very high volume polymer—the United States production of PET fiber and plastic was over 9.5 billion pounds in 2001. The global production is about 6 times that of the United States. These figures are especially impressive when we note that PET was not introduced as a commercial product until 1953. Because of its high crystalline melting temperature (270°C) and stiff polymer chains, PET has good mechanical strength, toughness, and fatigue resistance up to 150–175°C as well as good chemical, hydrolytic, and solvent resistance. Fiber applications account for about 45% of the total PET production. Poly(ethylene terephthalate) fiber has outstanding crease resistance, has good abrasion resistance, can be treated with crosslinking resins to impart permanent-press (wash-and-wear) properties, and can be blended with cotton and other cellulosic fibers to give better feel and moisture permeation. Fiber applications include wearing apparel, curtain, upholstery, thread, tire cord, and fabrics for industrial filtration. More than 5 billion pounds of PET per year find applications as plastics, mostly for
Fig. 2-12 Schematic representation of industrial process for synthesis of poly(ethylene terephthalate). After Ellwood [1967] (by permission of American Chemical Society, Washington, DC).
blow-molded bottles for soft drinks, beers, spirits, and other food products—a result of the outstanding barrier properties of PET. Film applications include photographic, magnetic, and X-ray films or tapes, metallized films, and electrical insulation. PET also finds use as an engineering plastic where it replaces steel, aluminum, and other metals in the manufacture of precision moldings for electrical and electronic devices, domestic and office appliances, and automobile parts. In these engineering applications PET is often reinforced with glass fiber or compounded with silicones, graphite, or Teflon to improve strength and rigidity. The glass reinforced grades of PET are rated for continuous use at temperatures up to 140–155°C.

The use of PET as an engineering plastic has been somewhat limited by its relatively low rate of crystallization. Thus results in increased processing costs due to long mold recycle times. (The addition of nucleating agents such as talc, MgO, calcium silicate, zinc stearate, or plasticizers such as long-chain fatty esters helps overcome this problem.) Poly(butylene terephthalate) [IUPAC: poly(oxybutane-1,4-diyl oxyterephthaloyl)] (PBT), produced by substituting 1,4-butanediol for ethylene glycol, crystallizes much faster than PET, and competes with PET in engineering plastics applications. Its maximum use temperature is 120–140°C, slightly lower than that of PET.

Poly(ethylene 2,6-naphthalate) [IUPAC: poly(oxyethyleneoxycarbonylnaphthalene-2,6-diylcarbonyl)] (PEN) is produced from ethylene glycol and 2,6-naphthalenedicarboxylic acid (2,6-naphthalic acid). The rigidity of the naphthalene ring results in increased strength, heat stability, and barrier properties compared to PET. Among the anticipated applications are specialty photographic and electronic films, and food and beverage bottles that require filling at higher temperatures.

Other polyesters of commercial importance are polycarbonates, liquid crystal polyesters, unsaturated polyesters, and copolymers (Sects. 2-8e, 2-14g, 2-12, 2-13).

Completely aliphatic polyesters, made from aliphatic diacid and aliphatic diol components, are not of major industrial importance because of their low melting temperatures and poor hydrolytic stability. (Low-molecular-weight aliphatic polyesters are used as plasticizers and prepolymer reactants in the synthesis of polyurethanes; see Sects. 2-12e, 2-13c-2).

2-8e Polycarbonates

Polycarbonates are polyesters of carbonic acid. The most important commercial polycarbonate is that based on 2,2’-bis(4-hydroxyphenyl)propane (bisphenol A) [Freitag et al., 1988; Sehanobish et al., 1996]. It has been synthesized by the reaction of the dihydric phenol with phosgene or by ester interchange with diphenyl carbonate:

\[
\text{HO-C H}_3\overset{\text{CH}_3\text{OH}}{\text{C}}\overset{\text{C H}_3}{\text{C}}\overset{\text{OH}}{\text{C}}\overset{\text{HO}}{\text{C}}+\text{Cl-}\overset{\text{C-Cl}}{\text{C}}\overset{-\text{HCl}}{\text{C}}\overset{\text{+6O-C-O} }{\text{C}}\overset{-6\text{OH}}{\text{C}}\overset{\text{n}}{\text{O-C-O-C}}
\]

(2-127)
Polymerization by the ester interchange route is carried out as a two-stage melt polymerization very similar to that described for poly(ethylene terephthalate). However, most industrial processes involve the phosgene reaction in a stirred interfacial polymerization. Overall economics and easier control of polymer molecular weight favor the phosgene process over ester interchange. Organic solvents such as chlorobenzene, 1,2-dichloroethane, tetrahydrofuran (THF), anisole, and dioxane are used. The bisphenol A is usually dissolved in aqueous alkali to form the phenolate salt and then the organic solvent added followed by phosgene. The organic solvent prevents the loss of phosgene by hydrolysis and precipitation of the polymer before it has reached the desired molecular weight. Reaction temperatures in the range 0–50°C are used. Phase-transfer catalysts, such as quaternary ammonium and sulfonium salts and crown ethers, may be added to enhance the transfer of the phenolate salt across the interfacial boundary into the organic phase. The polymerization is usually a two-stage reaction. Oligomers are formed in the first stage. Tertiary amines are added in the second stage to catalyze the further reaction to high-molecular-weight polymer. (An alternate route to polycarbonates, the ring-opening polymerization of cyclic polycarbonate oligomers, has some potential advantages over the step polymerization route; see Sec. 7-5c.)

The IUPAC name of the polycarbonate based on bisphenol A is poly(oxy carbonyloxy-1,4-phenylenedimethylmethylene-1,4-phenylene) (trade names: Lexan, Merlon, Calibre); it is usually referred to as polycarbonate or PC. Although it can be crystallized ($T_m = 270°C$), most polycarbonates are amorphous ($T_g = 150°C$). Chain stiffening due to a combination of the benzene rings and bulky tetrasubstituted carbons in the polymer chain and the high $T_g$ result in a good combination of mechanical properties over a considerable temperature range (15–130°C). PC has excellent resistance to acids and oxidants, better than PET, but is somewhat less resistant to bases compared to PET. Polycarbonate is comparable to PET in resistance to organic solvents at ambient temperature. At higher temperatures, PC is more resistant to aliphatic and aromatic solvents but less resistant to polar organic solvents.

Although its upper temperature limit (120°C for reinforced grades) and resistance to some solvents are low compared to other engineering plastics, polycarbonate finds many uses because of its exceptional transparency and impact resistance (toughness) as well as good dimensional and creep resistances. Applications include compact disks, glazing (windows, doors, face shields, sunglasses, aircraft interiors), automotive (instrument panels and components, exterior panels, wheel covers), medical (components for dialysis, blood collection, and surgical devices), and other uses (power tool and appliance housings, refrigerator interiors, safety helmets, electrical connectors). The United States production of polycarbonates was more than 800 million pounds in 2001; the global production was about 3 billion pounds.

2-8f Polyamides

The synthesis of polyamides follows a different route from that of polyesters. Although several different polymerization reactions are possible, polyamides are usually produced either by direct amidation of a diacid with a diamine or the self-amidation of an amino acid. The polymerization of amino acids is not as useful because of a greater tendency toward cyclization (Sec. 2-5b). Ring-opening polymerization of lactams is also employed to synthesize polyamides (Chap. 7). Poly(hexamethylen adipamide) [IUPAC: poly(iminohexanediylimino hexane-1,6-diyl)] or poly(iminoadipoyl iminohexane-1,6-diyl)], also referred to as nylon 6/6, is synthesized from hexamethylene diamine and adipic acid [Zimmerman, 1988; Zimmerman and Kohan, 2001]. A stoichiometric balance of amine and carboxyl groups is readily obtained by the preliminary formation of a 1 : 1 ammonium salt (XIII) in aqueous solution at a concentration of 50%. The salt is often referred to as a nylon salt. Stoichiometric
balance can be controlled by adjusting the pH of the solution by appropriate addition of either diamine or diacid. The aqueous salt solution is concentrated to a slurry of approximately 60% or higher salt content by heating above 100°C. Polymerization is carried out by raising the temperature to about 210°C. Reaction proceeds under a steam pressure of ~250 psi (1.7 MPa), which effectively excludes oxygen. The pressure also prevents salt precipitation and subsequent polymerization on heat-transfer surfaces.

Unlike polyester synthesis, polyamidation is carried out without an external strong acid, since the reaction rate is sufficiently high without it. Further, amidation may not be an acid-catalyzed reaction. The equilibrium for polyamidation is much more favorable than that for the synthesis of polyesters. For this reason the amidation is carried out without concern for shifting the equilibrium until the last stages of reaction. Steam is released to maintain the pressure at about 1.7 MPa, while the temperature is continuously increased to 275°C. When 275°C is reached the pressure is slowly reduced to atmospheric pressure and heating continued to drive the equilibrium to the right. The later stage of the reaction is a melt polymerization since the reaction temperature is above the \( T_m \). Figure 2-13 represents a commercial process for nylon 6/6 synthesis [Taylor, 1944].

Molecular weight control and stabilization are accomplished by addition of a calculated amount of a monofunctional acid such as acetic acid. Diamine loss during polymerization is unavoidable because of its volatility. The loss must be quantitatively taken into account by careful control of process conditions and initial charges of reactants.

The United States production of polyamides was more than 4 billion pounds in 2001. About two-thirds of that is nylon 6/6; the second most important polyamide is nylon 6, which is produced by the ring-opening polymerization of \( \epsilon \)-caprolactam (Sec. 7-3). Poly(hexamethylene adipamide) is an excellent fiber and engineering plastic with a high-crystalline melting temperature (265°C). Nylon 6/6 is moderately crystalline (~50%) as normally produced, but this is further increased for fiber applications by orientation via mechanical stretching. It has a very good combination of high strength, flexibility, toughness, abrasion resistance, dyeability, low coefficient of friction (self-lubricating), low creep, and resistance to solvents, oils, bases, fungi, and body fluids. The main limitation is its moisture pickup with resulting changes in dimensional and mechanical properties. Polyamides (PAs) are more resistant to alkaline hydrolysis than polyesters but not as resistant to acid hydrolysis. Polyamides have better resistance to a range of organic solvents compared to PET and PC.

More than 60% of nylon production is used in fiber applications—wearing apparel, carpets, upholstery, tire reinforcements, ropes, seatbelts, parachutes, fishing nets, and substrates for industrial coated fabrics. Nylon fiber has been losing market share to PET fiber for apparel applications since the latter is better for producing wrinkle-resistant apparel. However, nylon is still the fiber of choice for hosiery, stretch fabrics, and women’s undergarments. Nylons are the largest volume engineering plastic—more than 500 million pounds per year in the United States. Fiber and mineral reinforcements are widely used for engineering plastic uses. The upper temperature for continuous use is 65–75°C for unreinforced grades and 100–115°C for glass and mineral reinforced grades. Applications include almost every industry and market—transportation (auto fender extensions, engine fans, brake and power
steering reservoirs, valve covers, lamp housings, roof-rack components, light-duty gears for windshield wipers and speedometers), electrical/electronics (toggle switches, plugs, sockets, antenna-mounting devices, terminal blocks), industrial (self-lubricated gears and bearings, antifriction and snap-fit parts, parts for food and textile-processing equipment, valves, vending machines, pumps), film (meat and cheese packaging, cook-in-pouches, multilayer nylon–polyolefin protective barrier materials for oil and moisture resistance), and consumer (ski boots, racquet frames, kitchen utensils, toys, power tool housings).

Nylons 6/6 and 6 comprise more than 90% of the polyamide market. The two have similar properties but nylon 6 has a lower $T_m$ (223°C). Small amounts of nylons 6/9, 6/10, 6/12, 11, 12, 12/12, and 4/6 are produced as specialty materials. Those with more methylene groups than nylons 6/6 and 6 have better moisture resistance, dimensional stability, and electrical properties, but the degree of crystallinity, $T_m$, and mechanical properties are lower. Specialty nylons made from dimerized fatty acids find applications as hot-melt adhesives, crosslinking agents for epoxy resins, and thermographic inks.

The synthesis of aromatic polyamides (referred to as aramid polymers) is difficult to carry out using diacid and diamine reactants because of the lower reactivity of aromatic amines compared to aliphatic amines [Lenk, 1978]. The aromatic ring decreases the electron density of nitrogen through resonance interaction. The elevated temperatures required to achieve polymerization are generally too high, resulting in extensive side reactions that limit polymer molecular weight.
Aromatic polyamides are produced by using the faster reaction of a diamine with a diacid chloride, for example, for poly(m-phenylene isophthalamide) or poly(imino-1,3-phenylene-iminoisophthaloyl) (trade name: Nomex). The polymerization is carried out in solution at temperatures under 100°C with a tertiary base present to react with the liberated hydrogen chloride. Highly polar aprotic solvents such as dimethylacetamide, 1-methyl-2-pyrrolidinone (NMP), tetramethylurea, and hexamethylphosphoramide have been used to prevent premature precipitation of the growing polyamide chains. This is a significant problem in the synthesis of aromatic polyamides, since the reaction temperature is much lower than for aliphatic polyamides. The presence of LiCl or CaCl₂ promotes solubilization of the polymer, probably by coordination of the metal ion with the amide carbonyl, which decreases the hydrogen-bonding between amide groups [Kwolek and Morgan, 1977]. The resulting polymer solutions from these polymerizations are often used directly to spin fibers.

\[
\begin{align*}
H_2N & \quad \begin{array}{c}
\text{NH}_2 \\
\end{array} \\
& + \quad \begin{array}{c}
\text{Cl} \text{CO} \\
\end{array} \\
& \quad \begin{array}{c}
\text{CO} \text{Cl} \\
\end{array} \\
\end{align*}
\rightarrow \quad \begin{array}{c}
\text{NH} \\
\end{array} \begin{array}{c}
\begin{array}{c}
\text{NHCO} \\
\end{array} \\
\end{array} \begin{array}{c}
\begin{array}{c}
\text{CO} \\
\end{array} \\
\end{array}
\end{align*}
\]

There have been efforts to form aromatic polyamides directly from diacids at moderate temperatures by using various phosphorus compounds for in situ activation of the carboxyl groups [Arai et al., 1985; Higashi and Kobayashi, 1989; Krigbaum et al., 1985]. A useful agent is diphenyl(2,3-dihydro-2-thioxo-3-benzoxazolyl)phosphonate, which probably activates the carboxyl group by forming a mixed carboxylic-phosphoric anhydride [Ueda, 1999; Ueda et al., 1991].

Poly(imino-1,4-phenyleneiminoterephthaloyl) (XIV) (trade names: Kevlar, Twaron) is synthesized from the corresponding para-substituted diamine and diacid chloride. Poly(iminocarbonyl-1,4-phenylene) (XV) (also known as Kevlar) is based on p-aminobenzoic acid.

The totally aromatic structures of the aramid polymers give them exceptional heat and flame resistance, very high melting points (generally above their decomposition temperature, which are \(\geq 500^\circ\text{C}\)), ultrahigh strength, and better resistance to solvents, chemicals, and oxidizing agents compared to aliphatic polyamides. Kevlar has higher strength and modulus properties compared to Nomex. The para structure of the former gives a rodlike extended-chain structure that forms liquid crystal solutions. (Liquid crystal solutions are solutions in which there is a high degree of ordering of solute molecules; see Sec. 2-14g.) Polymer crystallization from liquid crystal solutions results in a highly oriented, extended-chain morphology in the bulk polymer, resulting in high strength and high modulus.
Aramid polymers are much more expensive than the aliphatic polyamides. The use of aramid polymers is limited to those applications that justify the high cost. The present U.S. market is about 20 million pounds per year. The applications are those where one needs very high flame resistance (clothing for firefighters and welders, welder’s protective shield, upholstery and drapes), heat resistance (ironing board covers, insulation film for electrical motors and transformers, aerospace and military), dimensional stability (fire hose, V- and conveyor belts), or strength and modulus (circuit boards, bulletproof vests, fiber optic and power lines, ship mooring ropes, automobile tire cord, puncture-resistant bicycle tires).

2-8g Historical Aspects

Wallace Carothers and coworkers at DuPont synthesized aliphatic polyesters in the 1930s [Furukawa, 1998; Hounshell and Smith, 1988]. These had melting points below 100°C, which made them unsuitable for fiber use. Carothers then turned successfully to polyamides, based on the theoretical consideration that amides melt higher than esters. Polyamides were the first synthetic fibers to be produced commercially. The polyester and polyamide research at DuPont had a major impact on all of polymer science. Carothers laid the foundation for much of our understanding of how to synthesize polymeric materials. Out of that work came other discoveries in the late 1930s, including neoprene, an elastomer produced from chloroprene, and Teflon, produced from tetrafluoroethylene. The initial commercial application for nylon 6/6 was women’s hosiery, but this was short-lived with the intrusion of World War II. The entire nylon 6/6 production was allocated to the war effort in applications for parachutes, tire cord, sewing thread, and rope. The civilian applications for nylon products burst forth and expanded rapidly after the war.

Carother’s work not only secured the future of the DuPont chemical empire but launched the synthetic fiber industry and changed the agricultural patterns of the Southern cotton states. Subsequent to the success of nylon, workers in the United Kingdom in the early 1950s achieved success in producing a polyester fiber by using terephthalate as the acid component. Cotton, no longer King of Fibers, accounts for less than 25% of the U.S. fiber market. Nylon, PET, and rayon (regenerated cellulose) account for the remainder.

2-9 MULTICHAIN POLYMERIZATION

2-9a Branching

The discussions until this point have been concerned with the polymerization of bifunctional monomers to form linear polymers. When one or more monomers with more than two functional groups per molecule are present the resulting polymer will be branched instead of linear. With certain monomers crosslinking will also take place with the formation of network structures in which a branch or branches from one polymer molecule become attached to other molecules. The structures of linear, branched, and crosslinked polymers are compared in Fig. 1-2.

Consider the polymerization of an A—B reactant in the presence of a small amount of a monomer A_f containing f functional groups per molecule. The value of f is termed the functionality of the monomer. The product of this polymerization will be a branched polymer in which f chains are attached to a central branch point (i.e., an A_f species). For the specific case of f = 3, polymerization of A—B in the presence of leads to the structure XVI.
careful consideration of this structure shows that there can be only one A reactant molecule incorporated into each polymer molecule. Further, crosslinked species will not be formed. Reactions between two polymer molecules of the type described above cannot occur since all growing branches possess A functional groups at their ends. Branch chains from one molecule cannot react with those from another. (This would not be true if A groups were capable of reacting with each other. However, that is not the usual situation.)

Polymerizations with extensive branching are considered elsewhere. Sections 2-10 and 2-16 discuss branching with and without crosslinking, respectively.

2-9b Molecular Weight Distribution

The molecular weight distribution in this type of nonlinear polymerization will be much narrower than for a linear polymerization. Molecules of sizes very much different from the average are less likely than in linear polymerization, since this would require having the statistically determined f branches making up a molecule all very long or all very short. The distribution functions for this polymerization have been derived statistically [Peebles, 1971; Schaefgen and Flory, 1948], and the results are given as

\[
X_n = \frac{(frp + 1 - rp)}{(1 - rp)}
\]  
(2-130)

\[
\overline{X}_w = \frac{(f - 1)^2(rp)^2 + (3f - 2)rp + 1}{(frp + 1 - rp)(1 - rp)}
\]  
(2-131)

The breadth of the distribution is characterized by

\[
\frac{\overline{X}_w}{X_n} = 1 + \frac{frp}{(frp + 1 - rp)^2}
\]  
(2-132)
which becomes
\[
\frac{X_w}{X_n} = 1 + \frac{1}{f} \tag{2-133}
\]
in the limit of \( p = r = 1 \).

The weight distribution (Eq. 2-131) is shown in Fig. 2-14 for several values of \( f \). The extents of reaction have been adjusted to maintain a constant number-average degree of polymerization of 80 in all four cases. The size distribution becomes progressively narrower with increasing functionality of \( A_f \). This is also evident from Eq. 2-133, where \( X_w/X_n \) decreases from 2 for \( f = 1 \) to 1.25 for \( f = 4 \) (at \( p = 1 \)). Linear polymers are formed for \( f \) values of 1 or 2, while branched polymers are formed when \( f \) is greater than 2. The case of \( f = 1 \) corresponds to the type 3 polymerization discussed in Sec. 2-6. The distribution is the exact same as the most probable distribution for linear polymerization (Sec. 2-7). Linear polymerization with \( f = 2 \) is of interest in that the distribution is narrower than that for the usual linear polymerization. The linking of two statistically independent \( A-B \) type polymer chains into one polymer molecule via an \( A-A \) molecule leads to a significantly narrower distribution than in the usual polymerizations of the \( A-B \) or \( A-A \) plus \( B-B \) types.

### 2-10 CROSSLINKING

Polymerization of the \( A-B \) plus \( A_f \) system (with \( f > 2 \)) in the presence of \( B-B \) will lead not only to branching but also to a crosslinked polymer structure. Branches from one polymer molecule will be capable of reacting with those of another polymer molecule because of the presence of the \( B-B \) reactant. Crosslinking can be pictured as leading to structure XVII.
which two polymer chains have been joined together (crosslinked) by a branch. The branch joining the two chains is referred to as a *crosslink*. A crosslink can be formed whenever there are two branches (e.g., those indicated in XVII by the arrows) that have different functional groups at their ends, that is, one has an A group and the other a B group. Crosslinking will also occur in other polymerizations involving reactants with functionalities greater than two. These include the polymerizations

\[
\begin{align*}
A - A &\quad + \quad B_f \\
A - A &\quad + \quad B - B &\quad + \quad B_f \\
A_f &\quad + \quad B_f \\
\end{align*}
\]

Crosslinking is distinguished by the occurrence of *gelation* at some point in the polymerization. At this point, termed the *gel point*, one first observes the visible formation of a *gel* or *insoluble polymer fraction*. (The gel point is alternately taken as the point at which the system loses fluidity as measured by the failure of an air bubble to rise in it.) The gel is insoluble in all solvents at elevated temperatures under conditions where polymer degradation does not occur. The gel corresponds to the formation of an infinite network in which polymer molecules have been crosslinked to each other to form a macroscopic molecules. The gel is, in...
fact, considered as one molecule. The nongel portion of the polymer remains soluble in solvents and is referred to as sol. As the polymerization and gelation proceed beyond the gel point, the amount of gel increases at the expense of the sol as more and more polymer chains in the sol are crosslinked to the gel. There is a dramatic physical change that occurs during the process of gelation. The reaction mixture is transformed into a polymer of infinite viscosity.

The crosslinking reaction is an extremely important one from the commercial standpoint. Crosslinked plastics are increasingly used as engineering materials because of their excellent stability toward elevated temperatures and physical stress. They are dimensionally stable under a wide variety of conditions due to their rigid network structure. Such polymers will not flow when heated and are termed thermostetting polymers or simply thermosets. More than 10 billion pounds of thermosets are produced annually in the United States. Plastics that soften and flow when heated, that is, uncrosslinked plastics, are called thermoplastics. Most of the polymers produced by chain polymerization are thermoplastics. Elastomers are a category of polymers produced by chain polymerization that are crosslinked (Sec. 1-3), but the crosslinking reactions are different from those described here (Sec. 9-2).

In order to control the crosslinking reaction so that it can be used properly, it is important to understand the relationship between gelation and the extent of reaction. Two general approaches have been used to relate the extent of reaction at the gel point to the composition of the polymerization system—based on calculating when $X_n$ and $X_w$, respectively, reach the limit of infinite size.

### 2-10a Carothers Equation: $X_n \rightarrow \infty$

#### 2-10a-1 Stoichiometric Amounts of Reactants

Carothers derived a relationship between the extent of reaction at the gel point and the average functionality $f_{\text{avg}}$ of the polymerization system for the case where the two functional groups A and B are present in equivalent amounts [Carothers, 1936]. The derivation follows in a manner similar to that for Eq. 2-78. The average functionality of a mixture of monomers is the average number of functional groups per monomer molecule for all types of monomer molecules. It is defined by

$$f_{\text{avg}} = \frac{\sum N_i f_i}{\sum N_i} \tag{2-134}$$

where $N_i$ is the number of molecules of monomer $i$ with functionality $f_i$, and the summations are over all the monomers present in the system. Thus for a system consisting of 2 mol of glycerol (a triol) and 3 mol of phthalic acid (a diacid) there is a total of 12 functional groups per five monomer molecules, and $f_{\text{avg}}$ is $\frac{12}{5}$ or 2.4. For a system consisting of an equimolar amounts of glycerol, phthalic anhydride, and a monobasic acid, there is a total of six functional groups per three molecules and $f_{\text{avg}}$ is $\frac{6}{3}$ or 2.

In a system containing equivalent numbers of A and B groups, the number of monomer molecules present initially is $N_0$ and the corresponding total number of functional groups is $N_0 f_{\text{avg}}$. If $N$ is the number of molecules after reaction has occurred, then $2(N_0 - N)$ is the number of functional groups that have reacted. The extent of reaction $p$ is the fraction of functional groups lost:

$$p = \frac{2(N_0 - N)}{N_0 f_{\text{avg}}} \tag{2-135}$$
while the degree of polymerization is

\[ X_n = \frac{N_0}{N} \]  

(2-136)

Combination of Eqs. 2-135 and 2-136 yields

\[ \bar{X}_n = \frac{2}{2 - p f_{avg}} \]  

(2-137)

which can be rearranged to

\[ p = \frac{2}{f_{avg}} - \frac{2}{\bar{X}_n f_{avg}} \]  

(2-138)

Equation 2-138, often referred to as the Carothers equation, relates the extent of reaction and degree of polymerization to the average functionality of the system.

An important consequence of Eq. 2-138 is its limiting form at the gel point where the number-average degree of polymerization becomes infinite. The critical extent of reaction \( p_c \) at the gel point is given by

\[ p_c = \frac{2}{f_{avg}} \]  

(2-139)

since the second term of the right side of Eq. 2-138 vanishes. Equation 2-139 can be used to calculate the extent of reaction required to reach the onset of gelation in a mixture of reacting monomers from its average functionality. Thus the glycerol–phthalic acid (2 : 3 molar ratio) system mentioned above has a calculated critical extent of reaction of 0.833.

**2-10a-2 Extension to Nonstoichiometric Reactant Mixtures**

Equations 2-138 and 2-139 apply only to systems containing stoichiometric numbers of the two different functional groups. For nonequivalent numbers of the functional groups, the average functionality calculated from Eq. 2-134 is too high. Thus, consider the extreme example of a mixture of 1 mol of glycerol and 5 mol of phthalic acid. Using Eq. 2-134, one calculates a value of \( \frac{13}{6} \) or 2.17 for \( f_{avg} \). This indicates that a high polymer will be obtained. Further, one would predict from Eq. 2-139 that crosslinking will occur at \( p_c = 0.922 \). Both of these conclusions are grossly in error. It is apparent from previous discussions (Sec. 2-6) that the gross stoichiometric imbalance between the A and B functional groups in this system \( (r = 0.3) \) precludes the formation of any but extremely low-molecular-weight species. The polymerization will stop with the large portion of the acid functional groups being unreacted.

The average functionality of nonstoichiometric mixtures has been deduced [Pinner, 1956] as being equal to twice the total number of functional groups that are not in excess divided by the total number of all molecules present. This simply takes into account the fact that the extent of polymerization (and crosslinking, if it can occur) depends on the deficient reactant. The excess of the other reactant is not useful; in fact, it results in a lowering of the functionality of the system. For the above nonstoichiometric mixture of 1 mol of glycerol and 5 mol of phthalic acid, the \( f_{avg} \) value is correctly calculated as 6/6 or 1.00. This low value of \( f_{avg} \) is indicative of the low degree of polymerization that will occur in the system.
In a similar manner the average functionality of nonstoichiometric mixtures containing more than two monomers has been obtained. Consider a ternary mixture of \( N_A \) moles of \( f_A \), \( N_C \) moles of \( f_C \), and \( N_B \) moles of \( f_B \) with functionalities \( f_A \), \( f_C \), and \( f_B \), respectively. In this system \( N_A \) and \( N_C \) contain the same functional groups (i.e., \( A \) groups) and the total number of \( A \) functional groups is less than the number of \( B \) groups (i.e., \( B \) groups are in excess). The average functionality in such a system is given by

\[
 f_{\text{avg}} = \frac{2(N_A f_A + N_C f_C)}{N_A + N_C + N_B} \tag{2-140}
\]

or

\[
 f_{\text{avg}} = \frac{2r f_A f_B f_C}{f_A f_C + r f_A f_B + r(1-r) f_B f_C} \tag{2-141}
\]

where

\[
 r = \frac{N_A f_A + N_C f_C}{N_B f_B} \tag{2-142}
\]

\[
 \rho = \frac{N_C f_C}{N_A f_A + N_C f_C} \tag{2-143}
\]

The term \( r \) is the ratio of \( A \) groups to \( B \) groups and has a value equal to or less than unity. \( r \) is comparable to the previously discussed stoichiometric imbalance. The term \( \rho \) is the fraction of all \( A \) functional groups that belong to the reactant with \( f > 2 \).

One can easily show by substitution of different values of \( r \), \( \rho \), \( f_A \), \( f_B \), and \( f_C \) into Eqs. 2-139 through 2-143 that crosslinking is accelerated (i.e., \( p_c \) decreases) for systems that contain closer to stoichiometric amounts of \( A \) and \( B \) functional groups (\( r \) closer to 1), systems with larger amounts of polyfunctional reactants (\( \rho \) closer to 1) and systems containing reactants of higher functionality (higher values of \( f_A \), \( f_B \), and \( f_C \)).

The Carothers equations and Eq. 2-78 overlap but are not equivalent. Recall the brief note in Sec. 2-6b that Eq. 2-78 does not apply to systems containing a monofunctional reactant unless it is present in addition to stoichiometric amounts of bifunctional reactants (either \( A = A + B = B \) or \( A = B \)). That is, for example, Eq. 2-78 applies to a reaction system of 10 mol each of \( A = A \) and \( B = B \) plus 1 mol \( B \) but does not apply to a system of 10 mol \( A = A \), 9 mol \( B = B \), and 1 mol \( B \). In reality, the two reaction systems yield very nearly the same degree of polymerization at any particular extent of reaction. The Carothers equation yields \( X_n \) values of 21.0 and 20.0, respectively, for the two systems at complete conversion. The use of Eq. 2-78 for the second reaction system yields a gross distortion. The value of \( r \) obtained from Eq. 2-80 would be unity (the same as for a perfectly stoichiometric system of 10 mol each of \( A = A \) and \( B = B \)) and this leads to a \( X_n \) value of infinity at complete conversion. This is correct for the stoichiometric system but clearly is incorrect for the reaction system containing the large amount of monofunctional \( B \) reactant. The use of Eq. 2-78 must be limited to situations in which there are stoichiometric amounts of bifunctional reactants (or \( A = A \)). Also, Eq. 2-78 is inapplicable to any systems containing a reactant with functionality greater than 2. The Carothers equation, without such limitations, has two general uses. First, it can be used in the form of Eq. 2-137 to calculate the degree of polymerization of a reaction system using the appropriate value of \( f_{\text{avg}} \) (whose calculation depends on whether stoichiometric or nonstoichiometric amounts are present). If one obtains a negative value of \( X_n \) in the calculation, it...
means that the system is past the gel point at that conversion. Second, the use of Eq. 2-139 allows one to calculate the critical extent of reaction at the gel point. Keep in mind that the extent of reaction calculated from Eq. 2-137 or 2-139 refers to the extent of reaction of the A functional groups (defined as those groups not in excess). The extent of reaction of the B functional groups is $r_B$ or $r_{Bc}$.

2-10b Statistical Approach to Gelation: $X_w \rightarrow \infty$

Flory [1941, 1953] and Stockmayer [1943, 1952, 1953] used a statistical approach to derive an expression for predicting the extent of reaction at the gel point by calculating when $X_w$ approaches infinite size. The statistical approach in its simplest form assumes that the reactivity of all functional groups of the same type is the same and independent of molecular size. It is further assumed that there are no intramolecular reactions between functional groups on the same molecule. (These assumptions are also inherent in the use of Eqs. 2-137 through 2-143). For this derivation the branching coefficient $\alpha$ is defined as the probability that a given functional group of a branch unit at the end of a polymer chain segment leads to another branch unit. For the polymerization of $A - A$ with $B - B$ and $A_f$ this corresponds to obtaining a chain segment of the type

$$ A-A + B-B + A_f \rightarrow A_{(f-1)} - A(B\rightarrow BA-A)_n B\rightarrow BA-A_{(f-1)} $$  \hspace{1cm} (2-144)

where $n$ may have any value from zero to infinity. The multifunctional monomer $A_f$ is considered a branch unit, while the segments between branch units are defined as chain segments. The branch units occur on a polymer chain at the branch points (Fig. 1-2). Infinite networks are formed when $n$ number of chains or chain segments give rise to more than $n$ chains through branching of some of them. The criterion for gelation in a system containing a reactant of functionality $f$ is that at least one of the $(f-1)$ chain segments radiating from a branch unit will in turn be connected to another branch unit. The probability for this occurring is simply $1/(f-1)$ and the critical branching coefficient $\alpha_c$ for gel formation is

$$ \alpha_c = \frac{1}{(f-1)} \hspace{1cm} (2-145) $$

The $f$ in Eq. 2-145 is the functionality of the branch units, that is, of the monomer with functionality greater than 2. It is not the average functionality $f_{avg}$ from the Carothers equation. If more than one type of multifunctional branch unit is present an average $f$ value of all the monomer molecules with functionality greater than 2 is used in Eq. 2-145.

When $\alpha(f-1)$ equals 1 a chain segment will, on the average, be succeeded by $\alpha(f-1)$ chains. Of these $\alpha(f-1)$ chains a portion $\alpha$ will each end in a branch point so that $\alpha^2(f-1)^2$ more chains are created. The branching process continues with the number of succeeding chains becoming progressively greater through each succeeding branching reaction. The growth of the polymer is limited only by the boundaries of the reaction vessel.

If, on the other hand, $\alpha(f-1)$ is less than 1, chain segments will not be likely to end in branch units. For a trifunctional reactant ($f = 3$) the critical value of $\alpha$ is $\frac{1}{3}$.

The probability $\alpha$ is now related to the extent of reaction by determining the probability of obtaining a chain segment of the type shown in Eq. 2-144. The extents of reaction of A and B functional groups are $p_A$ and $p_B$, respectively. The ratio of all A groups, both reacted and unreacted, that are part of branch units, to the total number of all A groups in the mixture is defined by $\rho$. This corresponds to the same definition of $\rho$ as in Eq. 2-143. The probability that a B group has reacted with a branch unit is $p_B \rho$. The probability that a B group has
reacted with a nonbranch A–A unit is \( p_B(1 - \rho) \). Therefore the probability of obtaining a segment of the type in Eq. 2-144 is given by 

\[
p_A(p_B(1 - \rho)p_A)^n p_B \rho.
\]

Summation of this over all values of \( n \) and then evaluation of the summation yields

\[
\alpha = \frac{p_A p_B \rho}{1 - p_A p_B(1 - \rho)}
\]  
(2-146)

Either \( p_A \) or \( p_B \) can be eliminated by using the ratio \( r \) of all A groups to all B groups to substitute \( p_A = r p_B \) into Eq. 2-146 to yield

\[
\alpha = \frac{p_A^2 \rho}{1 - p_A^2(1 - \rho)} = \frac{p_B^2 \rho}{r - p_B^2(1 - \rho)}
\]  
(2-147)

Equation 2-147 is combined with Eq. 2-145 to yield a useful expression for the extent of reaction (of the A groups) at the gel point

\[
p_c = \frac{1}{[r(1 + \rho(f - 2))]^{1/2}}
\]  
(2-148)

Several special cases of Eqs. 2-147 and 2-148 are of interest. When the two functional groups are present in equivalent numbers, \( r = 1 \) and \( p_A = p_B = p \), Eqs. 2-147 and 2-148 become

\[
\alpha = \frac{p^2 \rho}{1 - p^2(1 - \rho)}
\]  
(2-149)

and

\[
p_c = \frac{1}{[1 + \rho(f - 2)]^{1/2}}
\]  
(2-150)

When the polymerization is carried out without any A–A molecules (\( \rho = 1 \)) with \( r < 1 \) the equations reduce to

\[
\alpha = r p_A^2 = \frac{p_B^2}{r}
\]  
(2-151)

and

\[
p_c = \frac{1}{[r(1 + (f - 2))]^{1/2}}
\]  
(2-152)

If both of the conditions stated are present, that is, \( r = \rho = 1 \), Eqs. 2-147 and 2-148 become

\[
\alpha = p^2
\]  
(2-153)

and

\[
p_c = \frac{1}{[1 + (f - 2)]^{1/2}}
\]  
(2-154)
These equations do not apply for reaction systems containing monofunctional reactants and/or both A and B type of branch units. Consider the more general case of the system

\[ A_1 + A_2 + A_3 + \cdots + A_i + B_1 + B_2 + B_3 + \cdots + B_j \rightarrow \text{crosslinked polymer} \]  

(2-155)

where we have reactants ranging from monofunctional to \( i \)th functional for A functional groups and monofunctional to \( j \)th functional for B functional groups [Durand and Brunoeu, 1982a,b; Miller et al., 1979; Miller and Macosko, 1978; Stockmayer, 1952, 1953; Stafford, 1981.] The extent of reaction at the gel point is given by

\[ p_c = \frac{1}{\{r(f_{w,A} - 1)(f_{w,B} - 1)\}^{1/2}} \]  

(2-156)

where \( f_{w,A} \) and \( f_{w,B} \) are weight-average functionalities of A and B functional groups, respectively, and \( r \) is the stoichiometric imbalance (Sec. 2-6b). The functionalities \( f_{w,A} \) and \( f_{w,B} \) are defined by

\[ f_{w,A} = \frac{\sum f_{A,i}^2 N_{A_i}}{\sum f_{A,i}^2 N_{A_i}} \]  

(2-157)

\[ f_{w,B} = \frac{\sum f_{B,j}^2 N_{B_j}}{\sum f_{B,j}^2 N_{B_j}} \]  

(2-158)

The summations in Eq. 2-157 are for all molecules containing A functional groups with \( N_{A_i} \) representing the number of moles of reactant \( A_i \) containing \( f_{A_i} \) number of A functional groups per molecule. The summations in Eq. 2-158 are for all molecules containing B functional groups with \( N_{B_j} \) representing the number of moles of reactant \( B_j \) containing \( f_{B_j} \) number of B functional groups per molecule.

The utility of Eq. 2-156 can be illustrated for the system:

- 4 mol \( A_1 \)
- 2 mol \( B_1 \)
- 40 mol \( A_2 \)
- 50 mol \( B_2 \)
- 2 mol \( A_3 \)
- 3 mol \( B_3 \)
- 3 mol \( A_4 \)
- 3 mol \( B_5 \)

\( r, f_{w,A}, f_{w,B}, \) and \( p_c \) are calculated as

\[ r = \frac{1(4) + 2(40) + 3(2) + 4(3)}{1(2) + 2(50) + 3(3) + 5(3)} = 0.80952 \]  

(2-159)

\[ f_{w,A} = \frac{1^2(4) + 2^2(40) + 3^2(2) + 4^2(3)}{1(4) + 2(40) + 3(2) + 4(3)} = 2.25490 \]  

(2-160)

\[ f_{w,B} = \frac{1^2(2) + 2^2(50) + 3^2(3) + 5^2(3)}{1(2) + 2(50) + 3(3) + 5(3)} = 2.41270 \]  

(2-161)

\[ p_c = \frac{1}{\{0.80952(2.25490)(2.41270)\}^{1/2}} = 0.83475 \]  

(2-162)
Keeping in mind that $p_c$ is the gel point conversion for A groups since B groups are in excess (A groups are limiting), consider the effects of adding more monofunctional reagent to the system. The effect is different for adding A1 versus adding B1. For example, increasing A1 from 4 to 18 mol increases $r$ to 0.92063 and decreases $f_{w,A}$ to 2.10345, with $f_{w,B}$ unchanged. The changes in $r$ and $f_{w,A}$ cancel each other and Eq. 2-156 calculates that $p_c$ is unchanged at 0.83475. On the other hand, increasing B1 from 2 to 16 mol decreases $r$ to 0.72857 and also decreases $f_{w,B}$ to 2.27143, with $f_{w,A}$ unchanged. The changes in $r$ and $f_{w,A}$ reinforce each other and $p_c$ increases to 0.92750.

The effect of increasing A1 is different from increasing B1 because B groups are in excess. The additional A groups added by increasing A1 results only in changing some of the end groups of the polymer chains from B groups to A groups, with no effect on $p_c$. When B1 is increased, it tends to degrade the crosslinking process. The bifunctional and polyfunctional A reactants depend on the polyfunctional B reactants to build up the crosslinked network. Monofunctional B acts as a capping agent for chain ends to limit the extent of crosslinking and increase $p_c$.

2-10c Experimental Gel Points

The two approaches to the problem of predicting the extent of reaction at the onset of gelation differ appreciably in their predictions of $p_c$ for the same system of reactants. The Carothers equation predicts the extent of reaction at which the number-average degree of polymerization becomes infinite. This must obviously yield a value of $p_c$ that is too large because polymer molecules larger than $X_n$ are present and will reach the gel point earlier than those of size $X_n$. The statistical treatment theoretically overcomes this error, since it predicts the extent of reaction at which the polymer size distribution curve first extends into the region of infinite size.

The gel point is usually determined experimentally as that point in the reaction at which the reacting mixture loses fluidity as indicated by the failure of bubbles to rise in it. Experimental observations of the gel point in a number of systems have confirmed the general utility of the Carothers and statistical approaches. Thus in the reactions of glycerol (a triol) with equivalent amounts of several diacids, the gel point was observed at an extent of reaction of 0.765 [Kienle and Petke, 1940, 1941]. The predicted values of $p_c$, are 0.709 and 0.833 from Eqs. 148 (statistical) and 2-139 (Carothers), respectively. Flory [1941] studied several systems composed of diethylene glycol ($f = 2$), 1,2,3-propanetricarboxylic acid ($f = 3$), and either succinic or adipic acid ($f = 2$) with both stoichiometric and nonstoichiometric amounts of hydroxyl and carboxyl groups. Some of the experimentally observed $p_c$ values are shown in Table 2-9 along with the corresponding theoretical values calculated by both the Carothers and statistical equations.

### TABLE 2-9 Gel Point Determinations for Mixture of 1,2,3-Propanetricarboxylic Acid, Diethylene Glycol, and Either Adipic or Succinic Acid

<table>
<thead>
<tr>
<th>$r = \frac{[\text{CO}_2\text{H}]}{[\text{OH}]}$</th>
<th>Calculated from Eq. 2-139</th>
<th>Calculated from Eq. 2-148</th>
<th>Observed$^a$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.000</td>
<td>0.293</td>
<td>0.951</td>
<td>0.879</td>
</tr>
<tr>
<td>1.000</td>
<td>0.194</td>
<td>0.968</td>
<td>0.916</td>
</tr>
<tr>
<td>1.002</td>
<td>0.404</td>
<td>0.933</td>
<td>0.843</td>
</tr>
<tr>
<td>0.800</td>
<td>0.375</td>
<td>1.063</td>
<td>0.955</td>
</tr>
</tbody>
</table>

$^a$Data from Flory [1941].
The observed $p_c$ values in Table 2-9 as in many other similar systems fall approximately midway between the two calculated values. The Carothers equation gives a high value of $p_c$ for reasons mentioned above. The experimental $p_c$ values are close to but always higher than those calculated from Eq. 2-148. There are two reasons for this difference: the occurrence of intramolecular cyclization and unequal functional group reactivity. Both factors were ignored in the theoretical derivations of $p_c$. Intramolecular cyclization reactions between functional groups are wasteful of the reactants and require the polymerization to be carried out to a greater extent of reaction to reach the gel point. Stockmayer [1945] showed this to be the case for the reaction of pentaerythritol, C(CH$_2$OH)$_4$ ($f = 4$) with adipic acid. Gelation was studied as a function of concentration and the results extrapolated to infinite concentration where intramolecular reactions would be expected to be nil. The experimental $p_c$ value of 0.578 ± 0.005 compared exceptionally well with the theoretical value of 0.577. The value of $p_c$ calculated by the Carothers equation is 0.75 for this system.

In many reaction systems the difference between the observed $p_c$ values and those calculated from Eq. 2-148 are at least partially ascribed to the failure of the assumption of equal reactivity of all functional groups of the same type. An example is the glycerol-phthalic acid system previously mentioned. The difference between the calculated and observed values of $p_c$ (0.709 vs. 0.765) would be decreased, but not eliminated, if the calculation were corrected for the known lower reactivity of the secondary hydroxyl group of glycerol.

It is difficult to find crosslinking systems that are ideal in that all functional groups are of equal reactivity and intramolecular cyclization is negligible. The crosslinking of vinyl terminated poly(dimethylsiloxane) polymers with tri- and tetrafunctional silanes appears to be an exception. Thus the calculated and experimental $p_c$ values were 0.578 and 0.583, respectively, for the tetrafunctional silane and 0.708 and 0.703, respectively, for the trifunctional silane (with $r = 0.999$) [Valles and Macosko, 1979].

Although both the Carothers and statistical approaches are used for the practical predication of gel points, the statistical approach is the more frequently employed. The statistical method is preferred, since it theoretically gives the gel point for the largest-sized molecules in a size distribution. From the practical viewpoint the use of the Carothers approach alone can be disastrous, since the Carothers approach always predicts a higher $p_c$ than observed. Crosslinked polymer becomes intractable above $p_c$; the reaction must be stopped at an extent of reaction below $p_c$ before starting the technological step of fabricating the polymer into the shape of final desired product (see Sec. 2-12). Further, the statistical approach offers a greater possibility of adaption to various systems of reactants as well as the inclusion of corrections for the nonapplicability of the equal reactivity assumption and the occurrence of intramolecular reactions. Equation 2-148 and its modifications have been used extensively in the technology of crosslinked polymers.

**2-10d Extensions of Statistical Approach**

The statistical approach has been applied to systems containing reactants with functional groups of unequal reactivity [Case, 1957; Macosko and Miller, 1976; Miller and Macosko, 1978; Miller et al., 1979]. In this section we will consider some of the results for such systems. Figure 2-15 shows a plot of $M_w$ vs. extent of reaction for the various values of $s$ at $r = 1$ for the system

\[ \text{A} - \text{A} + \text{B} - \text{B'} \]
where the two functional groups in the B—B’ reactant have a difference in reactivity by a factor of \( s \). \( s \) is the ratio of the rate constants for B and B’ groups reacting with A groups. \( p_c \) is the value of \( p \) at which the curve becomes essentially vertical (i.e., \( M_w \rightarrow \infty \)). The curves shift to the right with increasing \( s \), although the shift becomes progressively smaller with increasing \( s \). The extent of reaction at the gel point increases as the B and B’ groups differ in reactivity. The more reactive B groups react to a greater extent earlier in the overall process, but gelation does not occur without reaction of the less reactive B’ groups. Overall there is a wastage of the more reactive B groups and \( p_c \) is increased. There is an upper limit to this wastage with increasing \( s \) and \( p_c \) levels off with increasing \( s \).

Figure 2-16 shows a \( p_c \) contour map for the system

\[
\begin{align*}
A & \rightarrow A' + B - B' \\
& \rightarrow A''
\end{align*}
\]

at \( r = 1 \) for various values of \( s_1 \) and \( s_2 \) with

\[
\begin{align*}
s_1 &= \frac{k}{k'} \\
s_2 &= \frac{k}{k''}
\end{align*}
\]

where \( k \), \( k' \), and \( k'' \) are the rate constants for the reactions of A, A’, and A” groups, respectively, with B groups. \( p_c \) increases as \( s_1 \) or \( s_2 \) becomes larger than 1. If both \( s_1 \) and \( s_2 \) are larger than 1, the increase in \( p_c \) is greater the larger is the difference between \( s_1 \) and \( s_2 \). Plots such as Figs. 2-15 and 2-16 can be used to calculate the expected \( p_c \) for a system where the reactivities of the functional groups are known or the relative reactivities (\( s \) in the first...
system, $s_1$ and $s_2$ (in the second system) in a particular reaction system can be determined from the measurement of $p_c$.

Some theoretical evaluations of the effect of intramolecular cyclization on gelation have been carried out [Gordon and Ross-Murphy, 1975; Kilb, 1958; Kumar et al., 1986; Stafford, 1981]. The main conclusion is that, although high reactant concentrations decrease the tendency toward cyclization, there is at least some cyclization occurring even in bulk polymerizations. Thus, even after correcting for unequal reactivity of functional groups, one can expect the actual $p_c$ in a crosslinking system to be higher than the calculated value.

Various relationships have been derived to describe the crosslinking density of a system past $p_c$ [Argyropoulos et al., 1987; Durand and Bruneau, 1982a,b; Dusek, 1979a,b; Dusek et al., 1987; Flory, 1953; Miller and Macosko, 1976] (see also Sec. 2-11). The density of crosslinks in a reaction system increases with conversion and with increasing functionality of reactants. For a system such as

$$A \rightarrow A + A_{--} + B--B$$

the crosslink density increases as $\rho$ increases. Varying the crosslink density by changing $\rho$ is of practical interest in that it allows one to control the flexibility or rigidity of the final crosslinked polymer.

2-11 MOLECULAR WEIGHT DISTRIBUTIONS IN NONLINEAR POLYMERIZATIONS

The molecular size distribution functions for three-dimensional polymers are derived in a manner analogous to those for linear polymers, but with more difficulty. The derivations have been discussed elsewhere [Flory, 1946, 1953; Somvarskey et al., 2000; Stockmayer,
1943, 1952, 1953], and only their results will be considered here. The number \( N_x \), number or mole fraction \( \frac{N_x}{N_0} \), and weight fraction \( w_x \) of \( x \)-mer molecules in a system containing monomer(s) with \( f > 2 \) are given, respectively, by

\[
N_x = N_0 \left[ \frac{(f - x)f}{x!(f - 2x + 3)!} \right] x^{-1} (1 - \alpha)^{f - 2x + 2} \quad (2-164)
\]

\[
N_x = \left[ \frac{(f - x)f}{x!(f - 2x + 3)!} \frac{(1 - \alpha)}{(1 - \alpha f/2) + 1} \right] x^{-1} (1 - \alpha)^{f - 2x + 2} \quad (2-165)
\]

\[
w_x = \left[ \frac{(f - x)f}{(x - 1)!(f - 2x + 3)!} \right] x^{-1} (1 - \alpha)^{f - 2x + 2} \quad (2-166)
\]

The number- and weight-average degrees of polymerization are given by

\[
\bar{X}_n = \frac{1}{1 - (\alpha f/2)} \quad (2-167)
\]

\[
\bar{X}_w = \frac{(1 + \alpha)}{1 - (f - 1)\alpha} \quad (2-168)
\]

\[
\frac{\bar{X}_w}{\bar{X}_n} = \frac{(1 + \alpha)(1 - \alpha f/2)}{1 - (f - 1)\alpha} \quad (2-169)
\]

These equations are general and apply equally for multifunctional reactions such as that of \( A_f \) with \( B_f \) or that of \( A_f \) with \( A - A \) and \( B - B \). Depending on which of these reactant combinations is involved, the value of \( \alpha \) will be appropriately determined by the parameters \( r, f, p, \) and \( \rho \). For convenience the size distributions in the reaction of equivalent amounts of multifunctional reactants alone, that is, where \( \alpha = p \), will be considered. A comparison of Eqs. 2-89 and 2-166 shows that the weight distribution of branched polymers is broader than that of linear polymers at equivalent extents of reaction. Furthermore, the distribution for the branched polymers becomes increasingly broader as the functionality of the multifunctional reactant increases. The distributions also broaden with increasing values of \( \alpha \). This is seen in Fig. 2-17, which shows the weight fraction of \( x \)-mers as a function of \( \alpha \) for the polymerization involving only trifunctional reactants.

![Fig. 2-17](image_url) Molecular weight distribution as a function of the extent of reaction for the polymerization of trifunctional reactants where \( \alpha = p \). After Flory [1946] (by permission of American Chemical Society, Washington, DC).
Figure 2-18 shows a plot of the weight fraction of different x-mers versus $a$ or $p$ for the trifunctional polymerization. The weight fraction $w_{\text{gel}}$ of the gel or $\infty$-mer is also plotted. A comparison of Figs. 2-17 and 2-18 with Fig. 2-9 for linear polymerization shows that the weight fraction of monomer is always greater than that of any one of the other species (up to the point where the curves for $w_1$ and $w_{\text{gel}}$ intersect). As the reaction proceeds, larger species are built up at the expense of the smaller ones, and a maximum is reached at a value of $p$ less than $\frac{1}{2}$. The maximum shifts to higher values of $p$ for the larger species. The distribution broadens and reaches maximum heterogeneity at the gel point ($a = \frac{1}{2}$), where the fraction of species that are highly branched is still small. The infinite network polymer is first formed at the gel point, and its weight fraction rapidly increases. The species in the sol (consisting of all species other than gel) decrease in average size because the larger, branched species are preferentially tied into the gel. Past the point of intersection for the $w_1$ and $w_{\text{gel}}$ curves gel is the most abundant species on a weight basis.

The broadening of the distribution with increasing $a$ can also be noted by the $\bar{X}_w/\bar{X}_n$ value. Equations 2-167 and 2-169 show that the difference between the number- and weight-average degrees of polymerization increases very rapidly with increasing extent of reaction. At the gel point the breadth of the distribution $\bar{X}_w/\bar{X}_n$ is enormous, since $\bar{X}_w$ is infinite, while $\bar{X}_n$ has a finite value of 4 (Fig. 2-19). Past the gel point the value of $\bar{X}_w/\bar{X}_n$ for the sol fraction decreases. Finally, at $a = p = 1$, the whole system has been converted to gel (i.e., one giant molecule) and $\bar{X}_w/\bar{X}_n$ equals 1.

As mentioned previously, the behavior of systems containing bifunctional as well as trifunctional reactants is also governed by the equations developed above. The variation of $w_1$ for the polymerization of bifunctional monomers, where the branching coefficient $a$ is varied by using appropriate amounts of a trifunctional monomer, is similar to that observed for the polymerization of trifunctional reactants alone. The distribution broadens with increasing extent of reaction. The effect of unequal reactivity of functional groups and intramolecular
cyclization is to broaden the molecular weight distribution [Case, 1957; Macosko and Miller, 1976; Miller and Macosko, 1980; Muller and Burchard, 1978].

**2-12 CROSSLINKING TECHNOLOGY**

Control of crosslinking is critical for processing thermoset plastics, both the reaction prior to the gel point and that subsequent to the gel point. The period after the gel point is usually referred to as the curing period. Too slow or too rapid crosslinking can be detrimental to the properties of a desired product. Thus, in the production of a thermoset foamed product, the foam structure may collapse if gelation occurs too slowly. On the other hand, for reinforced and laminated products the bond strength of the components may be low if crosslinking occurs too quickly.

The fabrication techniques for producing objects from thermosetting and thermoplastic polymers are vastly different. In the case of the thermoplastics the polymerization reaction is completed by the plastics manufacturer. The fabricator takes the polymer and applies heat and pressure to produce a flowable material that can be shaped into the desired finished object. The situation is quite different for thermosetting plastics. A completely polymerized thermoset is no longer capable of flow and cannot be processed into an object. Instead, the fabricator receives an incompletely polymerized polymer—termed a prepolymer—from the plastics manufacturer and polymerization (and crosslinking) is completed during the fabrication step. For example, a prepolymer can be poured into an appropriate mold and then solidified to form the desired finished object by completing the polymerization. The prepolymer is usually in the molecular weight range 500–5000 and may be either liquid or solid. The molds used for thermosets must be hinged so that they can be opened after crosslinking to remove the finished product.

Thermoset polymers are classified as A-, B-, and C-stage polymers according to their extent of reaction \( p \) compared to the extent of reaction at gelation \( p_c \). The polymer is an A-stage polymer if \( p < p_c \), B-stage if the system is close to the gel point \( (p_c) \), and C-stage when it is well past \( p_c \). The A-stage polymer is soluble and fusible. The B-stage

![Diagram](image.png) Fig. 2-19 Number- and weight-average degrees of polymerization as a function of \( \alpha \) for a trifunctional polymerization. The portions of the plots after the gel point \( (\alpha = \frac{1}{2}) \) are for the sol fraction only. After Flory [1946] (by permission of American Chemical Society, Washington, DC).
polymer is still fusible but is barely soluble. The C-stage polymer is highly crosslinked and both infusible and insoluble. The prepolymer employed by a fabricator is usually a B-stage polymer, although it may be an A-stage one. The subsequent polymerization of the prepolymer takes it through to the C stage.

Thermoset plastics can generally be grouped into two types depending on whether the same chemical reaction is used to both synthesize and crosslink the prepolymer. Generally, the older thermosetting materials involve the random crosslinking of bifunctional monomers with monomers of functionality greater than 2. The prepolymer is obtained in a first step by stopping the reaction, usually by cooling, at the desired extent of conversion (either A- or B-stage). Polymerization with crosslinking is completed during a second-step fabrication process, usually by heating. The newer thermosets involve prepolymer of a more specially designed structure. These prepolymer undergo crosslinking in the second step by a chemical reaction different from that for the first step. Because there is different chemistry in the two steps, one is not involved in any \( p_c \) considerations in the first step. The reactants are bifunctional with respect to the first-step chemistry. However, one or more of the reactants has some functional group capable of reaction under other conditions. Such prepolymer systems are advantageous because they generally offer greater control of the polymerization and crosslinking reactions, and very importantly, of the structure of the final product. The uses and markets for these newer thermosets are growing more rapidly than those of the older systems.

2-12a Polyesters, Unsaturated Polyesters, and Alkyds

Polyesters formed from phthalic anhydride and glycerol were among the first commercial crosslinked polyesters. Linear polyesters seldom are synthesized by the direct reactions of acids or acid anhydrides with alcohols because the higher temperatures required for high conversions lead to side reactions, which interfere with obtaining high molecular weights. This consideration is not overwhelmingly important for crosslinking systems, since crosslinking is achieved at far lower extents of reaction than are needed to obtain high polymer in a linear polymerization. Crosslinked polyesters are typically synthesized by direct esterification of acid or acid anhydride with alcohol.

\[
\begin{array}{c}
\text{OC} \quad \text{O} \\
\text{CO} \\
\end{array}
\quad +
\begin{array}{c}
\text{CH}_2\text{OH} \\
\text{CHOH} \\
\text{CH}_2\text{OH}
\end{array}
\quad \rightarrow
\begin{array}{c}
\text{O} \quad \text{O} \\
\text{CH}_2\text{CH} = \text{CH}_2 \quad \text{O} \\
\text{O} \\
\text{C} \quad \text{O} \\
\end{array}
\tag{2-170}
\]

Simple polyesters of the type described by Eq. 2-170 are too limited to be of commercial interest. Almost all crosslinked polyesters are either unsaturated polyesters or alkyd polyesters. These offer a greater ability to vary the final product properties to suit a targeted market. Also, they offer greater process control since different chemical reactions are involved in the polymerization and crosslinking reactions. A typical unsaturated polyester
is that obtained by the polymerization of maleic anhydride and ethylene glycol. Maleic anhydride is only a bifunctional reactant in the polyesterification reaction, but it has the potential for a higher functionality under the appropriate reaction conditions. The alkene double bond is reactive under radical chain polymerization conditions. Crosslinking is accomplished in a separate step by radical copolymerization with alkene monomers such as styrene, vinyl toluene, methyl methacrylate, triallyl cyanurate, and diallyl phthalate (Sec. 6-6a).

Fumaric and itaconic acids are also used as the diacid component. Most reaction formulations involve a mixture of a saturated diacid (iso- and terephthalic, adipic) with the unsaturated diacid or anhydride in appropriate proportions to control the density of crosslinking (which depends on the carbon–carbon double-bond content of the prepolymer) for specific applications [Parker and Peffer, 1977; Selley, 1988]. Propylene glycol, 1,4-butanediol, neopentyl glycol, diethylene glycol, and bisphenol A are also used in place of ethylene glycol as the diol component. Aromatic reactants are used in the formulation to improve the hardness, rigidity, and heat resistance of the crosslinked product. Halogenated reactants are used to impart flame resistance.

The United States production of unsaturated polyesters was more than 1.7 billion pounds in 2001. Almost all unsaturated polyesters are used with fibrous reinforcements or fillers. More than 80% of the market consists of structural applications that require the strengthening imparted by fibrous (usually fiber glass) reinforcement. The remainder is used without fibrous reinforcement but with inexpensive fillers to lower costs. Unsaturated polyesters have a good combination of resistance to softening and deformation at high temperature, electrical properties, resistance to corrosion, weak alkalies, and strong acids and possess very good weatherability. The liquid polyester prepolymer are especially easy to fabricate into infusible thermoset objects by casting in open molds, spray techniques as well as compression, hand layup, and resin-transfer molding. Unsaturated polyesters are used extensively in the construction (tub and shower units, building facades, specialty flooring, cultured onyx and marble, chemical storage tanks), transportation (truck cabs, auto body repair), and marine (boat hulls) industries as well as for business machine and electric handtool-molded parts.

Alkyds are unsaturated polyesters in which the unsaturation is located at chain ends instead of within the polymer chain [Lanson, 1986]. This is accomplished by using an unsaturated monocarboxylic acid in the polymerization (Eq. 2-172). Various unsaturated fatty acids are used. Some contain a single double bond (oleic, ricinoleic); others contain two or more double bonds, either isolated (linoleic, linolenic) or conjugated (eleostearic). The unsaturated fatty acid is typically used together with a saturated monocarboxylic acid (typically a fatty acid such as lauric, stearic, palmitic but also benzoic and p-t-butylbenzoic). (The unsaturated and saturated fatty acids are often referred to as drying and nondrying oils, respectively.) The fatty acid content is in the range 30–60% or higher and the alkyd is referred to as a short, medium or long oil alkyd depending on the fatty acid content. Although glycerol is the major polyhydric alcohol in alkyd formulations, a variety of other alcohols with functionality from 2 to 8 (diethylene glycol, sorbitol, pentaerythritol, tripentaerythritol) are used either alone or in combination. Alkyd prepolymer are crosslinked via oxidation with atmospheric oxygen.
(Sec. 9-2a). The crosslinking process is referred to as drying and is directly dependent on the content of unsaturated fatty acid. The crosslinking reaction involves chemical reactions different from those involved in prepolymer synthesis.

\[
\text{CH}_2\text{OH} + \text{CH}_2\text{OH} + \text{RCH} = \text{CH} - \text{R'} - \text{CO}_2\text{H} \rightarrow \text{RCH} - \text{CH} = \text{CH} - \text{CH}_2 - \text{C} - \text{C} - \text{O} - \text{CH}_2 - \text{CH}_2 - \text{O} - \text{CH}_2 - \text{OH} - \text{CHOH} - \text{CH}_2 - \text{OH} - \text{CH}_2 - \text{OH} - \text{CO}_2\text{H}^+ \quad (2-172)
\]

More than 200 million pounds of alkyds are produced annually in the United States. Most of this is used in coating applications. Alkyds undergo rapid drying and possess good adhesion, flexibility, strength, and durability. The upper temperature limit for continuous use for both alkyds and unsaturated polyesters is about 130°C. Considerable variations are possible in properties by manipulation of the alkyd formulation. For example, the use of higher-functionality alcohols allows an increase in the fatty acid content, which imparts faster drying as well as increased hardness, better gloss retention, and improved moisture resistance. Alkyds are used as architectural enamels, exterior paints, top-side marine paints, and various metal primers and paints. Alkyds with carboxyl end groups are modified by reaction with hydroxy groups of nitrocellulose to produce lacquers. Modifications with amino resins (Sec. 2-12b-2) yields resins suitable as baked-on enamels for metal cabinets, appliances, venetian blinds, and toys. Blends of chlorinated rubber with alkyds are used as paints for highway marking, concrete, and swimming pools.

Water-based alkyds now represent a significant part of the total market. Alkyd prepolymerers are rendered water-soluble or soluble in mixtures of water and alcohol (2-butoxyethanol, 2-butanol) by various changes in prepolymer synthesis. One approach is to introduce unesterified carboxyl groups into the polymer chain, for example, by using trimellitic anhydride (XVIII) or dimethylolpropionic acid (XIX). The carboxyl groups are neutralized with base to form carboxylate groups along the polymer chain to promote water solubility. Another approach is to use poly(ethylene oxide) (XX) with hydroxyl end groups as an alcohol in the prepolymer synthesis.

**2-12b Phenolic Polymers**

**2-12b-1 Resole Phenolics**

Phenolic polymers are obtained by the polymerization of phenol \((f = 3)\) with formaldehyde \((f = 2)\) [Bogan, 1991; Brydson, 1999; Kopf, 1988; Lenz, 1967; Manfredi et al., 2001; Peng...
and Riedel, 1995]. The polymerization rate is pH-dependent, with the highest rates occurring at high and low pH. The strong base-catalyzed polymerization yields resole prepolymer (resole phenolics), mixtures of mononuclear methylolphenols (XXI) and various dinuclear and polynuclear compounds such as XXII and XXIII. The specific compounds shown as XXI, XXII, and XXIII are only some of the possible products. The other products are those differing in the extent and position (o versus p) of substitution, and the type of bridge between rings (methylene versus ether). The polymerization is carried out using a molar ratio of formaldehyde to phenol of 1.2–3.0 : 1. A 1.2 : 1 ratio is the typical formulation. The formaldehyde is supplied as a 36–50% aqueous solution (referred to as formalin). The catalyst is 1–5% sodium, calcium or barium hydroxide. Heating at 80–95°C for 1–3 h is sufficient to form the prepolymer. Vacuum dehydration is carried out quickly to prevent overreaction and gelation.

$$\text{CH}_2\text{OH}$$

$$\text{HOCH}_2\text{CH}_2\text{OH}$$

XXIa

$$\text{HOCH}_2\text{CH}_2\text{OH}$$

XXIb

$$\text{HOCH}_2\text{CH}_2\text{OH}$$

XXII

$$\text{HOCH}_2\text{CH}_2\text{OH}$$

XXIII

Although phenol itself is used in the largest volume, various substituted phenols such as cresol (o-, m-, p-), p-butylphenol, resorcinol, and bisphenol A are used for specialty applications. Some use is also made of aldehydes other than formaldehyde—acetaldehyde, glyoxal, 2-furaldehyde.

The exact composition and molecular weight of the resole depend on the formaldehyde to phenol ratio, pH, temperature and other reaction conditions [Maciel et al., 1984; Werstler, 1986]. For example, higher formaldehyde compositions will yield resoles containing more of the mononuclear compounds. The resole prepolymer may be either a solid or liquid polymer and soluble or insoluble in water depending on composition and molecular weight. Molecular weights are in the range 500–5000; most are below 2000. The resoles are usually neutralized or made slightly acidic. The pH of the prepolymer together with its composition determine whether it will be slow curing or highly reactive. Crosslinking (curing) is carried out by heating at temperatures up to 180°C. The crosslinking process involves the same chemical reactions as for synthesizing the prepolymer—the formation of methylene and ether bridges between benzene rings to yield a network structure of type XXIV. The relative
importance of methylene and ether bridges is dependent on temperature [Lenz, 1967]. Higher curing temperatures favor the formation of methylene bridges but not to the exclusion of ether bridges.

The polymerization and crosslinking of phenol–formaldehyde is a highly useful industrial process. However, the reactions that take place are quite difficult to handle in a quantitative manner for a number of reasons. The assumption of equal reactivity of all functional groups in a monomer, independent of the other functional groups in the molecule and of whether the others are reacted, is dubious in this polymerization. Consider, for example, the routes by which trimethylolphenol (XXIb) can be produced in this system:
Table 2-10 shows the rate constants for the various reactions. It is apparent that there are significant differences in the reactivities of the different functional groups in phenol (i.e., in the different positions on the ring). The reaction between phenol and formaldehyde involves a nucleophilic attack by the phenolate anion on formaldehyde (Eq. 2-174) (or its hydrated form). The electron-donating methylol groups generally increase the reactivity of phenol toward further substitution although steric hindrance modifies this effect. It is difficult to quantitatively discuss the reasons for the specific differences in reactivity, since there is no general agreement on even the relative values of the seven different rate constants. The evaluation of the different rate constants is difficult from both the viewpoints of chemical analysis of the mono-, di-, and trimethylolphenols and the mathematical analysis [Katz and Zwei, 1978] of the kinetic data.

<table>
<thead>
<tr>
<th>Reaction</th>
<th>Rate Constant $\times 10^2$ (L mol$^{-1}$ s$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$k_1$</td>
<td>14.63</td>
</tr>
<tr>
<td>$k'_1$</td>
<td>7.81</td>
</tr>
<tr>
<td>$k_2$</td>
<td>13.50</td>
</tr>
<tr>
<td>$k'_2$</td>
<td>10.21</td>
</tr>
<tr>
<td>$k_3$</td>
<td>13.45</td>
</tr>
<tr>
<td>$k'_3$</td>
<td>8.43</td>
</tr>
</tbody>
</table>

$^a$ Data from, Zavitsas [1968]; Zavitsas et al., [1968].
$^b$ Reaction conditions: $\text{pH} = 8.3$, $T = 57^\circ\text{C}$.

Not only are the different ring positions on phenol of different reactivity, but one expects that the two functional groups of formaldehyde would also differ. The second functional group of formaldehyde actually corresponds to the methylol group, since the reaction of a methylolphenol with a phenol molecule (or with a second methylolphenol) probably proceeds by a sequence such as

$$
\text{O} \quad \text{+ CH}_2\text{O} \quad \rightarrow \quad \left[ \quad \text{O} \quad \text{H} \quad \text{CH}_2\text{O}^- \quad \right] \quad \rightarrow \quad \quad \text{O} \quad \text{CH}_2\text{OH}
$$

$$(2-174)$$
Direct kinetic measurements are not available to show the reactivity of the methylol group in this reaction compared to the initial reaction of formaldehyde. However, the general observation that the amounts of di- and polynuclear compounds present in resole prepolymers differ widely depending on the reaction condition (temperature, pH, specific catalyst used, concentrations of reactants) indicates that the two functional groups of formaldehyde differ in reactivity.

A further complication in the phenol-formaldehyde polymerization is that it may involve a decrease in functional group reactivity with molecular size. This can easily happen in systems that undergo extensive crosslinking. Such systems may cease to be homogeneous solutions before the experimentally determined gel point. The gel point may be preceded by the formation of microgel particles (Sec. 2-2d) which are too small to be visible to the naked eye [Katz and Zwei, 1978]. Functional groups in the microgel particles would be relatively unreactive because of their physical unavailability. Similar considerations would apply for the reaction period subsequent to the gel point. A decrease in reactivity with size may not be due to molecular size but a consequence of steric shielding of ortho or para positions of benzene rings within a chain compared to those positions on rings at the chain ends [Kumar et al., 1980].

2-12b-2 Novolac Phenolics

Phenol–formaldehyde prepolymers, referred to as novolacs, are obtained by using a ratio of formaldehyde to phenol of 0.75–0.85 : 1, sometimes lower. Since the reaction system is starved for formaldehyde, only low molecular weight polymers can be formed and there is a much narrower range of products compared to the resoles. The reaction is accomplished by heating for 2–4 h at or near reflux temperature in the presence of an acid catalyst. Oxalic and sulfuric acids are used in amounts of 1–2 and <1 part, respectively, per 100 parts phenol. The polymerization involves electrophilic aromatic substitution, first by hydroxymethyl carbocation and subsequently by benzyl carbocation—each formed by protonation of OH followed by loss of water. There is much less benzyl ether bridging between benzene rings compared to the resole prepolymers.
Some novolacs are synthesized without strong acid present by using a carboxylate salt of zinc, calcium, manganese, cobalt, or other divalent metal ion (2% or more relative to phenol). These novolacs contain a higher degree of ortho substitution on the benzene rings and cure faster compared to the novolacs synthesized with the stronger acids. The mechanism for this ortho effect probably involves simultaneous complexation of the divalent metal ion with the phenol and carbocation hydroxyl groups. Similar effects of divalent ions on the relative amounts of ortho and para substitution are observed in the formation of resole prepolymers on comparison of catalysis by divalent metal hydroxides versus monovalent metal hydroxides.

The reaction mixture is dehydrated at temperatures as high as 160°C (higher temperatures can be tolerated than with resoles). The prepolymer is cooled, crushed, blended with 5–15% hexamethylenetetramine, (CH₂)₆N₄, and sold to the fabricator. Hexamethylenetetramine, referred to as hexa, is the product of the reaction of 6 mol of formaldehyde and 4 mol of ammonia. Curing occurs rapidly on heating with the formation of both methylene and benzylamine crosslinking bridges between benzene rings. The crosslinked network is pictured as XXVI.
2-12b-3 Applications

Phenolic polymers, the first commercial synthetic plastics, were introduced by Leo Baekeland in 1909 through his Bakelite Company. Bakelite dominated this product until 1926 when its patent expired. Phenolic polymers are the largest-volume thermosetting plastics. The United States production of phenolics was about 4.5 billion pounds in 2001. Phenolics have high strength and dimensional stability combined with good resistance to impact, creep, solvents, and moisture. Most phenolics contain fillers or reinforcements. General-grade phenolics are filled with mica, clay, wood or mineral flour, cellulose, and chopped fabric. Engineering-grade phenolics, reinforced with glass or organic fibers, elastomers, graphite, and polytetrafluoroethylene, are rated for continuous use at 150–170°C.

The largest-volume application of phenolic polymers is the adhesive bonding material for the manufacture of plywood, particle board, wafer board, and fiberboard. The phenolic constitutes up to one-third of the weight of such products. Other adhesive applications include the binder for aluminum oxide or silicon carbide in abrasion wheels and disks and contact adhesives, usually blends of rubber and phenolic, used extensively in the furniture, automotive, construction, and footwear industries. Phenolics are used in a variety of coatings applications—baked-on coatings, coatings on cans, drums, metal pipe, electrical insulation, varnishes, and metal primers. The phenolic resins are generally too hard and brittle to be used alone for the coatings applications but blends with alkyds, polyethylene, and epoxy resins perform well. Laminates of cellulose paper, cotton fabric, glass and asbestos cloths, and wood veneer with phenolics are made in various forms (sheet, rod, tubes) that can be machined. These find wide uses as printed-circuit boards, gears, cams and protective and decorative surfaces for tables, furniture, kitchen and bathroom countertops, and walls. Composites containing phenolics are used as the ablative coating for space reentry vehicles, aircraft interiors, and brakes. Other applications of phenolics include molded objects (switches, pump housings, cutlery handles, oven and toaster parts), friction materials (brake lining, transmission bands), foam insulation, carbonless copy paper, and the binder for sand in the manufacture of foundry molds for molded-metal casing.

2-12c Amino Plastics

The amino resins or plastics, closely related to the phenolics in both synthesis and applications, are obtained by the polymerization of formaldehyde with urea (XXXVII) \((f = 4)\) or melamine (XXXVIII) \((f = 6)\). Synthesis of the amino plastics can be carried out either in alkaline or acidic conditions [Drumm and LeBlanc, 1972; Nair and Francis, 1983; Updegraff, 1985]. Control of the extent of reaction is achieved by \(pH\) and temperature control. The prepolymer can be made at various \(pH\) levels depending on the reaction temperature chosen. Polymerization is stopped by cooling and bringing the \(pH\) close to neutral. Curing of the prepolymer involves heating, usually in the presence of an added acid catalyst.

Polymerization of urea and formadehyde yields various methylureas such as XXIX and a mixture of higher oligomers as was the case for the phenolic prepolymers. The relative
amounts of the various components is dependent on reaction conditions. The crosslinking reaction involves methylene (XXX), methylene ether (XXXI), and cyclic (XXXII) bridges between urea units [Ebdon and Heaton, 1977; Tomita and Ono, 1979]. As in the

\[
\text{HOCH}_2\text{NHCONH}_2 \quad \text{(HOCH}_2\text{NCO(N(CH}_2\text{OH})}_2
\]

\[
\text{XXIXa} \quad \text{XXIXb}
\]

\[
\sim\text{CH}_2\text{NHCO}\sim\text{CH}_2\sim\text{NCO-NH}\sim
\]

\[
\text{XXX}
\]

\[
\sim\text{CH}_2\text{NHCO}\sim\text{CH}_2\sim\text{NCO-NH}\sim
\]

\[
\text{XXXI}
\]

\[
\sim\text{NHCO-N}\sim\text{CH}_2\sim\text{NCO-NH}\sim
\]

\[
\text{XXXII}
\]

phenol-formaldehyde system, there is considerable evidence that the assumption of equal reactivity of functional groups is invalid for both urea and formaldehyde [Kumar and Katiyar, 1990; Tomita and Hirose, 1977]. The formation and curing of prepolymer from formaldehyde and melamine (2,4,6-triamino-s-triazine) follows in a similar manner.

The United States production of amino plastics was more than 3 billion pounds in 2001. The urea-formaldehyde polymers account for slightly more than 85% of the total. The amino plastics are similar in properties to the phenolics but are clearer and colorless. They are also harder but have somewhat lower impact strength and resistance to heat and moisture. The melamine resins are better than the ureas in hardness and resistance to heat and moisture. The melamine and urea resins are rated for continuous use at temperatures of 130–150°C and 100°C, respectively. The general applications of the amino and phenolic plastics are the same but there are uses where the amino plastics are superior. The melamine resins find an important niche due to their combination of clarity and lack of color compared to the phenolics and their superior hardness and heat and moisture resistance compared to
urea resins. Molding and laminating techniques are used to produce colored dinnerware and
dinnerware with decorative patterns. A combination of phenolic and melamine plastics are
used to produce decorative laminated plastic sheets for tabletop and counters. The combina-
tion gives a superior product—a phenolic backing imparts superior mechanical properties
while a top melamine layer imparts outstanding clarity and hardness. Amino resins are
used to impart crease resistance and wash-and-wear properties to cellulosic fabrics. A gar-
ment with its appropriate creases and containing the low-molecular-weight amino resin is
heated to achieve curing. Curing involves reaction of the amino resin with hydroxyl groups
of the cellulosic fabric, and this “sets” the garment into its shape. Amino resins also find
extensive as automotive paints; the cheaper ureas are used as primers while the melamines
are used as topcoats.

2-12d  Epoxy Resins

Epoxy resins or plastics are typically formed by the reaction of epichlorohydrin and bisphen-
ol A [Dewprashad and Eisenbraun, 1994; McAdams and Gannon, 1988] (Eq. 2-177).

\[
(n + 2)\text{CH}_{2}\text{CHCH}_2\text{Cl} + (n + 1)\text{HO-CH(OH)CH}_2\text{C(\text{CH}_3)_2-CH(OH)} \rightarrow (n + 2)\text{HCl} + \\
\text{CH}_2\text{CHCH}_2\left[\text{O-C(\text{CH}_3)_2-CH(OH)}\right]_n\text{O-C(\text{CH}_3)_2-CH(OH)CH}_2\text{O} \\
\]

(2-177)

The reaction actually involves the sodium salt of bisphenol A since polymerization is carried
out in the presence of an equivalent of sodium hydroxide. Reaction temperatures are in the
range 50–95°C. Side reactions (hydrolysis of epichlorohydrin, reaction of epichlorohydrin
with hydroxyl groups of polymer or impurities) as well as the stoichiometric ratio need to
be controlled to produce a prepolymer with two epoxide end groups. Either liquid or solid
prepolymers are produced by control of molecular weight; typical values of \( n \) are less than 1
for liquid prepolymer and in the range 2–30 for solid prepolymer.

Epichlorohydrin is reacted with a variety of hydroxy, carboxy, and amino compounds to
form monomers with two or more epoxide groups, and these monomers are then used in the
reaction with bisphenol A [Lohse, 1987]. Examples are the diglycidyl derivative of cyclohex-
ane-1,2-dicarboxylic acid, the triglycidyl derivatives of \( p \)-aminophenol and cyanuric acid,
and the polyglycidyl derivative of phenolic prepolymer. Epoxidized diolefins are also
employed (Sec. 9-8).

A variety of coreactants are used to cure epoxy resins, either through the epoxide or
hydroxyl groups [Mezzenga et al., 2000; Mijovic and Wijaya, 1994; Trappe et al., 1991].
Polyamines are the most common curing agent with reaction involving ring-opening addition
of amine (Eq. 2-178). Both primary and secondary amines are used; primary amines are more
reactive than secondary amines [Glover et al., 1988; Zvetkov, 2002]. Since each nitrogen–
hydrogen bond is reactive in the curing reaction, primary and secondary amine groups are bi-
and monofunctional, respectively. A variety of amines are used as crosslinking agents,
including diethylene triamine \((f = 5)\), triethylene tetramine \((f = 6)\), 4,4′-diaminodiphenyl-
methane \((f = 4)\), and polyaminoamides (e.g., the diamide formed from diethylene triamine
and a dimerized or trimerized fatty acid). Other types of compounds have also been used to
cure epoxy resins via the epoxide groups, including polythiols, dicyandiamide (cyanoguanidine),
diisocyanates, and phenolic prepolymers. Some of these agents require weak bases
such as tertiary amines and imidazole derivatives to accelerate the curing process.

Crosslinking of epoxy plastics through the hydroxyl groups of the repeat unit is used for
prepolymers with low epoxide group contents. The most common curing agent is phthalic
anhydride although other acid anhydrides such as tetrahydrophthalic, nadic methyl, and
chloroendic anhydrides are used in specialty applications:

\[
\begin{align*}
\text{CH}_2\text{CH} = \text{CH}_2 \text{OCH}_2 \text{CH} &= \text{OH} \\
\text{CH}_2\text{CH} = \text{CH}_2 \text{N} &= \text{R} \text{OH} \\
\text{N} &= \text{R} \text{CH}_2 - \text{CH} - \text{CH}_2 \\
\text{CH}_2\text{CH} &= \text{OH}
\end{align*}
\]

Curing of epoxy resins can also be achieved by ring-opening polymerization of epoxide
groups using either Lewis acids (including those generated photochemically) or Lewis bases
(Sec. 7-2).

Most epoxy formulations contain diluents, fillers or reinforcement materials, and toughening
agents. Diluents may be reactive (mono- and diepoxides) or nonreactive (di-\text{\textit{n}}-butyl
phthalate). Toughening (flexibilizing) agents such as low-molecular-weight polyesters or
1,3-butadiene-acrylonitrile copolymers with carboxyl end groups or aliphatic diepoxides
participate in the crosslinking process.

Epoxy resins possess high chemical and corrosion resistance, toughness and flexibility,
good mechanical and electrical behavior, and outstanding adhesion to many different
substrates. A wide range of products varying in properties and curing temperature are obtained
for specific applications by proper selection of the monomers, additives, and curing agents.
Use temperatures are in the range 90–130°C. The United States production of epoxy polyme-
ners was about 700 million pounds in 2001. The applications for epoxies fall into two
categories—coatings and structural. Coatings applications include marine, maintenance, drum, and can coatings. Automotive primer coatings involve epoxy resins with ionic charges (either carboxylate or quaternary ammonium ion) that allow for electrodeposition of the resin. Waterborne epoxy coatings have been developed for beer and beverage containers. Structural composites are used in the military (missile casings, tanks), aircraft (rudders, wing skins, flaps), automobiles (leaf springs, drive shafts), and pipe in the oil, gas, chemical, and mining industries. Laminates are used in the electrical and electronics industries (circuitboard substrate, encapsulation of devices such as transistors, semiconductors, coils). Other applications include industrial and terrazzo flooring, repair of highway concrete cracks, coatings for roads and bridges, and a wide range of adhesive applications.

2-12e Polyurethanes

The synthesis of polyurethanes is usually presented as proceeding via the formation of carbamate (urethane) linkages by the reaction of isocyanates and alcohols:

\[
\begin{align*}
    n\text{HO}R\text{OH} + n\text{OCN}R'\text{NCO} & \rightarrow \\
    \text{HO} & \longrightarrow \text{R} - \text{OCONH}R'\text{NHCOO} - \bigg(\frac{1}{n-1}\bigg) \rightarrow \text{R} - \text{OCONH}R'\text{NCO}
\end{align*}
\]  

(2-180)

However, this is an oversimplification since other reactions are also usually involved [Backus, 1977; Backus et al., 1988; Occhiello and Corti, 2003]. Foamed products such as seat cushions and bedding are the largest applications of polyurethanes. Water is often deliberately added in the production of flexible polyurethane foams. Isocyanate groups react with water to form urea linkages in the polymer chain with the evolution of carbon dioxide. The carbon dioxide acts as the blowing agent to form the foamed structure of the final product. (Low-boiling solvents such as fluorotrichloromethane are usually added to act as blowing agents in the synthesis of rigid polyurethane foamed products.) Many polyurethanes are synthesized using mixtures of diols and diamines. The diamines react with isocyanate groups to introduce additional urea linkages into the polymer. Thus, the typical polyurethane actually contains both urethane and urea repeat units.

\[
\begin{align*}
    2\text{NCO} + \text{H}_2\text{O} & \rightarrow \text{NH} - \text{CO} - \text{NH} \sim + \text{CO}_2
\end{align*}
\]  

(2-181)

(There are even some instances where only diamines are used in the synthesis. The polymer is then a polyurea although the manufacturer typically refers to it as a polyurethane.)

The situation is even more complex since the N–H bonds of both urethane and urea linkages add to isocyanate groups to form allophanate and biuret linkages, respectively. These
reactions result in branching and crosslinking of the polymer. Equation 2-183 shows how a
diisocyanate crosslinks the urethane and urea groups from two different polymer chains. The

\[ \sim \text{NH}-\text{COO}\sim + \sim \text{NH}-\text{CO}-\text{NH}\sim + \text{OCN}-\text{R'}\sim \text{NCO} \longrightarrow \]

<table>
<thead>
<tr>
<th>Allophanate</th>
<th>Biuret</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\sim \text{N}-\text{COO}\sim)</td>
<td>(\sim \text{N}-\text{CO}-\text{NH}\sim)</td>
</tr>
</tbody>
</table>

relative amounts of allophanate and biuret crosslinks in the polymer depend on the relative
amounts of urea and urethane groups (which, in turn, depends on the relative amounts
of diamine and diol) and reaction conditions. There is a greater tendency to biuret linkages since
the urea N–H is more reactive than the urethane N–H.

Trimerization of isocyanate groups to form isocyanurates also occurs and serves as an
additional source of branching and crosslinking:

\[ 3 \sim \text{R'}-\text{NCO} \longrightarrow \sim \text{R'}-\text{N}-\text{N}-\text{R'} \sim \quad (2-184) \]

These reactions present a complexity in carrying out polymerization. Simultaneously, we
have the ability to vary polymer properties over a wide range by control of the relative
amounts of reactants and the polymerization conditions. Further control of the final
product is achieved by choice of monomers. Most polyurethanes involve a macroglycol (a
low-molecular-weight polymer with hydroxyl end groups), diol or diamine, and diisocyanate.
The macroglycol (also referred to as a polyol) is a polyether or polyester synthesized under
conditions that result in two or more hydroxyl end groups. (Details of polyurethane synthesis
involving macroglycols are described in Sec. 2-13c.) The diol monomers include ethylene
glycol, 1,4-butanediol, 1,6-hexanediol, and \(p\)-di(2-hydroxyethoxy)benzene. The diamine
monomers include diethyltoluenediamine, methylenebis\((p\)-aminobenzene\), and \(3,3'\)-
dichloro-4,4′-diaminodiphenylmethane. The diisocyanate monomers include hexamethylene
diisocyanate, toluene 2,4- and 2,6-diisocyanates, and naphthalene 1,5-diisocyanate. Alcohol
and isocyanate reactants with functionality greater than 2 are also employed.

The extent of crosslinking in polyurethanes depends on a combination of the amount of
polyfunctional monomers present and the extent of biuret, allophanate, and trimerization
reactions [Dusek, 1987]. The latter reactions are controlled by the overall stoichiometry
and the specific catalyst present. Stannous and other metal carboxylates as well as tertiary
amines are catalysts for the various reactions. Proper choice of the specific catalyst result
in differences in the relative amounts of each reaction. Temperature also affects the extents
of the different reactions. Polymerization temperatures are moderate, often near ambient and usually no higher than 100–120°C. Significantly higher temperatures are avoided because polyurethanes undergo several different types of degradation reactions, such as

\[
\begin{align*}
\text{NH} & \text{COO} - \text{CH}_2\text{CH}_2\text{NH} \quad \rightarrow \quad \text{NH}_2 + \text{CO}_2 + \text{CH} = \text{CH} \\
\text{NH} & \text{COO} - \text{CH}_2\text{CH}_2\text{NH} \quad \rightarrow \quad \text{CO}_2 + \text{NH} - \text{CH}_2\text{CH}_2
\end{align*}
\] (2-185) (2-186)

as well as decomposition back to the alcohol and isocyanate monomers. Overall control in the synthesis of polyurethane foamed products also requires a balance between the polymerization–crosslinking and blowing processes. An imbalance between the chemical and physical processes can result in a collapse of the foamed structures (before solidification by crosslinking and/or cooling) or imperfections in the foam structures, which yields poor mechanical strength and performance.

The wide variations possible in synthesis give rise to a wide range of polyurethane products including flexible and rigid foams and solid elastomers, extrusions, coatings, and adhesives. Polyurethanes possess good abrasion, tear, and impact resistance coupled with oil and grease resistance. The global production of polyurethanes was more than 15 billion pounds in 1997. Flexible foamed products include upholstered furniture and auto parts (cushions, backs, and arms), mattresses, and carpet underlay. Rigid foamed products with a closed-cell morphology possess excellent insulating properties and find extensive use in commercial roofing, residential sheathing, and insulation for water heaters, tanks, pipes, refrigerators, and freezers. Solid elastomeric products include forklift tires, skateboard wheels, automobile parts (bumpers, fascia, fenders, door panels, gaskets for trunk, windows, windshield, steering wheel, instrument panel), and sporting goods (golf balls, ski boots, football cleats). Many of these foam and solid products are made by reaction injection molding (RIM), a process in which a mixture of the monomers is injected into a mold cavity where polymerization and crosslinking take place to form the product. Reaction injection molding of polyurethanes, involving low-viscosity reaction mixtures and moderate reaction temperatures, is well suited for the economical molding of large objects such as automobile fenders. (Many of the elastomeric polyurethane products are thermoplastic elastomers; see Sec. 2-13c.)

2-12f Polysiloxanes

Polysiloxanes, also referred to as silicones, possess an unusual combination of properties that are retained over a wide temperature range (−100 to 250°C). They have very good low-temperature flexibility because of the low \( T_g \) value (−127°C). Silicones are very stable to high temperature, oxidation, and chemical and biological environments, and possess very good low-temperature flexibility because of the low \( T_g \) values (−127°C for dimethylsiloxane), a consequence of the long Si–O bond (1.64 Å compared to 1.54 Å for C–C) and the wide Si–O–Si bond angle (143° compared to 109.5° for C–C–C). The Si–O bond is stronger than the C–C bond (∼450 vs. 350 kJ/mol) and siloxanes are very stable to high temperature, oxidation, chemical and biological environments, and weathering, and also possess good dielectric strength, and water repellency. The United States production of polysiloxane fluids, resins, and elastomers was about 800 million pounds in 2001. Fluid applications include fluids for hydraulics, antifoaming, water-repellent finishes for textiles,
surfactants, greases, lubricants, and heating baths. Resins are used as varnishes, paints, molding compounds, electrical insulation, adhesives, laminates, and release coatings. Elastomer applications include sealants, caulks, adhesives, gaskets, tubing, hoses, belts, electrical insulation such as automobile ignition cable, encapsulating and molding applications, fabric coatings, encapsulants, and a variety of medical applications (antiflatulents, heart valves, encasing of pacemakers, prosthetic parts, contact lenses, coating of plasma bottles to avoid blood coagulation). Silicone elastomers differ markedly from other organic elastomers in the much greater effect of reinforcing fillers in increasing strength properties.

Polysiloxane fluids and resins are obtained by hydrolysis of chlorosilanes such as dichlorodimethyl-, dichloromethylphenyl-, and dichlorodiphenylsilanes [Brydson, 1999; Hardman and Torkelson, 1989]. The chlorosilane is hydrolyzed with water to a mixture of chlorohydrxy and dihydroxysilanes (referred to as silanols), which react with each other by dehydroxylation and dehydrochlorination. The product is an equilibrated mixture of approximately equal amounts of cyclic oligomers and linear polysiloxanes. The amount of cyclics can vary from 20 to 80% depending on reaction conditions. The major cyclic oligomer is the tetramer with progressively decreasing amounts of higher cyclics. After the initial equilibration, a disiloxane-terminating agent such as [(CH₃)₃Si]₂O is added to stabilize the reaction mixture by termination of the linear species. The process may be carried out under either acidic or basic conditions depending on the desired product molecular weight. Basic conditions favor the production of higher molecular weight. Mixtures of cyclic oligomers and linear polymer may be employed directly as silicone fluids, or the cyclic content may be decreased prior to use by devolatilization (heating under vacuum). The synthesis of silicone resins proceeds in a similar manner, except that the reaction mixture includes trichlorosilanes to bring about more extensive polymerization with crosslinking. Typically, the polymer product will be separated from an aqueous layer after the hydrolytic step, heated in the presence of a basic catalyst such as zinc octanoate to increase the polymer molecular weight and decrease the cyclic content, cooled, and stored. The final end-use application of this product involves further heating with a basic catalyst to bring about more extensive crosslinking.

Silicone elastomers are either room-temperature vulcanization (RTV) or heat-cured silicone rubbers depending on whether crosslinking is accomplished at ambient or elevated temperature. (The term vulcanization is a synonym for crosslinking. Curing is typically also used as a synonym for crosslinking but often refers to a combination of additional polymerization plus crosslinking.) RTV and heat-cured silicone rubbers typically involve polysiloxanes with degrees of polymerizations of 200–1500 and 2500–11,000, respectively. The higher-molecular-weight polysiloxanes cannot be synthesized by the hydrolytic step polymerization process. This is accomplished by ring-opening polymerization using ionic initiators (Sec. 7-11a). “One-component” RTV rubbers consist of an airtight package containing silanol-terminated polysiloxane, crosslinking agent (methyltriacetoxysilane, and catalyst (e.g., dibutyltin laurate). Moisture from the atmosphere converts the crosslinking agent to the
corresponding silanol (acetic acid is a by-product), \( \text{CH}_3\text{Si(OH)}_3 \), which brings about further polymerization combined with crosslinking of the polysiloxane:

\[
3\text{SiR}_2\text{OH} + \text{CH}_3\text{Si(OH)}_3 \rightarrow \text{SiR}_2\text{OSi(CH}_3\text{)}_2\text{CH}_2\text{SiR}_2 + \text{H}_2\text{O}
\]  
(2-188)

Two-component RTV formulations involve separate packages for the polysiloxane and crosslinking agent. Hydrosilation curing involves the addition reaction between a polysiloxane containing vinyl groups (obtained by including methylvinyldichlorosilane in the original reaction mixture for synthesis of the polysiloxane) and a siloxane crosslinking agent that contains \( \text{Si} - \text{H} \) functional groups, such as \( 1,1,3,3,5,5,7,7\)-octamethyltetrasiloxane (Eq. 2-189). The reaction is catalyzed by chloroplatinic acid or other soluble Pt compound. Hydride functional siloxanes can also crosslink silanol-terminated polysiloxanes. The reaction is catalyzed by tin salts and involves \( \text{H}_2 \) loss between \( \text{Si} - \text{C} \) and \( \text{Si} - \text{O} - \text{H} \) groups. Heat curing of silicone rubbers usually involves free-radical initiators such as benzoyl peroxide (Sec. 9-2c). Hydrosilation at 50–100°C is also practiced.

\[
\text{SiR}_2\text{O} + \text{Si(OSi(CH}_3\text{)}_2\text{H)}_4 \rightarrow \text{Si(O Si(CH}_3\text{)}_2\text{CH}_2\text{SiR}_2 \widetilde{\text{O}}} \quad \text{(2-189)}
\]

2-12g Polysulfides

Polysulfide elastomers are produced by the reaction of an aliphatic dihalide, usually bis-(2-chloroethyl)formal, with sodium polysulfide under alkaline conditions [Brydson, 1999; Ellerstein, 1988] (Eq. 2-190). The reaction is carried out with the dihalide suspended in an aqueous magnesium hydroxide phase. The value of \( x \) is slightly above 2. The typical polymerization system includes up to 2% 1,2,3-trichloropropane. The polymerization readily yields a polymer with a very high molecular weight, but this is not desirable until its end-use application. The molecular weight is lowered and the polysulfide rank (value of \( x \)) is simultaneously brought close to 2 by reductive treatment with \( \text{NaSH} \) and \( \text{Na}_2\text{SO}_3 \) followed by acidification. The result is a liquid, branched polysulfide with terminal thiol end groups and a molecular weight in the range 1000–8000. Curing to a solid elastomer is accomplished by oxidation of thiol to disulfide links by oxidants such as lead dioxide and \( p \)-quinone dioxime (Eq. 2-191).

\[
\text{ClCH}_2\text{CH}_2\text{OCH}_2\text{OCH}_2\text{CH}_2\text{Cl} + \text{Na}_2\text{S}_x \rightarrow \text{[CH}_2\text{CH}_2\text{OCH}_2\text{OCH}_2\text{CH}_2\text{S}_x]_n + \text{NaCl}
\]  
(2-190)
Polysulfides, often referred to as thiokols, are not produced in high volumes. These are specialty materials geared toward a narrow market. The annual production of polysulfides in the United States exceeds 50 million pounds. The advantages and disadvantages of polysulfides both reside in the disulfide linkage. They possess low temperature flexibility and very good resistance to ozone, weathering, oil, solvent (hydrocarbons as well as polar solvents such as alcohols, ketones, esters), and moisture. However, polysulfides have poor thermal stability and creep resistance, have low resilience, and are malodorous. (Aromatic polysulfides do not have the same deficiencies; see Sec. 2-14d.) The major applications of polysulfides are as sealants, caulks, gaskets, O-rings, and cements for insulating glass and fuel tanks, in marine applications, and in gasoline and fuel hose.

2-13 STEP COPOLYMERIZATION

It should be apparent that step polymerization is a versatile means of synthesizing a host of different polymers. The chemical structure of a polymer can be varied over a wide range in order to obtain a product with a particular combination of desirable properties. One can vary the functional group to produce a polyester, polyamide, or some other class of polymer as desired. Further, for any specific class of polymer, there is a considerable choice in the range of structures that can be produced. Consider, for example, that polyamides with either of the general structures XXXIII and XXXIV can be synthesized depending on whether one uses the reaction of a diamine with a diacid or the self-reaction of an amino acid. A range of different polyamides can be obtained by varying the choice of the R and R’ groups in structure XXXIII and the R group in structure XXXIV. Thus, for example, one can produce nylon 6/6 and nylon 6/10 by the reactions of hexamethylene diamine with adipic and sebacic acids, respectively. Nylon 6/10 is more flexible and moisture-resistant than nylon 6/6 because of the longer hydrocarbon segment derived from sebacic acid.

\[\text{XXXIII}\]
\[\text{XXXIV}\]

2-13a Types of Copolymers

Further variation is possible in the polymer structure and properties by using mixtures of the appropriate reactants such that the polymer chain can have different R and R’ groups. Thus polyamide structures of types XXXV and XXXVI are possible variations on structures XXXIII and XXXIV, respectively. A polymer such as XXXV or XXXVI has two different repeat units and is referred to as a copolymer; the process by which it is synthesized is
referred to as a copolymerization. Polymers with structures XXXIII and XXXIV, each containing a single repeat unit, may be referred to as homopolymers to distinguish them from copolymers.

\[ \text{---CO-R-CONH-R'-NHCO-R''-CONH-R'''-NH---} \]

XXXV

\[ \text{---NH-R-CO-NH-R''-CO---} \]

XXXVI

Different types of copolymers are possible with regard to sequencing of the two repeating units relative to each other. Thus a copolymer with an overall composition indicated by XXXV could have the alternating copolymer structure shown in XXXV, in which the R, R', R'', and R''' groups alternate in that order over and over again along the polymer chain; or the block copolymer structure XXXVII, in which blocks of one type of homopolymer structure are attached to blocks of another type of homopolymer structure; or the statistical copolymer structure, in which there is an irregular (statistical) distribution of R and R'' groups as well as R' and R''' groups along the copolymer chain. Similarly, one can have alternating, block, and statistical copolymers for the overall composition XXXVI.

\[ \left( \text{CO-R-CONH-R'-NH} \right)_m \left( \text{CO-R''-CONH-R'''-NH} \right)_p \]

XXXVII

For the statistical copolymer the distribution may follow different statistical laws, for example, Bernoullian (zero-order Markov), first- or second-order Markov, depending on the specific reactants and the method of synthesis. This is discussed further in Secs. 6-2 and 6-5. Many statistical copolymers are produced via Bernoullian processes wherein the various groups are randomly distributed along the copolymer chain; such copolymers are random copolymers. The terminology used in this book is that recommended by IUPAC [Ring et al., 1985]. However, most literature references use the term random copolymer independent of the type of statistical distribution (which seldom is known).

The alternating and statistical copolymer structures can be symbolized as

\[ \sim\text{ABABABABABABABABABABAB} \sim\]

Alternating copolymer

\[ \sim\text{AABABBBABAABAAAABBBABBAAAB} \sim\]

Statistical copolymer

where A and B represent two different repeating units. Different block copolymers are distinguished by the number of blocks per molecule, for example

\[ A_mB_p \quad A_mB_pA_m \quad A_mB_pA_mB_p \quad (A_mB_p)_n \]

Diblock Triblock Tetramer Multiblock

which are referred to as AB diblock, ABA triblock, ABAB tetrablock, and AB multiblock copolymers, respectively. For the various block copolymers the values of m and p as well
as \( n \) are average values; thus, there is a distribution of block lengths and number of blocks along the copolymer chain. There is considerable structural versatility possible for statistical and block copolymers in terms of the relative amounts of A and B in a copolymer. For block copolymers there is the additional variation possible in the number of blocks of A and B and their block lengths (values of \( m \) and \( p \)).

Alternating, statistical, and random copolymers are named by following the prefix \( \text{poly} \) with the names of the two repeating units. The specific type of copolymer is noted by inserting \(-alt-\), \(-stat-\), or \(-ran-\) in between the names of the two repeating units; \(-co-\) is used when the type of copolymer is not specified: poly(A\(-co\)-B), poly(A\(-alt\)-B, poly(A\(-stat\)-B), poly(A\(-ran\)-B). Block copolymers are named by inserting \(-block-\) in between the names of the homopolymers corresponding to each of the blocks. The di-, tri-, tetra-, and multiblock copolymers are named as polyA\(-block\)-polyB, PolyA\(-block\)-polyB\(-block\)-polyA, polyA\(-block\)-polyB\(-block\)-polyA\(-block\)-polyB, and poly(polyA\(-block\)-polyB), respectively. Adoption in the literature of some of these IUPAC recommendations for naming copolymers has been slow.

```
\[ \text{B} \]
\[ \text{B} \]
\[ \text{B} \]
\[ \text{B} \]
\[ \text{B} \]
\[ \text{B} \]
\[ \text{B} \]
\[ \text{B} \]
\[ \text{B} \]
\[ \text{B} \]
\[ \text{B} \]

Graft copolymer
```

A fourth type of copolymer is the \textit{graft copolymer} in which one or more blocks of homopolymer B are grafted as branches onto a main chain of homopolymer A. Graft copolymers are named by inserting \(-graft-\) in between the names of the corresponding homopolymers; the main chain is named first (e.g., polyA\(-graft\)-polyB). Graft copolymers are relatively unimportant for step polymerizations because of difficulties in synthesis. Graft copolymers are considered further in Sec. 9-8.

The discussion to this point has involved copolymers in which both repeating units have the same functional group. A second category of copolymer involves different functional groups in the two repeat units, for example, an amide–ester copolymer such as

\[
\text{—NH—R—CO—O—R”—CO—}
\]

XXXVIII

instead of the amide–amide copolymer XXXVI. Both categories of copolymers are important, although not in the same manner.
2-13b Methods of Synthesizing Copolymers

2-13b-1 Statistical Copolymers

The copolymerization of a mixture of monomers offers a route to statistical copolymers; for instance, a copolymer of overall composition \( \text{XXXV} \) is synthesized by copolymerizing a mixture of the four monomers

\[
\begin{align*}
\text{HO}_2\text{C} & - \text{R} - \text{CO}_2\text{H} \\
\text{HO}_2\text{C} & - \text{R''} - \text{CO}_2\text{H} \\
\text{H}_2\text{N} & - \text{R'} - \text{NH}_2 \\
\text{H}_2\text{N} & - \text{R'''} - \text{NH}_2
\end{align*}
\]  

\text{Copolymer of XXXV} \tag{2-192}

It is highly unlikely that the reactivities of the various monomers would be such as to yield either block or alternating copolymers. The quantitative dependence of copolymer composition on monomer reactivities has been described [Korshak et al., 1976; Mackey et al., 1978; Russell et al., 1981]. The treatment is the same as that described in Chap. 6 for chain copolymerization (Secs. 6-2 and 6-5). The overall composition of the copolymer obtained in a step polymerization will almost always be the same as the composition of the monomer mixture since these reactions are carried out to essentially 100% conversion (a necessity for obtaining high-molecular-weight polymer). Further, for step copolymerizations of monomer mixtures such as in Eq. 2-192 one often observes the formation of random copolymers. This occurs either because there are no differences in the reactivities of the various monomers or the polymerization proceeds under reaction conditions where there is extensive interchange (Sec. 2-7c). The use of only one diacid or one diamine would produce a variation on the copolymer structure with either \( \text{R} = \text{R''} \) or \( \text{R'} = \text{R'''} \) [Jackson and Morris, 1988].

Statistical copolymers containing repeating units each with a different functional group can be obtained using appropriate mixture of monomers. For example, a polyestermide can be synthesized from a ternary mixture of a diol, diamine, and diacid or a binary mixture of a diacid and amine-alcohol [East et al., 1989].

2-13b-2 Alternating Copolymers

The alternating copolymer of composition \( \text{XXXV} \) cannot be synthesized. However, it is possible to synthesize an alternating copolymer in which \( \text{R'''} = \text{R} \) by using a two-stage process [Ueda, 1999]. In the first stage, a diamine is reacted with an excess of diacid to form a trimer

\[
n\text{HO}_2\text{C} - \text{R} - \text{CO}_2\text{H} + n\text{H}_2\text{N} - \text{R'} - \text{NH}_2 \rightarrow n\text{HO}_2\text{C} - \text{R} - \text{CONH} - \text{R'} - \text{NHCO} - \text{R} - \text{CO}_2\text{H} \tag{2-193}
\]

The trimer is then reacted with an equimolar amount of a second diamine in the second stage:

\[
n\text{HO}_2\text{C} - \text{R} - \text{CONH} - \text{R'} - \text{NHCO} - \text{R} - \text{CO}_2\text{H} + n\text{H}_2\text{N} - \text{R'''} - \text{NH}_2 \rightarrow \text{HO} - \left(\text{CO} - \text{R} - \text{CONH} - \text{R'} - \text{NHCO} - \text{R} - \text{CONH} - \text{R'''} - \text{NH}\right)_n\text{H} + (2n-1)\text{H}_2\text{O} \tag{2-194}
\]

Alternating copolymers with two different functional groups are similarly synthesized by using preformed reactants [Adduci and Amone, 1989; Gopal and Srinivasan, 1986; Liou and
Hsiao, 2001b; Mormann et al., 1989]. For example, polyamideurethanes analogous to XXXIV and XXXV are obtained by the polymerizations

\[
OCN-R\rightarrow CONH-R'\rightarrow OSi(CH_3)_3 + HF \rightarrow CO-NH-R\rightarrow CO-NH-R'\rightarrow O + \frac{1}{n} \tag{2-195}
\]

\[
OCN-R\rightarrow CONH-R'\rightarrow NHCO-R\rightarrow NCO + HO-R''\rightarrow OH \rightarrow CONH-R\rightarrow CONH-R'\rightarrow NHCO-R\rightarrow NHCOO-R''\rightarrow O + \frac{1}{n} \tag{2-196}
\]

The silyl ether derivative of the alcohol is used in Eq. 2-195 since the corresponding alcohol \(OCN-R\rightarrow CONH-R'\rightarrow OH\) cannot be isolated because of the high degree of reactivity of isocyanate and alcohol groups toward each other.

2-13b-3 Block Copolymers

There are two general methods for synthesizing block copolymers [Gaymans et al., 1989; Hadjichristidis, 2002; Hedrick et al., 1989; Klein et al., 1988; Leung and Koberstein, 1986; Reiss et al., 1985; Speckhard et al., 1986]. The two methods, referred to here as the one-prepolymer and two-prepolymer methods, are described below for block copolymers containing different functional groups in the two repeat units. They are equally applicable to block copolymers containing the same functional group in the two repeating units. The two-prepolymer method involves the separate synthesis of two different prepolymers, each containing appropriate end groups, followed by polymerization of the two prepolymers via reaction of their end groups. Consider the synthesis of a polyester-block-polyurethane. A hydroxy-terminated polyester prepolymer is synthesized from \(HO-R\rightarrow OH\) and \(HOOC-R\rightarrow COOH\) using an excess of the diol reactant. An isocyanate-terminated polyurethane prepolymer is synthesized from \(OCN-R''\rightarrow NCO\) and \(HO\rightarrow R''\rightarrow OH\) using an excess of the diisocyanate reactant. The \(\alpha,\omega\)-dihydroxypolyester and \(\alpha,\omega\)-diisocyanatopolyurethane prepolymers, referred to as macrodiol and macrodiisocyanate respectively, are subsequently polymerized with each other to form the block copolymer.

\[
\rho \left\{ O\rightarrow R\rightarrow OOC\rightarrow R'\rightarrow CO \right\}_n OR\rightarrow OH + \\
\rho \left\{ R''\rightarrow NHCOO\rightarrow R''\rightarrow OOCNH \right\}_m R''\rightarrow NCO \rightarrow \\
\left\{ O\rightarrow R\rightarrow OOC\rightarrow R'\rightarrow CO \right\}_n OR\rightarrow OOCNH \left\{ R''\rightarrow NHCOO\rightarrow R''\rightarrow OOCNH \right\}_m R''\rightarrow NHCOO \rightarrow p \tag{2-197}
\]

The block lengths \(n\) and \(m\) can be varied separately by adjusting the stoichiometric ratio \(\rho\) of reactants and conversion in each prepolymer synthesis. In typical systems the prepolymers have molecular weights in the range 500–6000. The molecular weight of the block copolymer is varied by adjusting \(\rho\) and conversion in the final polymerization. A variation of the two-prepolymer method involves the use of a coupling agent to join the prepolymers. For example, a diacyl chloride could be used to join together two different macrodiols or two different macrodiamines or a macrodiol with a macrodiamine.
The one-prepolymer method involves one of the above prepolymers with two “small” reactants. The macrodiol is reacted with a diol and diisocyanate

\[
pH(O-R-OOC-R’-CO)\, OR-\text{OH} + mpHO-R”-\text{OH} + p \,(m + 1) \text{OCN}-R”-\text{NCO} \rightarrow
\]

\[
\left\{(O-R-OOC-R’-CO)\, OR-\text{OOCNH}(R”-\text{NCOO}-R”'-\text{OOCNH})_m\, R”'-\text{NHCO} \right\}_p
\]

(2-198)

The block lengths and the final polymer molecular weight are again determined by the details of the prepolymer synthesis and its subsequent polymerization. An often-used variation of the one-prepolymer method is to react the macrodiol with excess diisocyanate to form an isocyanate-terminated prepolymer. The latter is then chain-extended (i.e., increased in molecular weight) by reaction with a diol. The one- and two-prepolymer methods can in principle yield exactly the same final block copolymer. However, the dispersity of the polyurethane block length (\(m\) is an average value as are \(n\) and \(p\)) is usually narrower when the two-prepolymer method is used.

The prepolymers described above are one type of telechelic polymer. A telechelic polymer is one containing one or more functional end groups that have the capacity for selective reaction to form bonds with another molecule. The functionality of a telechelic polymer or prepolymer is equal to the number of such end groups. The macrodiol and macrodiisocyanate telechelic prepolymers have functionalities of 2. Many other telechelic prepolymers were discussed in Sec. 2-12. (The term functional polymer has also been used to describe a polymer with one or more functional end groups.)

2-13c Utility of Copolymerization

There has been enormous commercial success in the synthesis of various copolymers. Intense research activity continues in this area of polymer science with enormous numbers of different combinations of repeating units being studied. Copolymer synthesis offers the ability to alter the properties of a homopolymer in a desired direction by the introduction of an appropriately chosen second repeating unit. One has the potential to combine the desirable properties of two different homopolymers into a single copolymer. Copolymerization is used to alter such polymer properties as crystallinity, flexibility, \(T_m\), and \(T_g\). The magnitudes, and sometimes even the directions, of the property alternations differ depending on whether statistical, alternating, or block copolymers are involved. The crystallinity of statistical copolymers is lower than that of either of the respective homopolymers (i.e., the homopolymers corresponding to the two different repeating units) because of the decrease in structural regularity. The melting temperature of any crystalline material formed is usually lower than that of either homopolymer. The \(T_g\) value will be in between those for the two homopolymers. Alternating copolymers have a regular structure, and their crystallinity may not be significantly affected unless one of the repeating units contains rigid, bulky, or excessively flexible chain segments. The \(T_m\) and \(T_g\) values of an alternating copolymer are in between the corresponding values for the homopolymers. Block copolymers often show significantly different behavior compared to alternating and statistical copolymers. Each type of block in a block copolymer shows the behavior (crystallinity, \(T_m\), \(T_g\)) present in the corresponding homopolymer as long as the block lengths are not too short. This behavior is typical since A blocks from different polymer molecules aggregate with each other and, separately, B blocks from
different polymer molecules aggregate with each other. This offers the ability to combine the properties of two very different polymers into one block copolymer. The exception to this behavior occurs infrequently—when the tendency for cross-aggregation between A and B blocks is the same as for self-aggregation of A blocks with A blocks and B blocks with B blocks.

Most commercial utilizations of copolymerization fall into one of two groups. One group consists of various statistical (usually random) copolymers in which the two repeating units possess the same functional group. The other group of commercial copolymers consists of block copolymers in which the two repeating units have different functional groups. There are very few commercial statistical copolymers in which the two repeating units have different functional groups. The reasons for this situation probably reside in the difficulty of finding one set of reaction conditions for simultaneously performing two different reactions, such as amidation simultaneously with ether formation. Also, the property enhancements available through this copolymerization route are apparently not significant enough in most systems to motivate one to overcome the synthetic problem by the use of specially designed monomers. The same synthetic and property barriers probably account for the lack of commercial alternating copolymers in which the two repeating units have different functional groups. Similar reasons account for the general lack of commercial block copolymers in which the two repeating units have the same functional group. The synthetic problem here is quite different. Joining together blocks of the same type of repeat unit is not a problem, but preventing interchange (Sec. 2-7c) between the different blocks is often not possible. Scrambling of repeating units via interchange is also a limitation on producing alternating copolymers in which both repeating units have the same functional group. With all the present research activity in copolymer synthesis, one might expect the situation to be significantly different in the future.

### 2-13c-1 Statistical Copolymers

Statistical copolymerization is practiced in many of the polymerization systems discussed in Secs. 2-8 and 2-12. Mixtures of phenol with an alkylated phenol such as cresol or bisphenol A are used for producing specialty phenolic resins. Trifunctional reactants are diluted with bifunctional reactants to decrease the crosslink density in various thermosetting systems. Methylphenyl-, diphenyl-, and methylvinylchlorosilanes are used in copolymerization with dimethyl dichlorosilane to modify the properties of the polysiloxane. Phenyl groups impart better thermal and oxidative stability and improved compatibility with organic solvents. Vinyl groups introduce sites for crosslinking via peroxides (Sec. 9-2c). Polysiloxanes with good fuel and solvent resistance are obtained by including methyltrifluoropropylchlorosilane. Flame retardancy is imparted to the polycarbonate from bisphenol A (Eq. 2-127) by statistical or block copolymerization with a tetrabromo derivative of bisphenol A.

Statistical copolymerization of ethylene glycol and 1,4-butanediol with dimethyl terephthalate results in products with improved crystallization and processing rates compared to poly(ethylene terephthalate). Pol ary rates (trade names: Ardel, Arylon, Durel), copolymers of bisphenol A with iso- and terephthalate units, combine the toughness, clarity, and processability of polycarbonate with the chemical and heat resistance of poly(ethylene terephthalate). The homopolymer containing only terephthalate units is crystalline, insoluble, sometimes infusible, and difficult to process. The more useful copolymers, containing both tere- and isophthalate units, are amorphous, clear, and easy to process. Pol ary rates are used in automotive and appliance hardware and printed-circuit boards. Similar considerations in the copolymerization of iso- and terephthalates with 1,4-cyclohexanediethanol or hexa- methylene diamine yield clear, amorphous, easy-to-process copolyesters or copolyamides,
respectively, which are used as packaging film for meats, poultry, and other foods. The use of a mixture of unsaturated and saturated diacids or dianhydrides allows one to vary the crosslink density (which controls hardness and impact strength) in unsaturated polyesters (Sec. 2-12a). The inclusion of phthalic anhydride improves hydrolytic stability for marine applications.

2-13c-2 Block Copolymers

Polyurethane multiblock copolymers of the type described by Eqs. 2-197 and 2-198 constitute an important segment of the commercial polyurethane market. The annual global production is about 250 million pounds. These polyurethanes are referred to as thermoplastic polyurethanes (TPUs) (trade names: Estane, Texin). They are among a broader group of elastomeric block copolymers referred to as thermoplastic elastomers (TPEs). Crosslinking is a requirement to obtain the resilience associated with a rubber. The presence of a crosslinked network prevents polymer chains from irreversibly slipping past one another on deformation and allows for rapid and complete recovery from deformation.

Crosslinking in conventional elastomers is chemical; it is achieved by the formation of chemical bonds between copolymer chains (Sec. 9-2). Crosslinking of thermoplastic elastomers occurs by a physical process as a result of their microheterogeneous, two-phase morphology. This is a consequence of morphological differences between the two different blocks in the multiblock copolymer [Manson and Sperling, 1976]. One of the blocks, the polyester or polyether, is flexible (soft) and long while the other block, the polyurethane, is rigid (hard) and short. The rigidity of the polyurethane blocks is due to crystallinity and hydrogen bonding. (For other thermoplastic elastomers such as those based on styrene and 1,3-dienes, the rigidity of the hard polystyrene blocks is due to their glassy nature; see Sec. 5-4a.) The hard blocks from different copolymer molecules aggregate together to form rigid domains at ambient temperature. These rigid domains comprise a minor, discontinuous phase dispersed in the major, continuous phase composed of the rubbery blocks from different copolymer chains. The rigid domains act as physical crosslinks to hold together the soft, rubbery domains in a network structure. Physical crosslinking, unlike chemical crosslinking, is thermally reversible since heating over the $T_m$ of the hard blocks softens the rigid domains and the copolymer flows. Cooling reestablishes the rigid domains, and the copolymer again behaves as a crosslinked elastomer.

Thermoplastic elastomers have the important practical advantage over conventional elastomers that there is no need for the additional chemical crosslinking reaction, which means that fabrication of objects is achieved on conventional equipment for thermoplastics. The transition from a molten polymer to a solid, rubbery product is much faster and takes place simply on cooling. There are significant advantages in recycle times, the ability to recycle scrap, and overall production costs. However, thermoplastic elastomers generally are not as effective as chemically crosslinked elastomers in solvent resistance and resistance to deformation at high temperature. TPE is not used in applications such as automobile tires, where these properties are important. Thermoplastic polyurethanes are used in applications such as wire insulation, automobile fascia, footwear (lifts, ski boots, football cleats), wheels (industrial, skateboard), and adhesives, where such properties are not important. Two types of macrodiols are used in the synthesis of TPU—polyesters, as described in Eqs. 2-197 and 2-198, and $\alpha,\omega$-dihydroxy polyethers obtained by ring-opening polymerizations (Chap. 7) of ethylene and propylene oxides and tetrahydrofuran (THF). The polyester-based TPU is tougher and has better oil resistance while the polyether-based TPU shows better low temperature flexibility and better hydrolytic stability. Spandex (trade name: Lycra) fibers are
multiblock polyurethanes similar to TPU. Spandex typically differs from TPU in containing urea linkages instead of urethane in the hard blocks. These are obtained by using a diamine (instead of diol) to chain-extend isocyanate-terminated polyurethane prepolymers (synthesized from macroglycol and excess diisocyanate). Spandex fibers can undergo large, reversible deformations and are used in the manufacture of undergarments. The various multiblock polyurethanes are often referred to as segmented polyurethanes.

Other important thermoplastic elastomers are the multiblock polyetheresters (trade names: Hytrel, Lomod) and polyetheramides (trade names: Pebax, Estamid, Grilamid).

2-13c-3 Polymer Blends and Interpenetrating Polymer Networks

Polymer blends and interpenetrating polymer networks (IPNs) are different from copolymers but like copolymers are used to bring together the properties of different polymers [Paul et al., 1988]. The total of all polymer blends (produced by both step and chain reactions) is estimated at about 3% of the total polymer production—about 3 billion pounds per year in the United States. There is considerable activity in this area since “new” products can be obtained and markets expanded by the physical mixing together of existing products. No new polymer need be synthesized.

Polycarbonate is blended with a number of polymers including PET, PBT, acrylonitrile–butadiene–styrene terpolymer (ABS) rubber, and styrene–maleic anhydride (SMA) copolymer. The blends have lower costs compared to polycarbonate and, in addition, show some property improvement. PET and PBT impart better chemical resistance and processability, ABS imparts improved processability, and SMA imparts better retention of properties on aging at high temperature. Poly(phenylene oxide) blended with high-impact polystyrene (HIPS) (polybutadiene-graft-polystyrene) has improved toughness and processability. The impact strength of polyamides is improved by blending with an ethylene copolymer or ABS rubber.

The interpenetrating polymer network is a blend of two different polymer networks without covalent bonds between the two networks. An IPN is obtained by the simultaneous or sequential crosslinking of two different polymer systems [Kim et al., 1986; Klempner and Berkowski, 1987; Sperling, 1981, 1986, 1997]. IPN synthesis is the only way of achieving the equivalent of a physical blend for systems containing crosslinked polymers. A simultaneous IPN, referred to as SIN, is produced by reacting a mixture of the monomers, crosslinking reagents, and catalysts for the two crosslinking systems. A sequential IPN (SIPN) is produced by reacting a mixture of one crosslinked polymer and the ingredients for the other crosslinking system. Semi-IPN and pseudo-IPN refer to sequential and simultaneous synthesis, respectively, of interpenetrating polymer networks in which one of the polymers is not crosslinked. Interpenetrating polymer networks are possible for a pair of step polymerization systems, a pair of chain polymerization systems, or the combination of step and chain polymerization systems.

There are a number of commercial interpenetrating polymer networks, although they seldom are identified as IPNs. The inclusion of a thermoplastic with an unsaturated polyester decreases the amount of shrinkage of the latter on crosslinking. The inclusion of a polyurethane makes the unsaturated polyester tougher and more resilient. Other examples of useful IPNs are epoxy resin–polysulfide, epoxy resin–polyester, epoxy resin–polyurethane, polyurethane–poly(methyl methacrylate), polysiloxane–polyamide, and epoxy resin–poly (diallyl phthalate). Many of these are not “pure” IPNs as defined above because of the presence of grafting and crosslinking between the two components. This is usually an advantage in producing an IPN with minimal phase separation.
**2-13c-4 Constitutional Isomerism**

The previous discussions pertain to symmetric reactants such as adipic acid and hexamethylenediamine. The situation is more complicated for unsymmetric reactants such as tolylene 2,4-diisocyanate since the reactant can be incorporated into the polymer chain in two different ways. Unsymmetric reactants can be considered as having two different ends, a head (the more substituted end) and a tail (the less substituted end). The polymer has a head-to-tail (H-T) microstructure if successive monomer units are incorporated in the same way. The microstructure is head-to-head (H-H) whenever successive monomer units add in opposite ways. The H-H and H-T microstructures are constitutional isomers. The typical step polymerization is not regioselective and yields a random copolymer; specifically, H-T and H-H structures are randomly arranged in the polymer chain because the two functional groups do not differ sufficiently in reactivity and, more importantly, equilibration usually occurs between H-T and H-H units. There has been some recent success in synthesizing ordered polyamides and polyurethanes, all H-T and all H-H, by using preformed reactants [Li et al., 2001; Nishio et al., 2001; Ueda, 1999]. Some property differences between the ordered and random polymers have been observed, but the differences do not appear to be of major practical importance.

\[ \text{CH}_3 \text{CH}_3 \]

**2-14 HIGH-PERFORMANCE POLYMERS**

The driving force in polymer synthesis is the search for new polymers with improved properties to replace other materials of construction. Polymers are lightweight and can be processed easily and economically into a wide range of shapes and forms. The major synthetic efforts at present are aimed at polymers with high temperature, liquid crystal, conducting, and nonlinear optical properties [Maier et al., 2001; Sillion, 1999]. There is an interrelationship between these efforts as will become apparent.

**2-14a Requirements for High-Temperature Polymers**

There has been a continuing and strong effort since the late 1950s to synthesize high-temperature polymers. The terms heat-resistant and thermally stable polymer, used synonymously with high-temperature polymer, refer to a high-performance polymer that can be utilized at higher use temperatures; that is, its mechanical strength and modulus, stability to various environments (chemical, solvent, UV, oxygen), and dimensional stability at higher temperatures match those of other polymers at lower temperatures. The impetus for heat-resistant polymers comes from the needs in such technological areas as advanced air- and spacecraft, electronics, and defense as well as consumer applications. The advantages of heat-resistant polymers are the weight savings in replacing metal items and the ease of processing polymeric materials into various configurations. Lightweight polymers possessing high strength, solvent and chemical resistance, and serviceability at temperatures in excess of 250°C would find a variety of potential uses, such as automotive and aircraft components.
(including electrical and engine parts), nonstick and decorative coatings on cookware, structural components for aircraft, space vehicles, and missiles (including adhesives, gaskets, composite and molded parts, ablative shields), electronic and microelectronic components (including coatings, circuit boards, insulation), and components such as pipes, exhaust filter stacks, and other structural parts for the chemical and energy-generating (nuclear, geothermal) plants. The synthetic routes studied have involved inorganic and semiinorganic as well as organic systems. The efforts to date have been much more fruitful in the organic systems, which will be discussed in this section. Inorganic and semiinorganic systems will be considered separately in Sec. 2-15.

Both chemical and physical factors determine the heat resistance of polymers [Cassidy, 1980; Critchley et al., 1983; Hedrich and Labadie, 1996; Hergenrother, 1987; Marvel, 1975]. The strengths of the primary bonds in a polymer are the single most important determinant of the heat resistance of a polymer structure. This is especially critical with respect to the bonds in the polymer chain. Breakage of those bonds results in a deterioration of mechanical strength due to the drop in molecular weight. Bond breakages in pendant (side) groups on the polymer chain may not be as disastrous (unless it subsequently results in main-chain breakage). Aromatic ring systems (carbocyclic and heterocyclic) possess the highest bond strengths due to resonance stabilization and form the basis of almost all heat-resistant polymers. The inclusion of other functional groups in the polymer chain requires careful choice to avoid introducing weak links into an otherwise strong chain. Certain functional groups (ether, sulfone, imide, amide, CF$_2$) are much more heat-resistant than others (alkylene, alicyclic, unsaturated, NH, OH).

A number of other factors weaken or strengthen the inherent heat resistance of a polymer chain. Polymer chains based on aromatic rings are desirable not only because of the high primary bond strengths but also because their rigid (stiff) polymer chains offer increased resistance to deformation and thermal softening. Ladder or semiladder polymer structures are possible for chains constructed of ring structures. A ladder polymer has a double-strand structure with an uninterrupted sequence of rings in which adjacent rings have two or more atoms in common (see structure VII in Sec. 1-2c). A semiladder structure has single bonds interconnecting some of the rings. The ladder polymer is more desirable from the viewpoint of obtaining rigid polymer chains. Also, the ladder polymer may be more heat-resistant since two bond cleavages (compared to only one bond cleavage for the semiladder structure) in the same ring are required before there is a large drop in chain length and mechanical strength. Ladder polymers have been synthesized but have no practical utility because of a complete lack of processability. High molecular weight and crosslinking are desirable for the same reason. Strong secondary attractive forces (including dipole–dipole and hydrogen bond interactions) improve heat resistance. Crystallinity increases heat resistance by serving as physical crosslinks that increase polymer chain rigidity and the effective secondary attractions. Branching lowers heat resistance by preventing close packing of polymer chains.

The factors that lead to increased heat resistance also present problems with respect to the synthesis of polymers and their utilization. Rigid polymer chains lead to decreased polymer solubility, and this may present a problem in obtaining polymer molecular weights sufficiently high to possess the desired mechanical strength. Low-molecular-weight polymers may precipitate from the reaction mixture and prevent further polymerization. Polymers with highly rigid chains may also be infusible and intractable, which makes it difficult to process them by the usual techniques into various shapes, forms, and objects. The synthesis of heat-resistant polymers may then require a compromise away from polymer chains with maximum rigidity in order to achieve better solubility and processing properties. There are two general approaches to this compromise. One approach involves the introduction of some
flexibilizing linkages, such as isopropylidene, C=O, and SO₂, into the rigid polymer chain by using an appropriate monomer or comonomer. Such linkages decrease polymer chain rigidity while increasing solubility and processability. The other approach involves the synthesis of reactive telechelic oligomers containing functional end groups capable of reacting with each other. The oligomer, possessing a molecular weight of 500–4000 and two functional end groups, is formed into the desired end-use object by the usual polymer-processing techniques. Subsequent heating of the oligomer results in reaction of the functional end groups with each other. The oligomer undergoes polymerization to higher molecular weight (referred to as chain extension). Crosslinking may also occur depending on the functionality of the A groups.

A number of the polymers considered previously—polycarbonate, aramid, and polyarylate—were among the first commercial successes in the efforts to synthesize polymers with increasingly high use temperatures. In the following sections we will discuss some of the other commercially available heat-resistant polymers followed by a consideration of research efforts to move further up in the temperature scale.

### 2-14b Aromatic Polyethers by Oxidative Coupling

The oxidative coupling polymerization of many 2,6-disubstituted phenols to form aromatic polyethers is accomplished by bubbling oxygen through a solution of the phenol in an organic solvent (toluene) containing a catalytic complex of a cuprous salt and amine [Aycock et al., 1988; Finkbeiner et al., 1977; Hay, 1998, 1999; Jayakannan and Ramakrishnan, 2001; Kobayashi and Higashimura, 2003]. Amine complexes of other oxidants such as cobalt and manganese salts are also useful.

\[
\begin{align*}
n \text{HO} & \quad + \quad \frac{n}{2} \text{O}_2 \\
\rightarrow & \quad \text{Cu}^+ \quad \text{amine} \\
& \quad \text{O} \\
\rightarrow & \quad n \text{H}_2\text{O} \\
\end{align*}
\]

Amines such as diethylamine, morpholine, pyridine, and \(N, N, N', N'\)-tetramethylethylene-diamine are used to solubilize the metal salt and increase the pH of the reaction system so as to lower the oxidation potential of the phenol reactant. The polymerization does not proceed if one uses an amine that forms an insoluble metal complex. Some copper–amine catalysts are inactivated by hydrolysis via the water formed as a by-product of polymerization. The presence of a desiccant such as anhydrous magnesium sulfate or 4-Å molecular sieve in the reaction mixture prevents this inactivation. Polymerization is terminated by sweeping the reaction system with nitrogen and the catalyst is inactivated and removed by using an aqueous chelating agent.

Polymerization proceeds rapidly under mild conditions (25–50°C) for phenols containing small substituents. Phenols with one or more bulky \(o\)-substituents, such as isopropyl or \(t\)-butyl, undergo dimerization instead of polymerization (Eq. 2-200). Dimerization is also the major reaction for phenols with two \(o\)-methoxy substituents. The amine : cuprous ion ratio and the reaction temperature determine the extent of carbon–oxygen coupling (polymerization) relative to carbon–carbon coupling (dimerization), probably by affecting the nature of the complex formed among cuprous ion, amine, and reaction intermediate. Higher amine : cuprous ratios and lower reaction temperatures favor polymerization while dimerization is
favored by higher temperatures and lower amine/cuprous ratios. Phenols with only one ortho substituent undergo branching during polymerization. Polymerization of phenols with only one ortho substituent, and even phenol itself, has been achieved by using sterically hindered amine ligands for the cuprous ion or other catalytic oxidant [Almou et al., 1999; Higashimura et al., 2000a].

The mechanism of oxidative coupling polymerization of phenols involves the reaction sequence in Eqs. 2-201 through 2-205. The copper–amine complex functions as a catalyst for the oxidation by oxygen of the phenol to the monomeric phenoxy radical \( \text{XXXIX} \). The phenoxy radical then undergoes dimerization by carbon–oxygen coupling (Eq. 2-201). Polymerization proceeds by oxidation of the dimer to the corresponding phenoxy radical (Eq. 2-202) followed by carbon–oxygen coupling reactions with monomeric phenoxy radical (Eq. 2-203) and itself (Eq. 2-204). The trimer continues to grow by repeating the oxidation-coupling sequence; the tetramer continues its growth by dissociation (Eq. 2-205) into two phenoxy radicals (a monomer and a trimer) that can undergo coupling reactions. Growth to high-molecular-weight polymer proceeds by successive oxidation-coupling sequences.

The polymer from 2,6-dimethylphenol is the commercial product referred to as poly(p-phenylene oxide) or PPO. The IUPAC name is poly(oxy-2,6-dimethyl-1,4-phenylene). PPO possesses very little measurable crystallinity \( T_m = 262–267^\circ C, T_R = 205–210^\circ C \). There is very little neat PPO used commercially because its high melt viscosity makes processing too difficult. The commercially available products are blends of PPO with high-impact polystyrene (HIPS) (polybutadiene-graft-polystyrene). (Some blends with other rubbery polymers are also available.) Blending overcomes the processing problem by lowering the melt viscosity and also increases the impact strength. However, the continuous use temperature for the blend, referred to as modified PPO (trade name: Noryl), is decreased to the 80–110\(^\circ\)C range with the specific use temperature depending on the relative amount of polystyrene. Modified PPO has close to the lowest water absorption of all engineering plastics, and this imparts excellent electrical properties over a considerable humidity range. It has excellent resistance to aqueous environments, including acids, bases, and oxidants, but this is not matched by its resistance to organic solvents. The resistance of PPO to organic solvents is not as good as that of PET and is much poorer than the resistance of polyamides such as nylon 6/6. PPO has better resistance to aromatic, halogenated, and polar organic solvents compared to polycarbonate.

More than 350 million pounds of modified PPO were produced in the United States in 2001. As with all engineering plastics, the applications for modified PPO include both filled (including reinforced) and unfilled grades. The continuous use temperatures of 80–110\(^\circ\)C indicated above are the maximum use temperatures and these require reinforced grades (e.g., reinforced with fiber glass or carbon-black-filled). A wide range of applications are found for modified PPO: automotive (dashboard, wheel covers, metalized grilles, and trim), electrical (radomes, fuse boxes, wiring splice devices), consumer and business (refrigerator door liners, computer housing, keyboard frame, steam iron), and liquid handling (pipe, valves, pump housing, impellors).
STEP POLYMERIZATION

(2-201)

XXXIX

(2-202)

(2-203)

(2-204)

(2-205)
Polyetherketones and polyethersulfones, also referred to as polyketones and polysulfones, are synthesized by nucleophilic aromatic substitution between aromatic dihalides and bisphenolate salts [Cassidy, 1980; Clagett, 1986; Critchley et al., 1983; Harris and Johnson, 1989; Jayakannan and Ramakrishnan, 2001; Matsumura et al., 2001; May, 1988]. This is shown in Eq. 2-206, where X is halogen and Y is C=O or SO₂:

\[
\begin{align*}
X\text{--}\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\cdot\...
The resistance of polysulfones to aqueous environments, including acids, bases, and oxidants, is excellent. Their resistance to aromatic and halogenated organic solvents is comparable to PPO; PPO is better toward polar solvents but poorer toward aliphatics. Bisphenol A polysulfone differs from the other members of the polysulfone family because of the isopropylidene group. It has lower glass transition and use temperatures and is less resistant to organic solvents. More than 20 million pounds of polysulfones are produced annually in the United States. The very good thermal and hydrolytic stability of polysulfones makes them useful for microwave cookware and in medical, biological, and food-processing and service applications that require repeated cleaning with hot water or steam. Other applications include circuit breakers, electrical connectors, switch and relay bases, radomes, battery cases, camera bodies, aircraft interior parts, and membrane supports for reverse osmosis. Outdoor use is somewhat limited because of relatively low UV stability.

The polyketones are partially crystalline (approximately 35%). PEEK and PEK, respectively, have glass transition temperatures of 143 and 165°C and melting temperatures of 334 and 365°C. Both polyketones have excellent resistance to a wide range of aqueous and organic environments. Their resistance to organics matches that of the polyamides, while their resistance to aqueous environments matches that of the polysulfones. PEEK and PEK are rated for continuous service at temperatures of 240–280°C. These relatively new engineering plastics have an annual production in the United States of about one million pounds. The polyketones are finding applications in parts subjected to high temperature and aggressive environments: automotive (bearing, piston parts), aerospace (structural components), oil and chemical (pumps, compressor valve plates), and electrical–electronic (cable, insulation) applications.
2-14d Aromatic Polysulfides

Poly (p-phenylene sulfide) [IUPAC: poly(sulfanediyl-1,4-phenylene) (trade name: Ryton) (PPS) is synthesized by the reaction of sodium sulfide with p-dichlorobenzene in a polar solvent such as 1-methyl-2-pyrrolidinone (NMP) at about 250°C and 1.1 MPa (160 psi) [Fahey and Geibel, 1996; Hill and Brady, 1988; Lopez and Wilkes, 1989]. The reaction may be more complicated than a simple nucleophilic aromatic substitution [Koch and Heitz, 1983]. PPS undergoes a slow curing process when heated above the melting point in air. Curing involves chain extension, oxidation, and crosslinking, but is poorly understood. There is spectroscopic evidence for crosslinking via sulfur, oxygen, and aromatic bridges between polymer chains [Hawkins, 1976].

\[
\text{Cl} \quad \text{Cl} \quad + \quad \text{Na}_2\text{S} \quad \xrightarrow{-\text{NaCl}} \quad \left[ \text{\begin{array}{c} \text{\text{S}} \\ \text{n} \end{array}} \right]
\]

Uncrosslinked PPS is a highly (≈60%) crystalline polymer with \( T_m = 285°C \) and \( T_g = 85°C \). It is rated for continuous service at 200–240°C, placing PPS between the polysulfones and the polyketones. It has inherent flame resistance, and its stability toward both organic and aqueous environments is excellent. PPS is comparable to polysulfones and polyketones in resistance to acids and bases but is somewhat less resistant to oxidants. The resistance of PPS to organic solvents is comparable to that of polyamides and polyketones. More than 20 million pounds of PPS are produced annually in the United States. Applications of PPS include automotive (components requiring heat and fluid resistance, sockets and reflectors for lights), consumer (microwave oven components, hair-dryer grille), industrial (oilfield downhole components, motor insulation, pumps and valves), blends with fluoro-carbon polymers (release coating for cookware, appliances, molds), and protective coatings (valves, pipe, heat exchangers, electromotive cells). PPS is an alternative to traditional thermosetting plastics in some of these applications.

2-14e Aromatic Polyimides

Aromatic polyimides are synthesized by the reactions of dianhydrides with diamines, for example, the polymerization of pyromellitic anhydride with p-phenylenediamine to form poly(pyromellitimido-1,4-phenylene) (XLV) [de Abajo, 1988, 1999; Hergenrother, 1987; Johnston et al., 1987; Maier, 2001]. Solubility considerations sometimes result in using the half acid–half ester of the dianhydride instead of the dianhydride.

The direct production of high-molecular-weight aromatic polyimides in a one-stage polymerization cannot be accomplished because the polyimides are insoluble and infusible. The polymer chains precipitate from the reaction media before high molecular weights are obtained. Polymerization is accomplished by a two-stage process. The first stage involves an amidation reaction carried out in a polar aprotic solvent such as NMP or N,N-dimethylacetamide (DMAC) to produce a high-molecular-weight poly(amic acid) (XLIV). Processing of the polymer can be accomplished only prior to the second stage, at which point it is still soluble and fusible. It is insoluble and infusible after the second stage of the process. The poly(amic acid) is formed into the desired physical form of the final polymer product (e.g., film, fiber, laminate, coating) and then the second stage of the process is performed. The poly(amic acid) is cyclodehydrated to the polyimide (XLV) by heating at temperatures above 150°C.
The poly(amic acid) is kept in solution during the amidation by using mild temperatures, no higher than 70°C and usually lower than 30°C, to keep the extent of cyclization to a minimum. Less polar, more volatile solvents than NMP and DMAC are sometimes used to facilitate solvent evaporation in the second stage reaction. This requires the use of an acidic or basic catalyst since the reaction rate is decreased in a less polar solvent. The poly(amic acid) is prone to hydrolytic cleavage and has relatively poor storage stability unless kept cold and dry during storage. Temperatures as high as 300°C are used for the second-stage solid-state cyclization reaction, although the use of vacuum or dehydrating agents such as acetic anhydride-pyridine allow lower cyclization temperatures.

Polyimides (PIs) are mostly amorphous materials with high glass transition temperatures. The resistance of PI to organic solvents is excellent. Polyimides show good oxidation resistance and hydrolytic stability toward acidic environments, comparable to PET and better than nylon 6/6. However, PI undergoes hydrolytic degradation in strongly alkaline environments, comparable to polycarbonate and poorer than PET and nylon 6/6. The high temperature resistance of polyimides is excellent with continuous use temperatures of 300–350°C possible, especially for structures containing only aromatic rings. Wholly aromatic polyimides are generally too stiff for most applications, and their processability is limited by poor solubility and lack of melt flow at accessible temperatures.

One of the first commercial polyimides was the polymer obtained from 4,4’-diaminodiphenyl ether and pyromellitic dianhydride (trade names: Kapton, Vespel). This and other similar polyimides are available in the form of poly(amic acid) solutions that are used as high-temperature wire enamels and insulating varnishes and for coating fiber glass and other fabrics. Polyimide films find applications as insulation for electric motors and missile and aircraft wire and cable. There is also some processing of PI by powder technology (low-temperature forming followed by sintering) and compression molding (requiring higher pressures than normal) to form such automotive and aircraft engine parts as bushings, seals, piston rings, and bearings.

The lack of easy processability initially limited the utilization of this high-performance material. Several different modifications of the polyimide system have successfully produced...
materials that are more readily processable at the fully imidized state. Appropriate dianhydrides and diamines are used to increase solubility and melt processability by decreasing molecular order and packing. This is done by introducing flexible segments [aliphatic, O, S, C=O, SO₂, C(CH₃)₂, C(CF₃)₂] into the polyimide chains or bulky side groups (phenyl, t-butyl) or using 1,3-disubstituted reactants instead of 1,4 reactants [de Abajo, 1999; Sillion, 1999; Yokota et al., 2001].

Polyetherimides (PEI) are polyimides containing sufficient ether as well as other flexibilizing structural units to impart melt processability by conventional techniques, such as injection molding and extrusion. The commercially available PEI (trade name: Ultem) is the polymer synthesized by nucleophilic aromatic substitution between 1,3-bis(4-nitrophthalimido) benzene and the disodium salt of bisphenol A (Eq. 2-209) [Clagett, 1986]. This is the same reaction as that used to synthesize polyethersulfones and polyetherketones (Eq. 2-206) except that nitrite ion is displaced instead of halide. Polymerization is carried out at 80–130°C in a polar solvent (NMP, DMAC). It is also possible to synthesize the same polymer by using the diamine–dianhydride reaction. Everything being equal (cost and availability of pure reactants), the nucleophilic substitution reaction is probably the preferred route due to the more moderate reaction conditions.

\[
\begin{align*}
\text{NaO} & \text{C(CH₃)₂} \quad \text{O} \quad \text{ONa} + \\
\text{NO₂} & \text{CO} \quad \text{N} \quad \text{N} \quad \text{NO₂} \\
\text{[} & \text{CO} \quad \text{N} \quad \text{N} \quad \text{CO} \quad \text{O} \quad \text{C(CH₃)₂} \quad \text{O} \text{]}_n \\
\rightarrow & \text{NaNO₂}
\end{align*}
\]

(2-209)

PEI is amorphous with a glass transition temperature of 215°C and continuous-use temperature of 170–180°C. The solvent and chemical resistance of PEI is comparable to that of polyimides as described above, except that it is soluble in partially halogenated organic solvents. Processability by conventional techniques coupled with a wide range of desirable properties has resulted in fast growth for this new polymer. PEI also has the advantage of not having any volatiles (water) produced during processing as occurs during the second-stage cyclization of poly(amic acids). Voids and strains can be generated as volatiles are lost during processing. PEI presently accounts for a major fraction of all polyimides. PEI resins are used in many industries: electrical–electronic (circuit boards, radomes, high-temperature switches), transportation (fuel system components, transmission and jet engine components, lamp sockets), medical (surgical instrument handles, trays, and other items requiring sterilization by steam, ethylene oxide, chemical means, or γ radiation), and consumer and business (microwave cookware, curling irons, food packaging, memory disks, fans for computer and other equipment).

Polyamideimides (PAIs) (trade name: Torlon), containing both amide and imide functional groups in the polymer chain, are produced by the reaction of trimellitic anhydride (or a derivative) with various diamines (Eq. 2-210). PAI resins are amorphous polymers
with glass transition temperatures of 270–285°C and continuous-use temperatures of 220–230°C. Polyamideimides have excellent resistance to organic solvents. PAI has good resistance to acids, bases, and oxidants but is attacked by bases at high temperature. Polyamideimides are used in various aircraft (jet engine, generator, and compressor components), automotive (universal joints, transmission seal rings and washers), and industrial (machine gears and other mechanical components, nonstick and low-friction coatings) applications. Polyesterimides have been commercialized using reactants that possess combinations of imide or imide-forming groups together with carboxyl and hydroxyl groups [Lienert, 1999].

**Bismaleimide** (BMI) polymers are produced by reaction of a diamine and a bismaleimide (Eq. 2-211) [de Abajo, 1988, 1999; Mison and Sillion, 1999]. Polymerization is carried out with the bismaleimide in excess to produce maleimide end-capped telechelic oligomers (XLVI). Heating at temperatures of 180°C and higher results in crosslinking via radical chain polymerization (Chap. 3) of the maleimide carbon–carbon double bonds (Eq. 2-212). The properties of the thermoset product can be varied by changing the Ar and Ar′ groups and the crosslink density. The latter depends on the bismaleimide : diamine ratio. (Further variations are possible by radical copolymerization (including allyl, alkyne, and cyanate functionalities) have been used to allow subsequent crosslinking [Enoki et al., 1995; Mison and Sillion, 1999; Wright and Schorzman, 2001].
BMI polymers have glass transition temperatures in excess of 260°C and continuous-use temperatures of 200–230°C. BMI polymers lend themselves to processing by the same techniques used for epoxy polymers. They are finding applications in high-performance structural composites and adhesives (e.g., for aircraft, aerospace, and defense applications) used at temperatures beyond the 150–180°C range for the epoxies. Bisnadimide (BNI) polymers are similar materials based on bisnadimides instead of bismaleimides.

2-14f Reactive Telechelic Oligomer Approach

We noted several successful alternatives—PEI, PAI, and BMI—used to overcome the inherent lack of processability of polyimides. The BMI approach can be considered a precursor of the reactive telechelic oligomer approach (also referred to as the polymeric monomer reactants approach) for overcoming processability problems in many of the more advanced heat-resistant polymer systems [Mison and Sillion, 1999; Yokota et al., 2001]. The polymer chains in those materials, consisting of heterocyclic and carbocyclic rings, often show poor processability. Even for systems where processability is not a problem, including previously discussed polymers such as polyketone and polysulfone, the reactive telechelic oligomer approach introduces the ability to form thermoset products in addition to thermoplastics. The reactive telechelic oligomer approach will be specifically described in this section for the polyimides, but it has been practiced for a large number of different polymers.

The reactive telechelic oligomer approach is relatively simple. Polymerization is carried out in the usual manner except that one includes a monofunctional reactant to stop reaction at the oligomer stage, generally in the 500–3000 molecular weight range. The monofunctional reactant not only limits polymerization but also end-caps the oligomer with functional groups capable of subsequent reaction to achieve curing of the oligomer (i.e., chain extension as well as crosslinking in most cases). Many different functional groups have been used for this purpose—alkyne, 5-norbornene (bicyclo[2.2.1]hept-4-ene), maleimide, biphenylene, nitrile, [2.2]paracyclophane, and cyanate. Maleimide end-capped oligomers are cured by heating as described above for the BMI polymers. Maleimide end groups can be introduced into polyimide oligomers simply by carrying out polymerization with a mixture of diamine, dianhydride, and maleic anhydride. An alternate approach is to polymerize the dianhydride in the presence of excess diamine to form an amine end-capped polyimide, which is then reacted with maleic anhydride [Lyle et al., 1989].

5-Norbornene end-capped polyimide oligomers (trade name: LARC) are obtained by including 5-norbornene-2,3-dicarboxylic anhydride (nadic anhydride) (XLVII) in the polymerization reaction between a dianhydride and diamine [de Abajo, 1988; Hergenrother, 1987]. Heating the oligomer at 270–320°C results in a thermoset product. The main reaction responsible for crosslinking probably involves a reverse (retro) Diels–Alder reaction of the 5-norbornene system to yield cyclopentadiene and maleimide end-capped oligomer (Eq. 2-213). This is followed by radical copolymerization of cyclopentadiene with the carbon–carbon double bond of maleimide (Eq. 2-214). Crosslinking appears to be more
complex, with additional reactions occurring simultaneously and to different extents depending on the cure temperature—copolymerization of cyclopentadiene with XLVIII as well as XLIX, Diels–Alder reaction of cyclopentadiene and XLVIII to form an adduct that copolymerizes with XLVIII and/or XLIX [Hay et al., 1989].

\[ \text{XLVIII} \xrightarrow{} \text{XLIX} \]

(2-213)

Alkyne end-capped polyimide oligomers are obtained by including an amine or anhydride that contains a triple bond in the polymerization mixture of diamine and dianhydride. Curing to a thermoset product takes place on heating with cyclotrimerization to an aromatic system (Eq. 2-215) as the crosslinking reaction. However, cyclotrimerization is not complete, and the details of the process are not well understood [Hergenrother, 1985; Takeichi and Stille, 1986; Yokota et al., 2001]. Nitrile (\(-\text{C}≡\text{N}\)) and cyanate (\(-\text{O}–\text{C}≡\text{N}\)) groups also undergo cyclotrimerization, but the thermoset structures are not as stable as those formed using alkyne functional groups [Harrys and Spinelli, 1985; Temin, 1982–1983].

Many other functional groups been studied, including [2.2]paracyclophane (L) and allyl 5-norbornene (LI) [Renner and Kramer, 1989; Tan and Arnold, 1988; Upshaw and Stille, 1988]. The curing process due to [2.2]paracyclophane units probably occurs from an initial homolytic breakage at the bond connecting the two methylene groups followed by various radical–radical coupling reactions. Curing due to allyl 5-norbornene units involves both Diels–Alder and ene reactions.
Liquid crystal polymers (LCP) are polymers that exhibit liquid crystal characteristics either in solution (lyotropic liquid crystal) or in the melt (thermotropic liquid crystal) [Ballauf, 1989; Finkelmann, 1987; Morgan et al., 1987]. We need to define the liquid crystal state before proceeding. Crystalline solids have three-dimensional, long-range ordering of molecules. The molecules are said to be ordered or oriented with respect to their centers of mass and their molecular axes. The physical properties (e.g., refractive index, electrical conductivity, coefficient of thermal expansion) of a wide variety of crystalline substances vary in different directions. Such substances are referred to as anisotropic substances. Substances that have the same properties in all directions are referred to as isotropic substances. For example, liquids that possess no long-range molecular order in any dimension are described as isotropic.

Not all crystalline substances lose all long-range molecular order on melting. Some crystalline substances retain one- or two-dimensional long-range molecular order above the crystalline melting point. Such substances are then described as being in the liquid crystal state. They show the flow behavior of isotropic liquids but appear to possess some kind of long-range molecular order greater than the isotropic liquid state but less than the true crystal state. Heating a thermotropic liquid crystal eventually results in its transformation to the liquid state at some temperature, \( T_{lc} \), referred to as the liquid crystal–isotropic phase transformation temperature for thermotropic liquid crystals.

Our understanding of lyotropic liquid crystals follows in a similar manner. The action of solvent on a crystalline substance disrupts the lattice structure and most compounds pass into solution. However, some compounds yield liquid crystal solutions that possess long-range ordering intermediate between solutions and crystal. The lyotropic liquid crystal can pass into the solution state by the addition of more solvent and/or heating to a higher temperature. Thermotropic and lyotropic liquid crystals, both turbid in appearance, become clear when they pass into the liquid and solution states, respectively.

Liquid crystal behavior is due chiefly to molecular rigidity that excludes more than one molecule occupying a particular volume, rather than intermolecular attractive forces. The requirement for a substance to exhibit liquid crystal behavior is molecular shape anisotropy, which is not affected by conformational changes. Some biological molecules (e.g., tobacco mosaic virus, polypeptides, and cellulose) are liquid crystals because of their rigid helical rod conformations. This is not the case for synthetic polymers. The typical polymer liquid crystal is a rigid-rod molecule. (Theoretical studies indicate the molecular length must exceed the diameter by a factor greater than 6 [Flory and Ronca, 1979].) Other anisotropic molecular shapes (e.g., disks) also show liquid crystal behavior but these are much more rare for polymers. Polymer liquid crystals typically show either smectic or nematic liquid crystal behavior. These are shown in Fig. 2-20, where each line (—) represents a polymer molecule. There is a parallel arrangement of the long molecular axes in both nematic and smectic liquid crystals. Smectic liquid crystals are more ordered than nematic liquid crystals as a result of differences in the orientation of their molecular chain ends. Molecular chain ends are coterminus (i.e., lined up next to each other) in smectics but are out of register (i.e., have no particular orientation) in nematics. Another difference between smectic and nematic liquid crystals is that smectics are layered while nematics are seldom layered. (A third type of liquid crystal, cholesteric, involves nematic packing in planes with the molecular axes in each plane turned at an angle relative to those in the next plane, but is rarely observed in polymers.) Smectic liquid crystals, being more ordered, are more viscous than nematics (everything else being equal). Microscopic observations are of prime importance in distinguishing nematic and smectic structures [Demus and Richter, 1978].
Rigid-rod liquid crystal polymer molecules result from having rigid groups either within the polymer chain or as side groups on the polymer chain. These two types of LC polymers, referred to as main-chain and side-chain LC polymers, respectively, are depicted in Fig. 2-21. The rigid groups are referred to as mesogens or mesogenic groups. The mesogens are shown as rigid-rod groups, but other shapes (e.g., disks) are also possible. The collection of mesogenic units results in a molecule that is a rigid rod with molecular shape anisotropy and liquid crystal behavior.

Liquid crystal behavior in polymers has practical consequences. Liquid crystal melts or solutions have lower viscosities than melts or solutions of random-coil polymers and are easier to process. More importantly, the extension and orientation of polymer chains during processing yields highly crystalline products with high modulus and high strength. The moduli and strengths of chain-extended LC polymers is considerably higher than those of...
the chain-folded crystalline polymers formed from non-LC polymers. LC polymers also have significantly increased crystalline melting temperatures as a result of the extended-chain morphology. Thus, the synthetic guidelines are the same for synthesis of heat-resistant and LC polymers—build rigid polymer chains.

Poly(1,4-oxybenzoyl) \((LII)\) [IUPAC: poly(oxy-1,4-phenylenecarbonyl), obtained by self-reaction of \(p\)-hydroxybenzoic acid, and the various aramids (Sec. 2-8f) were among the first LC polymers studied. The experience in commercializing poly(1,4-oxybenzoyl) and the aramids illustrates that one can have “too much of a good thing.” None of these polymers can be melt processed since they undergo decomposition before melting \((T_m > 500^\circ C)\). The aramids are spin processed into fibers using lyotropic solutions in sulfuric acid. It would be preferable to melt-process the polymers or, at least, to use a less aggressive or less dangerous solvent, but these options do not exist. Poly(1,4-oxybenzoyl) \((Ekonol)\) has found limited utility due to a lack of easy processability. It does not have sufficient solubility even in an aggressive solvent to allow solution processing. It can be processed by plasma spraying or powder sintering.

There is a need to decrease the crystalline melting temperature in such very-high-melting LC polymers to achieve a degree of processability. Copolymerization is used to alter the polymer chains in the direction of decreased rigidity but one needs to do it carefully to retain as high modulus, strength, and \(T_m\) as possible. Chain rigidity can be lowered by reducing molecular linearity by incorporating a less symmetric comonomer unit (\(o-\) and \(m-\) instead of \(p-\) or naphthalene rings, other than 1,4-disubstituted, instead of the 1,4-phenylene unit), a comonomer containing a flexible spacer (single bond, oxygen, or methylene between mesogenic monomer units) or a comonomer with flexible side groups [Jin and Kang, 1997; Yamana et al., 1999]. This approach has been successfully applied to poly(1,4-oxybenzoyl). Two copolyesters are commercial products. \(Vecta\) is a copolymer of \(p\)-hydroxybenzoic acid with 6-hydroxy-2-naphthoic acid; \(Xydar\) is a copolymer of \(p\)-hydroxybenzoic acid with \(p,p'\)-biphenol and terephthalic acid. These polymers have continuous service temperatures up to 240°C and find applications for microwave ovenware, automotive components, components for chemical pumps and distillation towers, and electronic devices.

Many of the polymers discussed in the following sections exhibit liquid crystal behavior.

2-14h 5-Membered Ring Heterocyclic Polymers

Polyimides are obtained from amine and carboxyl reactants when the ratio of amine to acid functional groups is 1:2. If reactants with the reverse ratio of amine to acid functional groups are employed, polybenzimidazoles (PBI) are produced; for instance, polymerization of 3,3'diaminobenzidine and diphenyl isophthalate yields poly\([\{(5,5'-bi-1H-benzimidazole)-2,2'-diyl\}-1,3-phenylene\]} (\(LIIa\)) (Eq. 2-216) [Buckley et al., 1988; Hergenrother, 1987;
Marvel, 1975; Ueda et al., 1985]. The reaction probably proceeds by a sequence of two nucleophilic reactions: a nucleophilic substitution to form an amine–amide (Eq. 2-217) followed by cyclization via nucleophilic addition (Eq. 2-218).

Polymerization is often carried out as a two-stage melt polymerization. Oxygen is removed from the reaction system by vacuum and the system purged with nitrogen to avoid loss of stoichiometry by oxidation of the tetramine reactant. The reaction mixture is heated to about 290°C in the first stage with the reaction starting soon after the reactants form a melt (150°C). The high-volume foam produced in this stage is removed, cooled, and crushed to a fine powder. The second-stage reaction involves heating of the powder at 370–390°C under nitrogen.
Considerable efforts have centered on carrying out the synthesis of polybenzimidazoles at more moderate temperatures. Polymerization of the isophthalic acid or its diphenyl ester have been successfully carried out in polyphosphoric acid or methanesulfonic acid–phosphorous pentoxide at 140–180°C, but the reaction is limited by the very low solubilities (<5%) of the reactants in that solvent. The lower reaction temperature is a consequence of activation of the carboxyl reactant via phosphorylation. Lower reaction temperatures are also achieved in hot molten nonsolvents such as sulfolane and diphenyl sulfone, but the need to remove such solvents by a filtration or solvent extraction is a disadvantage.

The PBI in Eq. 2-216 is commercially available in the form of fiber, composite resin, and formed objects (trade name: Celazole). It has good stability and mechanical behavior up to 300°C and higher (about 25°C higher than the most stable polyimides), does not burn and is self-extinguishing. PBI has better hydrolytic stability than aromatic polyamides and polyimides. It has been used to make flight suits for Apollo, Skylab, MIR, and ISS astronauts and cosmonauts, and escape suits for Space Shuttle astronauts. Fiber is spun from PBI using lyotropic solutions of the polymer in solvents such as N,N-dimethylacetamide, in which it is reasonably soluble at the processing temperature of 250°C. Sulfonated PBI has potential for clothes for firefighters. PBI itself is not appropriate for such use since it undergoes extensive shrinkage when exposed to flames. Sulfonation of PBI (on the aromatic rings) greatly reduces this shrinkage problem. Other applications include bushings in injection-molding equipment, electrical connectors in aircraft engines, and ball valve seats in hot-fluid-handling piping.

It should be noted that structure \( \text{LIIIa} \) is an oversimplification for the polymer formed from 3,3-diaminobenzidine and diphenyl isophthalate. Dehydration after ring closure can occur toward either of the two nitrogens, and one would expect more or less random placements of the carbon–nitrogen double bonds. Thus, the PBI structure is a random copolymer of repeating units \( \text{LIIIa}, \text{LIIib}, \) and \( \text{LIIic} \).

\[
\text{LIIib} \quad \text{LIIic}
\]

Polybenzoxazoles (PBO) and polybenzthiazoles (PBT) are related to and synthesized in a manner similar to polybenzimidazoles [Chow et al., 1989; Evers et al., 1981; Hergenrother, 1987; Krause et al., 1988; Maier, 2001; Maruyama et al., 1988; So et al., 1998; Wolfe, 1988]. Synthesis of PBO (\( \text{LIV} \)) and PBT (\( \text{LV} \)) is accomplished by the reactions of a dicarboxyl reactant with a bis-o-aminophenol (\( X = O \)) and bis-o-aminothiophenol (\( X = S \)), respectively (Eqs. 2-219 and 2-220).
A wide range of polymers based on other heterocyclic 5-membered rings have been investigated, including oxadiazole, pyrazole, triazole, tetrazole, and thiophene [Bass et al., 1987; Briffaud et al., 2001; Cassidy, 1980; Critchley et al., 1983; Gebben et al., 1988; Ueda and Sugita, 1988].

Polyquinolines (PQ) are obtained by the Friedlander reaction of a bis-$\alpha$-aminoaromatic aldehyde (or ketone) with an aromatic bisketomethylene reactant [Concilio et al., 2001; Stille, 1981]. The quinoline ring is formed by a combination of an aldol condensation and imine formation (Eq. 2-221). Polymerization is carried out at 135°C in $m$-cresol with poly (phosphoric acid) as the catalyst. The reaction also proceeds under base catalysis, but there...
are more side reactions. There has been a considerable effort to use the reactive telechelic oligomer approach to producing crosslinking polyquinolines [Sutherline and Stille, 1986]. PQs in the repeating unit have been obtained by reactions other than the Friedlander reaction [Moore and Robello, 1986; Ruan and Litt, 1988].

Polyphenylquinoxalines (PPQ) are obtained by the polymerization of aromatic bis-o-diamine and bis-\(\alpha\)-ketoaldehyde reactants in \(m\)-cresol at \(\sim80^\circ\)C [Hergenrother, 1988; Klein et al., 2001]:

\[
\begin{align*}
\text{H}_2\text{N} & \quad \text{NH}_2 \\
\text{H}_2\text{N} & \quad \text{NH}_2
\end{align*}
\begin{align*}
\text{+ H-CO-CO} & \quad \text{CO-CO-H} \\
\end{align*}
\begin{align*}
\text{[N} & \quad \text{N} \\
\text{N} & \quad \text{N} \\
\text{N} & \quad \text{N} \\
\text{N} & \quad \text{N} \\
\text{]} & \quad n
\end{align*}
\]

Reaction temperatures above \(100^\circ\)C are avoided to prevent branching. PPQs can also be synthesized from monomers that contain the quinoxaline ring [Maier, 2001].

Most PQ and PPQ polymers are amorphous, although a few show some crystalline behavior. PQ and PPQ are promising materials as they possess a very good combination of properties: excellent thermal and oxidative stability, resistance to acids and bases, high glass transition temperature, and high strength and modulus. These properties are coupled with a significant ability to be processed. This is especially the case for PPQ polymers. There is a considerable range between the glass transition temperature and the decomposition temperature, which allows for thermoplastic processing. Also, PPQ is soluble in phenolic and chlorinated solvents, although PQ is soluble only in phenolic solvents. The favorable combination of properties has resulted in considerable efforts to explore the synthetic and practical limits of the PQ and PPQ systems. A number of ladder PQ and PPQ polymers have been studied, but the results have been disappointing, as is the case with other ladder polymers. Nonladder PQ and PPQ polymers in the form of films, composites, and adhesives show good high-temperature properties, but their utilization is impeded by high costs.

Many other 6-membered ring systems have been explored as the basis for high-temperature polymers, including anthrazoline, quinazolone, benzoxazinone, and \(s\)-triazine [Cassidy, 1980; Critchley et al., 1983].

\[\text{Anthrazoline} \quad \text{Quinazoline} \quad \text{Benzoxazinone} \quad \text{\(s\)-Triazine}\]

2-14j Conjugated Polymers

There has been a large effort to synthesize organic conjugated polymers [Aldissi, 1989; Fromer and Chance, 1986; Kraft et al., 1998; Maier, 2001; Potember et al., 1987; Pron
and Rannou, 2002; Yamamoto, 2002] because such polymers have potential as semiconducting, conducting, and light-emitting (optoelectronic) materials. Organic polymers offer potential advantages over the traditional inorganic and nonpolymeric materials used for these purposes. First, processing of organic conjugated polymers by molding and other plastics processing techniques into various electrical, electronic, and optoelectronic devices and forms is potentially easier and more economical compared to processes used for inorganic and nonpolymeric materials. Second, the lightweight property of polymer materials would make certain types of applications more practical and economical.

One potential application for conjugated polymers is lightweight rechargeable batteries for portable devices and vehicles. Conducting polymers would serve both current-carrying and ion conduction functions by replacing traditional electrode and electrolyte substances. Another area of application for conducting polymers is their use in building circuitry elements, both passive (conducting circuits) and active (p–n and Schottky junctions). Other potential applications include transparent antistatic coatings for metals and electronic devices, electromagnetic shielding, light-emitting diodes (LEDs), electrodes, biosensors, transistors, and ultrathin, flexible screens for computer and TV monitors.

The structural requirement for a conducting polymer is a conjugated $\pi$-electron system. The typical polymers studied are based on a $\pi$-conjugated electron system constituting the polymer backbone, but conducting polymers are also possible when the $\pi$-conjugated electron system is present as side chains. Polymers with conjugated $\pi$-electron systems display unusual electronic properties, including high electron affinities and low ionization potentials. Such polymers are easily oxidized or reduced by charge-transfer agents (dopants) that act as electron acceptors or electron donors, respectively. This could result in poly(radical–cation)- or poly(radical–anion)-doped conducting materials ($p$-type and $n$-type, respectively) with near-metallic conductivity in some cases. Electrons are removed from or added to the conjugated $\pi$-electron system to form extra holes or electrons, respectively, which carry current by wandering through the polymer chain. The dopant plays an additional role other than bringing about oxidation or reduction. It acts as the bridge or connection for carrying current between different polymer chains. Oxidative dopants include AsF$_5$, I$_2$, AlCl$_3$, and MoCl$_5$. Sodium, potassium, and lithium naphthalides are reductive dopants. The dopant, necessary to impart electrical conduction, often decreases but does not eliminate the processability of a polymer.

A number of other characteristics are required in order to ensure a viable polymeric conductor. Chain orientation is needed to enhance the conducting properties of a polymeric material, especially the intermolecular conduction (i.e., conduction of current from one polymer molecule to another). This is a problem with many of the polymers that are amorphous and show poor orientation. For moderately crystalline or oriented polymers, there is the possibility of achieving the required orientation by mechanical stretching. Liquid crystal polymers would be especially advantageous for electrical conduction because of the high degree of chain orientation that can be achieved. A problem encountered with some doped polymers is a lack of stability. These materials are either oxidants or reductants relative to other compounds, especially water and oxygen.

The first polymer shown to have conducting behavior was polyacetylene (Sec. 8-6c). Some of the polymers investigated as heat-resistant polymers have conjugated $\pi$-electron systems and offer potential as conducting polymers. Among the polymers we have covered up to this point, poly($p$-phenylene sulfide), polyquinoline, and polyquinoxaline have shown some promise as conducting polymers. We now consider a number of other polymers which are more promising as conducting polymers.
2-14j-1 Oxidative Polymerization of Aniline

Passage of current through a solution results in oxidation (electron loss) at the anode and reduction (electron gain) at the cathode. This process is referred to as electrochemical polymerization when polymer is formed. Polyaniline [IUPAC: poly(imino-1,4-phenylene)] is obtained by the oxidative polymerization of aniline in aqueous HCl solution, either by electrochemical polymerization or by using a chemical oxidant such as ammonium persulfate, (NH₄)₂S₂O₈ [Macdiarmid et al., 1987; Mav and Zignon, 2001; Tejskal and Gilbert, 2002; Wei, 2001; Wei et al., 1989, 1990]. Polymerization proceeds by a chain polymerization mechanism, but is included in this section on conjugated polymers for convenience.

Initiation involves a loss of two electrons and one proton from aniline to form a nitrenium ion (Eq. 2-223), which subsequently attacks aniline by electrophilic substitution (Eq. 2-224). Propagation proceeds in a similar manner by oxidation of the primary amine end of a growing polymer chain (Eq. 2-225) followed by electrophilic substitution (Eq. 2-226). The process has been referred to as reactivation chain polymerization to highlight the fact that the chain end formed after each addition of aniline must be reactivated to the nitrenium ion by oxidation and proton loss. The product formed directly from oxidative polymerization is not the neutral structure shown in Eq. 2-226. The polymer has the positively charged structure LVI, which is referred to as emeraldine salt, and it is the conducting form of polyaniline. Other forms of polyaniline can be obtained after synthesis by varying the applied voltage and pH [Sherman et al., 1994]. Polyaniline offers considerable promise for commercialization. There have been extensive studies using substituted anilines alone or in copolymerization with aniline to alter the conducting and optoelectronic properties of the polymer as well as their solubility characteristics.

\[
\begin{align*}
&\text{(2-223)} \\
&\text{(2-224)} \\
&\text{(2-225)} \\
&\text{(2-226)}
\end{align*}
\]

Oxidative polymerizations of thiophene and pyrrole and their derivatives are also under study to obtain polymers with conducting and optoelectronic properties [Jin et al., 2000;
Kraft et al., 1998; Lowen and Van Dyke, 1990; Wei and Tian, 1993]. Reactions other than oxidative polymerization are also being studied for producing polyaniline and polythiophene [Kraft et al., 1998; Loewe et al., 2001]. An example is the Pd-catalyzed dehydrohalogenation between aryl dihalides and aryl primary diamines to synthesize polyanilines [Kanbara et al., 2000].

2-14j-2 Poly(p-phenylene)

One of the earliest attempts to synthesize heat-resistant polymers was the oxidative polymerization of benzene to poly(p-phenylene) [IUPAC: poly(1,4-phenylene)] (Eq. 2-227) [Jones and Kovacic, 1987; Kovacic and Jones, 1987]. The reaction requires the presence of both a Lewis acid catalyst and an oxidant, such as aluminum chloride and cupric chloride. Poly (p-phenylene) is of interest not only for heat resistance but also as a conducting polymer. Unfortunately, the oxidative route yields an insoluble and intractable product of low molecular weight and irregular structure (a mixture of o and p substitution). Similar results have been found for polymerization of biphenyl, p-terphenyl, and naphthalene.

Alternate approaches to the poly(p-phenylene) system have been more successful [Kraft et al., 1998; Schluter, 2001]. The emphasis in these approaches has been on substituted poly(p-phenylene)s with suitable side groups that solubilize the polymer. Also of interest are chromophores as side groups to impart light-emitting properties for specific wavelengths of light. One of the reactions successfully employed is the Suzuki coupling between arylboronic acids (or their esters) and aryl bromides (Eq. 2-228) [Hu, 2003; Schluter and Wegner, 1993]. Another useful reaction is the coupling of aryl dihalides with zinc (Eq. 2-229). These
reactions have been adapted for synthesis of other conjugated polyaromatic polymers, for example, polyfluorenes (LVII).

\[
\text{LVII}
\]

2-14j-3 Poly(p-phenylene Vinylene)

Poly(p-phenylene vinylene) [IUPAC: poly(1,4-phenyleneethene-1,2-diyl)] (PPV) (LVIII) is obtained by the sequence in Eq. 2-230 involving successive base- and heat-induced eliminations of dialkyl sulfide and hydrogen halide [Cho, 2002; Kraft et al., 1998; Lenz et al., 1988; van Breemen et al., 2001]. PPV can also be synthesized by the Heck coupling of aryl halides with alkenes (Eq. 2-231).

\[
\text{LVIII}
\]

The corresponding azomethine polymers (LIX) have been synthesized by the reaction of the appropriate diamine and dialdehyde [Farcas and Grigoras, 2001; Gutch et al., 2001; Morgan et al., 1987].

\[
\text{LIX}
\]
The drive for heat-resistant polymers has led to an exploration of polymers based on inorganic elements since bond energy considerations indicate that such polymers should be superior to organic polymers in thermal stability [Allcock et al., 2003; Archer, 2001; Manners, 1996; Nguyen et al., 1999; Ray, 1978]. Both inorganic and organometallic polymers have been studied. Inorganic polymers are polymers containing no organic groups, while organometallic polymers contain a combination of inorganic and organic groups. Inorganic and organometallic polymers would have potential for a variety of uses—as partial or complete substitutes for organic fibers, elastomers, and plastics where flame and heat resistance are important; as marine antifoulants, bactericides, medicinals, fungicides, adhesives, photoresists, photosensitizers, photostabilizers; and as conducting polymers. In general much of this potential is unrealized, although significant exceptions exist—the polysiloxanes (Secs. 2-12f and 7-11a), poly(p-phenylene sulfide) (Sec. 2-14d), polyphosphazenes (Sec. 7-11b), and polysilanes (Sec. 2-15b-3) are commercial polymers.

2-15a Inorganic Polymers

The synthesis of high-molecular-weight inorganic polymers is more difficult than that of organic polymers. Chain polymerization through multiple bonds is routinely used for organic monomers such as ethylene. This route is not readily available for inorganic polymers because monomers with multiple bonds between inorganic elements are generally unstable. Chain polymerization of cyclic monomers (ring-opening polymerization) offers more promise and is discussed in Chap. 7. Step polymerization using monomers with two different functional groups, relatively easy to accomplish with organic molecules, is more difficult for synthesizing inorganic polymers. The chemistry of inorganic functional groups is not well understood, and monomers of high purity are difficult to prepare. Thus, it is difficult to achieve the polymer molecular weights needed to obtain materials with sufficient mechanical strength for fabrication into plastic, elastomers, and fibers.

With almost no exceptions attempts to synthesize inorganic polymers that can directly substitute for organic polymers have been unsuccessful. Although the intrinsic thermal stability is often good, a variety of difficulties must be overcome before a usable polymer is obtained. Inorganic polymers typically suffer from various combinations of poor hydrolytic stability, low polymer molecular weights, and low chain flexibility. For example, inorganic polymers with high molecular weights and good hydrolytic stability are often highly inflexible. A large deficiency for many polymers is their intractability to current techniques of fabricating polymers into products such as film, fiber, tubing, and other objects. This does not mean that inorganic polymers are useless. Inorganic polymers comprise many of the materials that are employed at home, industry, and elsewhere. Let us briefly consider some of those materials. [Several wholly inorganic polymers, polysulfur, polyselenium, polythiazyl, and poly(dichlorophosphazene), are discussed in Chap. 7.]

2-15a-1 Minerals

A variety of mineral-type materials are inorganic polymers [Ray, 1978]. Silica [(SiO$_2$)$_n$] is found in nature in various crystalline forms, including sand, quartz, and agate. The various crystalline forms of silica consist of three-dimensional, highly crosslinked polymer chains composed of SiO$_4$ tetrahedra where each oxygen atom is bonded to two silicon atoms and each silicon atoms is bonded to four oxygen atoms. Silicates, found in most clay, rocks, and
soils, are also based on SiO₄ tetrahedra. However, they differ from silica in having Si : O ratios under 1 : 2 (compared to 1 : 2 for silica) and contain Si–O⁻ groups with associated metal cations. Single-strand, double-strand (ladder), sheet (composed of multiple-double-strand sheets analogous to graphite), and three-dimensional polymer chains occur depending on the Si : O ratio, cation : Si ratio, and charge on the cation. Talc contains magnesium and possesses a sheet silicate structure. Tremolite, an asbestos mineral, has a double-strand structure and contains calcium and magnesium. The silicates, similar to silica itself, are highly rigid materials because of their ladder, sheet, and three-dimensional structure. Even the single-strand chains are rigid since the cations act to hold together adjacent polymer chains.

2-15a-2 Glasses

Silicate glasses are produced by melting and rapidly cooling silica or a mixture of silica with other materials [Thornton and Colangelo, 1985]. The product is an amorphous glass since molten silica has a strong tendency to supercool. (Special procedures with regard to heating and cooling rates are required to achieve crystallization.) Silica glass differs from crystalline silica in that there is less than full coordination of all silicon and oxygen atoms; that is, not every silicon is coordinated to four oxygens, and not every oxygen is coordinated to two silicons. Fused-silica glass, consisting of virtually pure silica, is the most chemically resistant of glasses and exhibits the maximum continuous service temperature (900°C). Its relatively high cost limits its use to special applications such as the fiber optics used in information and image transmission and medical fiberscopes for internal examination of humans and animals. The most commonly encountered glass, referred to as soda-lime glass, is made by incorporating various amounts of calcium, sodium, and potassium into the silicate by adding the appropriate compounds, such as sodium and calcium carbonates or oxides, to molten silica. The properties of the glass (e.g., hardness, softening temperature) are varied by varying the relative amounts of the different cations. This is the glass used for windows, lightbulbs, bottles, and jars. Optical glass is similar to soda-lime glass but is much harder because it contains less sodium ad more potassium. Colored glasses are obtained by the addition of appropriate compounds; for example, chromium(III) and cobalt(II) oxides yield green and blue glasses, respectively. Photochromic glasses, which darken reversibly on exposure to light, are obtained by including silver halide in the glass formulation. Vitreous enamels on metal objects and glazes on pottery are glass coatings obtained by covering the item with a paste of the appropriate oxides and heating to a high temperature.

Borosilicate and aluminosilicate glasses are produced by adding B₂O₃ (borax) and Al₂O₃ (alumina), respectively, to molten silica. This produces a structure where boron and aluminum atoms, respectively, replace some silicon atoms in the silicate polymer chain. Laboratory glassware is manufactured from borosilicate glass, which additionally contains sodium and calcium (trade name: Pyrex). The very low coefficient of thermal expansion of borosilicate glasses makes them far less prone to breakage on heating and cooling and especially useful for volumetric glassware. This glass also has very good chemical resistance. Greater chemical resistance, when required, is obtained by using borosilicate glasses with a very high (99.6%) silica content. Pyrex-type borosilicate glasses contain 70–80% silica. (Quartz glassware is used for very special applications.) Aluminosilicate glasses containing calcium and magnesium are used for cookware. There are many naturally occurring aluminosilicate minerals, such as feldspars and zeolites, which contain various combinations of sodium, potassium, and calcium.

A variety of other glassy inorganic polymers are known [Ray, 1978]. Polymetaphosphates are linear polymers produced by heating an alkali dihydrogen phosphate (Eq. 2-232).
Polyultraphosphates, the corresponding branched and crosslinked analogs, are obtained by having phosphoric acid present in the reaction mixture. Chalcogenide glasses are crosslinked polymers formed by the fusion of a chalcogen (S, Se, Te) with one or more of various polyvalent elements (e.g., As, Cd, Ge, P, Si, Sn). Some of these polymers are useful as infrared transparent windows in applications such as infrared detectors and for encapsulating photosensitive transistors.

\[
\text{NaH}_2\text{PO}_4 \xrightarrow{-\text{H}_2\text{O}} \quad \left[ \begin{array}{c} \text{O} \\ \text{P} - \text{O} \\ \text{OH} \end{array} \right]_n
\]

(2-232)

2-15a-3 Ceramics

Ceramic materials have higher heat resistance than do their corresponding glass compositions. The traditional ceramics, such as brick, pottery, and porcelain, are aluminosilicates derived from clay as the main raw material [Jastrzebski, 1976; Thornton and Colangelo, 1985]. These are heterogeneous materials in which microcrystals are embedded in a glass matrix. Clays are produced by the weathering of the mineral feldspar, an aluminosilicate containing sodium and potassium ions. Weathering of feldspar produces kaolinite, empirical formula \( \text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4 \), in the form of small thin platelets. Clays are mixtures of kaolinite with small amounts of feldspar, sand, and other minerals. Most clays are reddish because of the presence of iron(III) oxide as an impurity. Ceramic objects are made by working a mixture of clay with water. Other silicate materials are often added depending on the desired properties in the final product. The presence of water renders the mixture pliable as kaolinite platelets can slide over one another. Firing (heating) of the shaped object results in a complex set of reactions. Water is lost during the process, and the kaolinite platelets can no longer slip past one another. In addition, an aluminosilicate glassy network with its associated cations is formed. The resulting ceramic consists of kaolinite platelets distributed in a glassy aluminosilicate matrix. The partially crystalline nature of these ceramics results in denser materials with higher strength, heat conduction, and heat resistance compared to glasses. Traditional ceramics find a range of applications: pottery, construction bricks, whitewares (porcelain coatings on various household items, and spark plugs, ovenware), and refractory (furnace bricks, mortar, liners, coatings). Most of these applications require the heat-resistant properties inherent in the ceramic materials. However, the strength requirements are not very high in such applications. A second group of ceramic materials, often referred to as new ceramics or high-performance ceramics, have been developed in more recent years [Baldus and Jansen, 1997; Corriu, 2000; Segal, 1991]. These include various pure and mixed oxides, carbides, nitrides, borides, and silicides, (e.g., BeO, ZrO, \( \alpha\)-\( \text{Al}_2\text{O}_3 \), \( \alpha\)-\( \text{SiC} \), \( \text{B}_4\text{C} \), \( \text{TiC} \), \( \text{BN} \), \( \text{AlN} \), \( \text{Si}_3\text{N}_4 \), \( \text{ZrB}_2 \), \( \text{TaB}_2 \); empirical formulas). The new ceramics are used in applications requiring high strength at high temperature, such as parts for gas and jet engines, nuclear plants, high-temperature chemical plants and abrasives, cutting tools, and dies for high-speed machining of metals. Silicon carbide is used for the heat-resistant tiles that protect the space shuttle during reentry into the earth’s atmosphere. Many of the new ceramics are close to being completely crystalline materials. Others consist of crystalline material embedded in a glassy matrix, but the amount of crystalline phase is typically greater than that for the traditional ceramics. Synthesis of the various materials used for the newer ceramics typically requires high-temperature processes; for instance, SiC is produced by the reaction of silica and...
anthracite coal or coke in an electric resistance furnace. The production of objects from the newer ceramics follows in the same manner as the traditional ceramics but with higher firing temperatures (800–1800°C). The firing process at these higher temperatures is referred to as sintering.

The formation of objects from glass and ceramic (especially the new ceramic) materials is achieved only at very high temperatures where there are considerable limitations on the manipulative techniques available to form desired shapes and forms. Two new methods hold considerable promise for producing glass and ceramic objects more easily and at much more moderate temperatures. The key to both methods is the use of very different chemical reactions, based on organic derivatives of the inorganic element, to form the glass or ceramic compound(s). The preceramic polymer method is described in Sec. 2-15b-3. The sol-gel method involves the in situ generation of silica by the base- or acid-catalyzed hydrolysis of tetramethoxy- or tetraethoxysilane in an alcohol–water mixture (Eq. 2-233) [Brinker et al., 1984; Celzard and Mareche, 2002; Corriu, 2000; Corriu and Leclercq, 1996; Hench and West, 1990]. The polymerization conditions (temperature, reactant and catalyst concentrations) may be varied to yield reaction times from minutes to hours or days for completion. Polymerization generally involves initial reaction at ambient temperature followed by an aging process at 50–80°C to develop a controlled network structure. The acid-catalyzed process is slower and easier to control compared to the base-catalyzed process. Tetraacetoxy-silanes have also been used as the silica precursor.

\[
\text{Si(OR)}_4 + \text{H}_2\text{O} \xrightarrow{\text{ROH}} \left\{\text{SiO}_2\right\}_n
\]  

The reaction mixture consists of a silica gel swollen with solvent (alcohol and water) after aging. Densification occurs by a drying step in which solvent is evaporated from the reaction mixture. The product after densification is a microporous, low-density silica referred to as a xerogel or aerogel depending on the conditions of solvent removal. Normal solvent evaporation of the open (to the atmosphere) reaction mixture results in a xerogel. Bleeding solvents slowly from a closed reaction mixture kept under conditions where the solvents are above their critical conditions results in an aerogel. The aerogel is generally lower in density than the xerogel, but both have very low densities and offer potential as lightweight thermal insulators and perhaps even as materials of construction. The last phase of densification may involve temperatures considerably in excess of 100°C to complete the polymerization reaction and drive off the last amounts of solvent. Fabrication of the silica gel, such as by coating onto some object or deice or pouring into a mold, can be carried out at various times during the overall process depending on the specific application. A variety of mixed silicate glasses can be obtained by including other compounds in the reaction mixture. Borosilicate, aluminosilicate, and mixed borosilicate glasses containing various additional cations (e.g., sodium, barium, potassium) are produced by polymerizing a mixture of tetraalkoxysilane with the appropriate alkoxides, acetates, or nitrates of the other metals.

Nonhydrolytic sol-gel synthesis is a more recent variation on the sol–gel method. A metal halide is reacted with an oxygen derivative of the metal (Eq. 2-234). The reaction is catalyzed by Lewis acids such as FeCl₃ and alkyl halide is a by-product [Hay and Raval, 2001]. The reaction has been used to produce alumina (Al₂O₃) and titania (TiO₂) as well as silica [Corriu and Leclercq, 1996].

\[
\text{Si(OR)}_4 \xleftarrow{-\text{RCI}} \text{SiCl}_4 \xrightarrow{\text{ROH}} \left\{\text{SiO}_2\right\}_n
\]  

INORGANIC AND ORGANOMETALLIC POLYMERS
2-15b Organometallic Polymers

Although inorganic polymers find important applications as glasses and ceramics, their high rigidity make them unsuitable for replacement of organic polymers. Organometallic polymers, a compromise between inorganic and organic polymers, have been studied in the effort to achieve the goal of heat-resistant polymers processable by the techniques used for organic polymers. The general approach involves decreasing the extent of ladder, sheet, and three-dimensional structures as well as bridging between different chains through cation–oxygen anion interactions by replacing some of the oxygen linkages to metal atoms by organic linkages. The model for this approach is the polysiloxane system, where the presence of two organic groups attached to each silicon atom greatly changes chain rigidity compared to silica. Although many systems have and are being investigated, commercial success in this field is limited at present.

2-15b-1 Polymerization via Reaction at Metal Bond

Many polymerizations used to synthesize organometallic polymers involve cleavage of a bond to the metal atom of one reactant followed by attachment at that metal of a fragment derived from a second reactant [Carraher et al., 1978; Kaliyappan and Kannan, 2000; Manners, 1996; Nguyen et al., 1999; Pittman et al., 1987; Sheets et al., 1985].

A wide range of reactions have been used, but only a few are illustrated here. Carboxylate and sulfide groups have been used to obtain organometallic polymers (Eqs. 2-235 and 2-236). These types of reactions have been used to synthesize organometallic polymers of a wide variety of other metals (e.g., Zr, Hf, Si, Ge, Pb, As, Sb, Bi, Mn, B, Se). The polymer obtained in Eq. 2-236 contains the titanocene group in which two cyclopentadienyl ligands are coordinated to titanium. Organometallic polymers containing coordinate-bonded metal atoms are referred to as coordination polymers.

The phthalocyanine moiety (LXa), where M represents a coordinated metal, has been incorporated into polymer structures. LXa is abbreviated by structure LXb. One reaction
used for this purpose is the nucleophilic substitution on a phthalocyanine dichloride by a diphenol reactant (Eq. 2-237) [Snow and Griffith, 1988].

\[
\begin{align*}
\text{M} & \quad \text{Cl} \\
\text{Cl} & \\
\text{M} + \text{HO}-\text{Ar}-\text{OH} & \rightarrow \\
\text{M} & \quad \text{O} \\
\text{Ar} & \\
\text{O} & \quad n
\end{align*}
\] (2-237)

2-15b-2 Polymerization without Reaction at Metal Bond

An alternate synthetic approach to organometallic polymers is to perform reactions where the metal atom is not the reaction site. An example is a polyesterification between an organometallic monomer containing two carboxyl groups and a diol (Eq. 2-238). Reaction of the diacid with a diamine would yield an organometallic polymer via polyamidation. A wide range of other reactions covered in this chapter can be used to synthesize organometallic polymers.

\[
\begin{align*}
\text{Co}^+\text{PF}_6^- & \quad \text{COOH} \\
\text{HOOC} & \quad \text{HO}-\text{R}-\text{OH} \\
\text{COO}^-\text{R}-\text{OCO} & \quad \text{Co}^+\text{PF}_6^- \\
\end{align*}
\] (2-238)

2-15b-3 Polysilanes

Polysilanes are polymers in which there is catenation of silicon, that is, where silicon atoms are bonded to each other in a continuous manner. Synthesis of polysilanes involves the Wurtz coupling of diorganodichlorosilanes with sodium metal (Eq. 2-239) [Baldus and Jansen, 1997; Corriu, 2000; Manners, 1996; Miller and Michl, 1989; West, 1986; West and Maxka, 1988; Yajima et al., 1978]. The reaction is typically carried out in a hydrocarbon solvent such as toluene, xylene, or octane at temperatures above 100°C. Polymerization can be achieved at ambient temperature in the presence of ultrasound, which produces high temperature and
pressures locally for short bursts [Kim and Matyjaszewski, 1988]. The mechanism for this reaction is not established, but most evidence indicates polymerization is a complex process involving some combination of radical, anionic, and silylene (the Si analog of carbene) intermediates [Gauthier and Worsfold, 1989; Matyjaszewski et al., 1988]. Furthermore, although included in this chapter, the polymerization is probably a chain reaction. It is included here because of its technological importance in complementing the sol–gel process for producing ceramics. The corresponding polystannanes and polygermanes (Sn and Ge in place of Si) have also been synthesized by the Wurtz coupling reaction.

Polysilanes have been synthesized with various combinations of alkyl and aryl substituents. Polysilanes, such as polydimethylsilane or polydiphenylsilane, with symmetric substitution are highly crystalline and show little or no solubility in a range of organic solvents. (The IUPAC names of the two polymers are poly(dimethylsilanediyl) and poly(diphenylsilanediyl), respectively. They have also been referred to as polydimethylsilylene and polydiphenylsilylene.) Crystallinity is decreased and solubility increased when R and R' are different or for copolymers derived from two different symmetrically substituted dichlorosilanes. There is considerable interest in polysilanes from several viewpoints. Many of the interesting properties of polysilanes result from the relative ease of delocalization of the electrons in the catenated Si–Si σ-bonds as evidenced by the strong ultraviolet absorption at 300–400 nm. Polysilanes undergo photolytic radical cleavage with a high quantum yield and offer potential as radical initiators and positive photoresists. (In a positive photoresist application, the portions of a polymer not protected by a mask are degraded by irradiation and then dissolved by solvent or photovolatilized.) Polysilanes also offer potential as semiconductor, photoconductor and nonlinear optical materials.

The greatest interest in polysilanes is probably in their use as preceramic polymers. The normal powder metallurgy techniques for processing ceramic materials limits the complexity of the objects that can be produced. Polysilane chemistry offers an alternate with good potential for making a variety of objects, including fiber. Thermolysis of a polysilane in an inert atmosphere at 450°C yields a polycarbosilane through a complex rearrangement process. For example, poly(dimethylsilanediyl) yields poly(methylsilanediylmethylene) (LXI) (Eq. 2-240). A soluble portion of the polycarbosilane is isolated by fractional precipitation from n-hexane and used as a ceramic precursor. The soluble polycarbosilane can be formed into objects (including fibers) and then pyrolyzed at 1200°C to yield the corresponding crystalline β-silicon carbide ceramic objects. Other organometallic polymers are being studied for use as precursor polymers for other ceramic systems, such as polysilazanes for silicon nitride [Baldus and Jansen, 1997; Baney and Chandra, 1988].

![Equation 2-240](image)

LXI

The use of a monoalkyltrichlorosilane in the Wurtz-type polymerization is reported to yield (RSi)_n, referred to as polyanalkylsilylene [Bianconi et al., 1989]. The elemental composition and NMR spectra of the polymer suggest a three-dimensional crosslinked structure.

2-16 DENDRITIC (HIGHLY BRANCHED) POLYMERS

There is an ongoing effort to synthesize different, well-defined polymer architectures. A considerable thrust in this direction has been the synthesis of dendritic polymers [Bosman et al.,
Dendritic polymers are highly branched polymers—polymers with treelike branching, where there are branches on branches on branches, and so on. Dendritic polymers differ considerably from linear (and also from lightly branched) polymers in their molecular shapes. Dendritic polymers have globular shapes, whereas linear polymers have elongated shapes. The term globular shape indicates that the dimensions of the polymer molecule are about the same in all directions, whereas the term elongated shape indicates that the dimensions are much greater in one direction than the other directions. [In the extreme, the globular shape is illustrated by a sphere or ellipsoid (where no axis is much longer than the other axes) and the elongated shape, by a cylinder (where the length of the cylinder is much greater than the diameter)].

The difference in molecular shape leads to differences in the attractive secondary forces present in linear and dendritic polymer molecules. The attractive secondary forces are greater for linear (elongated) polymers because the molecules pack together and attract each other over a larger surface area than is possible for dendritic (globular) polymer molecules. Also, dendritic polymer molecules do not undergo chain entanglements as do linear polymers. Thus, unlike linear polymers, dendritic polymers rarely have sufficient strength to be useful as fibers, rubbers, and plastics. However, because of their low secondary forces, dendritic polymers have higher solubility and miscibility with other materials, including other polymers. The globular shape of dendritic polymers also results in lower hydrodynamic volume and lower viscosity compared to linear polymers. Dendritic polymers have potential for use as additives to polymers and oils to modify their viscosity, melt behavior, and lubricating properties; and to aid in compatibilizing mixtures of different materials. The difference between linear and dendritic polymers has an analogy in nature. For example, there are globular and elongated (more often called fibrous) proteins. The fibrous proteins have strong secondary attractive forces and are used to construct such materials as bone, skin, and nails. Globular protein molecules do not attract each other strongly and are soluble in aqueous media, and this fits their biological functions. Globular proteins perform catalytic, transport, regulatory, hormonal, and other functions that require their solubility in blood and the other aqueous media of cells and tissues.

Another (obvious) difference between linear and dendritic polymers is that dendritic polymers have a much larger number of chain ends. The interesting situation arises when the dendritic polymers are synthesized by methods that result in functional groups such as NH$_2$, OH, or COOH at the chain ends. Such polymers carry a large number of derivitizable functional groups and hold promise as carrier molecules for drug delivery, gene therapy, catalysis, and sensors [Frechet and Tomalia, 2002; Stiriba et al., 2002].

Two types of dendritic polymers have been developed: hyperbranched polymers and dendrimers.

### 2-16a Random Hyperbranched Polymers

Hyperbranched polymers are produced in a one-pot synthesis using a multifunctional monomer such as AB$_f$ where $f$ is 2 or greater [Bolton and Wooley, 2002; Galina et al., 2002; Kim, 1998; Voit, 2000]. Hyperbranched polymers are more correctly called random hyperbranched polymers because the branching occurs in a random manner. For an AB$_2$ multifunctional monomer such as a diamino or dihydroxy carboxylic acid, $f = 2$ and the product has a structure described by LXII. With increasing conversion AB$_2$ adds to LXII to produce higher $X_n$ polymer. The random hyperbranched polymer at every stage of its growth has a single...
unreacted A group. The number of unreacted B groups is given by Eq. 2-241 [Kim, 1998]. LXII has $X_n = 13$ and 14 unreacted B groups. The number of unreacted B groups increases with increasing $X_n$ and $f$.

![Diagram of polymer structure](image)

Unreacted B groups = $[1 + X_n(f - 1)]$ \hspace{1cm} (2-241)

A hyperbranched polymer is often characterized by the degree of branching DB [Holter et al., 1997; Jo and Lee, 2001; Kim, 1998; Lee et al., 2000]. For the hyperbranched polymer produced from AB$_2$, there are three different types of repeat units: dendritic, linear, and terminal units defined as units having two, one, and no B groups reacted, respectively. The degree (fraction) of branching (DB) is given by

$$DB = \frac{D + T}{D + T + L}$$ \hspace{1cm} (2-242)

where $D$, $L$, and $T$ are the mole fractions of dendritic, linear, and terminal units. For high molecular weight polymers, $D$, $L$, and $T$ have limiting values of 0.25, 0.25, and 0.50, respectively, and DB is 0.50. (For linear polymers, DB is zero. DB is 1 for dendrimers—Sec. 2-16b.)

Hyperbranched polymers are similar to linear polymers in that they show molecular weight polydispersity. There is also polydispersity due to constitutional isomerism, resulting from the different placements of monomer units. For example, LXII has many isomers, such as those arising from placement of the lower leftmost AB$_2$ unit at any of the other positions around the perimeter of the molecule. The synthesis of hyperbranched polymers has inherent difficulties which limit molecular weight or shape. One is the occurrence of intramolecular cyclization, which decreases the functional groups available for polymerization. Another difficulty is the steric crowding that occurs within and/or at the periphery of hyperbranched molecules with increasing conversion and molecular size. (This steric crowding effect, discussed extensively for dendrimers, is called de Gennes dense packing [de Gennes and Hervet, 1983].) Although steric crowding may not limit polymer molecular weight (as it does for dendrimers), it will affect molecular shape. Functional groups in some regions become inaccessible for reaction, but growth proceeds in other regions where functional groups are accessible. Steric crowding in a region is relieved by an increase of linear (one unreacted
B group) units and fewer dendritic (no unreacted B groups) units. The polydispersity in molecular weight and isomerism, the intramolecular cyclization, and the molecular shape variations due to steric crowding contribute to the random nature of hyperbranched polymers.

Hyperbranched polymers can also be synthesized from the following systems [Jikei and Kakimotoa, 2001]:

\[
\begin{align*}
AB_2 + AB \\
AB_2 + B_3 \\
A_2 + B_3 
\end{align*}
\]

The \( AB_2 + AB \) system is equivalent to \( AB \) 2 except that \( AB \) 2 units are separated from each other by \( AB \) units. The \( AB_2 + B_3 \) system modifies the \( AB \) 2 system by using \( B_3 \) as a central core from which polymerization radiates and offers greater control of molecular shape. The \( A_2 + B_3 \) system is one of the standard systems used to produce crosslinked polymers (Sec. 2-10). It is useful for synthesizing hyperbranched polymers only when crosslinking is minimized by limiting conversion and/or diluting the reactants with solvent.

Hyperbranched polymers can also be synthesized by chain polymerization, ring-opening polymerization, and combinations of ring-opening and step polymerization [Kim, 1998; Voit, 2000] (Secs. 3-6e, 3-15b-4, 3-15b-5, 3-15c, 5-4c).

2-16b Dendrimers

**Dendrimers** are dendritic (highly branched) polymers with a more controlled structure than the hyperbranched polymers [Bosman et al., 1999; Fischer and Vogtle, 1999; Grayson and Frechet, 2001; Hecht, 2003; Newkome et al., 1999; Simanek and Gonzalez, 2002; Tomalia, 2001; Tomalia and Frechet, 2002; Vogtle et al., 2000]. Other terms have also been used to describe various dendritic polymers—*arborol, cascade, cauliflower, starburst*. The synthesis of dendrimers differs greatly from the one-pot procedure for hyperbranched polymers. Dendrimers are synthesized by more complicated processes involving sequential reactions. There are two different methods: divergent and convergent. The divergent method starts with a core molecule and builds outward by attaching to the core successive layers (or generations) of monomer units one at a time. A large variety of reactions (organometallic as well as organic) have been used in synthesizing dendrimers.

The divergent method is illustrated in Fig. 2-22 for the synthesis of polyamidoamine (PAMAM) dendrimers [Tomalia et al., 1990]. A repetitive sequence of two reactions are used—the Michael addition of an amine to an \( \alpha,\beta \)-unsaturated ester followed by nucleophilic substitution of ester by amine. Ammonia is the starting core molecule. The first step involves reaction of ammonia with excess methyl acrylate (MA) to form \( LXIII \) followed by reaction with excess ethylenediamine (EDA) to yield \( LXIV \). \( LXV \) is a schematic representation of the dendrimer formed after four more repetitive sequences of MA and EDA.

Dendrimers are characterized by the number of *generations*, the number of layers or shells of repeat units, analogous to the layering of an onion. The number of generations is the number of repetitive sequences of the Michael addition and nucleophilic substitution reactions. \( LXIV \) and \( LXV \) correspond to generations 1 and 5, respectively. \( LXIV \) has three arms or three \( \text{NH}_2 \) groups. Each generation doubles the number of arms or \( \text{NH}_2 \) groups. The fifth-generation dendrimer (\( LXV \)) has 48 arms or \( \text{NH}_2 \) groups.
The convergent method of dendrimer synthesis is shown in Fig. 2-23 for a dendrimer of five generations. Dendrimeric fragments are synthesized by repetitive reactions, and then several (three for the dendrimer in Fig. 2-23) are joined together in the last step by using a central core molecule to form the dendrimer. The method requires the use of appropriate reactants and chemical reactions. The functional group $Z$ has an identity such that smaller fragments can be linked together to form a larger fragment, either by direct reaction with each other or with a coupling agent. The larger fragment also has a $Z$ group because of the choice of appropriate reactants or coupling agent, and the linking of fragments continues in a repetitive manner. In some systems $Z$ is a protected functional group that is deprotected at the appropriate time.
The convergent method also allows the synthesis of dendrimers of regular shapes other than spheres. Ellipsoid- and rod-shaped dendrimers can be synthesized by using appropriate core molecules [Tomalia, 2001].

Dendrimers have the potential for greater structural regularity and narrower molecular weight distribution than hyperbranched polymers. However, there are problems inherent in dendrimer synthesis that must be controlled to achieve this potential. There are many reactions to carry out, and each reaction includes physical manipulations to wash the product free of reagents. Each of these reactions and physical manipulations must be carried out with 100% efficiency to achieve a monodisperse product. For example, if a fraction of the second generation dendrimer is not perfect, that is, if some functional groups are unreacted, this imperfection is carried through each subsequent generation, and new imperfections in subsequent generations accumulate and carry forward to the higher generations. This is less of a problem for the convergent method than for the divergent method since the latter requires the
carrying out of a much greater number of reactions on a single molecule. The application of solid-phase synthetic techniques (Sec. 9-14) appears useful for increasing the efficiency of dendrimer synthesis [Lebreton et al., 2001].

It becomes progressively more difficult to form each new generation in the divergent synthetic method because of the de Gennes dense packing effect. The steric crowding within a dendrimer molecule and among its peripheral functional groups increases progressively for higher-generation dendrimers. This results in structural defects by distorting the shape of the dendrimer molecule and preventing complete reaction of all functional groups. Steric crowding becomes quite significant after about five generations, and the purity of higher-generation dendrimers decreases fairly rapidly. There are very few reports of dendrimers containing more than 10–15 generations. Steric crowding would appear at first glance to be not as important in the convergent synthetic method because the dendrimer fragments are relatively small compared to the dendrimer molecule. However, steric crowding is present when a number of dendrimer fragments (e.g., three for the synthesis described in Fig. 2-23) need to be joined together by reaction with a central core molecule to form the dendrimer. The steric crowding can be relieved by using a larger and more flexible central core molecule.

How do dendrimers and hyperbranched polymers compare from an industrial viewpoint? Dendrimers offer the potential for producing polymers whose molecular size and structure are more regular and less polydisperse. Hyperbranched polymers are easier and cheaper to synthesize—a one-pot synthesis compared to the multipot synthesis for dendrimers. However, not too many ABₙ monomers are readily available, and this may modify the overall economics. Hyperbranched polymers will probably find use in larger-scale or commodity applications where lower cost is a necessity and dendrimers in specialty applications where higher cost is justified.

2-17 MISCELLANEOUS TOPICS

2-17a Enzymatic Polymerizations

2-17a-1 In Vivo (within Living Cells)

Plants and animals synthesize a number of polymers (e.g., polysaccharides, proteins, nucleic acids) by reactions that almost always require a catalyst. The catalysts present in living systems are usually proteins and are called enzymes. Reactions catalyzed by enzymes are called enzymatic reactions; polymerizations catalyzed by enzymes are enzymatic polymerizations. Humans benefit from naturally occurring polymers in many ways. Our plant and animal foodstuffs consist of these polymers as well as nonpolymeric materials (e.g., sugar, vitamins, minerals). We use the polysaccharide cellulose (wood) to build homes and other structures and to produce paper.

Various microorganisms, such as yeast and bacteria, have been used in industrial bioreactors to produce a host of important products, including alcoholic beverages, penicillin, and carbohydrates (including polysaccharides such as starch). More recently, proteins have been produced for therapeutic purposes by recombinant DNA technology [Blei and Odian, 2000]. Diabetics who lack insulin have until now taken insulin derived from other animals such as pigs and beef. Pig and beef insulins are close to but not exactly the same in structure as human insulin. The bacterium *Escherichia coli* has been used to produce human insulin by recombinant DNA technology. The bacterial DNA is altered in the laboratory to contain the gene for human insulin and then inserted into the organism by various techniques.
(chemical or thermal shock, viral vectors, microinjection). The *E. coli* are fooled into using the altered DNA to produce the desired human protein. The protein is then harvested by breaking the bacterial cell walls and using an appropriate separation technique. This approach offers much potential for producing a host of therapeutic proteins.

There has been an effort to use microorganisms to produce commodity polymers for use as plastics, elastomers, and fibers as a supplement to the polymers produced by the traditional methods such as those described throughout this chapter. Some species of bacteria produce poly(hydroxyalkanoate) (PHA) storage (reserve) polymers when growth is restricted by some nutrient other than their carbon-containing food source [Jung et al., 2000; Shah et al., 2000]. (This is analogous to the storage in higher animals of carbohydrates and lipids as glycogen and triacylglycerols, respectively [Blei and Odian, 2000].) Bacterial cultures such as *Pseudomonas oleovorans* and *Ralstonia eutropha* have been used to produce PHA polymers in the laboratory. The polyester structure can be varied to some extent by controlling the organic feed. *Biopol* is a small-scale commercial product—a copolymer of 3-hydroxybutanoate and 3-hydroxypropionate repeat units. Such polymers are of interest because they are environmentally degradable and offer an alternative to recycling the large volumes of non-degradable polymer wastes.

The mechanism for bacterial synthesis of PHA is not the simple dehydration reaction between alcohol and carboxyl groups. It is more complicated and involves the coenzyme A thioester derivative of the hydroxyalkanoic acid monomer (produced from the organic feedstock available to the bacteria) [Kamachi et al., 2001]. Growth involves an acyl transfer reaction catalyzed by the enzyme *PHA synthase* (also called a polymerase) [Blei and Odian, 2000]. The reaction is not a step polymerization but is a chain polymerization with the characteristics of a living polymerization [Su et al., 2000] (Secs. 3-15, 5-2g, Chap. 7).

### 2-17a-2 In Vitro (outside Living Cells)

The *in vivo* production of commodity polymers has been limited by the difficulties of controlling these processes, including the control of the reaction conditions required to maintain a bacterial culture and the conditions needed to harvest the polymer product. In addition, the *in vivo* method, although applicable for a few polymers, is not useful for the full range of polymers produced by the typical chemical processes. An alternate to the *in vivo* method is the use of enzymes to catalyze in vitro polymerizations. In *in vitro* enzymatic polymerizations are enzyme-catalyzed polymerizations taking place outside cells, that is, taking place in glass and metal reactors. Biochemists carry out *in vitro* enzymatic polymerizations using the same reactants present in *living* cells for the purpose of understanding the reactions within living cells [Kamachi et al., 2001]. For polymer chemists, the major effort is the use of enzymes extracted from living cells to carry out *in vitro* polymerizations of nonnatural substrates to produce polymers for industrial use [Gross et al., 2001; Kobayashi, 1999; Kobayashi et al., 2001].

*Lipases* are enzymes that catalyze the *in vivo* hydrolysis of lipids such as triacylglycerols. Lipases are not used in biological systems for ester synthesis, presumably because the large amounts of water present preclude ester formation due to the law of mass action which favors hydrolysis. A different pathway (using the coenzyme A thioester of a carboxylic acid and the enzyme *synthase* [Blei and Odian, 2000]) is present in biological systems for ester formation. However, lipases do catalyze the *in vitro* esterification reaction and have been used to synthesize polyesters. The reaction between alcohols and carboxylic acids occurs in organic solvents where the absence of water favors esterification. However, water is a by-product and must be removed efficiently to maximize conversions and molecular weights.
The reaction mechanism for the polymerization of a hydroxyalkanoic acid (Eqs. 2-243 through 2-246) is a chain polymerization, often called an *activated monomer polymerization*. The active site of lipase is its serine \( \alpha \)-amino acid unit, which contains a hydroxyl group. The acyl carbon of the hydroxyalkanoic acid undergoes nucleophilic attack by the hydroxyl group of serine to form lipase-activated monomer (Eq. 2-243). Initiation consists of reaction between monomer and lipase-activated monomer by nucleophilic attack of the hydroxyl group of monomer on the acyl carbon of lipase activated monomer, with regeneration of lipase (Eq. 2-244). Propagation proceeds in a similar manner—nucleophilic attack by the hydroxyl end group of a propagating chain on the acyl carbon of lipase-activated monomer, with regeneration of lipase. The reaction can also be considered as an *acyl transfer* reaction to emphasize the transfer of an acyl group from lipase-activated monomer to the hydroxyl group of the propagating chain. Lipases also produce polyesters when anhydrides or esters are used as reactants in place of acids. Ring-opening polymerizations catalyzed by enzymes have also been studied (Sec. 7-5).

Among other in vitro enzymatic polymerizations that have been studied are the oxidative polymerizations of 2,6-disubstituted phenols to poly(\( p \)-phenylene oxide)s (Sec. 2-14b) catalyzed by horseradish peroxidase [Higashimura et al., 2000b] and the polymerization of \( \beta \)-celllobiosyl fluoride to cellulose catalyzed by cellulase [Kobayashi, 1999; Kobayashi et al., 2001].

In vitro enzymatic polymerizations have the potential for processes that are more regioselective and stereoselective, proceed under more moderate conditions, and are more benign toward the environment than the traditional chemical processes. However, little of this potential has been realized. A major problem is that the reaction rates are slow compared to non-enzymatic processes. Enzymatic polymerizations are limited to moderate temperatures (often no higher than 50–75°C) because enzymes are denatured and deactivated at higher temperatures. Also, the effective concentrations of enzymes in many systems are low because the enzymes are not soluble. Research efforts to address these factors include enzyme immobilization to increase enzyme stability and activity, solubilization of enzymes by association with a surfactant or covalent bonding with an appropriate compound, and genetic engineering of enzymes to tailor their catalytic activity to specific applications.
2-17b Polymerization in Supercritical Carbon Dioxide

A supercritical fluid (SCF) is a substance above its critical temperature and critical pressure. The critical temperature is the highest temperature at which a substance can exist as a gas. The critical pressure is the pressure needed at the critical temperature to liquify a gas. Above the critical temperature and critical pressure, a substance has a density characteristic of a liquid but the flow properties of a gas, and this combination offers advantages as a reaction solvent. The liquidlike density allows the supercritical fluid to dissolve substances, while the gaslike flow properties offer the potential for fast reaction rates. Supercritical carbon dioxide (scCO$_2$) has a critical temperature of 31°C and critical pressure of 73 atm.

Supercritical carbon dioxide has found uses in a number of applications. These applications take advantage of the safety and ease of removal of carbon dioxide compared to organic compounds. Decaffeination processes for coffee and tea now use scCO$_2$ instead of methylene chloride, which is a carcinogen. Supercritical carbon dioxide is also used to extract the flavors and fragrances from lemons, nutmeg, and other spices. Other applications include auto bumper coating and dry cleaning. DuPont has recently announced it will use scCO$_2$ technology to produce some fluorinated polymers (Sec. 3-14e).

Supercritical carbon dioxide has been studied as a solvent for various polymerizations, including step, chain, and ring-opening polymerization [Kendall et al., 1999; Wells and DeSimone, 2001]. These results to date indicate that scCO$_2$ will probably not find widespread utilization in polymerizations, primarily because scCO$_2$ is not a good solvent for most polymers (even though it is a good solvent for many small molecules). However, this does not preclude applications in specific polymerizations such as those producing polysiloxanes and fluorinated polymers, which show significant solubility in scCO$_2$, or in applications involving low-molecular-weight polymers.

2-17c Cycloaddition (Four-Center) Polymerization

The Diels–Alder reaction, involving the [4 + 2]-cycloaddition of an unsaturated group (dieneophile) to a 1,3-diene, has been studied for the synthesis of ladder polymers, such as the reaction of 2-vinyl-1,3-butadiene with benzoquinone [Bailey, 1972] (Eq. 2-247). Related polymerizations are those utilizing the [2 + 2]-cycloaddition reaction [Dilling, 1983]. While [4 + 2]-cycloaddition reactions are thermally induced, [2 + 2]-cycloaddition reactions are photochemically induced. The self-addition of alkene double bonds is the most extensively studied [2 + 2]-cycloaddition reaction, such as the polymerization of 2,5-distyrylpyrazine
(Eq. 2-248) [Braun and Wegner, 1983; Hasegawa et al., 1988, 1998]. This polymerization is a solid-state reaction involving irradiation of crystalline monomer with ultraviolet or ionizing radiation. The reaction is a topocchemical or lattice-controlled polymerization in which reaction proceeds either inside the monomer crystal or at defect sites where the product structure and symmetry are controlled by the packing of monomer in the lattice or at defect sites, respectively.

\[
\phi\text{CH}=\text{CH}-\phi\text{N}-\phi\text{CH}=\text{CH}\phi \xrightarrow{\text{hv}} \left[\begin{array}{c}
\phi \\
\text{N}
\end{array}\right]_n
\]

(2-248)

### 2-17d Spiro Polymers

Polymer chains based on spiro structures have been studied as another route to heat-resistant polymers [Kurita et al., 1979]. A spiro structure is a double-strand structure (Sec. 1-2c) in which the uninterrupted sequence of rings have one atom in common between adjacent rings. (Adjacent rings in ladder polymers have two or more atoms in common.) An example of a spiro polymer is the polyspiroketal synthesized from 1,4-cyclohexanedione and pentaerythritol (Eq. 2-249). The low solubility and intractability of spiro polymers makes it difficult to synthesize or utilize high-molecular-weight polymers.

\[
\text{HO-CH}_2\text{C-CH}_2\text{OH} + \text{HO-CH}_2\text{C-CH}_2\text{OH} \xrightarrow{\text{H}^+} \left[\begin{array}{c}
\text{O} \\
\text{O}
\end{array}\right]_n
\]

(2-249)

### 2-17e Pseudopolyrotoxanes and Polyrotoxanes

*Pseudopolyrotoxanes* and *polyrotoxanes* are polymers composed of a linear polymer chain threaded through one or more cyclic species [Gibson and Mahan, 2000; Raymo and Stoddart, 1999]. Synthesis of pseudopolyrotoxanes and polyrotoxanes involves polymerization of monomer(s) in the presence of the cyclic species. Cyclodextrins, crown ethers, paraquots, and other macrocyclics are used as the cyclic component. Both step and chain polymerizations have been successfully used.
There is a statistical extent of threading of the linear polymer chain through the macrocycles present in the reaction system. The extent of threading is greater for larger macrocycles. Threading is reversible and is dependent on enthalpic and entropic factors. The difference between pseudopolyrotaxanes and polyrotaxanes is the placement of bulky groups (Z), referred to as *stoppers*, along the linear polymer for polyrotaxanes. The stoppers prevent unthreading of the macrocycles from the linear polymer chain.

There are many variations on the structures possible for polyrotaxanes. One variation is the number of macrocycles per linear polymer chain. Another is the placement of the stopper groups. One may have stopper groups only at the two chain ends of the polymer. Alternately, there may be many stopper groups distributed randomly along the polymer chain between different cyclic species. In step polymerization, one may achieve the first situation by adding a reactant with the stopper groups at the end of the polymerization—to end-cap the linear polymer. The second situation can be achieved by including a monomer with stopper groups as part of the reaction system at the beginning of polymerization. In chain polymerization, the two different situations can be achieved by using appropriate initiators and terminating agents, or monomers containing the stopper groups.

Another variation for both pseudopolyrotaxanes and polyrotaxanes is the placement of the cyclic component on linear side chains during a graft polymerization process.

REFERENCES


REFERENCES


REFERENCES


PROBLEMS

2-1 Derive an expression for the rate of polymerization of stoichiometric amounts of adipic acid and hexamethylene diamine. Indicate the assumptions inherent in the derivation. Derive an expression for the rate of polymerization of nonstoichiometric amounts of the two reactants.

2-2 A 21.3-g sample of poly(hexamethylene adipamide) is found to contain $2.50 \times 10^{-3}$ mol of carboxyl groups by both titration with base and infrared spectroscopy. From these data the polymer is calculated to have a number-average molecular weight of 8520. What assumption is made in the calculation? How can one experimentally obtain the correct value of $M_n$?

2-3 Describe and draw the structure of the polyester obtained in each of the following polymerizations:

a. $\text{HO}_2\text{C} \rightarrow \text{R} \rightarrow \text{CO}_2\text{H} + \text{HO} \rightarrow \text{R}' \rightarrow \text{OH}$

b. $\text{HO}_2\text{C} \rightarrow \text{R} \rightarrow \text{CO}_2\text{H} + \text{HO} \rightarrow \text{R}'' \rightarrow \text{OH}$

c. $\text{HO}_2\text{C} \rightarrow \text{R} \rightarrow \text{CO}_2\text{H} + \text{HO} \rightarrow \text{R}'' \rightarrow \text{OH} + \text{HO} \rightarrow \text{R}' \rightarrow \text{OH}$

Will the structure of the polymer produced in each case depend on the relative amounts of the reactants? If so, describe the differences.

2-4 Describe and draw the structure of the polyester obtained in each of the following polymerizations:

a. $\text{HO} \rightarrow \text{R} \rightarrow \text{CO}_2\text{H}$

b. $\text{HO} \rightarrow \text{R} \rightarrow \text{CO}_2\text{H} + \text{HO} \rightarrow \text{R}' \rightarrow \text{OH}$

c. $\text{HO} \rightarrow \text{R} \rightarrow \text{CO}_2\text{H} + \text{HO} \rightarrow \text{R}'' \rightarrow \text{OH}$

d. $\text{HO} \rightarrow \text{R} \rightarrow \text{CO}_2\text{H} + \text{HO} \rightarrow \text{R}' \rightarrow \text{OH} + \text{HO} \rightarrow \text{R}'' \rightarrow \text{OH}$

Will the structure of the polymer produced in each of cases b, c, and d depend on the relative amounts of the reactants? If so, describe the differences.

2-5 Compare the molecular weight distributions that are expected for the polymerizations in Problems 2-3a, 2-4a, 2-4b, and 2-4c.
2-6 Discuss the possibility of cyclization in the polymerization of
a. $\text{H}_2\text{N}-(\text{CH}_2)_m\text{-CO}_2\text{H}$

b. $\text{HO}-(\text{CH}_2)_2\text{-OH} + \text{HO}_2\text{C}-(\text{CH}_2)_m\text{-CO}_2\text{H}$

for the cases where $m$ has values from 2 to 10? At what stage(s) in the reaction is cyclization possible? What factors determine whether cyclization or linear polymerization is the predominant reaction?

2-7 Show that the time required to go from $p = 0.98$ to $p = 0.99$ is very close to the time to reach $p = 0.98$ from the start of polymerization for the external acid-catalyzed polymerization of an equimolar mixture of a diol and diacid.

2-8 The polymerization between equimolar amounts of a diol and diacid proceeds with an equilibrium constant of 200. What will be the expected degree of polymerization and extent of reaction if the reaction is carried out in a closed system without removal of the by-product water? To what level must $[\text{H}_2\text{O}]$ be lowered in order to obtain a degree of polymerization of 200 if the initial concentration of carboxyl groups is 2 $M$?

2-9 A heat-resistant polymer *Nomex* has a number-average molecular weight of 24,116. Hydrolysis of the polymer yields 39.31% by weight $m$-aminoaniline, 59.81% terephthalic acid, and 0.88% benzoic acid. Write the formula for this polymer. Calculate the degree of polymerization and the extent of reaction. Calculate the effect on the degree of polymerization if the polymerization had been carried out with twice the amount of benzoic acid.

2-10 Calculate the number-average degree of polymerization of an equimolar mixture of adipic acid and hexamethylene diamine for extents of reaction 0.500, 0.800, 0.900, 0.950, 0.970, 0.990, 0.995.

2-11 Calculate the feed ratio of adipic acid and hexamethylene diamine that should be employed to obtain a polyamide of approximately 15,000 molecular weight at 99.5% conversion. What is the identity of the end groups of this product? Do the same calculation for a 19,000-molecular-weight polymer.

2-12 What proportion of benzoic acid should be used with an equimolar mixture of adipic acid and hexamethylene diamine to produce a polymer of 10,000 molecular weight at 99.5% conversion? Do the same calculation for 19,000 and 28,000 molecular weight products.

2-13 Calculate the extent of reaction at which gelation occurs for the following mixtures:

a. Phthalic anhydride and glycerol in stoichiometric amounts.
b. Phthalic anhydride and glycerol in the molar ratio 1.500 : 0.980
c. Phthalic anhydride, glycerol, and ethylene glycol in the molar ratio 1.500 : 0.990 : 0.002
d. Phthalic anhydride, glycerol, and ethylene glycol in the molar ratio 1.500 : 0.500 : 0.700

Compare the gel points calculated from the Carothers equation (and its modifications) with those using the statistical approach. Describe the effect of unequal functional groups reactivity (e.g., for the hydroxyl groups in glycerol) on the extent of reaction at the gel point.
2-14 Show by equations the polymerization of melamine and formaldehyde to form a crosslinked structure.

2-15 Describe by means of equations how random and block copolymers having the following compositions could be synthesized:

a. \[ \left( \text{CO} - \begin{array}{c} \text{(CH}_2\text{)}_3\text{NH} \\ \text{m} \end{array} \right) \left( \text{CO} - \begin{array}{c} \text{NH} \\ \text{m} \end{array} \right) \]

b. \[ \left( \text{CO} - \begin{array}{c} \text{CO}_2 - \text{(CH}_2\text{)}_2\text{O}_2\text{C - (CH}_2\text{)}_4\text{CO}_2 - \text{(CH}_2\text{)}_2\text{O} \\ \text{n} \end{array} \right) \]

2-16 How would you synthesize a block copolymer having segments of the following structures?

\[ \left( \text{CH}_3\text{CH}_2\text{CH}_2\text{O} \right) \text{m} \text{ and } \left( \text{O - CH}_2\text{CH}_2\text{OCONH} - \begin{array}{c} \text{CH}_3 \\ \text{NHCO} \end{array} \right) \text{p} \]

2-17 Distinguish between spiro, ladder, and semiladder polymers. Give examples of each.

2-18 Describe the difference between the convergent and divergent approaches to synthesizing dendrimers.

2-19 For each of the following reactions system indicate whether the product is a linear, branched, crosslinked, or hyperbranched polymer.

a. \( A_2 + B_2 \)

b. \( AB_2 \)

c. \( AB_3 \)

d. \( A_2 + B_3 \)

e. \( AB_2 + B_3 \)

f. \( AB + B_3 \)
CHAPTER 3

RADICAL CHAIN POLYMERIZATION

In the previous chapter, the synthesis of polymers by step polymerization was considered. Polymerization of unsaturated monomers by chain polymerization will be discussed in this and several of the subsequent chapters. Chain polymerization is initiated by a reactive species \( R^* \) produced from some compound \( I \) termed an *initiator*:

\[
I \xrightarrow{\text{initiator}} R^* \quad (3-1)
\]

The reactive species, which may be a free radical, cation, or anion, adds to a monomer molecule by opening the \( \pi \)-bond to form a new radical, cation, or anion center, as the case may be. The process is repeated as many more monomer molecules are successively added to continuously propagate the reactive center:

\[
\begin{align*}
R^* & \quad \text{CH}_2=\text{CHY} & R-\text{CH}_2-\text{CHY} & \quad \text{CH}_2=\text{CHY} & R-\text{CH}_2-\text{CH}_2-\text{CHY} & R^* \\
& \quad \text{CH}_2=\text{CHY} & R-\text{CH}_2-\text{C}^* & \quad \text{CH}_2=\text{C}^* & R-\text{CH}_2-\text{C}^* & R^* \\
& \quad \text{CH}_2=\text{C}^* & R-\text{CH}_2-\text{C}^* & \quad \text{CH}_2=\text{C}^* & R-\text{CH}_2-\text{C}^* & R^* \\
& \quad \text{CH}_2=\text{C}^* & R-\text{CH}_2-\text{C}^* & \quad \text{CH}_2=\text{C}^* & R-\text{CH}_2-\text{C}^* & R^* \\
\end{align*}
\]  

(3-2)

Polymer growth is terminated at some point by destruction of the reactive center by an appropriate reaction depending on the type of reactive center and the particular reaction conditions.

*Principles of Polymerization, Fourth Edition.* By George Odian
3-1 NATURE OF RADICAL CHAIN POLYMERIZATION

3-1a Comparison of Chain and Step Polymerizations

Chain polymerization proceeds by a distinctly different mechanism from step polymerization. The most significant difference is that high-molecular-weight polymer is formed immediately in a chain polymerization. A radical, anionic, or cationic reactive center, once produced, adds many monomer units in a chain reaction and grows rapidly to a large size. The monomer concentration decreases throughout the course of the reaction as the number of high-polymer molecules increases. At any instant the reaction mixture contains only monomer, high polymer, and the growing chains. The molecular weight of the polymer is relatively unchanged during the polymerization, although the overall percent conversion of monomer to polymer increases with reaction time.

The situation is quite different for a step polymerization. Whereas only monomer and the propagating species can react with each other in chain polymerization, any two molecular species present can react in step polymerization. Monomer disappears much faster in step polymerization as one proceeds to dimer, trimer, tetramer, and so on. The molecular weight increases throughout the course of the reaction, and high-molecular-weight polymer is not obtained until the end of the polymerization. Long reaction times are necessary for both high percent conversion and high molecular weights.

3-1b Radical versus Ionic Chain Polymerizations

3-1b-1 General Considerations of Polymerizability

Whether a particular monomer can be converted to polymer depends on both thermodynamic and kinetic considerations. The polymerization will be impossible under any and all reaction conditions if it does not pass the test of thermodynamic feasibility. Polymerization is possible only if the free-energy difference $\Delta G$ between monomer and polymer is negative (Sec. 3-9b). A negative $\Delta G$ does not, however, mean that polymerization will be observed under a particular set of reaction conditions (type of initiation, temperature, etc.). The ability to carry out a thermodynamically feasible polymerization depends on its kinetic feasibility—on whether the process proceeds at a reasonable rate under a proposed set of reaction conditions. Thus, whereas the polymerization of a wide variety of unsaturated monomers is thermodynamically feasible, very specific reaction conditions are often required to achieve kinetic feasibility in order to accomplish a particular polymerization.

Although radical, cationic, and anionic initiators are used in chain polymerizations, they cannot be used indiscriminately, since all three types of initiation do not work for all monomers. Monomers show varying degrees of selectivity with regard to the type of reactive center that will cause their polymerization. Most monomers will undergo polymerization with a radical initiator, although at varying rates. However, monomers show high selectivity toward ionic initiators. Some monomers may not polymerize with cationic initiators, while others may not polymerize with anionic initiators. The variety of behaviors can be seen in Table 3-1. The types of initiation that bring about the polymerization of various monomers to high-molecular-weight polymer are indicated. Thus, although the polymerization of all the monomers in Table 3-1 is thermodynamically feasible, kinetic feasibility is achieved in many cases only with a specific type of initiation.

The carbon–carbon double bond in vinyl monomers and the carbon–oxygen double bond in aldehydes and ketones are the two main types of linkages that undergo chain
polymerization. The polymerization of the carbon–carbon double bond is by far the most important of the two types of monomers. The carbonyl group is not prone to polymerization by radical initiators because of its polarized nature:

\[
\begin{align*}
\text{O} & \quad \text{C}^- & \quad \text{C}^+ \\
\end{align*}
\]

Aldehydes and ketones are polymerized by both anionic and cationic initiators (Chap. 5).

### 3-1b-2 Effects of Substituents

Unlike the carbonyl linkage, the carbon–carbon double bond undergoes polymerization by both radical and ionic initiators. The difference arises because the \(\pi\)-bond of a vinyl monomer can respond appropriately to the initiator species by either homolytic or heterolytic bond breakage:

\[
\begin{align*}
\text{O} & \quad \text{C}^- & \quad \text{C}^+ \\
\end{align*}
\]

A wide range of carbon–carbon double bonds undergo chain polymerization. Table 3-1 shows monomers with alkyl, alkenyl, aryl, halogen, alkoxy, ester, amide, nitrile, and heterocyclic substituents on the alkene double bond.

Whether a vinyl monomer polymerizes by radical, anionic, or cationic initiators depends on the inductive and resonance characteristics of the substituent(s) present. The effect of the

### Table 3-1 Types of Chain Polymerization Undergone by Various Unsaturated Monomers

<table>
<thead>
<tr>
<th>Monomers</th>
<th>Type of Initiation</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Radical</td>
</tr>
<tr>
<td>Ethylene</td>
<td>+</td>
</tr>
<tr>
<td>1-Alkyl alkenes ((\alpha)-olefins)</td>
<td>-</td>
</tr>
<tr>
<td>1,1-Dialkyl alkenes</td>
<td>-</td>
</tr>
<tr>
<td>1,3-Dienes</td>
<td>+</td>
</tr>
<tr>
<td>Styrene, (\alpha)-methyl styrene</td>
<td>+</td>
</tr>
<tr>
<td>Halogenated alkenes</td>
<td>+</td>
</tr>
<tr>
<td>Vinyl esters (CH(_2=\text{CHCOR}))</td>
<td>+</td>
</tr>
<tr>
<td>Acrylates, methacrylates</td>
<td>+</td>
</tr>
<tr>
<td>Acrylonitrile, methacrylonitrile</td>
<td>+</td>
</tr>
<tr>
<td>Acrylamide, methacrylamide</td>
<td>+</td>
</tr>
<tr>
<td>Vinyl ethers</td>
<td>-</td>
</tr>
<tr>
<td>(\alpha)-Vinyl carbazole</td>
<td>+</td>
</tr>
<tr>
<td>(\alpha)-Vinyl pyrrolidine</td>
<td>+</td>
</tr>
<tr>
<td>Aldehydes, ketones</td>
<td>-</td>
</tr>
</tbody>
</table>

\(^a\)Includes anionic coordination initiation (Chap. 8).
substituent manifests itself by its alteration of the electron-cloud density on the double bond and its ability to stabilize the possible radical, anion, or cation formed. Electron-donating substituents such as alkoxy, alkyl, alkenyl, and phenyl increase the electron density on the carbon–carbon double bond and facilitate its bonding to a cationic species. Further,

\[ \text{CH}_2=\text{CH} \quad \overset{\delta^{-}}{\longrightarrow} \quad \overset{\delta^{+}}{Y} \]

these substituents stabilize the cationic propagating species by resonance, for example, in the polymerization of vinyl ethers:

\[ \text{H} \quad \overset{\mathrm{CH}_2}{\mathrm{C}^+} \quad \overset{\mathrm{CH}_2}{\mathrm{C}^+} \quad \overset{\mathrm{CH}_2}{\mathrm{C}^+} \quad \overset{\mathrm{CH}_2}{\mathrm{C}^+} \quad (3-5a) \]

The alkoxy substituent allows a delocalization of the positive charge. If the substituent were not present (e.g., in ethylene), the positive charge would be localized on the single \( \alpha \)-carbon atom. The presence of the alkoxy group leads to stabilization of the carbocation by delocalization of the positive charge over two atoms—the carbon and the oxygen. Similar delocalization effects occur with phenyl, vinyl, and alkyl substituents, for example, for styrene polymerization:

\[ \text{H} \quad \overset{\mathrm{CH}_2}{\mathrm{C}^+} \quad \overset{\mathrm{CH}_2}{\mathrm{C}^+} \quad \overset{\mathrm{CH}_2}{\mathrm{C}^+} \quad \overset{\mathrm{CH}_2}{\mathrm{C}^+} \quad \overset{\mathrm{CH}_2}{\mathrm{C}^+} \quad (3-5b) \]

Thus monomers such as isobutylene, styrene, methyl vinyl ether, and isoprene undergo polymerization by cationic initiators. The effect of alkyl groups in facilitating cationic polymerization is weak, and it is only the 1,1-dialkyl alkenes that undergo cationic polymerization.

Electron-withdrawing substituents such as cyano and carbonyl (aldehyde, ketone, acid, or ester) facilitate the attack of an anionic species by decreasing the electron density on the double bond:

\[ \text{CH}_2=\text{CH} \quad \overset{\delta^{+}}{\longrightarrow} \quad \overset{\delta^{-}}{Y} \]

They stabilize the propagating anionic species by resonance, for example, for acrylonitrile polymerization:

\[ \text{H} \quad \overset{\mathrm{CH}_2}{\mathrm{C}^-} \quad \overset{\mathrm{CH}_2}{\mathrm{C}^-} \quad \overset{\mathrm{CH}_2}{\mathrm{C}^-} \quad \overset{\mathrm{CH}_2}{\mathrm{C}^-} \quad (3-6) \]
Stabilization of the propagating carbanion occurs by delocalization of the negative charge over the \(\alpha\)-carbon and the nitrogen of the nitrile group. Alkenyl and phenyl substituents, although electron-withdrawing inductively, can resonance stabilize the anionic propagating species in the same manner as a cyano group. Monomers such as styrene and 1,3-butadiene can, therefore, undergo anionic as well as cationic polymerization. Halogens withdraw electrons inductively and push electrons by resonance, but both effects are relatively weak and neither anionic nor cationic polymerization is appreciably facilitated for halogenated monomers such as vinyl chloride.

Contrary to the high selectivity shown in cationic and anionic polymerization, radical initiators bring about the polymerization of almost any carbon–carbon double bond. Radical species are neutral and do not have stringent requirements for attacking the \(\pi\)-bond or for the stabilization of the propagating radical species. Resonance stabilization of the propagating radical occurs with almost all substituents, for example

\[
\begin{align*}
\text{CH}_2\text{C} \equiv \text{CH} \quad & \leftrightarrow \quad \text{CH}_2\text{C} \equiv \text{C} \\
\text{CH}_2\text{C} \equiv \text{C} \quad & \leftrightarrow \quad \text{CH}_2\text{C} \equiv \text{C} \quad \text{CH}_2\text{C} \equiv \text{C} \\
\text{CH}_2\text{C} \equiv \text{C} \quad & \leftrightarrow \quad \text{CH}_2\text{C} \equiv \text{C} \\
\end{align*}
\]

Thus, almost all substituents are able to stabilize the propagating radical by delocalization of the radical over two or more atoms. The remainder of this chapter will be concerned with the detailed characteristics of radical chain polymerization. Ionic chain polymerizations will be considered in Chap. 5.

### 3-2 STRUCTURAL ARRANGEMENT OF MONOMER UNITS

#### 3-2a Possible Modes of Propagation

There are two possible points of attachment on monosubstituted (\(X = H\)) or 1,1-disubstituted monomers for a propagating radical—on either carbon 1

\[
\begin{align*}
\text{R} \cdot + \text{C} = \text{CH}_2 & \rightarrow \text{R} - \text{C} = \text{CH}_2 \cdot \\
\end{align*}
\]
If each successive addition of monomer molecules to the propagating radical occurs in the same manner as Eq. 3-9 or Eq. 3-8, the final polymer product will have an arrangement of monomer units in which the substituents are on alternate carbon atoms:

\[
\begin{align*}
&\text{CH}_2\text{C} - \text{CH}_2\text{C} - \text{CH}_2\text{C} - \text{CH}_2\text{C} - \text{CH}_2\text{C} - \text{CH}_2\text{C} - \text{CH}_2\text{C} - \\
&\quad \text{Y} \quad \text{Y} \quad \text{Y} \quad \text{Y} \quad \text{Y} \quad \text{Y}
\end{align*}
\]

This type of arrangement (III) is usually referred to as a head-to-tail (H-T) or 1,3-placement of monomer units. An inversion of this mode of addition by the polymer chain propagating alternately via Eqs. 3-9 and 3-8 would lead to a polymer structure with a 1,2-placement of substituents at one or more places in the final polymer chain. 1,2-Placement is usually referred to as head-to-head (H-H) placement.

The head-to-tail placement would be expected to be overwhelmingly predominant, since successive propagations by Eq. 3-9 are favored on both steric and resonance grounds. The propagating radical (radical II) formed by attachment of a radical at carbon 2 is the more stable one. Radical II can be stabilized by the resonance effects of the X and Y substituents. The substituents cannot stabilize radical I, since they are not attached to the carbon bearing the unpaired electron. Further, the approach (and subsequent attachment) of a propagating radical at the unsubstituted carbon (carbon 2) of a monomer molecule is much less sterically hindered compared to the approach at the substituted carbon (carbon 1). A propagation proceeding with predominantly H-T placement is a regioselective process, that is, one orientation (H–T) is favored over another (H–H). The term isoregic has been used to indicate a polymer structure with exclusive head-to-tail placements. The terms syndioregic and aregic would be used for polymer structures with alternating and random arrangements, respectively, of H–T and H–H placements.

3-2b Experimental Evidence

These theoretical predictions have been experimentally verified for a number of polymers. The presence of no more than 1–2% head-to-head placement in various polymers of vinyl
esters such as poly(vinyl acetate) has been determined by hydrolysis of the polymer to poly(vinyl alcohol) and the periodate oxidation of the 1,2-glycol units [Hayashi and Ostu, 1969].

\[
\text{CH}_2=\text{CH}-(\text{OH})_2 \xrightarrow{\text{IO}_4^-} \text{CH}_2=\text{CH} + \text{O}-(\text{OH})_2
\] (3-10)

Although appropriate chemical reactions do not exist to detect the occurrence of head-to-head propagation in all but a few polymers, the use of high-resolution nuclear magnetic resonance spectroscopy (including \(^1\text{H}, ^{13}\text{C}, \text{and} ^{19}\text{F}\)) has greatly increased our knowledge in this area [Bovey and Mirau, 1996; Bovey et al., 1977]. It is now clear that H–T propagation is the predominant (>98–99%) mode of propagation in chain polymerization. For some polymers such as polystyrene there is no detectable H–H placement (Hensley et al., 1995). The only exceptions occur when the substituents on the double bond are small (and do not offer appreciable steric hindrance to the approaching radical) and do not have a significant resonance-stabilizing effect, specifically when fluorine is the substituent. Thus, the extents of H–H placements in poly(vinyl fluoride), poly(vinylidene fluoride), poly(trifluoroethylene), and poly(chlorotrifluoroethylene) are about 10, 5, 12, and 2%, respectively [Cais and Kometani, 1984, 1988; Guiot et al., 2002; Ovenall and Uschold, 1991].

The effect of increasing the polymerization temperature is an increase in the extent of H–H placement, but the effect is small. Thus the H–H content in poly(vinyl acetate) increases from 1 to 2% when the temperature is increased from 40 to 100°C; the increase is from 10 to 14% for poly(trifluoroethylene) when the temperature is increased from –80 to 80°C.

### 3-2c Synthesis of Head-to-Head Polymers

Some polymers consisting entirely of head-to-head placements have been deliberately synthesized to determine if significant property differences exist compared to the head-to-tail polymers. The synthetic approach involves an appropriate choice of monomer for the particular H–H polymer. For example, H–H poly(vinyl chloride) is obtained by chlorination of 1,4-poly-1,3-butadiene,

\[
\begin{align*}
\text{CH}_2=\text{CH}=(\text{CH}_2)_n + & \text{Cl}_2 \rightarrow \text{CH}_2=\text{CH}(\text{Cl})_n \\
\end{align*}
\] (3-11)

and H–H polystyrene by hydrogenation of 1,4-poly-2,3-diphenylbutadiene,

\[
\begin{align*}
\text{CH}_2=\text{C}=(\text{C}_\phi \text{C}_\phi)_n + & \text{H}_2 \rightarrow \text{CH}_2=\text{C}(\text{C}_\phi \text{C}_\phi)_n \\
\end{align*}
\] (3-12)

[Kawaguchi et al., 1985; Vogl; 2000; Vogl et al., 1999].

### 3-3 RATE OF RADICAL CHAIN POLYMERIZATION

#### 3-3a Sequence of Events

Radical chain polymerization is a chain reaction consisting of a sequence of three steps—initiation, propagation, and termination. The initiation step is considered to involve two
reactions. The first is the production of free radicals by any one of a number of reactions. The usual case is the homolytic dissociation of an initiator species \( I \) to yield a pair of radicals \( R^\cdot \)

\[
I \xrightarrow{k_d} 2R^\cdot
\]  

(3-13)

where \( k_d \) is the rate constant for the catalyst dissociation. The second part of the initiation involves the addition of this radical to the first monomer molecule to produce the chain-initiating radical \( M_1^\cdot \)

\[
R^\cdot + M \xrightarrow{k_i} M_1^\cdot
\]  

(3-14a)

where \( M \) represents a monomer molecule and \( k_i \) is the rate constant for the initiation step (Eq. 3-14a). For the polymerization of \( CH_2=CHY \), Eq. 3-14a takes the form

\[
R^\cdot + CH_2=CHY \xrightarrow{H, Y} RCH_2CHY^\cdot
\]  

(3-14b)

The radical \( R^\cdot \) is often referred to as an initiator radical or primary radical to distinguish it from the chain-initiating species \( (M_1^\cdot) \).

Propagation consists of the growth of \( M_1^\cdot \) by the successive additions of large numbers (hundreds and perhaps thousands) of monomer molecules according to Eq. 3-2. Each addition creates a new radical that has the same identity as the one previously, except that it is larger by one monomer unit. The successive additions may be represented by

\[
M_1^\cdot + M \xrightarrow{k_p} M_2^\cdot
\]  

(3-15a)

\[
M_2^\cdot + M \xrightarrow{k_p} M_3^\cdot
\]  

(3-15b)

\[
M_3^\cdot + M \xrightarrow{k_p} M_4^\cdot
\]  

(3-15c)

e tc., etc.

or in general terms

\[
M_n^\cdot + M \xrightarrow{k_p} M_{n+1}^\cdot
\]  

(3-15d)

where \( k_p \) is the rate constant for propagation. Propagation with growth of the chain to high-polymer proportions takes place very rapidly. The value of \( k_p \) for most monomers is in the range \( 10^2 \text{--} 10^4 \text{ L mol}^{-1} \text{ s}^{-1} \). This is a large rate constant—much larger than those usually encountered in step polymerizations (see Table 2-8).

At some point, the propagating polymer chain stops growing and terminates. Termination with the annihilation of the radical centers occurs by bimolecular reaction between radicals. Two radicals react with each other by combination (coupling) or, more rarely, by disproportionation, in which a hydrogen radical that is beta to one radical center is transferred to another radical center. This results in the formation of two polymer molecules—
one saturated and one unsaturated:

\[
\text{Termination can also occur by a combination of coupling and disproportionation. The two different modes of termination can be represented in general terms by}
\]

\[
M_n \cdot + M_m \cdot \xrightarrow{k_{tc}} M_{n+m}
\]

\[
M_n \cdot + M_m \cdot \xrightarrow{k_{td}} M_n + M_m
\]

where \(k_{tc}\) and \(k_{td}\) are the rate constants for termination by coupling and disproportionation, respectively. One can also express the termination step by

\[
M_n \cdot + M_m \cdot \xrightarrow{k_t} \text{dead polymer}
\]

where the particular mode of termination is not specified and

\[
k_t = ak_{tc} + (1 - a)k_{td}
\]

where \(a\) and \((1 - a)\) are the fractions of termination by coupling and disproportionation, respectively.

The term “dead polymer” signifies the cessation of growth for the propagating radical. The propagation reaction would proceed indefinitely until all the monomer in a reaction system were exhausted if it were not for the strong tendency toward termination. Typical termination rate constants are in the range of \(10^6\)–\(10^8\) L mol\(^{-1}\) s\(^{-1}\) or orders of magnitude greater than the propagation rate constants. The much greater value of \(k_t\) (whether \(k_{tc}\) or \(k_{td}\)) compared to \(k_p\) does not prevent propagation because the radical species are present in very low concentrations and because the polymerization rate is dependent on only the one-half power of \(k_t\) (as will be discussed in Sec. 3-4a-2). (Polymerizations with little or no termination occur under special conditions—Sec. 3-15).

### 3-3b Rate Expression

Equations 3-13 through 3-19 constitute the detailed mechanism of a free-radical-initiated chain polymerization. The chain nature of the process resides in the propagation step (Eq. 3-15) in which large numbers of monomer molecules are converted to polymer for each initiating radical produced in the first step (Eq. 3-14). In order to obtain a kinetic expression for the rate of polymerization, it is necessary to assume that \(k_p\) and \(k_t\) are independent of the size of the radical. This assumption is inherent in the notation used in Eqs. 3-15 through 3-18. It is exactly the same assumption—the equal-reactivity assumption—that was employed in deriving the kinetics of step polymerization. Very small radicals are more reactive than propagating radicals, but this effect is not important because the effect of size vanishes at the dimer or trimer size [Gridnev and Ittel, 1996; Kerr, 1973]. There are limitations to the equal-reactivity assumption with respect to the sizes of propagating radicals, and this is discussed in Secs. 3-10 and 3-11b.
Monomer disappears by the initiation reaction (Eq. 3-14) as well as by the propagation reactions (Eq. 3-15). The rate of monomer disappearance, which is synonymous with the rate of polymerization, is given by

$$\frac{-d[M]}{dt} = R_i + R_p$$  

(3-20)

where $R_i$ and $R_p$ are the rates of initiation and propagation, respectively. However, the number of monomer molecules reacting in the initiation step is far less than the number in the propagation step for a process producing high polymer. To a very close approximation the former can be neglected and the polymerization rate is given simply by the rate of propagation

$$\frac{-d[M]}{dt} = R_p$$  

(3-21)

The rate of propagation, and therefore the rate of polymerization, is the sum of many individual propagation steps. Since the rate constants for all the propagation steps are the same, one can express the polymerization rate by

$$R_p = k_p[M_r][M]$$  

(3-22)

where [M] is the monomer concentration and [M_r] is the total concentration of all chain radicals, that is, all radicals of size $M_1^*$ and larger.

Equation 3-22 for the polymerization rate is not directly usable because it contains a term for the concentration of radicals. Radical concentrations are difficult to measure quantitatively, since they are very low ($\sim 10^{-8} M$), and it is therefore desirable to eliminate [M_r] from Eq. 3-22. In order to do this, the steady-state assumption is made that the concentration of radicals increases initially, but almost instantaneously reaches a constant, steady-state value. The rate of change of the concentration of radicals quickly becomes and remains zero during the course of the polymerization. This is equivalent to stating that the rates of initiation $R_i$ and termination $R_t$ of radicals are equal or

$$R_i = R_t = 2k_t[M_r]^2$$  

(3-23)

The steady-state assumption is not unique to polymerization kinetics. It is often used in developing the kinetics of many small-molecule reactions that involve highly reactive intermediates present at very low concentrations—conditions that are present in radical chain polymerizations. The theoretical validity of the steady-state assumption has been discussed [Kondratiev, 1969] and its experimental validity shown in many polymerizations. Typical polymerizations achieve a steady-state after a period, which may be at most a minute.

The right side of Eq. 3-23 represents the rate of termination. There is no specification as to whether termination is by coupling or disproportionation since both follow the same kinetic expression. The use of the factor of 2 in the termination rate equation follows the generally accepted convention for reactions destroying radicals in pairs. It is also generally used for reactions creating radicals in pairs as in Eq. 3-13. This convention is now the IUPAC-preferred convention. In using the polymer literature, one should be aware that the factor of 2 has not always been followed. Rearrangement of Eq. 3-23 to

$$[M_r] = \left(\frac{R_t}{2k_t}\right)^{1/2}$$  

(3-24)
and substitution into Eq. 3-22 yields

\[ R_p = k_p[M]\left(\frac{R_i}{2k_t}\right)^{1/2} \]  \hspace{1cm} (3-25)

for the rate of polymerization. It is seen that Eq. 3-25 has the significant conclusion of the dependence of the polymerization rate on the square root of the initiation rate. Doubling the rate of initiation does not double the polymerization rate; the polymerization rate is increased only by the factor \( \sqrt{2} \). This behavior is a consequence of the bimolecular termination reaction between radicals.

### 3-3c Experimental Determination of \( R_p \)

It is appropriate at this point to briefly discuss the experimental procedures used to determine polymerization rates for both step and radical chain polymerizations. \( R_p \) can be experimentally followed by measuring the change in any property that differs for the monomer(s) and polymer, for example, solubility, density, refractive index, and spectral absorption [Collins et al., 1973; Giz et al., 2001; McCaffery, 1970; Stickler, 1987; Yamazoe et al., 2001].

Some techniques are equally useful for step and chain polymerizations, while others are more appropriate for only one or the other. Techniques useful for radical chain polymerizations are generally applicable to ionic chain polymerizations. The utility of any particular technique also depends on its precision and accuracy at low, medium, and high percentages of conversion. Some of the techniques have the inherent advantage of not needing to stop the polymerization to determine the percent conversion, that is, conversion can be followed versus time on the same reaction sample.

#### 3-3c-1 Physical Separation and Isolation of Reaction Product

This technique involves isolating (followed by drying and weighing) the polymer from aliquots of the polymerization system as a function of reaction time. Polymer is typically isolated by precipitation by addition of a nonsolvent. The technique is primarily useful for chain polymerizations, which consist of monomer and high-molecular-weight polymer, differing greatly in their solubility. It is not generally useful for step polymerization, since they consist of monomers and a range of different low-molecular-weight products (until very high conversions) whose solubility differences are typically not too different. Even when applicable, the technique is very time-consuming and requires great care to obtain accurate results.

A modification of this technique, applicable to many step polymerizations, involves the continuous monitoring of the small-molecule by-product. For example, for polyesterification between a diol and diacid above 100°C, water distills out of the reaction vessel and its volume can be measured by condensation and collection in a calibrated trap.

#### 3-3c-2 Chemical and Spectroscopic Analysis

Chemical analysis of the unreacted monomer functional groups as a function of time is useful for step polymerizations. For example, polyesterification can be followed accurately by titration of the carboxyl group concentration with standard base or analysis of hydroxyl groups by reaction with acetic anhydride. The rate of chain polymerization of vinyl monomers can be followed by titration of the unreacted double bonds with bromine.
The disappearance of monomer or appearance of polymer can be followed by infrared (IR), ultraviolet (UV), and nuclear magnetic resonance (NMR) and other spectroscopies. One can follow the decrease in absorption signal(s) due to monomer and/or increase in absorption signal(s) due to polymer. For example, for styrene polymerization, proton NMR signals characteristic of the monomer, which decrease with conversion, include signals for the CH2=CH protons (5.23, 5.73, and 6.71 ppm); simultaneously, signals characteristic of the CH2 and CH protons of polymer appear at 1.44 and 1.84 ppm, respectively. The accuracy of the spectroscopic technique is high when the monomer and polymer signals do not overlap. Spectroscopy allows the continuous monitoring of a polymerization without periodic sample removal for analysis. The polymerization is performed in a sample tube placed in the spectrometer and equilibrated at the desired reaction temperature [Aquilar et al., 2002]. Periodic spectral analysis allows one to follow conversion versus time. More elaborate instrumentation allows the simultaneous analysis of conversion and molecular weight versus time [Chauvin et al., 2002; Grassl and Reed, 2002].

3-3c-3 Other Techniques

Dilatometry utilizes the volume change that occurs on polymerization. It is an accurate method for some chain polymerizations because there is often a high-volume shrinkage when monomer is converted to polymer. For example, the density of poly(methyl methacrylate) is 20.6% lower than that of its monomer. Polymerization is carried out in a calibrated reaction vessel and the volume recorded as a function of reaction time. Dilatometry is not useful for the usual step polymerization where there is a small molecule by-product that results in no significant volume change on polymerization.

The heat of polymerization can be measured accurately by differential scanning calorimetry and is directly related to conversion. Other techniques that have been used include light scattering and refractive index.

3-4 INITIATION

The derivation of Eq. 3-25 is general in that the reaction for the production of radicals (Eq. 3-13) is not specified and the initiation rate is simply shown as $R_i$. A variety of initiator systems can be used to bring about the polymerization. (The term catalyst is often used synonymously with initiator, but it is incorrect in the classical sense, since the initiator is consumed. The use of the term catalyst may be condensed since very large numbers of monomer molecules are converted to polymer for each initiator molecule that is consumed.) Radicals can be produced by a variety of thermal, photochemical, and redox methods [Bamford, 1988; Denisova et al., 2003; Eastmond, 1976a,b,c; Moad et al., 2002]. In order to function as a useful source of radicals an initiator system should be readily available, stable under ambient or refrigerated conditions, and possess a practical rate of radical generation at temperatures which are not excessive (approximately $<150^\circ$C).

3-4a Thermal Decomposition of Initiators

3-4a-1 Types of Initiators

The thermal, homolytic dissociation of initiators is the most widely used mode of generating radicals to initiate polymerization—for both commercial polymerizations and theoretical studies. Polymerizations initiated in this manner are often referred to as thermal initiated or...
thermal catalyzed polymerizations. The number of different types of compounds that can be used as thermal initiators is rather limited. One is usually limited to compounds with bond dissociation energies in the range 100–170 kJ mol$^{-1}$. Compounds with higher or lower dissociation energies will dissociate too slowly or too rapidly. Only a few classes of compounds—including those with O–O, S–S, or N–O bonds—possess the desired range of dissociation energies. However, it is the peroxides which find extensive use as radical sources. The other classes of compounds are usually either not readily available or not stable enough. Several different types of peroxy compounds are widely used [Sheppard, 1988]. These are acyl peroxides such as acetyl and benzoyl peroxides

\[
\begin{align*}
\text{CH}_3\text{C}=\text{O} & \quad \rightarrow \quad \text{CH}_3\text{C}^\bullet \text{O}, \\
\text{O} & \quad \phi\text{C}=\text{O} \quad \rightarrow \quad 2\phi\text{C}^\bullet \text{O}.
\end{align*}
\]

alkyl peroxides such as cumyl and tert-butyl peroxides

\[
\begin{align*}
\text{CH}_3 & \quad \phi\text{C}=\text{O} \quad \rightarrow \quad 2\phi\text{C}^\bullet \text{O}, \\
\text{CH}_3 & \quad \phi\text{C}=\text{O} \quad \rightarrow \quad 2\phi\text{C}^\bullet \text{O}.
\end{align*}
\]

hydroperoxides such as tert-butyl and cumyl hydroperoxides

\[
\begin{align*}
\text{CH}_3 & \quad \phi\text{C}=\text{O} \quad \rightarrow \quad 2\phi\text{C}^\bullet \text{O}, \\
\text{CH}_3 & \quad \phi\text{C}=\text{O} \quad \rightarrow \quad 2\phi\text{C}^\bullet \text{O}.
\end{align*}
\]

and peresters such as tert-butyl perbenzoate:

\[
\begin{align*}
\text{O} & \quad \phi\text{C}=\text{O} \quad \rightarrow \quad \phi\text{C}^\bullet \text{O}, \\
\text{O} & \quad \phi\text{C}=\text{O} \quad \rightarrow \quad \phi\text{C}^\bullet \text{O}.
\end{align*}
\]

Other peroxides used to initiate polymerization are acyl alkylsulfonyl peroxides (Va), dialkyl peroxydicarbonates (Vb), diperoxyketals (Vc), and ketone peroxides (Vd).

\[
\begin{align*}
\text{R}\text{SO}_2\text{O} & \quad \text{O} \quad \text{R} \quad \rightarrow \quad \text{RO} \quad \text{O} \quad \text{C}-\text{O} \quad \text{C}-\text{O} \quad \text{R} \quad \text{R} \quad \text{C}(\text{OOH})_2 \\
\text{Va} & \quad \text{Vb} & \quad \text{Vc} & \quad \text{Vd}
\end{align*}
\]
Aside from the various peroxy compounds, the main other class of compound used extensively as initiators are the azo compounds. 2,2′-Azobisisobutyronitrile (AIBN) is the most important member of this class of initiators, although other azo compounds such as

\[
\begin{align*}
\text{CH}_3 - \text{C} = \text{N} = \text{N} - \text{C} - \text{CH}_3 & \quad \rightarrow \quad 2 \text{CH}_3 - \text{C} \cdot + \text{N}_2 \\
\text{CN} & \quad \text{CN} & \quad \text{CN} & \quad \text{CN} & \quad \text{CN} & \quad \text{CN} & \quad \text{CN}
\end{align*}
\]

(3-26h)

2,2′-azobis(2,4-dimethylpentanenitrile), 4,4′-azobis(4-cyanovaleric acid), and 1,1′-azobis(cyclohexanecarbonitrile) are also used [Sheppard, 1985]. The facile dissociation of azo compounds is not due to the presence of a weak bond as is the case for the peroxy compounds. The C–N bond dissociation energy is high (~290 kJ mol⁻¹), but the driving force for homolysis is the formation of the highly stable nitrogen molecule.

Among other initiators that have been studied are disulfides

\[
\text{RS} - \text{SR} \quad \rightarrow \quad 2\text{RS} \cdot
\]

(3-26i)

and tetrazenes

\[
\text{R}_2\text{N} - \text{N} = \text{N} - \text{NR}_2 \quad \rightarrow \quad 2\text{R}_2\text{N} \cdot + \text{N}_2
\]

(3-26j)

[Oda et al., 1978; Sato et al., 1979a, b].

The various initiators are used at different temperatures depending on their rates of decomposition. Thus azobisisobutyronitrile (AIBN) is commonly used at 50–70°C, acetyl peroxide at 70–90°C, benzoyl peroxide at 80–95°C, and dicumyl or di-t-butyl peroxide at 120–140°C. The value of the decomposition rate constant \( k_d \) varies in the range \( 10^{-4} - 10^{-9} \text{ s}^{-1} \) depending on the initiator and temperature [Eastmond, 1976a, b, c]. Most initiators are used at temperatures where \( k_d \) is usually \( 10^{-4} - 10^{-6} \text{ s}^{-1} \). The great utility of peroxide and azo compounds results from the availability in stable form of many different compounds with a range of use temperatures.

The differences in the rates of decomposition of the various initiators are related to differences in the structures of the initiators and of the radicals produced. The effects of structure on initiator reactivity have been discussed elsewhere [Bamford, 1988; Eastmond, 1976a, b, c; Sheppard, 1985, 1988]. For example, \( k_d \) is larger for acyl peroxides than for alkyl peroxides since the RCOO· radical is more stable than the RO· radical and for R=N=N=R, \( k_d \) increases in the order R = allyl, benzyl > tertiary > secondary > primary [Koenig, 1973].

The differences in the decomposition rates of various initiators can be conveniently expressed in terms of the initiator half-life \( t_{1/2} \) defined as the time for the concentration of I to decrease to one half its original value. The rate of initiator disappearance by Eq. 3-13 is

\[
-\frac{d[I]}{dt} = k_d[I]
\]

(3-27)

which on integration yields

\[
[I] = [I]_0 e^{-k_d t}
\]

(3-28a)

or

\[
\ln \frac{[I]_0}{[I]} = k_d t
\]

(3-28b)
where \([I]_0\) is the initiator concentration at the start of polymerization. \(t_{1/2}\) is obtained as
\[
 t_{1/2} = \frac{0.693}{k_d} 
\]  
(3-29)

by setting \([I] = [I]_0/2\). Table 3-2 lists the initiator half-lives for several common initiators at various temperatures.

### 3-4a-2 Kinetics of Initiation and Polymerization

The rate of producing primary radicals by thermal homolysis of an initiator \(R_d\) (Eqs. 3-13 and 3-26) is given by
\[
 R_d = 2f k_d[I] 
\]  
(3-30)

where \([I]\) is the concentration of the initiator and \(f\) is the **initiator efficiency**. The initiator efficiency is defined as the fraction of the radicals produced in the homolysis reaction that initiate polymer chains. The value of \(f\) is usually less than unity due to wastage reactions. The factor of 2 in Eq. 3-30 follows the convention previously discussed for Eq. 3-23.

The initiation reaction in polymerization is composed of two steps (Eqs. 3-13 and 3-14) as discussed previously. In most polymerizations, the second step (the addition of the primary radical to monomer) is much faster than the first step. The homolysis of the initiator is the rate-determining step in the initiation sequence, and the rate of initiation is then given by
\[
 R_i = 2f k_d[I] 
\]  
(3-31)

Substitution of Eq. 3-31 into Eq. 3-25 yields
\[
 R_p = k_p[M] \left( \frac{k_d[I]}{k_i} \right)^{1/2} 
\]  
(3-32)

### 3-4a-3 Dependence of Polymerization Rate on Initiator

Equation 3-32 describes the most common case of radical chain polymerization. It shows the polymerization rate to be dependent on the square root of the initiator concentration. This

---

**TABLE 3-2 Half-Lives of Initiators**

<table>
<thead>
<tr>
<th>Initiator</th>
<th>50°C</th>
<th>70°C</th>
<th>85°C</th>
<th>100°C</th>
<th>130°C</th>
<th>175°C</th>
</tr>
</thead>
<tbody>
<tr>
<td>Azobisisobutyronitrile</td>
<td>74 h</td>
<td>4.8 h</td>
<td>—</td>
<td>7.2 min</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td>Benzoyl peroxide</td>
<td>—</td>
<td>7.3 h</td>
<td>1.4 h</td>
<td>20 min</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td>Acetyl peroxide</td>
<td>158 h</td>
<td>8.1 h</td>
<td>1.1 h</td>
<td>—</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td>t-Butyl peracetate</td>
<td>—</td>
<td>—</td>
<td>88 h</td>
<td>13 h</td>
<td>18 min</td>
<td>—</td>
</tr>
<tr>
<td>Cumyl peroxide</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>1.7 h</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td>t-Butyl peroxide</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>218 h</td>
<td>6.4 h</td>
<td>—</td>
</tr>
<tr>
<td>t-Butyl hydroperoxide</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>338 h</td>
<td>—</td>
<td>4.81 h</td>
</tr>
</tbody>
</table>

*a Data from Brandrup and Immergut [1989], Brandrup et al. [1999], and Huyser [1970].

*b Half-life \((t_{1/2})\) values are for benzene or toluene solutions of the initiators.*
dependence has been abundantly confirmed for many different monomer–initiator combinations over wide ranges of monomer and initiator concentrations [Eastmond, 1976a,b,c; Kamachi et al., 1978; Santee et al., 1964; Schulz and Blaschke, 1942; Vrancken and Smets, 1959]. Figure 3-1 shows typical data illustrating the square-root dependence on [I]. Deviations from this behavior are found under certain conditions. The order of dependence of $R_p$ on [I] may be observed to be less than one-half at very high initiator concentrations. However, such an effect is not truly a deviation from Eq. 3-32. It may be due to a decrease in $f$ with increasing initiator concentration (Sec. 3-4g-2).

Fig. 3-1  Square root dependence of the polymerization rate $R_p$ on the initiator concentration [I]. ● = Methyl methacrylate, benzoyl peroxide, 50°C. After Schulz and Blaschke [1942] (by permission of Akademische Verlagsgesellschaft, Geest and Portig K.-G., Leipzig). ○, ● = Vinyl benzoate, azobisisobutyronitrile, 60°C. After Santee et al. [1964] and Vrancken and Smets [1959] (by permission of Huthig and Wepf Verlag, Basel and Wiley-VCH, Weinheim).
Alternately, the termination mode may change from the normal bimolecular termination between propagating radicals to primary termination, which involves propagating radicals reacting with primary radicals [Berger et al., 1977; David et al., 2001; Ito, 1980]:

$$M_n \cdot + R \cdot \stackrel{k_{tp}}{\rightarrow} M_n-R$$  \hspace{1cm} (3-33a)

This occurs if primary radicals are produced at too high a concentration and/or in the presence of too low a monomer concentration to be completely and rapidly scavenged by monomer (by Eq. 3-14a). If termination occurs exclusively by primary termination, the polymerization rate is given by

$$R_p = \frac{k_pk_i[M]^2}{k_{tp}}$$  \hspace{1cm} (3-33b)

Eq. 3-33b, derived by combining the rate expressions for Eqs. 3-14a, 3-15d, and 3-33a, shows that the polymerization rate becomes independent of the initiator concentration (but not $k_i$) and second-order in monomer concentration.

Primary termination and the accompanying change in the order of dependence of $R_p$ on [I] may also be found in the Trommsdorff polymerization region (Sec. 3-10). Situations also arise where the order of dependence of $R_p$ on [I] will be greater than one-half. This behavior may be observed in the Trommsdorff region if the polymer radicals do not undergo termination or under certain conditions of chain transfer or inhibition (Sec. 3-7).

Lower than one-half order dependence of $R_p$ on $[R_i]$ is also expected if one of the two primary radicals formed by initiator decomposition has low reactivity for initiation, but is still active in termination of propagating radicals. Modeling this situation indicates that the dependence of $R_p$ on $R_i$ becomes one-third order in the extreme of this situation where one of the primary radicals has no reactivity toward initiation, but still active for termination [Kaminsky et al., 2002].

### 3-4a-4 Dependence of Polymerization Rate on Monomer

The rate expression Eq. 3-32 requires a first-order dependence of the polymerization rate on the monomer concentration and is observed for many polymerizations [Kamachi et al., 1978]. Figure 3-2 shows the first-order relationship for the polymerization of methyl methacrylate [Sugimura and Minoura, 1966]. However, there are many polymerizations where $R_p$ shows a higher than first-order dependence on [M]. Thus the rate of polymerization depends on the $\frac{3}{2}$-power of the monomer concentration in the polymerization of styrene in chlorobenzene solution at 120°C initiated by $t$-butyl peresters [Misra and Mathiu, 1967]. The benzoyl peroxide initiated polymerization of styrene in toluene at 80°C shows an increasing order of dependence of $R_p$ on [M] as [M] decreases [Horikx and Hermans, 1953]. The dependence is 1.18-order at $[M] = 1.8$ and increases to 1.36-order at $[M] = 0.4$. These effects may be caused by a dependence of the initiation rate on the monomer concentration. Equation 3-28 was derived on the assumption that $R_i$ is independent of [M]. The initiation rate can be monomer-dependent in several ways. The initiator efficiency $f$ may vary directly with the monomer concentration

$$f = f'[M]$$  \hspace{1cm} (3-34)

which would lead (by substitution of Eq. 3-34 into Eqs. 3-31 and 3-32) to first-order dependence of $R_i$ on [M] and $\frac{3}{2}$-order dependence of $R_p$ on [M]. (This effect has been observed and
is discussed in Sec. 3-4f.) The equivalent result arises if the second step of the initiation reaction (Eq. 3-14) were to become the rate-determining step instead of the first step (Eq. 3-13). This occurs when \( k_d > k_i \) or when \([M]\) is low. It is also frequently encountered in polymerizations initiated photolytically or by ionizing radiation (Secs. 3-4c and 3-4d) and in some redox-initiated polymerizations (Sec. 3-4b).

In some systems it appears that the initiation step differs from the usual two-step sequence of Eqs. 3-13 and 3-14. Thus in the \( t \)-butyl hydroperoxide-styrene system only a minor part of the initiation occurs by the first-order homolysis reaction (Eq. 3-26f), which accounts for the complete decomposition of \( t \)-butyl hydroperoxide in the absence of styrene. Homolysis of the hydroperoxide occurs at a much faster rate in the presence of styrene than in its absence. The increased decomposition rate in the \( t \)-butyl hydroperoxide–styrene system occurs by a molecule-induced homolysis reaction which is first-order in both styrene and hydroperoxide [Walling and Heaton, 1965]. The initiation reaction may be written as

\[
M + I \rightarrow M\cdot + R\cdot
\]

and results in a \( \frac{3}{2} \)-order dependence of \( R_p \) on \([M]\). This initiation is probably best considered as an example of redox initiation (Sec. 3-4b).

Other exceptions to the first-order dependence of the polymerization rate on the monomer concentration occur when termination is not by bimolecular reaction of propagating radicals. Second-order dependence of \( R_p \) on \([M]\) occurs for primary termination (Eq. 3-33a) and certain redox-initiated polymerizations (Sec. 3-4b-2). Less than first-order dependence of \( R_p \) on \([M]\) has been observed for polymerizations (Sec. 9-8a-2) taking place inside a solid under conditions where monomer diffusion into the solid is slower than the normal propagation rate [Odian et al., 1980] and also in some redox polymerizations (Sec. 3-4b-2) [Mapunda-Vlckova and Barton, 1978].
3-4b Redox Initiation

Many oxidation–reduction reactions produce radicals that can be used to initiate polymerization [Sarac, 1999]. This type of initiation is referred to as redox initiation, redox catalysis, or redox activation. A prime advantage of redox initiation is that radical production occurs at reasonable rates over a very wide range of temperatures, depending on the particular redox system, including initiation at moderate temperatures of 0–50°C and even lower. This allows a greater freedom of choice of the polymerization temperature than is possible with the thermal homolysis of initiators. Some redox polymerizations can be initiated photolytically as well as thermally. A wide range of redox reactions, including both inorganic and organic components either wholly or in part, may be employed for this purpose. Some redox systems involve direct electron transfer between reductant and oxidant, while others involve the intermediate formation of reductant-oxidant complexes; the latter are charge-transfer complexes in some cases.

3-4b-1 Types of Redox Initiators

1. Peroxides in combination with a reducing agent are a common source of radicals; for example, the reaction of hydrogen peroxide with ferrous ion

\[ \text{H}_2\text{O}_2 + \text{Fe}^{2+} \rightarrow \text{HO}^- + \text{HO}^\cdot + \text{Fe}^{3+} \]  

(3-36a)

Ferrous ion also promotes the decomposition of a variety of other compounds including various types of organic peroxides [Bamford, 1988].

\[ \text{ROOR} \xrightarrow{\text{Fe}^{2+}} \text{RO}^- + \text{RO}^\cdot \]  

(3-36b)

\[ \text{ROOH} \xrightarrow{\text{Fe}^{2+}} \text{HO}^- + \text{RO}^\cdot \]  

(3-36c)

\[ \text{ROOCR} \xrightarrow{\text{Fe}^{2+}} \text{R}^\cdot \text{CO}^- + \text{RO}^\cdot \]  

(3-36d)

Other reductants such as Cr\(^{2+}\), V\(^{2+}\), Ti\(^{3+}\), Co\(^{2+}\), and Cu\(^{+}\) can be employed in place of ferrous ion in many instances. Most of these redox systems are aqueous or emulsion systems. Redox initiation with acyl peroxides can be carried out in organic media by using amines as the reductant [Morsi et al., 1977; O’Driscoll et al., 1965]. An interesting system is the combination of benzyol peroxide and an \(N,N\)-dialkylaniline. The difference in the rates of decomposition between such a redox system and the simple thermal homolysis of the peroxide alone is striking. The decomposition rate constant \(k_d\) for benzyol peroxide in styrene polymerization is \(1.33 \times 10^{-4}\) s\(^{-1}\) at 90°C, while that for the benzyol peroxide-\(N, N\)-diethylamline redox system is \(1.25 \times 10^{-2}\) L mol\(^{-1}\) s\(^{-1}\) at 60°C and \(2.29 \times 10^{-3}\) L mol\(^{-1}\) s\(^{-1}\) at 30°C. The redox system has a much larger decomposition rate. Radical production in this redox system appears to proceed via an initial ionic displacement by the nitrogen of the aniline on the peroxide linkage.

\[ \phi - \overset{\text{N}}{\text{R}} + \overset{\text{O}}{\text{C}} - \overset{\text{O}}{\text{O}} - \overset{\text{O}}{\text{C}} - \phi \rightarrow \left[ \phi - \overset{\text{N}}{\text{O}} - \overset{\text{O}}{\text{C}} - \phi \right]^+ \overset{\text{R}}{\phi} - \overset{\text{C}}{\text{O}} - \overset{\text{O}}{\text{C}} - \phi \]

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\[ \phi - \overset{\text{N}}{\text{R}} + \overset{\text{O}}{\text{C}} - \overset{\text{O}}{\text{O}} - \overset{\text{C}}{\text{O}} - \phi \]

(3-37)
In support of this mechanism, the rate of initiation increases with increasing nucleophilicity of the amine. Initiation is by the $\phi$COO• radical. The amino cation–radical is generally not an effective initiator as shown by the absence of nitrogen in the polymer; it apparently disappears by some unknown side reactions such as dimerization and/or deprotonation. (However, there is some evidence that the cation–radical produced by the interaction of benzoyl peroxide and N-vinylcarbazole (NVC) initiates cationic polymerization of NVC simultaneous with the radical polymerization [Bevington et al., 1978].) Other types of peroxides also appear susceptible to this type of acceleration. Peroxide decomposition is also accelerated by transition metal ion complexes such as copper (II) acetylacetonate [Ghosh and Maity, 1978; Shahani and Indictor, 1978]. Zinc chloride accelerates the rate of decomposition of AIBN in methyl methacrylate by a factor of 8 at 50°C, with a corresponding increase in polymerization rate [Lachinov et al., 1977]. The mechanism may be analogous to the amine–peroxide system. The effect of ZnCl₂ and other metal ions on accelerating $R_p$ is well established, although the mechanism in most cases appears to involve changes in $k_p$ and/or due to complexation of the metal ions with the monomer and/or propagating radicals.

2. The combination of a variety of inorganic reductants and inorganic oxidants initiates radical polymerization, for example

$$\text{Fe}^{2+} + \text{SO}_4^{2-} + \text{SO}_3^{-2} \rightarrow \text{Fe}^{3+} + \text{SO}_4^{2-} + \text{SO}_3^{-} \cdot \quad (3-38a)$$

$$\text{S}_2\text{O}_6^{2-} + \text{SO}_4^{-2} \rightarrow \text{SO}_2^{2-} + \text{SO}_4^{-} + \cdot\text{S}_2\text{O}_3^{-} \quad (3-38b)$$

Other redox systems include reductants such as HSO₃⁻, SO₃²⁻, S₂O₃²⁻, and S₂O₅²⁻ in combination with oxidants such as Ag⁺, Cu²⁺, Fe³⁺, ClO₃⁻, and H₂O₂.

3. Organic–inorganic redox pairs initiate polymerization, usually but not always by oxidation of the organic component, for example, the oxidation of an alcohol by Ce⁴⁺,

$$\text{R} = \text{CH}_2 = \text{OH} + \text{Ce}^{4+} \rightarrow \text{Ce}^{3+} + \text{H}^+ + \text{R} = \text{CH} = \text{OH} \quad (3-39)$$

or by V⁵⁺, Cr⁶⁺, Mn³⁺ [Fernandez and Guzman, 1989; Misra and Bajpai, 1982; Nayak and Lenka, 1980].

4. There are some initiator systems in which the monomer itself acts as one component of the redox pair. Examples are thiosulfate plus acrylamide or methacrylic acid and $N,N$-dimethylaniline plus methyl methacrylate [Manickam et al., 1978; Tsuda et al., 1984].

### 3-4b-2 Rate of Redox Polymerization

The kinetics of redox-initiated polymerizations generally fall into two categories depending on the termination mode. Many of these polymerizations proceed in the same manner as other polymerizations in terms of the propagation and termination steps; the only difference is the source of radicals for the initiation step. For these polymerizations where termination is by bimolecular reaction of propagating radicals, the initiation and polymerization rates will be given by appropriate expressions that are very similar to those developed previously:

$$R_i = k_i[\text{reductant}][\text{oxidant}] \quad (3-40)$$

$$R_p = k_p[M\left(\frac{k_i[\text{reductant}][\text{oxidant}]}{2k_i}\right)^{1/2}] \quad (3-41)$$
Equations 3-40 and 3-41 differ from those (Eqs. 3-31 and 3-32) discussed previously in that the factor of 2 is absent from the expression for $R_i$, since typically only one radical is produced per oxidant-reductant pair.

Some redox polymerizations involve a change in the termination step from the usual bimolecular reaction to monomolecular termination involving the reaction between the propagating radicals and a component of the redox system. This leads to kinetics that are appreciably different from those previously encountered. Thus, in the alcohol-Ce$^{4+}$ system (Eq. 3-39), termination occurs according to

$$M_{n}\cdot + Ce^{4+} \rightarrow Ce^{3+} + H^{+} + \text{dead polymer} \quad (3-42)$$

at high ceric ion concentrations. The propagating radical loses a hydrogen to form a dead polymer with a C=C and group. The rates of initiation and termination are given by

$$R_i = k_i[Ce^{4+}][\text{alcohol}] \quad (3-43)$$

$$R_t = k_t[Ce^{4+}][M] \quad (3-44)$$

By making the usual steady-state assumption (i.e., $R_i = R_t$), one obtains the polymerization rate as

$$R_p = \frac{k_d k_p [M][\text{alcohol}]}{k_t} \quad (3-45)$$

In many redox polymerizations, monomer may actually be involved in the initiation process. Although not indicated above, this is the case for initiations described under item 3b; and, of course, for item 4. $R_p$ will show a higher dependence on [M] in these cases than indicated by Eqs. 3-41 and 3-45. First-order dependence of $R_i$ on [M] results in $\frac{3}{2}$ and 2-order dependencies of $R_p$ on [M] for bimolecular and monomolecular terminations, respectively.

### 3-4c  Photochemical Initiation

*Photochemical* or *photoinitiated* polymerizations occur when radicals are produced by ultraviolet and visible light irradiation of a reaction system [Oster and Yang, 1968; Pappas, 1988]. In general, light absorption results in radical production by either of two pathways:

1. Some compound in the system undergoes excitation by energy absorption and subsequent decomposition into radicals.

2. Some compound undergoes excitation and the excited species interacts with a second compound (by either energy transfer or redox reaction) to form radicals derived from the latter and/or former compound(s).

The term *photosensitizer* was originally used to refer to the second pathway, especially when it involved energy transfer, but that distinction has become blurred. The mechanism for photoinitiation in a reaction system is not always clear-cut and may involve both pathways. *Photosensitizer* is now used to refer to any substance that either increases the rate of photoinitiated polymerization or shifts the wavelength at which polymerization occurs.

Photoinitiation offers several advantages. Polymerization can be spatially directed (i.e., confined to specific regions) and turned on and off by turning the light source off and on.
The initiation rates can be very fast and are controlled by a combination of the source of radicals, light intensity, and temperature. Industrial photopolymerizations typically use solvent-free systems, which offer advantages for both economic and/or environmental considerations. The significant limitation of photopolymerization is that penetration of light energy through a thickness of material is low. However, photopolymerization is well suited for surface and other thin-layer applications in the printing and coatings industries [Decker, 1996; Fouassier, 1995; Pappas, 1988]. Applications include the ultrafast drying of varnishes, printing inks, and coatings (decorative and protective) for metal, paper, wood, and plastics; in photolithography for producing integrated and printed circuits; in holography and stereolithography; and in curing dental restorations, bone cements, and adhesive formulations. Photopolymerization can be used with heat-sensitive substrates, since polymerization is rapid even at ambient temperatures. Laser light sources are becoming important in applications that take advantage of their higher intensities, resulting in higher reaction rates, improved imaging resolution, and deeper penetration into substrates.

Photopolymerization is used in the photoimaging industry. The reaction system for photoimaging applications is referred to as a photoresist. The development of a printed circuit involves coating a copper–laminate substrate with the photoresist followed by irradiation through a mask with transparent areas corresponding to the desired copper circuitry. The unexposed areas are uncured and easily dissolved by solvent. Copper is then selectively etched away from below the unexposed areas. The copper below the exposed areas is protected by a polymer coating during the etching process. Finally, that polymer coating is removed to yield the desired copper printed circuit.

Many of these applications involve a combination of polymerization and crosslinking. Crosslinking usually involves monomers with two or more double bonds per molecule (Sec. 6-6a). Acrylate, unsaturated polyester–styrene, and dithiol–diene systems are used [Decker, 1996]. (Curing of epoxy resins and vinyl ethers by ionic photoinitiators is also practiced commercially; see Secs. 5-2a-4, 7-2b-7.) Another approach for producing photo-crosslinked coatings is the crosslinking of preformed polymers. This requires the use of specially designed polymers with reactive functional groups (e.g., double bonds) and/or appropriate crosslinking agents.

3-4c-1 Bulk Monomer

The irradiation of some monomers results in the formation of an excited state $M^*$ by the absorption of light photons (quanta):

$$M + h\nu \rightarrow M^*$$

(3-46)

The excited species undergoes homolysis to produce radicals

$$M^* \rightarrow R^* + R'^*$$

(3-47)

capable of initiating the polymerization of the monomer. The identities of the radicals $R^*$ and $R'^*$ are seldom well established. Nor is it clear that photolysis of a bulk monomer always results in the simple homolysis to yield two radicals per one monomer molecule as described by Eq. 3-47. Initiation by photolysis of a monomer is limited to those monomers where the double bond is conjugated with other groups (e.g., styrene, methyl methacrylate) such that absorption will occur above the vacuum UV region (200 nm) where light sources are readily available. However, unless absorption occurs above 300–325 nm, there is the practical
limitation of the need for quartz reaction vessels, since glass does not transmit appreciable amounts of energy at wavelengths below 300–325 nm. A further practical limitation for most monomers is that the efficiency of initiation (quantum yield) by photolysis of bulk monomer is almost always considerably less than the initiator systems described below.

3-4c-2 Irradiation of Thermal and Redox Initiators

The various thermal and redox initiators described in Secs. 3-4a and 3-4b can also be used in photoinitiation. In the usual case irradiation yields the same radicals as described previously for thermal or redox initiation. However, not all thermal and redox initiators are equally useful as photoinitiators, since few of them absorb light in the practical wavelength region. On the other hand, the photochemical method allows the use of a wider range of compounds as initiators due to the higher selectivity of photolytic homolysis. For example, for compounds other than the thermal and redox initiators discussed previously, homolysis occurs at too high a temperature and usually results in the production of a wide spectrum of different radicals (and ions) as various bonds randomly break. A useful photoinitiator should absorb strongly in the wavelength range of the light source and possess a high quantum yield for radical production.

Although both aliphatic and aromatic ketones have been studied, the aromatic ketones are more useful in commercial practice, since their absorptions occur at longer wavelength (lower energy) and their quantum yields are higher [Ledwith, 1977; Pappas, 1988]. Ketones and their derivatives undergo homolysis by one or both (often simultaneously) of two processes: \( \alpha \)-scission and electron transfer [Padon and Scranton, 1999]. \( \alpha \)-Scission involves

\[
\begin{align*}
\text{Ar} - \overset{\text{O}}{\text{C}} - \text{Ar'} & \quad \text{hv} \quad \left( \text{Ar} - \overset{\text{O}}{\text{C}} - \text{Ar'} \right)^* \\
\text{Ar} - \overset{\text{O}}{\text{C}} - \text{Ar'} & \quad \overset{\text{O}}{\text{C}} + \text{Ar'}
\end{align*}
\]

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bond scission at the bond between the carbonyl carbon and the \( \alpha \)-carbon (Eq. 3-48) while electron transfer occurs only in the presence of an electron donor (RH) and involves electron transfer followed by proton transfer from the amine to the ketone:

\[
\begin{align*}
\text{Ar} - \overset{\text{O}}{\text{C}} - \text{Ar'} & + \text{R}_2\text{N}\text{CH}_2\text{R'} \\
\text{Ar} - \overset{\text{O}^-}{\text{C}} - \text{Ar'} & + \text{R}_2\text{N}^+\text{CH}_2\text{R'} \\
\text{Ar} - \overset{\text{O}}{\text{C}} - \text{Ar'} & + \text{R}_2\text{N}^-\text{CHR'}
\end{align*}
\]

(Tertiary amines with an \( \alpha \)-hydrogen are among the most effective electron donors; other electron donors include alcohols, amides, amino acids, and ethers. A third process, direct hydrogen atom transfer from RH to the ketone, is not common but does occur with some photoinitiators. The overall result is the same as the electron-transfer process. Although two radicals are produced by photolysis of the photoinitiator, only one of the radicals is typically active in initiation—the aroyl and amine radicals in Eqs. 3-48 and 3-49, respectively. The other radical may or may not initiate polymerization, but is active in termination. The decrease in photoinitiator concentration during polymerization is referred to as photobleaching.)
Similar photolytic reactions occur with benzoin (VIII), benzyl ketals (IX), aroylphosphine oxides (X), and \( \alpha \)-aminoalkylphenones (XI). These and related compounds are used as commercial photoinitiators, usually together with an amine [Decker et al., 2001; Encinas et al., 1989a,b; Fouassier, 1995; Padon and Scranton, 1999; Pappas, 1988]. The relative amounts of \( \alpha \)-scission and electron transfer vary with the initiator (which determines the relative stabilities of the radicals formed from the two processes) and also the electron donor used. The photoinitiator and electron donor are chosen to maximize energy absorption and radical yield.

Photoinitiation systems have been developed to take advantage of the lower cost of visible light sources compared to ultraviolet light sources. Many applications such as printing plates and lithography become more economical when using visible light. Visible light is preferable in biological applications (e.g., dental restorations and in vivo curing), since ultraviolet light is much more damaging to living cells. Many dyes and other compounds absorbing in the visible region have been used as photoinitiators, including methylene blue, eosin, ketocoumarins, cyanines, and fluorinated diaryl titanocenes. These compounds are used as part of a two- or three-component system. Two-component systems use an electron donor. Radicals are generated by the electron-transfer mechanism (Eq. 3-49). The dye-derived radical is inactive in polymerization, but active in termination. Three-component systems use an electron donor and a third component. The third component is often a diaryliodonium salt such as diaryliodonium chloride, \( \text{Ar}_2\text{I}^+\text{Cl}^- \). The third component increases the efficiency of photo-polymerization by reacting with the inactive dye radical to decrease the termination rate and increase the initiation rate by generating new radicals from fragmentation of the third component (e.g., \( \text{Ar}_2\text{I}^+\text{Cl}^- \) generates aryl radicals and aryl iodide) [Padon and Scranton, 2000]. In many cases, the reaction of the third component with the inactive dye radical regenerates the dye, that is, photobleaching does not occur. Other mechanisms have also been proposed for the three-component systems [Padon and Scranton, 1999]. More recently, two-component dye systems with organoborates such as tetramethylammonium triphenylbutylborate in place of amines have been found to be highly active in photoinitiation.

### 3-4c-3 Rate of Photopolymerization

The rate of photochemical initiation is given by

\[
R_i = 2\phi I_a \tag{3-50}
\]

where \( I_a \) is the intensity of absorbed light in moles (called einsteins in photochemistry) of light quanta per liter-second and \( \phi \) is the number of propagating chains initiated per light photon absorbed. \( \phi \) is referred to as the quantum yield for initiation. The factor of 2 in Eq. 3-50 is used to indicate that two radicals are produced per molecule undergoing photolysis. The factor of 2 is not used for those initiating systems that yield only one radical instead of two. Thus the maximum value of \( \phi \) is 1 for all photoinitiating systems. \( \phi \) is synonymous with \( f \) in that both describe the efficiency of radicals in initiating polymerization. (The reader is cautioned that this definition of \( \phi \) is not always used. An alternate approach is...
to replace $f$ by $f'f_0$, where $f'$ is the number of radicals produced per light photon absorbed and $f$ is the previously defined initiator efficiency. Also, quantum yields can be defined in terms of the quantum yield for reaction of the initiator species or quantum yield for monomer polymerized. These quantum yields are not synonymous with the quantum yield for initiation.)

An expression for the polymerization rate is obtained by combining Eqs. 3-50 and 3-25 to yield

$$R_p = k_p[M] \left( \frac{\phi I_a}{k_I} \right)^{1/2}$$

(3-51)

The absorbed light intensity $I_a$ is obtained from a consideration of the Beer–Lambert law in the form

$$I_a' = I_0 - I_0 e^{-\alpha[A]D}$$

(3-52)

where $I_0$ is the incident light intensity at the outer surface of the reaction system and $I_a'$ is the intensity of absorbed light on a layer at a distance $D$ (cm) into the reaction system. $I_a'$ is not the same as the quantity $I_a$ in Eqs. 3-50 and 3-51. $I_a$ is the volumetric light intensity (with units of mol cm\(^{-3}\) s\(^{-1}\) or, more often, mol L\(^{-1}\) s\(^{-1}\)). $I_a'$ and $I_0$ are surface area intensities (with units of mol cm\(^{-2}\) s\(^{-1}\)). $[A]$ is the molar concentration of light-absorbing photoinitiator. $\alpha$ is the absorption coefficient of A and varies with wavelength and temperature. $\alpha$ has units of L mol\(^{-1}\) cm\(^{-1}\). (The molar absorptivity $\epsilon$, formerly called the extinction coefficient, is often used instead of $\alpha$. $\alpha$ and $\epsilon$ are related by $\alpha = \epsilon \ln 10 = 2.3\epsilon$ and result from the use of the base $\epsilon$ instead of 10, respectively, in the Beer–Lambert law.)

$I_a$ and, therefore, $R_p$, vary with depth of penetration $D$ into the reaction system [Calvert and Pitts, 1967; Terrones and Pearlstein, 2001]. The variation of $I_a$ with $D$ is obtained as the differential of $I_a'$ with respect to $D$

$$I_a = \frac{dI_a'}{dD} = \alpha[A]I_0 10^3 e^{-\alpha[A]D}$$

(3-53)

The term $10^3$ is a conversion factor ($10^3$ mL L\(^{-1}\)) that converts $I_0$ from units of mol cm\(^{-3}\) s\(^{-1}\) to mol L\(^{-1}\) s\(^{-1}\). Combination of Eqs. 3-51 and 3-53 yields the polymerization rate as a function of $D$

$$R_p = k_p[M] \left( \frac{\phi\alpha[A]I_0 10^3 e^{-\alpha[A]D}}{k_I} \right)^{1/2}$$

(3-54)

$R_p$ is the “local” polymerization rate—the rate at a layer located a distance $D$ from the surface of the reaction system. Since $R_p$ varies with the depth of penetration into the reaction system, it is useful to calculate the layer-averaged polymerization rate $\bar{R}_p$, the average polymerization rate for a thickness $D$ of reaction system. $\bar{R}_p$ is obtained by integrating the local rate over the layer thickness $D$ and dividing by $D$ to give

$$\bar{R}_p = 2k_p[M] \left( \frac{\phi I_0 10^3}{\alpha[A]k_I} \right)^{1/2} \left( \frac{1 - e^{-\alpha[A]D/2}}{D} \right)$$

(3-55)

The light intensities delivered by light sources are usually expressed in units such as kcal s\(^{-1}\), kJ s\(^{-1}\), or erg s\(^{-1}\), and it is necessary to convert them into the appropriate units of mol L\(^{-1}\) s\(^{-1}\) before using them in the preceding equations. This is accomplished by a
knowledge of the wavelength \( \lambda \) or frequency \( \nu \) of the light energy employed. The energy in a mole (einstein) of light is \( Nh \nu \) or \( Nh c / \lambda \), where \( h \) is Planck’s constant, \( c \) is the speed of light, and \( N \) is Avogadro’s number.

3-4c-3-a Measurement of Absorbed Light. The use of Eqs. 3-54 and 3-55 may be avoided and Eq. 3-51 used instead by directly measuring \( I_a \) in a specific polymerization system. Measurement of light intensity is referred to as actinometry. Chemical, thermal, and electrical actinometers are used [Murov et al., 1993; Ranby and Rabek, 1975]. Thermal and electrical actinometers include photomultipliers, semiconductor photodetectors, and thermocouples that operate on the principle of converting photon energy to either electrical or thermal energy. The light intensity is measured by placing the electrical or thermal actinometer directly behind the reaction vessel and measuring the difference in intensity when the vessel is empty compared to when it holds the reaction system. A chemical actinometer involves using a chemical reaction whose quantum yield is known. The most frequently used chemical actinometer is probably potassium ferrioxalate. Irradiation of \( K_2Fe(C_2O_4)_3 \) as an aqueous acidified solution results in reduction of ferric ions to ferrous. Ferrous ions are followed by UV spectroscopy by forming the red-colored complex with 1,10-phenanthroline. Other chemical actinometers include uranyl oxalate (involving oxidation of oxalate ion) and benzophenone (reduction to benzhydrol). Chemical actinometry is performed in the same reaction vessels to be used for polymerization studies.

3-4c-3-b General Observations. If the term \( \alpha [A] D \) is sufficiently small, the exponential term in Eq. 3-53 has a value of one and there is no variation of \( I_a \) and \( R_p \) with \( D \). This occurs for very thin reaction systems with low photoinitiator concentration and small value of the absorption coefficient. Equation 3-54 becomes

\[
R_p = k_p [M] \left( \frac{\phi \alpha [A] I_0 10^{13}}{k_i} \right)^{1/2} \tag{3-56}
\]

under these conditions. Thus, \( R_p \) is first-order in \([M]\), \( 1/2 \)-order in both light intensity and photoinitiator concentration when there is negligible attenuation of light intensity in traversing the reaction system. When the photoexcitation process involves monomer \((A = M)\), the dependence of \( R_p \) on \([M]\) increases to \( 3/2 \)-order. The dependence of \( R_p \) on \([M]\) decreases to \( 1/2 \)-order in some systems with high monomer concentrations, such as in the photopolymerization of methyl methacrylate with ketone photoinitiators [Lissi et al., 1979]. With increasing \([M]\), monomer quenches the excited state for photoinitiation. Quenching is a generally observed phenomenon, leading to a lower than expected dependence of \( R_p \) on some component in the system that acts as the quencher. A quencher (which can be any compound present in the reaction system) undergoes energy transfer with the photoexcited species to dissipate the excitation energy.

For most practical photopolymerizations there is appreciable attenuation of light intensity with penetration and the dependence of polymerization rate on monomer, photoinitiator, and light intensity is more complex (see Eqs. 3-54 and 3-55 for exact definitions). Equation 3-54 is especially useful for analyzing the practical aspects of a photopolymerization. When polymerizing any specific thickness of reaction system it is important to know \( R_p \) at various depths (e.g., front, middle, and rear surfaces) than to know only the total \( R_p \) for that system thickness. If the thickness is too large, the polymerization rate in the rear (deeper) layers will be too low, and those layers will be only partially polymerized—the result would be detrimental because the product’s properties (especially the physical properties) would be
nonuniform. This problem is more severe for reactions carried out at high values of \([A]\) and \(\alpha\) because the variation of \(R_p\) with \(D\) is greater for larger values of \([A]\) and \(\alpha\) [Lee et al., 2001]. Uniformity of polymerization is increased by using lower concentrations of photoinitiators with lower \(\alpha\) values. However, there is a tradeoff between polymerization rate and uniformity of reaction.

The nonuniformity of polymerization with depth of penetration is less for photobleaching photoinitiators compared to photoinitiators that are regenerated. Photobleaching allows photon penetration deeper into the reaction system.

The nonuniformity of polymerization with depth of penetration is also minimized (but not completely overcome) by using a mixture of two photoinitiators (or one photoinitiator) with absorption bands at two different wavelength, one of which absorbs strongly (large \(\alpha\)) and the other weakly (small \(\alpha\)). The strong absorption band gives a high intensity at the surface of the reaction system, but the intensity rapidly decreases with penetration. The intensity of the weak absorption band is less effected by penetration and provides a more uniform intensity as a function of penetration. Dual photothermal initiation systems are also used. The specific photoinitiator initiates rapidly enough to generate sufficient heat to drive a thermal polymerization within the depth of the reaction system.

Performing photopolymerizations in air, which would simplify commercial practice, has a major complication due to two effects of oxygen. Oxygen acts as quencher of photoexcited states of molecules and also inhibits polymerization by its reaction with radicals (Sec. 3-7b). This problem can be avoided by performing the photopolymerization under an inert atmosphere (nitrogen, argon). Using a protective coating of a paraffin oil or some other compound has also been reported [Padon and Scranton, 2000]. These methods are usually avoided because of cost and other practical considerations. The use of an appropriate two-wavelength photoinitiator system overcomes the oxygen problem by having a higher intensity energy absorption in the surface layer.

### 3-4d Initiation by Ionizing Radiation

Radioactive sources and particle accelerators are used to initiate polymerizations. Electrons, neutrons, and \(\alpha\)-particles (He\(^2^+\)) are particulate radiations, while gamma and X rays are electromagnetic radiations. The interactions of these radiations with matter are complex [Chapiro, 1962; Wilson, 1974]. The chemical effects of the different types of radiation are qualitatively the same, although there are quantitative differences. Molecular excitation may occur with the subsequent formation of radicals in the same manner as in photolysis, but ionization of a compound \(C\) by ejection of an electron is more probable because of the higher energies of these radiations compared to visible or ultraviolet light energy. (Ionizing radiations have particle or photon energies in the range 10 keV–100 meV (1–16,000 J) compared to 1–6 eV for visible–ultraviolet photons.) For this reason such radiations are termed ionizing radiations. The cation formed in Eq. 3-67 is a radical–cation \(C^+\) formed by loss of a \(\pi\)-electron and has both radical and positive centers (Sec. 5-2a-6). The radical–cation can propagate at the radical and/or cationic centers depending on reaction conditions. The radical–cation can also dissociate to form separate radical and cationic species:

\[
\text{C} + \text{radiation} \rightarrow \text{C}^+ + e^- \quad (3-57)
\]

\[
\text{C}^+ \rightarrow \text{A}^+ + \text{B}^+ \quad (3-58)
\]
The initially ejected electron may be attracted to the cation $B^+$ with the formation of another radical:

$$B^+ + e^- \rightarrow B\cdot$$  \hspace{1cm} (3-59)

Radicals may also be produced by a sequence of reactions initiated by the capture of an ejected electron by $C$

$$C + e^- \rightarrow C^-$$  \hspace{1cm} (3-60)
$$C^- \rightarrow B\cdot + A^-$$  \hspace{1cm} (3-61)
$$A^- \rightarrow A\cdot + e^-$$  \hspace{1cm} (3-62)

where $C^-$ may or may not be an excited species depending on the energy of the electron.

The radiolysis of olefinic monomers results in the formation of cations, anions, and free radicals as described above. It is then possible for these species to initiate chain polymerizations. Whether a polymerization is initiated by the radicals, cations, or anions depends on the monomer and reaction conditions. Most radiation polymerizations are radical polymerizations, especially at higher temperatures where ionic species are not stable and dissociate to yield radicals. Radiolytic initiation can also be achieved using initiators, like those used in thermally initiated and photoinitiated polymerizations, which undergo decomposition on irradiation.

Radiation-initiated ionic polymerizations, however, have been established in a number of systems. This occurs under conditions where ionic species have reasonable stabilities and the monomer is susceptible to ionic propagation. Cationic polymerizations of isobutylene, vinyl ethers, epoxies, and styrene and anionic polymerization of acrylonitrile have been observed [Chapiro, 1962; Kubota et al., 1978; Wilson, 1974]. Ionic polymerizations have been observed at temperatures as high as 30–50°C, but lower temperatures are generally required, usually not because the ionic rates increase with decreasing temperature but because the radical contribution decreases. The role of reaction conditions has been well-established for styrene polymerization [Machi et al., 1972; Squire et al., 1972; Takezaki et al., 1978]. The dryness of the reaction system and the absence of any other species which can terminate ions (either those formed in the radiolytic reactions (Eqs. 3-57 through 3-62) or the ionic propagating species) is critical. Water and other similar compounds terminate ions by transferring a proton or negative fragment (see Chap. 5). Styrene monomer as normally purified and “dried” often has sufficient water present ($\sim 10^{-2}–10^{-4}$ $M$) to prevent ionic polymerization—only radical polymerization occurs. With superdried monomer ($([H_2O]<10^{-5}–10^{-7}$ $M$), one observes a bimodal molecular weight distribution. This indicates the simultaneous occurrence of cationic and radical polymerizations since the two are known to yield different-molecular-weight polymers. With decreasing water concentration ($\sim <10^{-7}–10^{-10}$ $M$) the polymerization proceeds entirely by cationic propagation as evidenced by a unimodal MWD, which is characteristic of the cationic MWD. The extent of the ionic contribution relative to radical polymerization also increases with increasing radiation intensity, perhaps due to the rapid depletion of water at the higher intensities. Other evidence for the ionic contributions include kinetic and activation energy data.

The kinetics of radiation-initiated polymerizations follow in a relatively straightforward manner those of photolytic polymerization. The initiation rate is determined by the radiation intensity and the concentration and susceptibility of the compound that radiolyses to yield the initiating species (ionic and/or radical). The final expression for $R_p$ is determined by the exact details of the initiation, propagation, and termination steps.
Radiation-initiated polymerization has achieved some commercial success. The most frequently used radiation is electrons, the technology is called electron-beam (EB) technology. Electrons as well as other ionizing radiations (except for α-particles) have a significant advantage over UV and visible radiation. The depth of penetration is much greater with less attenuation for ionizing radiations than for UV and visible. There are several areas of application for EB technology [Fouassier and Rabek, 1993]. Coatings and other thin reactions systems (involving mostly polymerization with crosslinking—Sec. 6-6a) are an area of application where EB competes directly against UV and visible light. EB is not used to the same extent as UV and visible because of the higher overall equipment costs and the perception that working with ionizing radiations is risky from a health–safety viewpoint. Other EB uses include the crosslinking of wire and cable insulation and packaging films (Sec. 9-2c). EB is the technology of choice in microelectronics fabrication.

3-4e Pure Thermal Initiation

Many monomers appear to undergo a spontaneous polymerization when heated in the apparent absence of catalysts. On careful investigation few of these involve the thermal production of radicals from the monomer. In most cases the observed polymerizations are initiated by the thermal homolysis of impurities (including peroxides or hydroperoxides formed due to O₂) present in the monomer. Most monomers, when exhaustively purified (and in exhaustively purified reaction vessels), do not undergo a purely thermal, self-initiated polymerization in the dark. Only styrene has been unequivocally shown to undergo self-initiated polymerization. Methyl methacrylate was also considered to undergo self-initiated polymerization, but more recent work indicates that most, but not all, of the previously reported self-initiated polymerization was caused by adventitious peroxides that were difficult to exclude by the usual purification techniques [Lehrle and Shortland, 1988]. Other monomers that may be susceptible to self-initiated polymerization are substituted styrenes, acenaphthylene, 2-vinylthiophene, and 2-vinylfuran as well as certain pairs of monomers [Brand et al., 1980; Hall, 1983; Lingnau et al., 1980; Sato et al., 1977]. The rate of self-initiated polymerization is much slower than the corresponding polymerization initiated by thermal homolysis of an initiator such as AIBN, but far from negligible; for example, the self-initiated polymerization rate for neat styrene at 60°C is 1.98 × 10⁻⁶ mol L⁻¹ s⁻¹ [Graham et al., 1979].

The initiation mechanism for styrene has been established [Graham et al., 1979; Kaufman, 1979; Kothe and Fischer, 2001; Mayo, 1968; Olaj et al., 1976, 1977a,b]. It involves the formation of a Diels–Alder dimer (XII) of styrene followed by transfer of a hydrogen atom from the dimer to a styrene molecule (Eq. 3-63). Whether formation of the

\[
2\phi CH=CH_2 \rightarrow \text{XII} \quad (3-63a)
\]

\[
\begin{align*}
\text{XII} + \phi CH=CH_2 & \rightarrow \phi CHCH_3 + \text{XII} \\
& \quad (3-63b)
\end{align*}
\]
Diels–Alder dimer or its reaction with styrene is the rate-determining step in initiation is not completely established. The dependence of \( R_p \) on [M] is closer to third-order than second-order, indicating that Eq. 3-63b is the slow step. The Diels–Alder dimer has not been isolated, but ultraviolet spectroscopy of the reaction system is entirely compatible with its presence. There are indications that the photopolymerization of neat styrene proceeds by a similar mechanism.

The initiation mechanism for methyl methacrylate appears to involve the initial formation of a biradical by reaction of two monomer molecules followed by hydrogen transfer from some species in the reaction system to convert the biradical to a monoradical (Eq. 3-64) [Lingnau and Meyerhoff, 1984a,b]. Spontaneous polymerization is also observed in certain pairs of monomers such as styrene-acrylonitrile and maleimide–vinyl ether [Decker, 2000; Liu et al., 1995]. These are monomer pairs in which one double bond is electron-rich and the other is electron-poor (Sec. 6-3b-3).

### 3-4f Other Methods of Initiation

Electrolysis of monomer solutions has been studied as a means of initiating polymerization [Olaj, 1987; Otero and Mugarz, 1987]. Aqueous and various organic solvents (e.g., DMF, methylene chloride, methanol) have been employed in the presence of various inorganic compounds. The latter are used either to conduct current or participate in the initiation process. Depending on the components present, radicals and/or ions are formed when current is passed through the reaction system, and these initiate polymerization. Such polymerizations are referred to as *electroinitiated* or *electrolytic polymerizations*. An interesting example is the electrolysis of an acetonitrile solution of acrylamide containing tetrabutylammonium perchlorate [Samal and Nayak, 1988]. Radical polymerization occurs at the anode initiated by \( \text{ClO}_4^- \) formed by oxidation of \( \text{ClO}_2 \). Anionic polymerization occurs at the cathode initiated by direct transfer of electrons to the monomer (Sec. 5-3a-2).

*Plasma* polymerization occurs when a gaseous monomer is placed in an electric discharge at low pressures under conditions where a plasma is created [Boenig, 1988; Yasuda, 1986]. A plasma consists of ionized gaseous molecules. In some cases, the system is heated and/or placed in a radiofrequency field to assist in creating the plasma. A variety of organic molecules including alkenes, alkynes, and alkanes undergo polymerization to high-molecular-weight products under these conditions. The propagation mechanisms appear to involve both ionic and radical species. Plasma polymerization offers a potentially unique method of forming thin polymer films for uses such as thin-film capacitors, antireflection coatings, and various types of thin membranes.

*Sonication*, the application of high-intensity ultrasound at frequencies beyond the range of human hearing (16 kHz), of a monomer results in radical polymerization. Initiation results from the effects of *cavitation*—the formation and collapse of cavities in the liquid. The collapse (implosion) of the cavities generates very high local temperatures and pressures. This results in the formation of excited states that leads to bond breakage and the formation of...
radicals. Polymerization to high-molecular-weight polymer is observed but the conversions are low (<15%). The polymerization is self-limiting because of the high viscosity produced even at low conversion. High viscosity hinders cavitation and radical production [Price et al., 1992].

3-4g Initiator Efficiency

3-4g-1 Definition of $f$

When a material balance is performed on the amount of initiator that is decomposed during a polymerization and compared with that which initiates polymerization, it is apparent that the initiator is inefficiently used. There is wastage of initiator due to two reactions. One is the induced decomposition of initiator by the attack of propagating radicals on the initiator, for example

\[
M_n\cdot + \phi\text{COO\text{-}OC\phi} \rightarrow M_n\text{-OC\phi} + \phi\text{CO}\cdot.
\] (3-65)

This reaction is termed chain transfer to initiator and is considered further in Sec. 3-6b. The induced decomposition of initiator does not change the radical concentration during the polymerization, since the newly formed radical (\(\phi\text{COO\cdot}\)) will initiate a new polymer chain. However, the reaction does result in a wastage of initiator. A molecule of initiator is decomposed without an increase in the number of propagating radicals or the amount of monomer being converted to polymer.

The second wastage reaction is that involving the side reaction(s) of the radicals formed in the primary step of initiator decomposition. Some of the radicals formed in the primary decomposition step, for example, in the reaction

\[
\phi\text{COO\text{-}OC\phi} \rightarrow 2 \phi\text{COO\cdot}.
\] (3-66)

undergo reactions to form neutral molecules instead of initiating polymerization. It is this wastage reaction that is referred to when discussing the initiator efficiency $f$. The initiator efficiency $f$ is defined as the fraction of radicals formed in the primary step of initiator decomposition, which are successful in initiating polymerization. The initiator efficiency is considered exclusive of any initiator wastage by induced decomposition. The reader is cautioned, however, that reported literature values of $f$ do not always make this distinction. Very frequently, the calculations of $f$ neglect and do not correct for the occurrence of induced decomposition. Such $f$ values may be considered as the “effective” or “practical” initiator efficiency in that they give the net or overall initiation efficiency of the initial catalyst concentration. The preferred method of quantitatively handling induced decomposition of initiator, however, is that which is discussed in Sec. 3-6b-3.

3-4g-2 Mechanism of $f < 1$: Cage Effect

The values of $f$ for most initiators lie in the range 0.3–0.8. To understand why the initiator efficiency will be less than unity, consider the following reactions that occur in
polymerizations initiated by benzoyl peroxide:

\[
\begin{align*}
&\phi\text{COO} - \text{OOC}\phi \rightleftharpoons [2\phi\text{COO}^\cdot] \quad (3-67) \\
&[2\phi\text{COO}^\cdot] \rightarrow [\phi\text{COO}\phi + \phi\text{CO}_2] \quad (3-68) \\
&[2\phi\text{COO}^\cdot] + M \rightarrow \phi\text{CO}_2^\cdot + \phi\text{COOM}^\cdot \quad (3-69) \\
&[2\phi\text{COO}^\cdot] \rightarrow 2\phi\text{COO}^\cdot \quad (3-70) \\
&\phi\text{COO}^\cdot + M \rightarrow \phi\text{COOM}^\cdot \quad (3-71) \\
&\phi\text{COO}^\cdot \rightarrow \phi^\cdot + \text{CO}_2 \quad (3-72) \\
&\phi^\cdot + M \rightarrow \phi\text{M}^\cdot \quad (3-73) \\
&\phi^\cdot + \phi\text{COO}^\cdot \rightarrow \phi\text{COO}\phi \quad (3-74) \\
&2\phi^\cdot \rightarrow \phi\phi \quad (3-75)
\end{align*}
\]

The brackets around any species indicate the presence of a solvent cage, which traps the radicals for some short period before they diffuse apart. Equation 3-67 represents the primary step of initiator decomposition into two radicals, which are held within the solvent cage. The radicals in the solvent cage may undergo recombination (the reverse of Eq. 3-67), reaction with each other (Eq. 3-68), or reaction with monomer (Eq. 3-69), or may diffuse out of the solvent cage (Eq. 3-70). Once outside the solvent cage, the radicals may react with monomer (Eq. 3-71) or decompose according to Eq. 3-72 to yield a radical that may undergo various reactions (Eqs. 3-73 to 3-75). Reaction 3-72 probably also occurs within the solvent cage followed by diffusion of the two species.

Recombination of the primary radicals (Eq. 3-67) has no effect on the initiator efficiency. Initiation of polymerization occurs by Eqs. 3-69, 3-71, and 3-73. The initiator efficiency is decreased by the reactions indicated by Eqs. 3-68, 3-74, and 3-75, since their products are stable and cannot give rise to radicals. Of these reactions the decomposition within the solvent cage (Eq. 3-68) is usually much more significant than the others in decreasing the value of \( f \). That this reaction is competitive with those leading to initiation of polymerization can be seen by considering the timescale of the various events [Koenig and Fischer, 1973; Noyes, 1961]. The average life of neighboring radicals is perhaps \( 10^{-10} - 10^{-9} \) s. Since rate constants for radical–radical reactions are in the range \( 10^7 \) L mol\(^{-1}\) s\(^{-1}\) and higher, and the concentration of radicals in the solvent cage is about \( 10^M \), there is a reasonable probability that Reaction 3-68 will occur. Reaction 3-69 cannot compete effectively with Reaction 3-68, since radical addition reactions have much lower rate constants (\( 10^5 \) L mol\(^{-1}\) s\(^{-1}\)).

\[
\begin{align*}
&[2\phi\text{COO}^\cdot] \rightarrow [\phi\text{COO}^\cdot + \text{CO}_2 + \phi^\cdot] \quad (3-76) \\
&[\phi\text{COO}^\cdot + \text{CO}_2 + \phi^\cdot] \rightarrow [\text{CO}_2 + \phi\text{COO}\phi] \quad (3-77) \\
&[\phi\text{COO}^\cdot + \text{CO}_2 + \phi^\cdot] \rightarrow \phi\text{COO}^\cdot + \text{CO}_2 + \phi^\cdot \quad (3-78) \\
&[2\phi\text{COO}^\cdot] \rightarrow [2\text{CO}_2 + 2\phi^\cdot] \quad (3-79) \\
&[2\text{CO}_2 + 2\phi^\cdot] \rightarrow [2\text{CO}_2 + \phi\phi] \quad (3-80) \\
&[2\text{CO}_2 + 2\phi^\cdot] \rightarrow 2\text{CO}_2 + 2\phi^\cdot \quad (3-81)
\end{align*}
\]

Reactions 3-76 and 3-79 coupled, respectively, with Reactions 3-78 and 3-81 do not lower \( f \) but do lower \( f \) when coupled, respectively, with Reactions 3-77 and 3-80. The radicals that escape the solvent cage (Eqs. 3-78 and 3-81) then react as per Eqs. 3-71 through 3-75.
Lowering of $f$ by reactions analogous to Eq. 3-68 is referred to as the cage effect [Bamford, 1988; Koenig and Fischer, 1973; Martin, 1973]. It is a general phenomenon observed in almost all initiation systems. About the only exceptions are the initiation systems such as

$$\text{Fe}^{2+} + \text{H}_2\text{O}_2 \rightarrow \text{Fe}^{3+} + \text{H}^- + \text{HO}^-$$

which do not produce radicals in pairs. However, even in some such instances the radical may be capable of reacting with a nonradical species in the solvent cage.

Acetoxy radicals from acetyl peroxide undergo partial decarboxylation and radical combination within the solvent cage leads to stable products incapable of producing radicals:

\[
\text{CH}_3\text{COO}^- \text{OOCCH}_3 \rightarrow [2 \text{CH}_3\text{COO}^- \cdot] \quad (3-83a)
\]

\[
[\text{CH}_3\text{COOCH}_3 + \text{CO}_2] \quad (3-83b)
\]

The homolysis of AIBN occurs in a concerted process with simultaneous breakage of the two C–N bonds to yield nitrogen and 2-cyano-2-propyl radicals. Reaction of the radicals with each other can occur in two ways to yield tetramethylsuccinodinitrile and dimethyl-$N$-(2-cyano-2-isopropyl)ketenimine:

\[
\text{CN} \quad (\text{CH}_3)_2\text{C}=\text{N}=\text{N}=\text{C}(\text{CH}_3)_2 \rightarrow \left[ \begin{array}{c} \text{CN} \\ (\text{CH}_3)_2\text{C}=\text{C}=\text{N}=\text{C}(\text{CH}_3)_2 \end{array} \right] + \text{N}_2
\]

\[
\left[ \begin{array}{c} \text{CN} \\ (\text{CH}_3)_2\text{C}=\text{C}=\text{N}=\text{C}(\text{CH}_3)_2 \end{array} \right] \rightarrow (\text{CH}_3)_2\text{C}=\text{N}=\text{C}(\text{CH}_3)_2 + \text{N}_2
\]

\[
(\text{CH}_3)_2\text{C}=\text{N}=\text{N}=\text{C}(\text{CH}_3)_2 + \text{N}_2
\]

A minor reaction of 2-cyano-2-propyl radicals is disproportionation to methacrylonitrile and isobutyronitrile [Moad et al., 1984; Starnes et al., 1984]. This presents a complication for polymerizations carried out to high conversions where the methacrylonitrile concentration is significant since methacrylonitrile undergoes copolymerization with many monomers.

The cage effect has also been well documented as the cause of lowered $\phi$ values in photo-initiation [Berner et al., 1978; Braun and Studenroth, 1979]. Benzoin photolysis yields benzaldehyde:

\[
\phi\text{C}^-\text{C}=\phi \text{H} \rightarrow \left[ \begin{array}{c} \phi\text{C}^- \cdot \\ \phi\text{C}^-\phi \end{array} \right] \rightarrow 2\phi\text{C}^-\text{H}
\]

The photolysis of benzildimethylketal yields benzoyl and benzylketal radicals in the primary cleavage. The latter radical undergoes decay within the cage to yield methyl benzoate and...
methyl radical. Coupling of the methyl and benzoyl radicals decrease $f$:

$$
\phi \left( \begin{array}{c}
\text{O} \\
\text{CH}_3
\end{array} \right)
\longrightarrow
\phi \left( \begin{array}{c}
\text{O} \\
\text{CH}_3
\end{array} \right) + 
\phi \left( \begin{array}{c}
\text{O} \\
\text{CH}_3
\end{array} \right)
$$

$$
\left[ \phi \left( \begin{array}{c}
\text{O} \\
\text{CH}_3
\end{array} \right) + \cdot \text{CH}_3 + \text{CH}_3\text{O} \cdot \right]
\longrightarrow
\phi \left( \begin{array}{c}
\text{O} \\
\text{CH}_3
\end{array} \right) + \text{CH}_3\text{O} \cdot \phi
$$

The initiator efficiency and quantum yield for initiation are generally independent of monomer concentration and of the radical coupling reactions occurring outside the solvent cage (Eqs. 3-74, 3-75). The prime reason for $f < 1$ is the reactions occurring within the solvent cage. Once a radical has diffused out of the solvent cage, the reaction with monomer (Eq. 3-71) occurs predominantly in preference to other reactions [Fink, 1983]. Even if Reaction 3-72 occurs this will be followed by Reaction 3-73 in preference to the two radical combination reactions (Eqs. 3-74, 3-75). The preference for initiation of polymerization arises from the much greater monomer concentrations ($10^{-1}–10^{-2} M$) compared to the radical concentrations ($10^{-7}–10^{-9} M$) that are normally present in polymerization systems. However, one can observe a variation of $f$ with the monomer concentration at low monomer concentrations. Figure 3-3 shows this effect in the AIBN initiation of styrene polymerization. The initiator efficiency increases very rapidly with [M] and a limiting value is quickly reached. Theoretical predictions [Koenig and Fischer, 1973] indicate that an effect of [M] on $f$ would be expected at monomer concentrations below $10^{-1}–10^{-2} M$, and this is the general observation. $f$ is affected at lower concentrations as one increases the initiation rate, since the radical–radical reactions become more probable. An example is the photopolymerization of methyl methacrylate using benzoin methyl ether [Carlblom and Pappas, 1977],

![Graph showing the effect of styrene concentration on the initiator efficiency of azobisisobutyronitrile.](image)

**Fig. 3-3** Effect of styrene concentration on the initiator efficiency of azobisisobutyronitrile. ●, ○ and ◯ refer to experiments with initiator concentrations of 0.20, 0.50, and 1.00 g L$^{-1}$, respectively. After Bevington [1955] (by permission of Faraday Society, and Royal Society of Chemistry, London).
where $f$ decreases from 0.65 to 0.30 as the concentration of the photosensitizer increases from $10^{-3} M$ to $4 \times 10^{-2} M$.

The initiator efficiency varies to differing extents depending on the identities of the monomer, solvent, and initiator. $f$ decreases as the viscosity of the reaction medium increases. With increasing viscosity, the lifetimes of radicals in the solvent cage are increased—leading to greater extents of radical–radical reactions within the solvent cage. The effect of viscosity has been observed when viscosity was altered by using different solvents. The effect can be quite large, for example, $f$ for bis-azo-1,1'-cyclohexane nitrile at $0^\circ C$ decreases from 0.22 in benzene to 0.086 in diethyl phthalate [Fischer et al., 1969]. $f$ has also been observed to decrease during the course of a polymerization, since both [M] and viscosity increase with conversion [Russell et al., 1988]. For example, $f$ for AIBN in the polymerization of styrene decreases from 0.75 at conversions up to 30% to 0.20 at 90–95% conversion [Solomon and Moad, 1987]. In some cases $f$ varies with solvent as a result of the solvent reacting with radicals before the radicals can initiate polymerization. The initiator efficiencies of AIBN, benzoyl peroxide, and $t$-butyl hydroperoxide are lower in carbon tetrachloride or 1-chlorooctane than in aromatic solvents [Nozaki and Bartlett, 1946; Shahani and Indictor, 1978; Walling, 1954]. Reactions of radicals with solvents are discussed further in Sec. 3-6. The change in initiator efficiency with solvent may in a few instances be due to a solvation effect, for example, the specific solvation of electrophilic radicals by electron-donor solvents [Martin, 1973]. The initiator efficiency for any particular initiator may also vary for different monomers. Thus the value of $f$ for AIBN in the polymerizations of methyl methacrylate, vinyl acetate, styrene, vinyl chloride, and acrylonitrile ranged from 0.6 to 1.0, increasing in that order [Arnett and Peterson, 1952]. This order is a consequence of the relative rates with which radicals add to the different monomers.

3-4g-3 Experimental Determination of $f$

Various methods are employed for the experimental evaluation of the initiator efficiency. (These methods are generally also applicable to determining $\phi$ for photopolymerization). One method involves the determination and comparison of both the initiator decomposition and the production of polymer molecules. The initiator decomposition is best determined during an actual polymerization. Independent measurement of initiator decomposition in the absence of monomer can give erroneous results. The rates of decomposition of initiator can be quite different for pure initiator as compared to initiator in the presence of monomer, since $f$ varies with monomer concentration. Also in some cases monomer is involved in the initiation step [e.g., molecule-induced homolysis (Eq. 3-35), certain redox initiations described in Sec. 3-4b-1]. AIBN decomposition can be followed relatively easily by following the evolution of nitrogen. Measurement of the polymer number-average molecular weight allows a determination of $f$ by comparison of the number of radicals produced with the number of polymer molecules obtained. This method requires a knowledge of whether termination occurs by coupling or disproportionation, since the former results in two initiator fragments per polymer molecule and the latter in only one. The occurrence of induced decomposition must be taken into account in calculating the number of radicals produced. Induced decomposition is negligible for azonitriles but occurs to an appreciable extent with many peroxides.

The second method is a variation of the first in which the number of initiator fragments in the polymer is determined by direct analysis of the polymer end groups. The analysis is relatively difficult to perform accurately because of the low concentration of the end groups. For a 50,000-molecular-weight polymer, the end groups constitute only $\sim 0.1\%$ of the total
weight of the sample. The use of isotopically labeled initiators such as $^{14}$C-labeled AIBN and benzoyl peroxide and $^{35}$S-labeled potassium persulfate is a sensitive method for determining the number of initiator fragments [Bonta et al., 1976]. Isotopically labeled initiators also allow a quantitative analysis of the initiator radicals in systems where their identities are not clear-cut. For example, the use of benzoyl peroxide with $^{14}$C in the carbonyl carbon shows that $\phi$COO is responsible for 98% of initiation of styrene polymerization at 80°C, but this drops to about 60% (with $\phi$ initiating 40% of the propagating chains) at 30°C [Berger et al., 1977].

A third method involves the use of radical scavengers, which count the number of radicals in a system by rapidly stopping their growth. Three groups of radical scavengers are used [Bamford, 1988; Koenig and Fischer, 1973]. The first group consists of stable radicals such as 2,2-diphenylpicrylhydrazyl (DPPH) obtained by oxidation of diphenylpicrylhydrazine:

\[
\text{NO}_2\phi_2N-NH-\text{PH}_2 \xrightarrow{\text{PbO}_2} \phi_2N-N\phi_2N-\text{NO}_2
\]

(3-87)

The DPPH radical terminates other radicals, probably by the reaction

\[
R• + \phi_2N-N\phi_2N-\text{NO}_2 \rightarrow R-N-NH-\phi_2N-\text{NO}_2
\]

(3-88)

The reaction can be easily followed spectrophotometrically, since the DPPH radical is deep violet and the product is usually light yellow or colorless. Other stable radicals include TEMPO (2,2,6,6-tetramethyl-1-piperidinyloxy), 1,3,5-triphenylverdazyl, and galvinoxyl [Areizaga and Guzman, 1988; Braun and Czerwinski, 1987]. A second group reacts by fast hydrogen or halogen transfer and consists of thiols, iodine, bromine, and dihydroanthracene. The third group, consisting of molecules that react with radicals, includes duroquinone and $p$-benzoquinone [Janzen, 1971]. Nitroso and nitrone compounds have been found to be highly useful [Evans, 1979; Sato et al., 1977]. These compounds, called spin traps, react with radicals to form stable radicals. 2-Methyl-2-nitrosopropane (XIII) and phenyl-$N$-t-butylnitrone (XIV) have been used extensively:

\[
(CH_3)_3C-\text{N}=O + R• \rightarrow (CH_3)_3C-\text{N}=\dot{O} R
\]

(3-89)

\[
XIII \rightarrow NV
\]

\[
\phi-\text{CH}=N-C(CH_3)_3 + R• \rightarrow \phi-\text{CH}=N-C(CH_3)_3 R
\]

(3-90)

\[
XIV \rightarrow XVI
\]
Electron spin resonance (ESR) spectroscopy can be advantageously used to measure the radical concentrations of the nitroxide radicals (XV and XVI) produced, since these are much more stable than the R radicals. Of greater importance, ESR can be used to determine the structure of R, since the ESR of the nitroxide radical is quite sensitive to the structure of R. (For this purpose, nitroso spin traps are more useful, since the R group in the nitroxide radical is nearer to the lone electron.) This can allow a determination of the structures of radicals first formed in initiator decomposition, the radicals that actually initiate polymerization (if they are not identical with the former) as well as the propagating radicals [Rizzardo and Solomon, 1979; Sato et al., 1975].

The radical scavenging methods require the general caution that the stoichiometry of the reaction between scavenger and radical must be established. A problem with some scavengers is that their reaction with radicals may not be quantitative. The DPPH radical is an extremely efficient scavenger in many systems. It completely stops vinyl acetate and styrene polymerizations even at concentrations below 10^{-4} M [Bartlett and Kwart, 1950]. However, the scavenging effect of DPPH is not universally quantitative for all monomers.

A fourth method is the dead-end polymerization technique, which allows the simultaneous determination of $k_d$ [Catalgil and Baysal, 1987; Reimschuessel and Creasy, 1978; Stickler, 1979]. *Dead-end polymerization* refers to a polymerization in which the initiator concentration decreases to such a low value that the half-life of the propagating polymer chains approximates that of the initiator. Under such circumstances the polymerization stops short of completion, and one observes a limiting conversion of monomer to polymer at infinite reaction time. Consider a dead-end polymerization initiated by the thermal homolysis of an initiator. Equations 3-28a and 3-32 can be combined and rearranged to yield

$$\frac{-d[M]}{[M]} = k_p \left( \frac{k_d [I]_0}{k_i} \right)^{1/2} e^{-k_d t/2} dt$$

(3-91)

which on integration leads to

$$-\ln \left( \frac{M}{[M]_0} \right) = -\ln(1 - p) = 2k_p \left( \frac{f[I]_0}{k_i k_d} \right)^{1/2} (1 - e^{-k_d t/2})$$

(3-92)

where $p$ is the extent of conversion of monomer to polymer and is defined by $(M)_0 - [M])/ [M]_0$. At long reaction times ($t \to \infty$), [M] and $p$ reach the limiting values of [M]$_\infty$ and $p_\infty$, respectively, and Eq. 3-92 becomes

$$-\ln \left( \frac{M}{[M]_0} \right) = -\ln(1 - p) = 2k_p \left( \frac{f[I]_0}{k_i k_d} \right)^{1/2}$$

(3-93)

Dividing Eq. 3-92 by Eq. 9-93, rearranging, and then taking logarithms of both sides leads to

$$-\ln \left[ 1 - \frac{\ln(1 - p)}{\ln(1 - p_\infty)} \right] = k_d t$$

(3-94)

The value of $k_d$ is then found from the slope of a plot of the left side of Eq. 3-94 versus time. Figure 3-4 shows the plot for the AIBN-initiated polymerization of isoprene at three temperatures [Gobran et al., 1960]. Since $k_d$ is determined, $f$ can be obtained from either Eq. 3-32 or 3-93 if the ratio $k_p/k_i^{1/2}$ is known from other studies.
Equation 3-92 is also useful for determining the time needed to reach different extents of conversion for actual polymerization systems where both [M] and [I] decrease with time.

3-4h Other Aspects of Initiation

There are two possible modes of addition of a primary radical from initiator to the double bond of a monomer: head and tail additions, corresponding to Eqs. 3-8 and 3-9, respectively. Tail addition is favored over head addition for the same reasons head-to-tail propagation is favored over head-to-head propagation (Sec. 3-2a). This expectation is generally verified in the few systems which have been experimentally examined [Bevington, 1988; Moad et al., 1982, 1984; Solomon and Moad, 1987]. Tail addition occurs exclusively in the AIBN and t-butyl peroxide initiated polymerizations of styrene and the AIBN-initiated polymerization of vinyl chloride; there is no detectable head addition. The ratio of tail : head additions varies from 20 : 1 to 13 : 1, depending on the reaction conditions, for the benzoyl-peroxide-initiated polymerization of styrene. The extent of head addition increases for monomers where there is a smaller difference in stability between the two possible radicals. The tail : head ratio is about 5–6 for the t-butyl peroxide initiated polymerization of vinyl acetate. The various results, especially those with vinyl acetate, show that the selectivity between tail and head additions in the initiation step is not as great as the selectivity between head-to-tail and head-to-head additions in propagation, presumably because the typical primary radical is more reactive than the typical propagating radical.

The initiation process appears more complicated than described above, although data are not available in more than a few systems. The benzoyl peroxide initiated polymerization of styrene involves considerable substitution of initiator radicals on the benzene ring for polymerizations carried out at high conversions and high initiator concentrations. About one-third of the initiator radicals from t-butyl peroxide abstract hydrogen atoms from the \( \alpha \)-methyl groups of methyl methacrylate, while there is no such abstraction for initiator radicals from benzoyl peroxide or AIBN.

Fig. 3-4 Dead-end polymerization of isoprene initiated by azobisisobutyronitrile. After Gobran et al. [1960] (by permission of Wiley-Interscience, New York).
### 3-5 MOLECULAR WEIGHT

#### 3-5a Kinetic Chain Length

The kinetic chain length $\nu$ of a radical chain polymerization is defined as the average number of monomer molecules consumed (polymerized) per each radical, which initiates a polymer chain. This quantity will obviously be given by the ratio of the polymerization rate to the initiation rate or to the termination rate, since the latter two rates are equal.

$$\nu = \frac{R_p}{R_i} = \frac{R_p}{R_t}$$  \hspace{1cm} (3-95)

Combination of Eqs. 3-22, 3-23, and 3-95 yields

$$\nu = \frac{k_p[M]}{2k_t[M]}$$  \hspace{1cm} (3-96)

or

$$\nu = \frac{k_t^2[M]^2}{2k_tR_p}$$  \hspace{1cm} (3-97)

For polymerization initiated by the thermal homolysis of an initiator, Eq. 3-22 is substituted into Eq. 3-97 to yield

$$\nu = \frac{k_p[M]}{2\left(\frac{k_dk_i[I]}{C_138}\right)^{1/2}}$$  \hspace{1cm} (3-98)

#### 3-5b Mode of Termination

The number-average degree of polymerization $X_n$, defined as the average number of monomer molecules contained in a polymer molecule, is related to the kinetic chain length. If the propagating radicals terminate by coupling (Eq. 3-16a), a dead polymer molecule is composed of two kinetic chain lengths and

$$X_n = 2\nu$$  \hspace{1cm} (3-99a)

For termination by disproportionation (Eq. 3-16b) the kinetic chain length is synonymous with the number-average degree of polymerization

$$X_n = \nu$$  \hspace{1cm} (3-99b)

The number-average molecular weight of a polymer is given by

$$\overline{M}_n = M_oX_n$$  \hspace{1cm} (3-100)

where $M_o$ is the molecular weight of the monomer.

The mode of termination is experimentally determined from the observation of the number of initiator fragments per polymer molecule. This requires the analysis of the molecular
weight of a polymer sample as well as the total number of initiator fragments contained in
that sample. Termination by coupling results in two initiator fragments per polymer mole-
cule, while disproportionation results in one initiator fragment per polymer molecule. The
fractions of propagating chains, \( a \) and \( (1 - a) \), respectively, which undergo termination by
coupling and disproportionation can be related to \( b \), the average number of initiator frag-
ments per polymer molecule. For a reaction system composed of \( n \) propagating chains, cou-
pling yields \( an \) initiator fragments and \( an/2 \) polymer molecules, while disproportionation
yields \( (1 - a)n \) initiator fragments and \( (1 - a)n \) polymer molecules. The average number
of initiator fragments per polymer molecule, defined as the total initiator fragments divided
by the total number of polymer molecules, is given as

\[
b = \frac{an + (1 - a)n}{an/2 + (1 - a)n} = \frac{2}{2 - a}
\]

from which the fractions of coupling and disproportionation are obtained as

\[
a = \frac{2b - 2}{b} \\
1 - a = \frac{2 - b}{b}
\]

Equations 3-96 through 3-98 show a significant characteristic of radical chain polymer-
izations. The kinetic chain length is inversely dependent on the radical concentration or the
polymerization rate. This is of great practical significance—any attempt to increase the poly-
merization rate by increasing the radical concentration comes at the expense of producing
smaller polymer molecules. The kinetic chain length at constant polymerization rate is a
characteristic of the particular monomer and independent of the method of initiation.
Thus, for any monomer, \( v \) is independent of whether the polymerization is initiated by ther-
mal, redox, or photochemical means, whether initiators are used, or of the particular initiator
used, if \([R^*]_o \) or \( R_p \) is the same.

The general relationship between the degree of polymerization and the kinetic chain
length is

\[
\bar{X}_n = bv = \frac{2v}{(2 - a)}
\]

Although experimental data are not available for all monomers, most polymer radicals
appear to terminate predominately or entirely by coupling (except where chain transfer pre-
dominates). Studies with small, aliphatic radicals clearly predict this tendency [Tedder,
1974]. However, varying extents of disproportionation are observed depending on the reac-
tion system. Disproportionation increases when the propagating radical is sterically hindered
or has many \( \beta \)-hydrogens available for transfer. Thus, whereas styrene, methyl acrylate, and
acrylonitrile undergo termination almost exclusively by coupling, methyl methacrylate
undergoes termination by a combination of coupling and disproportionation [Ayrey et al.,
1977; Bamford, 1988; Bonta et al., 1976; Hensley et al., 1995]. Increased temperature
increases the extent of disproportionation, with the most significant effect for sterically hin-
dered radicals. The extent of disproportionation in methyl methacrylate increases from 67%
at 25°C to 80% at 80°C [Bamford et al.,1969b]. There appears to be a tendency toward
disproportionation for highly reactive radicals such as those in vinyl acetate and ethylene
polymerizations. However, the effect is relatively small as the extent of disproportionation in these two polymerizations is no greater than 10% at most [Bamford et al., 1969a,b].

3-6 CHAIN TRANSFER

3-6a Effect of Chain Transfer

In many polymerization systems the polymer molecular weight is observed to be lower than predicted on the basis of the experimentally observed extents of termination by coupling and disproportionation. This effect is due to the premature termination of a growing polymer by the transfer of a hydrogen or other atom or species to it from some compound present in the system—the monomer, initiator, or solvent, as the case may be. These radical displacement reactions are termed chain-transfer reactions and may be depicted as

\[ \text{M}_n \cdot + XA \xrightarrow{k_{tr}} \text{M}_n-X + A\cdot \quad (3-102) \]

where XA may be monomer, initiator, solvent, or other substance and X is the atom or species transferred. Chain transfer to initiator was referred to earlier as induced initiator decomposition (Sec. 3-4g-1).

The rate of a chain-transfer reaction is given by

\[ R_{tr} = k_{tr}[\text{M}]|\text{XA}| \quad (3-103) \]

where \( k_{tr} \) is the chain-transfer rate constant. Chain transfer results in the production of a new radical A\( \cdot \), which then reinitiates polymerization

\[ A\cdot + \text{M} \xrightarrow{k_a} \text{M}\cdot \quad (3-104) \]

Chain transfer is a chain-breaking reaction; it results in a decrease in the size of the propagating polymer chain. The effect of chain transfer on the polymerization rate is dependent on whether the rate of reinitiation is comparable to that of the original propagating radical. Table 3-3 shows the four main possible situations that may be encountered. Reinitiation is rapid in cases 1 and 2, and one observes no change in the polymerization rate. The same number of monomer molecules are consumed per unit time with the formation of larger numbers of smaller-sized polymer molecules. The relative decrease in \( \text{X}_n \) depends on the magnitude of the transfer constant. When the transfer rate constant \( k_{tr} \) is much larger than that for propagation (case 2) the result is a very small-sized polymer (\( \text{X}_n \approx 1-5 \))—referred to as a

<table>
<thead>
<tr>
<th>TABLE 3-3 Effect of Chain Transfer on ( R_p ) and ( \text{X}_n )</th>
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<tbody>
<tr>
<td>Relative Rate Constants for Transfer, Propagation, and Reinitiation</td>
</tr>
<tr>
<td>Case</td>
</tr>
<tr>
<td>1</td>
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<td>2</td>
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<td>3</td>
</tr>
</tbody>
</table>
When reinitiation is slow compared to propagation (cases 3 and 4) one observes a decrease in $R_p$ as well as in $\bar{X}_n$. The magnitude of the decrease in $R_p$ is determined by the relative values of $k_p$ and $k_{tr}$. The remainder of this section will be concerned with case 1. Cases 3 and 4 will be considered further in Sec. 3-7. Case 2 (telomerization) is not within the scope of this text.

For chain transfer by case 1 the kinetic chain length remains unchanged, but the number of polymer molecules produced per kinetic chain length is altered. The number-average degree of polymerization is no longer given by $n$ or $2n$ for disproportionation and coupling, respectively. Chain transfer is important in that it may alter the molecular weight of the polymer product in an undesirable manner. On the other hand, controlled chain transfer may be employed to advantage in the control of molecular weight at a specified level.

The degree of polymerization must now be redefined as the polymerization rate divided by the sum of the rates of all chain-breaking reactions (i.e., the normal termination mode plus all chain-transfer reactions). For the general case of a polymerization initiated by the thermal homolysis of a catalyst and involving termination by a combination of coupling and disproportionation and chain transfer to monomer, initiator, and the compound S (referred to as a chain-transfer agent), the number average degree of polymerization follows from Eq. 3-103 as

$$X_n = \frac{R_p}{(2-a)(R_t/2) + k_{tr,M}[M]*[M] + k_{tr,S}[M]*[S] + k_{tr,I}[M]*[I]}$$

The first term in the denominator denotes termination by a combination of coupling and disproportionation, and the other terms denote chain transfer by monomer, chain-transfer agent, and initiator, respectively.

Consider now the simpler case when disproportionation does not occur ($a = 1$). Equation 3-105 becomes

$$X_n = \frac{R_p}{(R_t/2) + k_{tr,M}[M]*[M] + k_{tr,S}[M]*[S] + k_{tr,I}[M]*[I]}$$

A chain-transfer constant $C$ for a substance is defined as the ratio of the rate constant $k_{tr}$ for the chain transfer of a propagating radical with that substance to the rate constant $k_p$ for propagation of the radical. The chain-transfer constants for monomer, chain-transfer agent, and initiator are then given by

$$C_M = \frac{k_{tr,M}}{k_p} \quad C_S = \frac{k_{tr,S}}{k_p} \quad C_I = \frac{k_{tr,I}}{k_p}$$

Combining Eqs. 3-22, 3-31, 3-32, 3-106, and 3-107 with $R_i = R_t$ yields

$$\frac{1}{X_n} = \frac{R_t}{2R_p} + C_M + C_S \frac{[S]}{[M]} + C_I \frac{[I]}{[M]} \quad (3-108a)$$

or

$$\frac{1}{X_n} = \frac{k_tR_p}{k^2_p[M]^2} + C_M + C_S \frac{[S]}{[M]} + C_I \frac{k_{tr}^2R_p^2}{k^3_p f_{kd}[M]^3} \quad (3-108b)$$

which show the quantitative effect of the various transfer reactions on the number-average degree of polymerization. Various methods can be employed to determine the values of the chain-transfer constants. Equation 3-108 is often called the Mayo equation.
When disproportionation is important, this can be taken into account by reverting back to Eq. 3-105 to derive the most general form of the Mayo equation:

\[
\frac{1}{X_n} = \frac{(2 - a)R_t}{2R_p} + C_M + C_S \frac{[S]}{[M]} + C_I \frac{[I]}{[M]}
\] (3-108c)

3-6b Transfer to Monomer and Initiator

3-6b-1 Determination of \(C_M\) and \(C_I\)

Two special cases of Eq. 3-108a,b are of interest. When a chain-transfer agent is absent, the term in \([S]\) disappears and

\[
\frac{1}{X_n} = \frac{k_t R_p}{k_p^2 [M]^2} + C_M + C_I \frac{k_t R_p^2}{k_p^2 f k_d [M]^3}
\] (3-109a)

or

\[
\frac{1}{X_n} = \frac{k_t R_p}{k_p^2 [M]^2} + C_M + C_I \frac{[I]}{[M]}
\] (3-109b)

Equation 3-109 is quadratic in \(R_p\) and the appropriate plot of \(1/X_n\) versus \(R_p\) in Fig. 3-5 for styrene polymerization shows the effect to varying degrees depending on the initiator [Baysal and Tobolsky, 1952]. The initial portion of the plot is linear, but at higher concentrations of initiator and therefore high values of \(R_p\) the plot deviates from linearity as the contribution of transfer to initiator increases. The intercept of the linear portion yields the value of \(C_M\). The slope of the linear portion is given by \(k_t/k_p^2 [M]^2\) from which the important quantity \(k_p^2/k_t\) can be determined since the monomer concentration is known. For systems in which chain transfer to initiator is negligible a plot of \(1/X_n\) versus \(R_p\) will be linear over the whole range.

Several methods are available for the determination of \(C_I\). Equation 3-109 can be rearranged and divided through by \(R_p\) to yield

\[
\left[ \frac{1}{X_n} - C_M \right] \frac{k_t}{R_p} = \frac{k_t}{k_p^2 [M]^2} + \frac{C_I k_t R_p}{k_p^2 f k_d [M]^3}
\] (3-110)

A plot of the experimental data as the left side of Eq. 3-110 versus \(R_p\) yields a straight line whose slope is \((C_I k_t/k_p^2 f k_d [M]^3)\). The initiator transfer constant can be determined from the slope because the various other quantities are known or can be related to known quantities through Eq. 3-32. When chain transfer to monomer is negligible, one can rearrange Eq. 3-109b to yield

\[
\left[ \frac{1}{X_n} - \frac{k_t R_p}{k_p^2 [M]^2} \right] = C_I \frac{[I]}{[M]}
\] (3-111)
A plot of the left side of Eq. 3-111 versus \([I]/[M]\) yields a straight line whose slope is \(C_I\).

Figure 3-6 shows the plot for the \(t\)-butyl hydroperoxide polymerization of styrene [Walling and Heaton, 1965].

3-6b-2 Monomer Transfer Constants

Using the methods described, the values of \(C_M\) and \(C_I\) in the benzoyl peroxide polymerization of styrene have been found to be 0.00006 and 0.055 respectively [Mayo et al., 1951]. The amount of chain transfer to monomer that occurs is negligible in this polymerization. The chain-transfer constant for benzoyl peroxide is appreciable, and chain transfer with initiator becomes increasingly important as the initiator concentration increases. These effects are shown in Fig. 3-7, where the contributions of the various sources of chain ends are indicated. The topmost plot shows the total number of polymer molecules per \(10^5\) styrene monomer units. The difference between successive plots gives the number of polymer molecules terminated by normal coupling termination, transfer to benzoyl peroxide, and transfer to styrene.
Fig. 3-6 Determination of initiator chain-transfer constants in the t-butyl hydroperoxide initiated polymerization of styrene in benzene solution at 70°C. After Walling and Heaton [1965] (by permission of American Chemical Society, Washington, DC).

Fig. 3-7 Contribution of various sources of chain termination in the benzoyl peroxide-initiated polymerization of styrene at 60°C. After Mayo et al. [1951] (by permission of American Chemical Society, Washington, DC).
The monomer chain-transfer constants are generally small for most monomers—in the range $10^{-5}$ to $10^{-4}$ (Table 3-4). Chain transfer to monomer places the upper limit to the polymer molecular weight that can be obtained, assuming the absence of all other transfer reactions. Transfer to monomer does not, however, prevent the synthesis of polymers of sufficiently high molecular weight to be of practical importance. $C_M$ is generally low because the reaction

$$M_n \cdot + CH_2=CH \rightarrow M_n-H + CH_2=CH \cdot$$

(3-112)

involves breaking the strong vinyl C–H bond. The largest monomer transfer constants are generally observed when the propagating radicals have very high reactivities, for example, ethylene, vinyl acetate, and vinyl chloride. Chain transfer to monomer for vinyl acetate had been attributed to transfer from the acetoxy methyl group [Nozakura et al., 1972]

$$M_n \cdot + CH_2=CHOCOC\cdot \rightarrow M_n-H + CH_2=CHOCOC\cdot$$

(3-113)

although experiments with vinyl trideuteroacetate and trideuterovinyl acetate indicate that more than 90% of the transfer occurs at the vinyl hydrogens [Litt and Chang, 1981].

The very high value of $C_M$ for vinyl chloride is attributed to a reaction sequence involving the propagating center XVIII formed by head-to-head addition [Hjertberg and Sorvik, 1983; Llauro-Darricades et al., 1989; Starnes, 1985; Starnes et al., 1983; Tornell, 1988]. Intramolecular migration of a chlorine atom (Eq. 3-114) yields the secondary radical XIX that subsequently transfers the chlorine atom to monomer (Eq. 3-115) to yield poly(vinyl chloride)

$$\sim CH_2-CH-CH-CH_2 \cdot + CH_2=CHCl \rightarrow \sim CH_2-CH-CH-CH_2Cl$$

(3-114)

$$\sim CH_2-CH=CH-CH_2Cl + ClCH=CHCl$$

(3-115)

### TABLE 3-4 Monomer Chain-Transfer Constants$^a$

<table>
<thead>
<tr>
<th>Monomer</th>
<th>$C_M \times 10^4$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Acrylamide</td>
<td>0.6, 0.12$^b$</td>
</tr>
<tr>
<td>Acrylonitrile</td>
<td>0.26–0.3</td>
</tr>
<tr>
<td>Ethylene</td>
<td>0.4–4.2</td>
</tr>
<tr>
<td>Methyl acrylate</td>
<td>0.036–0.325</td>
</tr>
<tr>
<td>Methyl methacrylate</td>
<td>0.07–0.10</td>
</tr>
<tr>
<td>Styrene</td>
<td>0.60–0.92$^c$</td>
</tr>
<tr>
<td>Vinyl acetate</td>
<td>1.75–2.8</td>
</tr>
<tr>
<td>Vinyl chloride</td>
<td>10.8–12.8</td>
</tr>
</tbody>
</table>

$^a$ All $C_M$ are for 60°C except where otherwise noted.  
$^b$ Value at 25°C.  
$^c$ Data from Braks and Huang [1978]; all other data from Brandrup et al. [1999].
(commonly referred to as PVC) with allyl chloride end groups (XX) and radical XXI. Radical XXI reinitiates polymerization to yield polymer molecules with 1,2-dichloroalkane end groups. Consistent with this mechanism, the amounts of allyl chloride and 1,2-dichloroalkane end groups are approximately equal (0.7–0.8 per polymer molecule).

The $C_M$ value of vinyl chloride is sufficiently high that the maximum number-average molecular weight that can be achieved is 50,000–100,000. This limit is still reasonable from the practical viewpoint—PVC of this molecular weight is a very useful product.

Not only the case of vinyl chloride but also styrene shows that the observed chain transfer to monomer is not the simple reaction described by Eq. 3-112. Considerable evidence [Olaj et al., 1977a,b] indicates that the experimentally observed $C_M$ may be due in large part to the Diels–Alder dimer XII transferring a hydrogen (probably the same hydrogen transferred in the thermal initiation process) to monomer.

### 3-6b-3 Initiator Transfer Constants

Different initiators have varying transfer constants (Table 3-5). Further, the value of $C_I$ for a particular initiator also varies with the reactivity of the propagating radical. Thus there is a fivefold difference in $C_I$ for cumyl hydroperoxide toward poly(methyl methacrylate) radical compared to polystyryl radical. The latter is the less reactive radical; see Sec. 6-3b.

Azonitriles have generally been considered to be “cleaner” initiators in the sense of being devoid of transfer, but this is not true [Braks and Huang, 1978]. The transfer with azonitriles probably occurs by the displacement reaction

$$\text{M}_n \cdot + \text{RN} = \text{NR} \rightarrow \text{M}_n - \text{R} + \text{N}_2 + \cdot \text{R} \cdot \quad (3-116)$$

Many peroxides have significant chain-transfer constants. Dialkyl and diacyl peroxides undergo transfer by

$$\text{M}_n \cdot + \text{RO} = \text{OR} \rightarrow \text{M}_n - \text{OR} + \text{RO} \cdot \quad (3-117)$$

where $R = \text{alkyl or acyl}$. The acyl peroxides have higher transfer constants than the alkyl peroxides, due to the weaker $\text{O} - \text{O}$ bond of the former. The hydroperoxides are usually

<table>
<thead>
<tr>
<th>Initiator</th>
<th>Styrene</th>
<th>Methyl Methacrylate</th>
<th>Acrylamide</th>
</tr>
</thead>
<tbody>
<tr>
<td>2,2-Azobisisobutyronitrile$^c$</td>
<td>0.091–0.14</td>
<td>0</td>
<td>—</td>
</tr>
<tr>
<td>$t$-Butyl peroxide</td>
<td>0.0003–0.00086</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td>Lauroyl peroxide (70°C)</td>
<td>0.024</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td>Benzoyl peroxide</td>
<td>0.048–0.10</td>
<td>0–0.02</td>
<td>—</td>
</tr>
<tr>
<td>$t$-Butyl hydroperoxide</td>
<td>0.035</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td>Cumyl hydroperoxide</td>
<td>0.063</td>
<td>0.33</td>
<td>—</td>
</tr>
<tr>
<td>Persulfate (40°C)</td>
<td>—</td>
<td>—</td>
<td>0.0028</td>
</tr>
</tbody>
</table>

$^a$ Data from Brandrup et al. [1999].

$^b$ All $C_I$ values are for 60°C except where otherwise noted.

$^c$ Ayrey and Haynes [1974]; Braks and Huang [1978].
the strongest transfer agents among the initiators. Transfer probably involves hydrogen atom abstraction

\[
M_n^\cdot + \text{ROO}^-H \rightarrow M_n^\cdot -H + \text{ROO}^\cdot
\]  

(3-118)

The typical effect of initiator chain transfer [Baysal and Tobolsky, 1952] can be seen graphically in Fig. 3-6. The decrease of polymer size due to chain transfer to initiator is much less than indicated from the \(C_1\) values because it is the quantity \(C_1[I]/[M]\), which affects \(X_n\) (Eq. 3-109b). The initiator concentrations are quite low \((10^{-4}–10^{-2}M)\) in polymerization, and the ratio \([I]/[M]\) is typically in the range \(10^{-3}–10^{-5}\).

### 3-6c Transfer to Chain-Transfer Agent

#### 3-6c-1 Determination of \(C_S\)

The second special case of Eq. 3-108 consists of the situation where transfer with the chain-transfer agent is most important. In some instances the chain-transfer agent is the solvent, while in others it is an added compound. In such a case the third term on the right side of Eq. 3-108 makes the biggest contribution to the determination of the degree of polymerization. By the appropriate choice of polymerization conditions, one can determine the value of \(C_S\) for various chain-transfer agents [Gregg and Mayo, 1948]. By using low concentrations of initiators or initiators with negligible \(C_1\) values (e.g., AIBN), the last term in Eq. 3-108 becomes negligible. The first term on the right side of the equation may be kept constant by keeping \(R_p/[M]^2\) constant by appropriately adjusting the initiator concentration throughout a series of separate polymerizations. Under these conditions, Eq. 3-108 takes the form

\[
1/X_n = 1/X_{n0} + C_S \frac{[S]}{[M]}
\]  

(3-119)

where \((1/X_{n0})\) is the value of \((1/X_n)\) in the absence of the chain-transfer agent. \((1/X_{n0})\) is the sum of the first, second, third, and fourth terms on the right side of Eq. 3-108a.b. \(C_S\) is then determined as the slope of the linear plot of \((1/X_n)\) versus \([S]/[M]\). Such plots are shown in Fig. 3-8 for several chain-transfer agents in styrene polymerization. This method is of general use for determining \(C_S\) values.

The data can also be handled by plotting \([d(1/X_n) – (1/X_{n0})]/d[M]\) versus \([S]/[M]\). Under conditions where \(R_p/[M]^2\) is not constant, one may plot \([d(1/X_n) – k_5R_p/k_5^2[M]^2]/d[S]/d[M]\) versus \([S]/[M]\). Another method involves dividing the rate expression for transfer (Eq. 3-104) by that for propagation (Eq. 3-112) to yield

\[
\frac{d[S]/dt}{d[M]/dt} = \frac{k_{tr,S}[S]}{k_p[M]} = C_S \frac{[S]}{[M]}
\]  

(3-120)

The value of \(C_S\) is obtained as the slope of the line obtained by plotting the ratio of the rates of disappearance of transfer agent and monomer \(d[S]/d[M]\) versus \([S]/[M]\).

A useful alternate to the Mayo plot for determining \(C_S\) (as well as other transfer constants) is the \textit{chain length distribution} (CLD) method based on the molecular weight distributions obtained from size exclusion chromatography (SEC) [Christie and Gilbert, 1996, 1997; Heuts et al., 1998, 1999; Moad and Moad, 1996]. The limiting slope \(\Lambda_{\text{HIGH}}\) of a
plot of \( \ln X_i \) versus \( i \) at the high-molecular-weight portion of an SEC plot is the negative of the right side of the Mayo equation (Eq. 3-108c):

\[
\Lambda_{\text{HIGH}} = \lim_{i \to \infty} \frac{d(\ln X_i)}{di} = -\left( \frac{2 - a)R_i}{2R_p} + C_M + C_S \frac{[S]}{[M]} \right) \tag{3-121}
\]

The \( C_I[M] \) term is left out of Eq. 3-121 because in the limit of high \( i \) the initiator concentration becomes vanishingly small and there is negligible chain transfer to initiator. \( C_S \) is obtained by measuring \( \Lambda_{\text{HIGH}} \) as a function of \([S]/[M]\) and then plotting \(-\Lambda_{\text{HIGH}}\) against \([S]/[M]\), a plot often called a CLD plot. \( C_S \) is the straight line slope of the CLD plot. \( C_M \) can be obtained from polymerizations at very low initiator concentrations and no chain-transfer agent present. The last term on the right side of Eq. 3-121 is zero, and the first term is very small. Under these conditions the slope of the CLD plot is \( C_M \). Chain transfer constants obtained by the CLD method are essentially indistinguishable from those of the Mayo plot [Heuts et al., 1999].

### 3-6c-2 Structure and Reactivity

The transfer constants for various compounds are shown in Table 3-6. These data are useful for the information they yield regarding the relationship between structure and reactivity in radical displacement reactions. Aliphatic hydrocarbons such as cyclohexane with strong C–H bonds show low transfer constants. Benzene has an even lower \( C_S \) value because of
the stronger C–H bonds. Transfer to benzene appears not to involve hydrogen abstraction but addition of the propagating radical [Deb and Ray, 1978] to the benzene ring. The presence of the weaker benzylic hydrogens in toluene, ethylbenzene, and isopropylbenzene leads to higher \( C_S \) values relative to benzene. The benzylic C–H is abstracted easily because the resultant radical is resonance-stabilized:

\[
\begin{align*}
\text{C} & \quad \text{CH}_2 \\
\text{C} & \quad \text{CH}_2 \\
\text{C} & \quad \text{CH}_2 \\
\text{C} & \quad \text{CH}_2
\end{align*}
\]

(3-122)

The transfer constant for \( t \)-butylbenzene is low, since there are no benzylic C–H bonds present. Primary halides such as \( n \)-butyl chloride and bromide behave similar to aliphatics with low transfer constants, corresponding to a combination of either aliphatic C–H bond breakage or the low stability of a primary alkyl radical on abstraction of Cl or Br. The iodide,
on the other hand, transfers an iodide atom and shows a much higher $C_S$ value due to the weakness of the $C–I$ bond. Secondary halides have somewhat higher $C_S$ values because of the greater stability of the secondary radical formed.

Acids, carbonyl compounds, ethers, amines, and alcohols have transfer constants higher than those of aliphatic hydrocarbons, corresponding to $C–H$ breakage and stabilization of the radical by an adjacent $O$, $N$, or carbonyl group.

The weak $S–S$ bond leads to high transfer constants for disulfides:

$$M_n \cdot + RS−SR \rightarrow M_nSR + RS \cdot$$  \hspace{5cm} (3-123)

The high $C_S$ values for carbon tetrachloride and carbon tetrabromide are due to the weak carbon–halogen bonds. These bonds are especially weak because of the excellent stabilization of the trihalocarbon radicals formed by resonance involving the halogen free pairs of electrons:

$$\begin{align*}
\text{Cl} \text{Cl} \text{Cl} \text{Cl} & \rightarrow \text{Cl} \text{Cl} \text{Cl} \text{Cl} \\
\text{Cl} \text{Cl} & \rightarrow \text{Cl} \text{Cl} \text{Cl} \text{Cl} \\
\text{Cl} \text{Cl} & \rightarrow \text{Cl} \text{Cl} \text{Cl} \text{Cl} \\
\text{Cl} \text{Cl} & \rightarrow \text{Cl} \text{Cl} \text{Cl} \text{Cl} \\
\text{Cl} \text{Cl} & \rightarrow \text{Cl} \text{Cl} \text{Cl} \text{Cl} \\
\end{align*}$$  \hspace{5cm} (3-124)

The greater transfer constant for carbon tetrabromide compared to the tetrachloride is due to the weaker $C–Br$ bond. The low $C_S$ value for chloroform compared to carbon tetrachloride is explained by $C–H$ bond breakage in the former. The thiols have the largest transfer constants of any known compounds due to the weak $S–H$ bond.

Two interesting observations are made when the $C_S$ values for various compounds are compared in the polymerization of various different monomers. The absolute value of the transfer constant for any one compound may change very significantly depending on the monomer being polymerized. This is clearly seen in Table 3-6, where many of the transfer agents are 1–2 orders of magnitude more active in vinyl acetate polymerization compared to styrene polymerization. This effect is a consequence of the greater reactivity of the vinyl acetate propagating radical. The chain-transfer constant for any one compound generally increases in the order of increasing radical reactivity. The order of radical reactivity is vinyl chloride $>$ vinyl acetate $>$ acrylonitrile $>$ methyl acrylate $>$ methyl methacrylate $>$ styrene $>$ 1,3-butadiene. Radical reactivity is discussed in greater detail in Sec. 6-3b.

The order of reactivity of a series of transfer agents usually remains the same irrespective of the monomer when the transfer agents are relatively neutral in polarity. However, there are many very significant deviations from this generalization for polar transfer agents. Table 3-7 shows data for carbon tetrachloride and triethylamine with several monomers. The monomers are listed in decreasing order of reactivity for transfer reactions with neutral transfer agents such as hydrocarbons. It is apparent that the electron-rich (electron-donor) transfer agent triethylamine has enhanced reactivity with the electron-poor (electron-acceptor) monomers, especially acrylonitrile. The electron-poor (electron-acceptor) transfer agent carbon tetrachloride has enhanced reactivity with the electron-rich (electron-donor) monomers vinyl acetate and styrene and markedly lowered reactivity with the electron-poor monomers.

The enhancement of chain-transfer reactivity has been postulated [Patnaik et al., 1979; Walling, 1957] as occurring by stabilization of the respective transition states for the transfer
reactions by contributions from polar structures such as

\[
\begin{align*}
\text{CHCH}_2 \text{CHCH}_2 \text{Cl} \text{CCl}_3 \text{Cl}^+ + \text{CH}_2 \text{CH} \text{CN} \text{CH} \text{N(C}_2\text{H}_5)_2 \text{H} \text{CH}^+ & \\
\text{CHCH}_2 \text{CHCH}_2 \text{Cl} \text{CCl}_3 \text{Cl}^+ + \text{CH}_2 \text{CH} \text{CN} \text{CH} \text{N(C}_2\text{H}_5)_2 \text{H} \text{CH}^+ & \\
\end{align*}
\]

in which there is partial charge transfer between an electron donor and an electron acceptor. This type of polar effect is a general one often encountered in free-radical reactions [Huyser, 1970]. One usually observes the reactivity of an electron-donor radical to be greater with an electron-acceptor substrate than with an electron-donor substrate. The reverse is true of an electron-acceptor radical. The effect of polar effects on radical addition reactions will be considered in Sec. 6-3b-3.

### 3-6c-3 Practical Utility of Mayo Equation

The use of the Mayo equation (Eq. 3-108 in its various forms) allows one to quantitatively determine the effects of normal termination and transfer to monomer, initiator, and solvent on the molecular weight of the product and then adjust the reaction parameters to obtain the desired molecular weight. Two cases are encountered.

Case 1 involves a reaction system that yields a molecular weight lower than needed. One analyzes the different terms on the right side of the Mayo equation to determine which one(s) is (are) responsible for the low molecular weight and the reaction parameters are then adjusted accordingly to increase the molecular weight. The initiation rate would be lowered if the low molecular weight is due to an excessively high initiation rate. If the initiator or

<table>
<thead>
<tr>
<th>Monomer</th>
<th>(C_S \times 10^4)</th>
<th>(k_{tr})</th>
<th>(C_S \times 10^4)</th>
<th>(k_{tr})</th>
</tr>
</thead>
<tbody>
<tr>
<td>Vinyl acetate</td>
<td>10,700</td>
<td>2400</td>
<td>370</td>
<td>85</td>
</tr>
<tr>
<td>Acrylonitrile</td>
<td>0.85</td>
<td>0.17</td>
<td>3800</td>
<td>760</td>
</tr>
<tr>
<td>Methyl acrylate</td>
<td>1.25(^c)</td>
<td>0.26(^c)</td>
<td>400</td>
<td>84</td>
</tr>
<tr>
<td>Methyl methacrylate</td>
<td>2.4</td>
<td>0.12</td>
<td>1900</td>
<td>98</td>
</tr>
<tr>
<td>Styrene</td>
<td>110</td>
<td>1.8</td>
<td>7.1</td>
<td>0.12</td>
</tr>
</tbody>
</table>

\(^a\) \(C_S\) values from Brandrup et al. [1999], Eastmond [1976a,b,c] and are for 60\(^\circ\)C unless otherwise noted.

\(^b\) \(k_{tr}\) values were calculated from Eq. 3-107 using \(k_p\) values from Table 3-11.

\(^c\) \(C_S\) value is at 80\(^\circ\)C. The \(k_{tr}\) was calculated using the \(k_p\) value for 60\(^\circ\)C.
solvent are too active in transfer, a less active initiator or solvent would be chosen. If the monomer itself is too active in transfer, it sets the upper limit of the molecular weight that can be achieved as long as all other factors are optimized.

Case 2 involves a reaction system that yields too high a polymer molecular weight. The simplest method of lowering molecular weight is to add a chain-transfer agent. Equation 3-119 is used to determine the transfer agent and concentration needed to obtain a specifically desired molecular weight. When used in this manner, transfer agents are called regulators or modifiers. Transfer agents with transfer constants of one or greater are especially useful, since they can be used in low concentrations. Thus, thiols such as 1-dodecanethiol are used in the industrial emulsion copolymerization of styrene and 1,3-butadiene for SBR rubbers. The production of very low-molecular-weight polymers by chain transfer (telomerization) is an industrially useful process. Ethylene polymerized in chloroform yields, after fluorination of its end groups, a starting material for fluorinated lubricants. Low-molecular-weight acrylic ester polymers have been used as plasticizers.

It is also useful to point out that chain-transfer studies yield further corroboration of the concept of functional group reactivity independent of molecular size. Thus one can vary the degree of polymerization for a monomer by using different chain-transfer agents or different concentrations of the same transfer agent. Under these conditions the propagation rate constant $k_p$ is found to be independent of $\bar{X}_n$. Further, the transfer constant $k_{tr}$ for a particular transfer agent is also independent of the size of the propagating radical.

### 3-6d Chain Transfer to Polymer

The previous discussion has ignored the possibility of chain transfer to polymer molecules. Transfer to polymer results in the formation of a radical site on a polymer chain. The polymerization of monomer at this site leads to the production of a branched polymer, for example

\[
M_n\cdot + \overset{Y}{\sim}CH_2\overset{Y}{\sim}CH_2H \rightarrow M_nH + \overset{Y}{\sim}CH_2\overset{Y}{\sim}CH_2\overset{Y}{\sim}CH_2M_m
\]

Ignoring chain transfer to polymer does not present a difficulty in obtaining precise values of $C_1$, $C_M$, and $C_S$, since these are determined from data at low conversions. Under these conditions the polymer concentration is low and the extent of transfer to polymer is negligible.

Transfer to polymer cannot, however, be neglected for the practical situation where polymerization is carried to complete or high conversion. The effect of chain transfer to polymer plays a very significant role in determining the physical properties and the ultimate applications of a polymer [Small, 1975]. As indicated in Chap. 1, branching drastically decreases the crystallinity of a polymer.

The transfer constant $C_P$ for chain transfer to polymer is not easily obtained [Yamamoto and Sugimoto, 1979]. $C_P$ cannot be simply determined by introducing the term $C_P[P]/[M]$ into Eq. 3-108. Transfer to polymer does not necessarily lead to a decrease in the overall degree of polymerization. Each act of transfer produces a branched polymer molecule of
larger size than initially present in addition to prematurely terminating a propagating polymer chain.

The evaluation of \( C_P \) involves the difficult determination of the number of branches produced in a polymerization relative to the number of monomer molecules polymerized. This can be done by polymerizing a monomer in the presence of a known concentration of polymer of known molecular weight. The product of such an experiment consists of three different types of molecules:

*Type 1.* Unbranched molecules of the initial polymer.
*Type 2.* Unbranched molecules produced by polymerization of the monomer.
*Type 3.* Branched molecules arising from transfer of type 2 radicals to type 1 molecules.

The number of new polymer molecules produced in the system yields the number of type 2 molecules. The total number of branches is obtained by performing a mass balance on the system and assuming the size of a branch is the same as a type 2 molecule. This experimental analysis is inherently difficult and is additionally complicated if chain transfer to initiator, monomer, or some other species is occurring simultaneously. Other methods of determining the polymer transfer constant have also been employed but are usually not without ambiguity. Thus, for example, \( C_P \) for poly(vinyl acetate) has been determined by degradative hydrolysis [Lindeman, 1967]. This method assumes that transfer occurs at the acetoxy methyl group leading to polymer branches

\[
\sim CH_2 - CH \sim \quad O
\]
\[
\sim C=O
\]
\[
\sim CH_2
\]
\[
M_n \sim
\]

XXII

which can be cleaved from the original polymer molecule by ester hydrolysis of the linkage [Britton et al., 1998]. However, there is considerable evidence [Clarke et al., 1961] that the tertiary hydrogen in the polymer is abstracted easier than the acetoxy methyl hydrogen by a factor of 2–4.

Because of the experimental difficulties involved, there are relatively few reliable \( C_P \) values available in the literature. The values that are available [Eastmond, 1976a,b,c; Ham, 1967] for any one polymer often vary considerably from each other. It is often most useful to consider the small model compound analog of a polymer (e.g., ethylbenzene or isopropylbenzene for polystyrene) to gain a correct perspective of the importance of polymer chain transfer. A consideration of the best available \( C_P \) values and those of the appropriate small-model compounds indicates that the amount of transfer to polymer will not be high in most cases even at high conversion. \( C_P \) values are about \( 10^{-4} \) or slightly higher for many polymers such as polystyrene and poly(methyl methacrylate).
Flory [1947] derived the equation

$$r = -C_P \left[ 1 + \frac{(1/p)}{\ln(1/p)} \right]$$

(3-127)

to express the branching density $r$ as a function of the polymer transfer constant $C_P$ and the extent of reaction $p$. The branching density $r$ is the number of branches per monomer molecule polymerized [Fanood and George, 1988; Hutchinson, 2001]. Equation 3-127 indicates that branching increases rapidly during the later stages of a polymerization. Using a $C_P$ value of $1.0 \times 10^{-4}$, one calculates from Eq. 3-127 that there is 1.0, 1.6, and 2.2 branches for every $10^4$ monomer units polymerized at 80, 90, and 95% conversion, respectively. Experimental data verify this result quite well. For styrene polymerization at 80% conversion, there is about one branch for every $4 \times 10^3$ monomer units for polymer molecular weights of $10^4$–$10^6$. This corresponds to about 1 polymer chain in 10 containing a branch [Bevington et al., 1947].

The extent of branching is greater in polymers, such as poly(vinyl acetate), poly(vinyl chloride), and polyethylene, which have very reactive propagating radicals. Poly(vinyl acetate) has a $C_P$ value that is probably in the range $2-5 \times 10^{-4}$. Further, vinyl acetate monomer was noted earlier (Table 3-4) as having a large $C_M$ value. Transfer to monomer yields a species that initiates polymerization at its radical center and, at its double bond, enters the propagation reaction. The result is extensive branching in poly(vinyl acetate) since a branch is formed for each act of transfer to either monomer or polymer [Stein, 1964; Wolf and Burchard, 1976].

The extent of branching in polyethylene varies considerably depending on the polymerization temperature and other reaction conditions (Sec. 3-13b-1), but may reach as high as 15–30 branches per 500 monomer units. The branches in polyethylene are of two types: short branches (less than 7 carbons) and long branches. The long branches, formed by the "normal" chain transfer to polymer reaction (Eq. 3-127), affect the melt flow (viscosity) properties of the polymer and thus greatly influence its processing characteristics [Jacovic et al., 1979; Starck and Lindberg, 1979]. The short branches, which outnumber the long branches by a factor of 20–50, have a very significant effect on the polymer crystallinity. Radical-polymerized polyethylene has a maximum crystallinity of 60–70%, due to the presence of the short branches. The identity of the short branches has been established by high-resolution $^{13}$C NMR spectroscopy as well as infrared spectroscopy, and radiolytic and pyrolytic fragmentation studies [Baker et al., 1979; Bovey et al., 1976; Bowmer and O’Donnell, 1977; Hay et al., 1986; Randall, 1978; Sugimura et al., 1981; Usami and Takayama, 1984]. The presence of ethyl, $n$-butyl, $n$-amy, and $n$-hexyl branches has been clearly established. Although the relative amounts of the different branches varies considerably depending on the polymerization conditions, $n$-butyl branches are the most abundant for most polyethylenes [Axelson et al., 1979]. Most polyethylenes contain 5–15 $n$-butyl branches and 1–2 each of ethyl, $n$-amy, and $n$-hexyl branches per 1000 carbon atoms. Some polyethylenes possess more ethyl than $n$-butyl branches. Small amounts of methyl, $n$-propyl, and other branches have been detected in some studies.

The generally accepted mechanism for the formation of short branching in polyethylene involves a backbiting intramolecular transfer reaction in which the propagating radical XXIII abstracts hydrogens from the fifth, sixth, and seventh methylene groups from the radical end (Eqs. 3-128a,b,c). The resulting radicals XXIVa,b,c propagate with monomer to form $n$-hexyl, $n$-amy, and $n$-butyl branches, respectively. The general predominance of $n$-butyl
branches is ascribed to the fact that it is formed through a 6-membered transition state (consisting of the five carbons and the hydrogen being abstracted). Ethyl branches arise from radical XXIVc undergoing a second intramolecular transfer reaction after the addition of one ethylene molecule prior to further propagation, leading to 1,3-diethyl (Eq. 3-130a) and 2-ethylhexyl branches (Eq. 3-130b).

Short branching has also been verified in poly(vinyl acetate), poly(vinyl chloride), and various polyacrylates. Branching in poly(vinyl acetate) and polyacrylates involve the intramolecular backbiting mechanism as in polyethylene [Adelman and Ferguson, 1975; Heatley...
et al., 2001; Morishima and Nozakura, 1976; Nozakura et al., 1976]. Short branching in poly(vinyl chloride) is a more complex process [Hjerto berg and Sorvik, 1983; Starnes, 1985; Starnes et al., 1983, 1992, 1995]. 2-chloroethyl and 2,4-dichloro-n-butyl branches are formed via the backbites, with the latter more abundant (~1 per 1000 monomer units) than the former. However, the most abundant branches are chloromethyl groups—up to 4–6 per 1000 monomer units. Chloromethyl groups occur when radical $XIX$ (formed via Eq. 3-114) undergoes propagation:

$$\text{CH}_2\text{CHCl} \cdot + \text{CH}_2=\text{CHCl} \rightarrow \text{CH}_2\text{ClCHCH}_2\text{CH}_2\text{Cl} \quad (3-131)$$

$XIX$

Long branches in PVC, up to about one branch per 2000 monomer units, arise from hydrogen abstraction at the CHCl group in the polymer chain.

### 3-6e Catalytic Chain Transfer

Certain cobalt(II) complexes such as the cobaloxime $XXVIIa$ and the corresponding boron fluoride $XXVIIb$ (L is a ligand) terminate propagating chains by a transfer reaction called 

catalytic chain transfer (CCT) [Chiefari and Rizzardo, 2002; Gridnev, 2000; Gridnev and Ittel, 2001; Heuts et al., 2002; Roberts et al., 2003]. The overall result is the transfer of an H atom from a propagating chain to monomer, but the process occurs by a two-step mechanism (Eqs. 3-132, 3-133) in which Co(II) acts as a catalyst. In the first step, an H atom is transferred from the propagating chain to Co(II) to form Co(III) hydride, which subsequently transfers the H atom to monomer to reinitiate polymerization. Note that catalytic chain transfer differs from chain transfer to monomer (Sec. 3-6b-2). Chain transfer to monomer results
in a polymer molecule with a saturated end group by transfer of an H or other atom from monomer to propagating chain. Catalytic chain transfer involves transfer of an H atom in the opposite direction (from propagating chain to monomer) and results in a polymer molecule with an unsaturated end group. The reaction is catalytic because the transfer agent is regenerated in the second step.

Various cobaloximes and cobaloxime boron fluorides have been examined. R can be alkyl or aryl. Various ligands have been used, including Cl, P\(_\text{3}\), methanol, and pyridine, and combinations thereof. Cobalt prophyrins have also been found to be effective CCT agents. Active CCT agents based on metals other than cobalt have not yet been found. Catalytic chain-transfer agents are much more active in chain transfer than the most active conventional chain-transfer agents discussed previously. Thiols have the highest chain-transfer constants for conventional transfer agents, as high as 10\(^{-20}\) (see 1-butanethiol in Table 3-6). Catalytic chain-transfer constants (\(C_C\)) are even higher, in the range 10\(^{2}\)–10\(^{4}\). For example, \(C_C\) is 3.2 \(\times\) 10\(^{4}\) for CCT agent XXVIIb (with \(R = \text{CH}_3\), \(L = \text{isopropyl, pyridine}\)) in the polymerization of methyl methacrylate at 60°C [Kowollik and Davis, 2000].

For the polymerization of a monomer such as methyl methacrylate, two types of unsaturated end groups are possible—the vinylidene end group shown in Eq. 3-132 (H atom transfer from \(\text{CH}_3\)) and trisubstituted double-bond end groups (via an H atom abstraction from \(\text{CH}_2\)). The more substituted trisubstituted double bond might be expected to predominate since it is the more stable double bond, but the opposite is observed. This is probably due to the steric bulk of the cobalt catalyst, with abstraction of an H atom occurring more easily at the less substituted, more accessible \(\text{CH}_3\) group compared to the more substituted, less accessible \(\text{CH}_2\) group. (This result is analogous to what is observed in dehydrohalogenations of alkyl halides—bulky bases yield the less substituted, less stable double bond, whereas nonbulky bases yield the more substituted, more stable double bond.)

CCT agents offer two advantages over conventional transfer agents: (1) low-molecular-weight polymers can be produced without having to use large amounts of conventional chain-transfer agents or high initiator : monomer ratios or high temperatures (which generally increase transfer compared to propagation); and (2) polymers with unsaturated end groups are produced. Both of these advantages are important in certain applications, such as coatings. High solid levels are advantageous in coating formulations, but this results in high viscosity when higher polymer molecular weights are used. The high viscosity, a major limitation in the fast application of uniform coatings, is overcome by using low-molecular-weight polymers as long as the polymers can undergo polymerization to higher molecular weight during the coating process. Thus, one needs low-molecular-weight polymers with unsaturated end groups, and this is obtained by using CCT agents. Polymers with end groups capable of polymerization (and/or crosslinking) are called *macromonomers*. Macromonomers are under study for other uses, including graft and hyperbranched polymers and other polymers with unique structures [Gridnev, 2000; Gridnev and Ittel, 2001].

### 3-7 INHIBITION AND RETARDATION

The addition of certain substances suppresses the polymerization of monomers. These substances act by reacting with the initiating and propagating radicals and converting them to either nonradical species or radicals of reactivity too low to undergo propagation. Such polymerization suppressors are classified according to their effectiveness. *Inhibitors* stop every radical, and polymerization is completely halted until they are consumed. *Retarders* are less efficient and stop only a portion of the radicals. In this case, polymerization occurs,
but at a slower rate and lower polymer molecular weight. The difference between inhibitors and retarders is simply one of degree and not kind. Figure 3-9 shows these effects in the thermal polymerization of styrene [Schulz, 1947]. Polymerization is completely stopped by benzoquinone, a typical inhibitor, during an induction or inhibition period (plot 2). At the end of this period, when the benzoquinone has been consumed, polymerization proceeds at the same rate as in the absence of inhibitor (plot 1). Nitrobenzene, a retarder, lowers the polymerization rate without an inhibition period (plot 3). The behavior of nitrosobenzene, \( \phi \text{NO} \), is more complex (plot 4). It is initially an inhibitor but is apparently converted to a product that acts as a retarder after the inhibition period. This latter behavior is not at all uncommon. Inhibition and retardation are usually the cause of the irreproducible polymerization rates observed with insufficiently purified monomers. Impurities present in the monomer may act as inhibitors or retarders. On the other hand, inhibitors are invariably added to commercial monomers to prevent premature thermal polymerization during storage and shipment. These inhibitors are usually removed prior to polymerization or, alternatively, an appropriate excess of initiator may be used to compensate for their presence.

### 3-7a Kinetics of Inhibition or Retardation

The kinetics of retarded or inhibited polymerization can be analyzed using a scheme consisting of the usual initiation (Eq. 3-14), propagation (Eq. 3-15), and termination (Eq. 3-16) reactions in addition to the inhibition reaction

\[
M_n^\cdot + Z \xrightarrow{k_i} M_n + Z^\cdot \quad \text{and/or} \quad M_nZ^\cdot
\]  

(3-134)

where \( Z \) is the inhibitor or retarder. \( Z \) acts either by adding to the propagating radical to form \( M_nZ^\cdot \) or by chain transfer of hydrogen or other radical to yield \( Z^\cdot \) and polymer. The kinetics are simplified if one assumes that \( Z^\cdot \) and \( M_nZ^\cdot \) do not reinitiate polymerization and also that they terminate without regeneration of \( Z \).

The steady-state assumption for the radical concentration leads to

\[
\frac{d[M^\cdot]}{dt} = R_i - 2k_i[M]^2 - k_i[Z][M^\cdot] = 0
\]  

(3-135)
which can be combined with Eq. 3-22 to yield

\[
\frac{2R_p^2k_i}{k_p^2[M]^2} + \frac{R_p[Z]k_z}{k_p[M]} - R_i = 0
\]  

(3-136)

Equation 3-136 has been used to correlate rate data in inhibited polymerizations. A consideration of Eq. 3-136 shows that \(R_p\) is inversely proportional to the ratio \(k_z/k_p\) of the rate constants for inhibition and propagation. This ratio is often referred to as the inhibition constant \(z\):

\[
z = \frac{k_z}{k_p}
\]  

(3-137)

It is further seen that \(R_p\) depends on \(R_i\) to a power between one-half and unity depending on the relative magnitudes of the first two terms in Eq. 3-136. Two limiting cases of Eq. 3-136 exist. When the second term is negligible compared to the first, the polymerization is not retarded, and Eq. 3-136 simplifies to Eq. 3-25.

For the case where retardation is strong (\(k_z/k_p \gg 1\)), normal bimolecular termination is negligible. Under these conditions the first term in Eq. 3-136 is negligible and one has

\[
\frac{R_p[Z]k_z}{k_p[M]} - R_i = 0
\]  

(3-138a)

or

\[
R_p = \frac{k_p[M]R_i}{k_z[Z]} = -\frac{d[M]}{dt}
\]  

(3-138b)

Equation 3-138 shows the rate of inhibited polymerization to be dependent on the first power of the initiation rate. Further, \(R_p\) is inversely dependent on the inhibitor concentration. The induction period observed for inhibited polymerization is directly proportional to the inhibitor concentration.

The inhibitor concentration will decrease with time and \([Z]\) at any time is given by

\[
[Z] = [Z]_0 - \frac{R_i t}{y}
\]  

(3-139)

where \([Z]_0\) is the initial concentration of \(Z\), \(t\) is time, and \(y\) is the number of radicals terminated per inhibitor molecule. Combination of Eqs. 3-137, 3-138b, and 3-139 yields

\[
-\frac{d[M]}{dt} = \frac{R_i[M]}{z([Z]_0 - R_i t/y)}
\]  

(3-140a)

or, by rearrangement:

\[
\frac{-1}{d\ln[M]/dt} = \frac{z}{R_i} \frac{[Z]_0 - \frac{zt}{y}}{y}
\]  

(3-140b)

A plot of the left side of Eq. 3-140b versus time is linear, and the values of \(z\) and \(y\) can be obtained from the intercept and slope, respectively, if \([Z]_0\) and \(R_i\) are known. The method
involves difficult experimentation, since the polymerization rates being measured are quite small, especially if $z$ is large. Figure 3-10 shows Eq. 3-140b plotted for vinyl acetate polymerization inhibited by 2,3,5,6-tetramethylbenzoquinone (duroquinone) [Bartlett and Kwart, 1950]. Table 3-8 shows selected $z$ values for various systems.

A careful consideration of Eq. 3-140b shows that for a strong retarder ($z \gg 1$), the polymerization rate will be negligible until the inhibitor concentration is markedly reduced. When the inhibitor concentration becomes sufficiently low, propagation can become competitive with the inhibition reaction. This is more readily seen by considering the equation

$$
\frac{d[Z]}{d[M]} = \frac{z[Z]}{[M]}
$$

obtained by dividing the rate expression for the disappearance of inhibitor (Eq. 3-134) by that for monomer disappearance (Eq. 3-16). Integration of Eq. 3-141 yields

$$
\log \left( \frac{[Z]}{Z_0} \right) = z \log \left( \frac{[M]}{[M]_0} \right)
$$

(3-142)

where $[Z]_0$ and $[M]_0$ are initial concentrations. It is apparent from this expression that the inhibitor must be almost completely consumed before the monomer can be polymerized. Equation 3-142 can also be used to determine the inhibition constant from the slope of a plot of log $[Z]$ versus log $[M]$. 

Fig. 3-10  Inhibition of the benzoyl peroxide–initiated polymerization of vinyl acetate by duroquinone at $45^\circ$C. The three lines are for different concentrations of duroquinone. After Bartlett and Kwart [1950] (by permission of American Chemical Society, Washington, DC).
Because of the experimental difficulty involved in determining $z$ values, many workers take an alternate and experimentally simpler approach to expressing the effect of inhibitors and retarders on polymerization. They treat these compounds as chain-transfer agents and calculate chain-transfer constants from measurements of polymer molecular weights as described in Sec. 3-6 [Valdebenito et al., 2001]. Table 3-9 shows such pseudo-chain-transfer constants for various inhibitors and retarders. In fact, some $z$ values reported in the literature are actually $C_S$ values, and it is not always easy to tell what is reported in handbooks or papers. Keep in mind that chain-transfer agents and inhibitors/retarders are different. True chain-transfer agents lower polymer molecular weights but do not affect polymerization rates. Retarders and inhibitors lower polymerization rates and polymer molecular weights. Nevertheless, $C_S$ values for retarders and inhibitors give useful practical information.

3-7b Types of Inhibitors and Retarders

As with chain-transfer agents, one observes that the inhibition constant for any particular compound varies considerably depending on the reactivity and polarity of the propagating...
stable free radicals that are too stable to initiate polymerization but that can still react with radicals are one type of radical terminator. DPPH is such a radical and its use as a radical scavenger has been discussed (Sec. 3-4g-3). The stoichiometry between the number of kinetic chains terminated, and the number of DPPH radicals consumed is 1:1.

The most useful class of inhibitors are molecules that react with chain radicals to yield radicals of low reactivity. Quinones such as benzoquinone and chloranil (2,3,5,6-tetrachlorobenzoquinone) are an important class of inhibitor. The behavior of quinones is quite complex [Eastmond, 1976a,b,c; George, 1967; Small, 1975; Yamamoto and Sugimoto, 1979; Yassin and Risk, 1978a, 1978b]. Two major types of products are obtained—quinone and ether—formed by reaction at the C and O atoms of a quinone, respectively. Attack of a propagating radical at oxygen yields the aryloxy radical XXVIII, which can terminate by coupling and/or disproportionation with another propagating radical (or itself) or add monomer. Attack on the ring carbon yields radical XXIX, which can react with another

\[
M_n\cdot + \text{O}=\text{O} \rightarrow M_n-\text{O}-\text{O}\cdot \quad (3-143)
\]

**TABLE 3-9 Retarder/Inhibitor Chain-Transfer Constants\textsuperscript{a,b}**

<table>
<thead>
<tr>
<th>Monomer</th>
<th>Compound</th>
<th>(C_z \times 10^4)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Acrylonitrile</td>
<td>Aniline</td>
<td>44</td>
</tr>
<tr>
<td></td>
<td>(p)-Benzoquinone</td>
<td>(1.3 \times 10^4)</td>
</tr>
<tr>
<td>Methyl methacrylate</td>
<td>Aniline (60°C)</td>
<td>4.2</td>
</tr>
<tr>
<td></td>
<td>(p)-Benzoquinone</td>
<td>(4.5 \times 10^4)</td>
</tr>
<tr>
<td></td>
<td>Hydroquinone (45°C)</td>
<td>7.0</td>
</tr>
<tr>
<td></td>
<td>Phenol</td>
<td>2.5</td>
</tr>
<tr>
<td></td>
<td>Pyrogallol (45°C)</td>
<td>26</td>
</tr>
<tr>
<td></td>
<td>4-(t)-Butyl catechol (45°C)</td>
<td>45</td>
</tr>
<tr>
<td>Styrene</td>
<td>Aniline</td>
<td>20</td>
</tr>
<tr>
<td></td>
<td>(p)-Benzoquinone (60°C)</td>
<td>(23 \times 10^5)</td>
</tr>
<tr>
<td></td>
<td>Hydroquinone (60°C)</td>
<td>3.6</td>
</tr>
<tr>
<td></td>
<td>Phenol (60°C)</td>
<td>14</td>
</tr>
<tr>
<td></td>
<td>2,4,6-Trinitrophenol</td>
<td>(2.1 \times 10^5)</td>
</tr>
<tr>
<td></td>
<td>Pyrogallol (60°C)</td>
<td>370</td>
</tr>
<tr>
<td></td>
<td>4-(t)-Butyl catechol (60°C)</td>
<td>(36 \times 10^2)</td>
</tr>
<tr>
<td>Vinyl acetate</td>
<td>Aniline</td>
<td>149</td>
</tr>
<tr>
<td></td>
<td>Hydroquinone</td>
<td>(70 \times 10^2)</td>
</tr>
<tr>
<td></td>
<td>Phenol (45°C)</td>
<td>120</td>
</tr>
<tr>
<td></td>
<td>(p)-Nitrophenol</td>
<td>(8.9 \times 10^4)</td>
</tr>
<tr>
<td></td>
<td>Pyrogallol</td>
<td>(50 \times 10^3)</td>
</tr>
<tr>
<td></td>
<td>4-(t)-Butyl catechol (60°C)</td>
<td>(36 \times 10^2)</td>
</tr>
</tbody>
</table>

\textsuperscript{a} Data from Brandrup et al. [1999].

\textsuperscript{b} All data are for 50°C except where otherwise noted.
propagating radical (Eq. 3-144) to form the quinone \( \text{XXX} \). The latter may itself be an inhibitor. An alternate route for radical \( \text{XXIX} \) is rearrangement to \( \text{XXXI} \) followed by coupling or termination with other radicals. The overall stoichiometry (i.e., the value of \( y \) in Eqs. 3-139 and 3-140) between the number of kinetic chains terminated and the number of the original quinone molecules consumed varies considerably depending on the particular quinone and radical. Although \( y \) often is 1, both pathways (Eqs. 3-143 and 3-144/3-145) can yield \( y \) values larger than 1 (up to 2) depending on the reactivities of \( \text{XXVIII} \) and \( \text{XXX} \).

Polar effects appear to be of prime importance in determining the effect of quinones. \( p \)-Benzoquinone and chloranil (which are electron-poor) act as inhibitors toward electron-rich propagating radicals (vinyl acetate and styrene) but only as retarders toward the electron-poor acrylonitrile and methyl methacrylate propagating radicals. A further observation is that the inhibiting ability of a quinone toward electron-poor monomers can be increased by the addition of an electron-rich third component such as an amine. Thus the presence of triethylamine converts chloranil from a very weak retarder to an inhibitor toward methyl methacrylate.

Oxygen is a powerful inhibitor, as seen from the very large \( z \) values. Oxygen reacts with radicals to form the relatively unreactive peroxy radical that reacts with itself or another propagating radical by coupling and disproportionation reactions to form inactive products (probably peroxides and hydroperoxides) [George and Ghosh, 1978; Kishore and Bhanu, 1988; Koenig and Fischer, 1973; Maybod and George, 1977]. Peroxy radicals can also slowly add monomer to yield an alternating copolymer [Kishore et al., 1981]. The action of oxygen is anomalous in that it is known to initiate some polymerizations. Some commercial processes for ethylene polymerization involve initiation by oxygen [Tatsukami et al., 1980]. Initiation probably occurs by thermal decomposition of the peroxides and hydroperoxides formed from the monomer (or from impurities present in the system). Whether oxygen is an inhibitor or, more rarely, an initiator will be highly temperature-dependent. Initiation will occur at higher temperatures where the peroxides and hydroperoxides are unstable.

Contrary to the general impression, phenol and aniline are poor retarders even toward highly reactive radicals such as the poly(vinyl acetate)-propagating radical (Table 3-8). Phenols with electron-donating groups (and, to some extent, similarly substituted anilines)
act as more powerful retarders; for example, \( z \) is 5.0 for 2,4,6-trimethylphenol compared to 0.012 for phenol toward vinyl acetate polymerization. The presence of an electron-withdrawing group on the phenol ring decreases its activity as an inhibitor. Most phenols are active, or much more active, only in the presence of oxygen [Kurland, 1980; Levy, 1985; Prabha and Nandi, 1977; Zahalka et al., 1988]. The mechanism for inhibition by phenols has been attributed to hydrogen transfer to the propagating radical (Eq. 3-147), but this does not explain the synergistic effect of oxygen. The inhibiting effect of phenols in the presence of oxygen is probably a consequence of the transfer reaction (Eq. 3-148) being faster than the reaction in Eq. 3-146; that is, phenols scavenge peroxo radicals more effectively than do alkyl (carbon) radicals. Most phenols have \( y \) values close to 3, indicating that the peroxo radical formed in Eq. 3-148 reacts with propagating radicals (carbon and/or peroxo). This probably involves

\[
M_n\cdot + ArOH \rightarrow M_nH + ArO\cdot
\]  
(3-147)

the propagating radical adding to the ring or abstracting hydrogen from a methyl group on the ring for methyl-substituted phenols. In contrast to phenol and substituted phenols, di- and trihydroxybenzenes such as hydroquinone, \( t \)-butylcatechol (1,2-dihydroxy-4-\( t \)-butylbenzene), and pyrogallol (1,2,3-trihydroxybenzene) are generally stronger retarders or inhibitors. The mechanism for their action may involve oxidation by adventitious oxygen to quinones instead of or in addition to the reactions described by Eqs. 3-147 and 3-148 [Georgieff, 1965].

Substituted anilines behave similarly to the phenols, although relatively little data are available. \( N \)-phenyl-\( N' \)-isopropyl-\( p \)-phenylenediamine is an efficient inhibitor in the polymerization of styrene only in the presence of oxygen [Winkler and Nauman, 1988]. However, the effectiveness of phenothiazine as an inhibitor in the polymerization of acrylic acid is independent of oxygen [Levy, 1985].

Aromatic nitro compounds terminate propagating chains, with a greater effect for more reactive and electron-rich radicals. Nitro compounds inhibit vinyl acetate, retard styrene, but have little effect on methyl acrylate and methyl methacrylate [Eastmond, 1976a,b,c; Schulz, 1947; Tabata et al., 1964]. The effectiveness increases with the number of nitro groups on the ring. 1,3,5-Trinitrobenzene has \( z \) values that are 1–2 orders of magnitude greater than nitrobenzene (Table 3-8). The mechanism of radical termination involves attack on both the aromatic ring and the nitro group. Attack on the aromatic ring yields radical XXXII, which reacts with another propagating radical (Eq. 3-149) or with monomer (Eq. 3-150).

\[
\begin{align*}
\text{XXXII} & \quad \text{M}_{n}\cdot + \text{M} \rightarrow \text{M}_{n}-\text{H} + \text{HM}\cdot
\end{align*}
\]  
(3-150)
Attack on the nitro group leads to radical XXXIII, which can react with other propagating radicals (Eqs. 3-151 and 3-152) or cleave to nitrosobenzene and $M_n-O$ radical (Eq. 3-153). Both nitrosobenzene and $M_n-O$ can react with and terminate other propagating radicals.

$$\begin{align*}
\phi-\text{NO}_2 & \xrightarrow{M_n} \phi-N\text{OM}_n \xrightarrow{M_n^*} \phi-N=O + M_n-O-M_n \\
\text{XXXIII} & \\
M_n-\hat{O} & + \phi-\text{NO} \\
& \text{(3-153)}
\end{align*}$$

The reaction in Eq. 3-152 probably also involves disproportionation—hydrogen atom transfer from the propagating radical to XXXII. Overall, one observes high y values—up to 5 or 6 for 1,3,5-trinitrobenzene.

Oxidants such as FeCl$_3$ and CuCl$_2$ are strong inhibitors, terminating radicals by the reactions [Billingham et al., 1980; Chetia and Dass, 1976; Matsuo et al., 1977]:

$$\begin{align*}
\text{CH}_2\text{CH} & + \text{FeCl}_3 \\
\sim\text{CH}_2\text{CH}\phi & + \text{FeCl}_2 \\
\sim\text{CH} & + \text{HCl} + \text{FeCl}_2 \\
& \text{(3-154a)} \\
\sim\text{CH}_2\text{CHCl}\phi & + \text{FeCl}_2 \\
& \text{(3-154b)}
\end{align*}$$

Reductants also terminate propagating radicals, but much less effectively.

Other inhibitors include sulfur, carbon, aromatic azo compounds, and chlorophosphines [Nigenda et al., 1977; Uemura et al., 1977].

### 3-7c Autoinhibition of Allylic Monomers

An especially interesting case of inhibition is the internal or autoinhibition of allylic monomers ($\text{CH}_2=\text{CH}-\text{CH}_2\text{Y}$). Allylic monomers such as allyl acetate polymerize at abnormally low rates with the unexpected dependence of the rate on the first power of the initiator concentration. Further, the degree of polymerization, which is independent of the polymerization rate, is very low—only 14 for allyl acetate. These effects are the consequence of degradative chain transfer (case 4 in Table 3-3). The propagating radical in such a polymerization is very reactive, while the allylic C–H (the C–H bond alpha to the double bond) in the monomer is quite weak—resulting in facile chain transfer to monomer.

$$\begin{align*}
\sim\text{CH}_2\text{C} & + \text{CH}_2=\text{CH}\text{CY} \\
\text{H} & \text{H} \\
\sim\text{CH}_2=\text{CH}_2 & + \text{CH}_2=\text{CH}\sim\text{CY} \\
\text{H} & \text{H} \\
\sim\text{CH}_2 & + \text{CH} & \text{CY} \\
\text{H} & \text{H} \\
\sim\text{CH}_2=\text{CH} & \text{CY} \\
\text{H} & \text{H} \\
\sim\text{CH}_2 & + \text{CH} & \text{CY} \\
\text{H} & \text{H} \\
\text{XXXIV}
\end{align*}$$

(3-155)
The weakness of the allylic C–H bond arises from the high resonance stability of the allylic radical (XXXIV) that is formed. Degradative chain transfer competes exceptionally well with normal propagation, and the polymer chains are terminated by transfer after the addition of only a very few monomer units. That the allylic C–H bond is the one broken in the transfer reaction has been shown [Bartlett and Tate, 1953] by experiments with CH₂=CH–CD₂OCOCH₃. The deuterated allyl acetate polymerizes 1.9–2.9 times as fast as normal allyl acetate and has a degree of polymerization 2.4 times as large under the same conditions. This is what would be expected since the C–D bond is stronger than the C–H bond because of its lower zero-point energy and degradative chain transfer would therefore be decreased in the deuterated monomer.

The allylic radicals that are formed are too stable to initiate polymerization, and the kinetic chain also terminates when the transfer occurs. The allylic radicals undergo termination by reaction with each other or, more likely, with propagating radicals [Litt and Eirich, 1960]. Reaction 3-155 is equivalent to termination by an inhibitor, which is the monomer itself in this case. In this polymerization the propagation and termination reactions will have the same general kinetic expression with first-order dependencies on initiator and monomer concentrations, since the same reactants and stoichiometry are involved. The degree of polymerization is simply the ratio of the rate constants for propagation and termination and is independent of the initiator concentration.

The low reactivity of α-olefins such as propylene or of 1,1-dialkyl olefins such as isobutylene toward radical polymerization is probably a consequence of degradative chain transfer with the allylic hydrogens. It should be pointed out, however, that other monomers such as methyl methacrylate and methacrylonitrile, which also contain allylic C–H bonds, do not undergo extensive degradative chain transfer. This is due to the lowered reactivity of the propagating radicals in these monomers. The ester and nitrile substituents stabilize the radicals and decrease their reactivity toward transfer. Simultaneously the reactivity of the monomer toward propagation is enhanced. These monomers, unlike the α-olefins and 1,1-dialkyl olefins, yield high polymers in radical polymerizations.

3-8 DETERMINATION OF ABSOLUTE RATE CONSTANTS

3-8a Non-Steady-State Kinetics

Five different types of rate constants are of concern in radical chain polymerization—those for initiation, propagation, termination, chain transfer, and inhibition. The use of polymerization data under steady-state conditions allows the evaluation of only the initiation rate constant \( k_i \) (or \( k_t \) for thermal initiation). The ratio \( k_p/k_i^{1/2} \) or \( k_p^2/k_i \) can be obtained from Eq. 3-25, since \( R_p, R_i \), and [M] are measurable. Similarly, the chain-transfer constant \( k_{tr}/k_p \) and the inhibition constant \( k_z/k_p \) can be obtained by any one of several methods discussed. However, the evaluation of the individual \( k_p, k_i, k_{tr}, \) and \( k_z \) values under steady-state conditions requires the accurate determination of the propagating radical concentration. This would allow the determination of \( k_p \) from Eq. 3-22 followed by the calculation of \( k_i, k_{tr} \), and \( k_z \) from the ratios \( k_p/k_i^{1/2}, k_{tr}/k_p, \) and \( k_z/k_p \).

Measurements of \( k_p \) were performed by the rotating sector method and its variations until the late 1980s [Flory, 1953; Odian, 1991; Walling, 1957]. In the late 1980s advances in pulsed laser technology and size exclusion chromatography resulted in the development of a technique called pulsed laser polymerization–size exclusion chromatography (PLP-SEC) [Beuermann and Buback, 2002; Beuermann et al., 1997, 2000; Buback et al., 1986, 1992,
Both the rotating sector and PLP-SEC methods are considered below. Both methods involve polymerizations under non-steady-state conditions. Most of the rate constants available in the literature were obtained using the rotating sector method, although the method is no longer in general use. The rotating sector method uses polymerization rates to obtain $k_p$, whereas the PLP-SEC method uses polymer molecular weights.

### 3-8b Rotating Sector Method

The rotating sector method requires the introduction of the parameter $\tau_s$, defined as the average lifetime of a growing radical under steady-state conditions. The radical lifetime is given by the steady-state radical concentration divided by its steady-state rate of disappearance:

$$\tau_s = \frac{[M_i]}{2k_t[M]^2} = \frac{1}{2k_t[M]^2}$$  (3-156)

Combination of Eqs. 3-156 and 3-22 at steady state yields

$$\tau_s = \frac{k_p[M]}{2k_t(R_p)_s}$$  (3-157)

The ratio $k_p/k_t$ can be obtained from Eq. 3-157 from $\tau_s$ and the rate of polymerization under steady-state conditions. (The subscript $s$ in Eq. 3-157 and subsequent equations in this section refers to steady-state values; the absence of $s$ denotes non-steady-state values.) The individual rate constants $k_p$ and $k_t$ can be determined by combining $k_p/k_t$ with $k_p/k_t^{1/2}$ obtained from Eq. 3-25. Thus, the objective of the rotating sector method is the measurement of $\tau_s$.

The most recent versions of the rotating sector method use a pulsed laser as the light source for a photopolymerization involving the alternating of light and dark periods. The original rotating sector experiment used a nonlaser light source, and the equivalent of pulsing was achieved by rotating a sector or disk in between the polymerization system and the light source [Nagy et al., 1983]. Pulsing was achieved by cutting a portion out of the sector.

The rotating sector method requires a study of the polymerization rate as a function of the ratio $r$ of the length $t'$ of the dark period to the length $t$ of the light period. The cycle time is the sum of $t'$ and $t$. These parameters are varied experimentally by varying the laser pulse width and/or frequency. Two situations occur depending on the cycle time in relation to $\tau_s$. If the cycle time is very long compared to $\tau_s$ (slow on–off), the observed $R_p$ will be equal to $(R_p)_s$ during the entire light period and zero during the entire dark period. The reason for this is that the times for the radical concentration to reach steady-state or to decay to zero are small compared to times $t$ and $t'$, respectively. The ratio of the average polymerization rate $\bar{R}_p$ over one complete cycle to the steady-state rate is given by

$$\frac{\bar{R}_p}{(R_p)_s} = \frac{1}{1 + r}$$  (3-158)

since the fraction of time that the system is illuminated is $1/(1 + r)$.

If the cycle time is reduced (fast on–off), radical decay during the dark period is incomplete and the steady-state concentration is not reached during the light period. The polymerization rate averaged over a cycle will be greater than $(R_p)_s/(1 + r)$ because the radical decay during a dark period is less than the buildup during a light period. A very fast cycle
time maintains the radical concentration at approximately a constant value and is equivalent to polymerization under constant illumination at an intensity $1/(1 + r)$ times that actually used [Flory, 1953; Walling, 1957]. The ratio of the average polymerization rate $(R_p)_\infty$ at very short cycle time to the steady-state rate is given by

$$\frac{(R_p)_\infty}{(R_p)_s} = \frac{1}{(1 + r)^{1/2}}$$

(3-159)

Thus, the average polymerization rate increases by a factor of $(1 + r)^{1/2}$ as the cycle (pulse) frequency increases from a low value to a very high value compared with $1/\tau_s$.

The mathematical treatment of pulsing illumination has been described [Briers et al., 1926]. After a number of cycles, the radical concentration oscillates uniformly with a constant radical concentration $[M^*]_1$ at the end of each light period of duration $t$ and a constant radical concentration $[M^*]_2$ at the end of each dark period of duration $t' = rt$. The two radical concentrations are related by

$$\tanh^{-1}\left(\frac{[M^*]_1}{[M^*]_2}\right) - \tanh^{-1}\left(\frac{[M^*]_2}{[M^*]_1}\right) = \frac{t}{\tau_s}$$

(3-160)

and

$$\frac{[M^*]_1}{[M^*]_2} = \frac{rt}{\tau_s}$$

(3-161)

The maximum and minimum values of the ratios $[M^*]_1/[M^*]_s$ and $[M^*]_2/[M^*]_s$ can be calculated from Eqs. 3-160 and 3-161 for given values of $r$ and $t/\tau_s$. The average radical concentration $[M^*]$ over a cycle or several cycles is given by

$$[M^*](t + rt) = \int_0^t [M^*] dt + \int_0^t [M^*] d'$$

(3-162)

where the first integral (for the light period) is given by Eq. 3-160 and the second integral (for the dark period) is given by Eq. 3-161. Evaluation of the integrals in Eq. 3-162 yields

$$\frac{[M^*]}{[M^*]_s} = (r + 1)^{-1}\left[1 + \frac{\tau_s}{t} \ln\left(\frac{[M^*]_1/[M^*]_2 + [M^*]_3/[M^*]_s}{1 + [M^*]_1/[M^*]_s}\right)\right]$$

(3-163)

Using Eq. 3-163 with Eqs. 3-160 and 3-161, one can calculate the ratio $[M^*]/[M^*]_s$ as a function of $t/\tau_s$ for a fixed value of $r$. A semilog plot of such data for $r = 3$ is shown in Fig. 3-11.

To obtain $\tau_s$, the steady-state polymerization rate $(R_p)_s$ is first measured at constant illumination (no pulsing). Then the average rate $\bar{R}_p$ is measured as a function of $r$ and $t$. The data are plotted as the rate ratio $\bar{R}_p/(R_p)_s$ versus $\log t$. Alternately, one can plot the data as the rate ratio $\bar{R}_p/(R_p)_\infty$ since this ratio is related to $\bar{R}_p/(R_p)_s$ through Eq. 3-159. The theoretical plot (e.g., Fig. 3-11) for the same $r$ value is placed on top of the experimental plot and shifted on the abscissa ($\alpha$ axis) until a best fit is obtained. The displacement on the abscissa of one plot from the other yields $\log \tau_s$ since the abscissa for the theoretical plot is $\log t - \log \tau_s$.

The experimental determination of $\tau_s$ allows the calculation of $k_p, k_r$, and $k_c, k_p/k_t$ and $k_p/k_t^{1/2}$, obtained from Eqs. 3-157 and 3-25 (non-steady-state and steady-state experiments, respectively), are combined to yield the individual rate constants $k_p$ and $k_t$. Quantities such as
Rt and \( \frac{[M]}{[M]^s} \) are calculated from Eqs. 3-22 and 3-23, respectively. \( k_{tr} \) and \( k_z \) are calculated from the values of chain transfer and inhibition constants.

The measurement of \( \tau_s \) also allows an evaluation of the validity of the usual steady-state assumption in radical chain polymerization from the relationship [Flory, 1953]

\[
\frac{[M]^s}{[M]^s} = \frac{R_p}{(R_p)_s} = \tanh \left( \frac{t}{\tau_s} \right)
\]  

The time required for \( [M]^s \) and \( R_p \) to reach their steady-state values is calculated as 65, 6.5, and 0.65 s, respectively, for \( \tau_s \) values of 10, 1, and 0.1 s. Thus, in the usual polymerization the steady-state assumption is valid after a minute or so at most.

### 3-8c PLP-SEC Method

An examination of the literature, including the *Polymer Handbook* [Brandrup et al., 1999], often shows fairly wide disparities in the values of various rate constants. Much of this is due to experimental difficulties with the rotating sector method as well as the fact that different workers studied polymerizations under widely different reaction conditions. There has been a concerted effort in recent years to bring some order to the situation. A group of polymer scientists organized under the auspices of the IUPAC Working Party on “Modeling of Kinetics and Processes of Polymerization” has made good progress in this direction by standardization of the reaction conditions for measuring rate constants and the use of the PLP-SEC method. Unlike the rotating sector method, the PLP-SEC method allows the measurement of \( k_p \) directly without the need to couple it to the termination rate constant.

The PLP-SEC method, like the rotating sector method, involves a non-steady-state photopolymerization [Beuermann, 2002; Beuermann and Buback, 2002; Kornherr et al., 2003; Nikitin et al., 2002]. Under pulsed laser irradiation, primary radicals are formed in very short times (\(~10\,\text{ns}\) pulse width) compared to the cycle time (\(~1\,\text{s}\)). The laser pulse width is also very short compared to both the lifetimes of propagating radicals and the times for conversion of primary radicals to propagating radicals. The PLP-SEC method for measuring \( k_p \) requires that reaction conditions be chosen so that no significant chain transfer is present. The first laser pulse generates an almost instantaneous burst of primary radicals at high
concentration ($\sim 10^{-6}$ mol L$^{-1}$). During the dark period that follows the pulse most of the primary radicals form propagating radicals, which then propagate, but some primary radicals terminate by coupling. Normal coupling and disproportionation occur during the dark period, but a large fraction of propagating chain do not terminate because the cycle time is short. The second laser pulse again produces a burst of primary radicals. Most surviving propagating chains from the dark period between the first and second laser pulses are almost instantaneously terminated by the high concentration of primary radicals formed in the second laser pulse. But some of the propagating chains survive and continue to propagate during the second dark period. Some of the primary radicals in the second laser pulse initiate polymerization that proceeds in the second dark period, at the same time that some propagating chains from the first dark period are propagating for a second dark period. The process continues in a similar manner with each laser burst and subsequent dark period. Sufficient laser pulses are used so that the amount of polymer produced is sufficient for analysis by size exclusion chromatography. The amount of conversion is only about 2–3%, which means that the monomer concentration is essentially constant over the course of the experiment.

Some propagating chains terminate by normal coupling and/or disproportionation during the dark periods, but most do not. Most of the polymer produced consists of propagating chains that have propagated for different multiples of the time of a dark period $t_p$. $t_p$ is essentially the same as the cycle time because the pulse width is so much shorter than $t_p$. Chains propagate for $1t_p$, $2t_p$, $3t_p$, and so on. The degree of polymerization for chains terminated by primary radicals is given by

$$L_i = ik_p[M]t_p$$  \hspace{1cm} (3-165)

where $L_i$ is the degree of polymerization for chains that have propagated through $i$ cycles. $L_i$ is obtained from the SEC measurement of the polymer molecular weight distribution. Figure 3-12 shows a plot of the molecular weight distribution for a polymerization of dodecyl acrylate polymerization at $-4^\circ$C and 200 bar in 36 wt% CO$_2$. $w$ is the weight fraction of polymer having molecular weight $M$. After Beuermann and Buback [2002] by permission of Elsevier, Oxford; an original plot, from which this figure was drawn, was kindly supplied by Dr. S. Beuermann.

![Fig. 3-12 Plots of $w(\log M)$ (solid plot) and $dw(\log M)/d\log M$ (dotted plot) versus $\log M$ for dodecyl acrylate polymerization at $-4^\circ$C and 200 bar in 36 wt% CO$_2$. $w$ is the weight fraction of polymer having molecular weight $M$. After Beuermann and Buback [2002] by permission of Elsevier, Oxford; an original plot, from which this figure was drawn, was kindly supplied by Dr. S. Beuermann.](image-url)
acrylate as \( w(\log M) \) versus \( \log M \) [Beuermann and Buback, 2002]. \( w \) is the weight fraction of polymer having molecular weight \( M \). (The symbol \( L \) is the same as \( X \), used extensively throughout the text. \( L \) is used here not to deliberately add confusion, but because it is used almost exclusively in the PLP-SEC literature.)

\( L_t \) is obtained from the first point of inflection on the low-molecular-weight side of the major peak of the molecular weight distribution plot. In practice this is most easily determined from the maxima in a differential plot of the molecular weight distribution, \( dw(\log M)/d \log M \) versus \( \log M \), the dotted plot in Fig. 3-12. For this polymerization it is easy to detect not only \( L_1 \), but also \( L_2 \), \( L_3 \), and \( L_4 \). The detection of several \( L_i \) values acts as an internal check on the PLP-SEC method. For Fig. 3-12, the \( k_p \) values calculated from \( L_1 \), \( L_2 \), and \( L_3 \) are within 2% of each other; the value from \( L_4 \) is within 6–7% of the other values. In practice, closeness between \( k_p \) values from \( L_1 \) and \( L_2 \) are considered sufficient to validate the PLP-SEC method.

\( k_p \) values can be obtained if chain-transfer constants are known from Mayo or CLD plots (Sec. 3-6, Eqs. 3-108, 3-121). \( k_{p,S} \) can be obtained directly from PLP-SEC polymerization by choosing reaction conditions that minimize normal termination, namely, long cycle times, low \( [I] \), and high \( [S] \).

\( k_i \) can be obtained directly from PLP-SEC polymerizations using the relationship

\[
k_i = \frac{k_p^2 [M]^2 (3 - \delta)}{r L_w} \tag{3-166}
\]

where \( r \) and \( L_w \) are the polymerization rate and weight-average degree of polymerization in the PLP-SEC experiment and \( \delta \) is the relative contribution of disproportionation to termination, defined as the ratio \( k_{ad}/(k_{ad} + k_{ic}) \) [Beuermann and Buback, 2002].

### 3-8d Typical Values of Reaction Parameters

Table 3-10 shows the values of the various concentrations, rates, and rate constants involved in the photopolymerization of methacrylamide as well as the range of values that are generally encountered in radical chain polymerizations. For the methacrylamide case, the experimentally determined quantities were \( R_i \), \( (R_p)_s \), \([M] \), \([I] \), \( k_p/k_i \), \( \tau_s \), and \( k_p/k_i \). All of the other

| TABLE 3-10 Reaction Parameters in Radical Chain Polymerization |
|-------------------|-----------------|------------------|------------------|
| Quantity          | Units           | General Range of Values | Methacrylamide Photopolymerization<sup>a</sup> |
| \( R_i \)         | mol L<sup>–1</sup> s<sup>–1</sup> | \( 10^{-8} – 10^{-10} \) | \( 8.75 \times 10^{-9} \) |
| \( k_d \)         | s<sup>–1</sup>   | \( 10^{-4} – 10^{-6} \) | —                |
| \([I]\)           | mol L<sup>–1</sup> | \( 10^{-2} – 10^{-4} \) | \( 3.97 \times 10^{-2} \) |
| \([M]_s\)         | mol L<sup>–1</sup> | \( 10^{-7} – 10^{-9} \) | \( 2.30 \times 10^{-8} \) |
| \( (R_p)_s \)     | mol L<sup>–1</sup> s<sup>–1</sup> | \( 10^{-4} – 10^{-6} \) | \( 3.65 \times 10^{-6} \) |
| \([M]\)           | mol L<sup>–1</sup> | \( 10^{-1} \) | \( 0.20 \) |
| \( k_p \)         | L mol<sup>–1</sup> s<sup>–1</sup> | \( 10^{-2} – 10^{2} \) | \( 7.96 \times 10^{2} \) |
| \( R_i \)         | mol L<sup>–1</sup> s<sup>–1</sup> | \( 10^{-8} – 10^{-10} \) | \( 8.73 \times 10^{-9} \) |
| \( k_i \)         | L mol<sup>–1</sup> s<sup>–1</sup> | \( 10^{8} – 10^{9} \) | \( 8.25 \times 10^{9} \) |
| \( \tau_s \)      | s<sup>–1</sup>   | \( 10^{-1} \) | \( 2.62 \) |
| \( k_p/k_i \)     | none            | \( 10^{-4} – 10^{-6} \) | \( 9.64 \times 10^{-5} \) |
| \( k_p k_i^{1/2} \)| L<sup>1/2</sup> mol<sup>–1/2</sup> s<sup>–1/2</sup> | \( 1–10^{-2} \) | \( 2.77 \times 10^{-1} \) |

<sup>a</sup> Values are taken directly or recalculated from Dainton and Sisley [1963].
parameters were then calculated in the appropriate manner. These values are typical of radical polymerizations. The \( k_p \) value \((\sim 10^3)\) is larger by many orders of magnitude than the usual reaction rate constant (for example, Tables 2-1, 2-2, and 2-10 show rate constants of approximately \(10^{-3}, 10^{-2}, \) and \(10^{-6}\) for esterification, urethane formation, and phenol-formaldehyde polymerization, respectively). Propagation is therefore rapid, and high polymer is formed essentially instantaneously. However, the even larger \( k_t \) value \((\sim 10^7)\) leads to quick termination, low radical concentrations \((\sim 10^{-8} M)\), and short radical lifetimes. The radical lifetime for methacrylamide in these experiments was 2.62 s, but it can be shorter or longer under other conditions or for other monomers. It is interesting to compare the experimental value \((8.75 \times 10^{-9})\) of \( R_t \) with the calculated value \((8.73 \times 10^{-9})\) of \( R_t \). The excellent agreement of the two indicates the validity of the steady-state assumption.

The rate constants for propagation and termination have been determined for many monomers. Table 3-11 lists values for some of the common monomers. These data were based on rotating sector experiments. The monomers have been listed in order of decreasing \( k_p \) values (which does not necessarily correspond to the exact order of decreasing \( k_t \) values). The order of \( k_p \) values is discussed in Sec. 6-3b, since \( k_p \) is a function of both monomer reactivity and radical reactivity.

The reader is cautioned that there is often a considerable divergence in the literature for values of rate constants [Buback et al., 1988, 2002]. One needs to examine the experimental details of literature reports to choose appropriately the values to be used for any needed calculations. Apparently different values of a rate constant may be a consequence of experimental error, experimental conditions (e.g., differences in conversion, solvent viscosity), or method of calculation (e.g., different workers using different literature values of \( k_d \) for calculating \( R_t \), which is subsequently used to calculate \( k_p/k_t^{1/2} \) from an experimental determination of \( R_p \)).

A prime purpose of the IUPAC Working Party on "Modeling of Kinetics and Processes of Polymerization" has been standardization of the experimental conditions and calculation methods for obtaining rate constants and other parameters. Table 3-12 shows the PLP-SEC values of the propagation rate parameters for a number of monomers. For many monomers there is good agreement between the values obtained from the rotating sector and PLP-SEC methods.

### Table 3-11 Kinetic Parameters in Radical Chain Polymerization\(^{a,b,c,d}\)

<table>
<thead>
<tr>
<th>Monomer</th>
<th>( k_p \times 10^{-3} )</th>
<th>( E_p )</th>
<th>( A_p \times 10^{-7} )</th>
<th>( k_t \times 10^{-7} )</th>
<th>( E_t )</th>
<th>( A_t \times 10 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Vinyl chloride (50°C)</td>
<td>11.0</td>
<td>16</td>
<td>0.33</td>
<td>210</td>
<td>17.6</td>
<td>600</td>
</tr>
<tr>
<td>Tetrafluoroethylene (83°C)</td>
<td>9.10</td>
<td>17.4</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td>Vinyl acetate</td>
<td>2.30</td>
<td>18</td>
<td>3.2</td>
<td>2.9</td>
<td>21.9</td>
<td>3.7</td>
</tr>
<tr>
<td>Acrylonitrile</td>
<td>1.96</td>
<td>16.2</td>
<td>—</td>
<td>7.8</td>
<td>15.5</td>
<td>—</td>
</tr>
<tr>
<td>Methyl acrylate</td>
<td>2.09</td>
<td>29.7</td>
<td>10</td>
<td>0.95</td>
<td>22.2</td>
<td>15</td>
</tr>
<tr>
<td>Methyl methacrylate</td>
<td>0.515</td>
<td>26.4</td>
<td>0.087</td>
<td>2.55</td>
<td>11.9</td>
<td>0.11</td>
</tr>
<tr>
<td>2-Vinylpyridine</td>
<td>0.186</td>
<td>33</td>
<td>—</td>
<td>3.3</td>
<td>21</td>
<td>—</td>
</tr>
<tr>
<td>Styrene</td>
<td>0.165</td>
<td>26</td>
<td>0.45</td>
<td>6.0</td>
<td>8.0</td>
<td>0.058</td>
</tr>
<tr>
<td>Ethylene</td>
<td>0.242</td>
<td>18.4</td>
<td>—</td>
<td>54.0</td>
<td>1.3</td>
<td>—</td>
</tr>
<tr>
<td>1,3-Butadiene</td>
<td>0.100</td>
<td>24.3</td>
<td>12</td>
<td>—</td>
<td>—</td>
<td>—</td>
</tr>
</tbody>
</table>

\( a \) \( k_p \) and \( k_t \) values are for 60°C unless otherwise noted. The units for \( k_p \) and \( k_t \) are L mol\(^{-1}\) s\(^{-1}\).

\( b \) \( E_p \) and \( E_t \) values are in kJ mol\(^{-1}\).

\( c \) \( A_p \) and \( A_t \) values are in L mol\(^{-1}\) s\(^{-1}\).

\( d \) Data are from Brandrup and Immergut [1989], Brandrup et al [1999], Eastmond [1976a,b,c], and Walling [1957].
ESR spectroscopy would clearly be the most direct method for determining $k_p$. Measurement of the propagating radical concentration together with the steady-state polymerization rate and monomer concentration allows the calculation of $k_p$ from Eq. 3-22. However, the propagating radical concentrations are too low in most polymerizations to easily and accurately determine by ESR. Some success has been achieved by ESR, but by using reaction conditions that are usually atypical—using initiation rates 1–2 orders higher than normal [Kamachi, 2002; Yamada et al., 1999]. For example, $k_p$ values of 150, 256, 510, and 4500 L mol$^{-1}$ C$^{-1}$ s$^{-1}$ have been obtained for 1,3-butadiene (5°C), styrene (50°C), methyl methacrylate (60°C), and vinyl acetate (5°C), in reasonable agreement with those obtained by the other methods. The general use of ESR for determining $k_p$ will probably increase in the future, especially if further advances in ESR instrumentation and techniques allow measurements at the radical concentrations present in typical polymerizations.

### 3-9 ENERGETIC CHARACTERISTICS

#### 3-9a Activation Energy and Frequency Factor

The effect of temperature on the rate and degree of polymerization is of prime importance in determining the manner of performing a polymerization. Increasing the reaction temperature usually increases the polymerization rate and decreases the polymer molecular weight. Figure 3-13 shows this effect for the thermal, self-initiated polymerization of styrene. However, the quantitative effect of temperature is complex since $R_p$ and $X_n$ depend on a combination of three rate constants—$k_i$, $k_p$, and $k_t$. Each of the rate constants for initiation, propagation, and termination can be expressed by an Arrhenius-type relationship

$$k = Ae^{-E/RT}$$  \hspace{1cm} (3-167a)

or

$$\ln k = \ln A - \frac{E}{RT}$$  \hspace{1cm} (3-167b)

where $A$ is the collision frequency factor, $E$ the Arrhenius activation energy, and $T$ the Kelvin temperature. A plot of ln $k$ versus $1/T$ allows the determination of both $E$ and $A$ from the slope and intercept, respectively. Values of $E_p$, the activation energy for propagation, and $E_t$, the activation energy for termination, for several monomers are shown in Tables 3-11 and 3-12.

<table>
<thead>
<tr>
<th>Monomer</th>
<th>$T$ (°C)</th>
<th>$k_p \times 10^{-3}$</th>
<th>$E_p$</th>
<th>$A_p \times 10^{-7}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Methyl acrylate</td>
<td>20</td>
<td>11.6</td>
<td>17.7</td>
<td>1.66</td>
</tr>
<tr>
<td>Vinyl acetate</td>
<td>50</td>
<td>6.30</td>
<td>19.8</td>
<td>1.0</td>
</tr>
<tr>
<td>Methyl methacrylate</td>
<td>50</td>
<td>0.648</td>
<td>22.4</td>
<td>0.267</td>
</tr>
<tr>
<td>Chloroprene</td>
<td>30</td>
<td>0.500</td>
<td>26.6</td>
<td>2.0</td>
</tr>
<tr>
<td>Styrene</td>
<td>40</td>
<td>0.160</td>
<td>31.5</td>
<td>2.88</td>
</tr>
<tr>
<td>1,3-Butadiene</td>
<td>30</td>
<td>0.057</td>
<td>35.7</td>
<td>8.05</td>
</tr>
<tr>
<td>Ethene</td>
<td>30</td>
<td>0.016</td>
<td>34.3</td>
<td>1.88</td>
</tr>
<tr>
<td>Dimethyl itaconate</td>
<td>30</td>
<td>0.011</td>
<td>24.9</td>
<td>0.020</td>
</tr>
</tbody>
</table>

aData from Beuermann and Buback [2002].
Note that the variations in the values of $A_p$, the frequency factor for propagation, are much greater than those in $E_p$—indicating that steric effects are probably the more important factor in determining the absolute value of $k_p$. Thus the more hindered monomers, such as methyl methacrylate and dimethyl itaconate (dimethyl 2-methylenebutanedioic acid), have lower $k_p$ and $A_p$ values than the less hindered monomers. The $A_p$ values in general are much lower than the usual value ($10^{11}$–$10^{13}$) of the frequency factor for a bimolecular reaction—probably due to a large decrease in entropy on polymerization. The variations in $A_t$, the frequency factor for termination, generally follow along the same lines as the $A_p$ values. The $A_t$ values in general are larger than the $A_p$ values.

### 3-9a-1 Rate of Polymerization

Consider the activation energy for various radical chain polymerizations. For a polymerization initiated by the thermal decomposition of an initiator, the polymerization rate depends on the ratio of three rate constants $k_p \left( k_d/k_t \right)^{1/2}$ in accordance with Eq. 3-32. The temperature dependence of this ratio, obtained by combining three separate Arrhenius-type equations, is given by

$$
\ln \left[ k_p \left( k_d/k_t \right)^{1/2} \right] = \ln \left[ A_p \left( A_d/A_t \right)^{1/2} \right] - \frac{[E_p + (E_d/2) - (E_t/2)]}{RT}
$$

(3-168)
The composite or overall activation energy for the rate of polymerization $E_R$ is $[E_p + (E_d/2) - (E_i/2)]$. Since $R_p$ is given by Eq. 3-32, one can write Eq. 3-168 as

$$ \ln R_p = \ln \left[ A_p \left( \frac{A_d}{A_i} \right)^{1/2} \right] + \ln \left[ \left( \frac{f[I]}{[M]} \right)^{1/2} \right] - \frac{E_R}{RT} \quad (3-169) $$

$E_R$ and $A_p (A_d/A_i)^{1/2}$ can then be obtained from the slope and intercept, respectively, of a plot of $\ln R_p$ versus $1/T$ (similar to Fig 3-13).

$E_d$, the activation energy for thermal initiator decomposition, is in the range 120–150 kJ mol$^{-1}$ for most of the commonly used initiators (Table 3-13). The $E_p$ and $E_t$ values for most monomers are in the ranges 20–40 and 8–20 kJ mol$^{-1}$, respectively (Tables 3-11 and 3-12). The overall activation energy $E_R$ for most polymerizations initiated by thermal initiator decomposition is about 80–90 kJ mol$^{-1}$. This corresponds to a two- or threefold rate increase for a 10°C temperature increase. The situation is different for other modes of initiation. Thus redox initiation (e.g., Fe$^{2+}$ with thiosulfate or cumene hydroperoxide) has been discussed as taking place at lower temperatures compared to the thermal polymerizations. One indication of the difference between the two different initiation modes is the differences in activation energies. Redox initiation will have an $E_d$ value of only about 40–60 kJ mol$^{-1}$, which is about 80 kJ mol$^{-1}$ less than for the thermal initiator decomposition [Barb et al., 1951]. This leads to an $E_R$ for redox polymerization of about 40 kJ mol$^{-1}$, which is about one half the value for nonredox initiators.

For a purely photochemical polymerization, the initiation step is temperature-independent ($E_d = 0$) since the energy for initiator decomposition is supplied by light quanta. The overall activation for photochemical polymerization is then only about 20 kJ mol$^{-1}$. This low value of $E_R$ indicates the $R_p$ for photochemical polymerizations will be relatively insensitive to temperature compared to other polymerizations. The effect of temperature on photochemical polymerizations is complicated, however, since most photochemical initiators can also decompose thermally. At higher temperatures the initiators may undergo appreciable thermal decomposition in addition to the photochemical decomposition. In such cases, one must take into account both the thermal and photochemical initiations. The initiation and overall activation energies for a purely thermal self-initiated polymerization are approximately the same as for initiation by the thermal decomposition of an initiator. For the thermal, self-initiated polymerization of styrene the activation energy for initiation is 121 kJ mol$^{-1}$ and $E_R$ is 86 kJ mol$^{-1}$ [Barr et al., 1978; Hui and Hamielec, 1972]. However, purely thermal polymerizations proceed at very slow rates because of the low probability of the initiation process due to the very low values ($10^4$–$10^6$) of the frequency factor.

<table>
<thead>
<tr>
<th>Initiator</th>
<th>$k_d \times 10^5$</th>
<th>$T , (^\circ C)$</th>
<th>$E_d$</th>
</tr>
</thead>
<tbody>
<tr>
<td>2,2’-Azobisisobutyronitrile</td>
<td>0.845</td>
<td>60</td>
<td>123</td>
</tr>
<tr>
<td>Acetyl peroxide</td>
<td>2.39</td>
<td>70</td>
<td>136</td>
</tr>
<tr>
<td>Benzoyl peroxide</td>
<td>5.50</td>
<td>85</td>
<td>124</td>
</tr>
<tr>
<td>Cumyl peroxide</td>
<td>1.56</td>
<td>115</td>
<td>170</td>
</tr>
<tr>
<td>$t$-Butyl peroxide</td>
<td>3.00</td>
<td>130</td>
<td>147</td>
</tr>
<tr>
<td>$t$-Butyl hydroperoxide</td>
<td>0.429</td>
<td>155</td>
<td>171</td>
</tr>
</tbody>
</table>

* All data are for decompositions in benzene solution.

* Data from Brandrup et al. [1999].

* The units of $k_d$ are s$^{-1}$; the units of $E_d$ are kJ mol$^{-1}$. 

---

**TABLE 3-13  Thermal Decomposition of Initiators**

---
3-9a-2 Degree of Polymerization

To determine the effect of temperature on the molecular weight of the polymer produced in a thermally catalyzed polymerization where transfer reactions are negligible, one must consider the ratio \( \frac{k_p}{(k_d k_t)^{1/2}} \), since it determines the degree of polymerization (Eq. 3-98). The variation of this ratio with temperature is given by

\[
\ln \left( \frac{k_p}{(k_d k_t)^{1/2}} \right) = \ln \left( \frac{A_p}{(A_d A_t)^{1/2}} \right) - \frac{[E_p - (E_d/2) - (E_t/2)]}{RT} \tag{3-170}
\]

where the energy term \([E_p - (E_d/2) - (E_t/2)]\) is the composite or overall activation energy for the degree of polymerization \( E_{X_n} \). For bimolecular termination, \( X_n \) is governed by Eqs. 3-98 and 3-99a and one can write

\[
\ln X_n = \ln \left( \frac{A_p}{(A_d A_t)^{1/2}} \right) + \ln \left( \frac{|M|}{|f||I|} \right)^{1/2} - \frac{E_{X_n}}{RT} \tag{3-171}
\]

\( E_{X_n} \) has a value of about \(-60 \text{ kJ mol}^{-1}\) for thermal initiator decomposition, and \( X_n \) decreases rapidly with increasing temperature. \( E_{X_n} \) is about the same for a purely thermal, self-initiated polymerization (Fig. 3-16). For a pure photochemical polymerization \( E_{X_n} \) is positive by approximately 20 kJ mol\(^{-1}\), since \( E_d \) is zero and \( X_n \) increases moderately with temperature. For a redox polymerization, \( E_{X_n} \) is close to zero, since \( E_d \) is 40–60 kJ mol\(^{-1}\), and there is almost no effect of temperature on polymer molecular weight. For all other cases, \( X_n \) decreases with temperature.

When chain transfer occurs in the polymerization, \( X_n \) is given by an appropriate form of Eq. 3-108. The temperature dependence of \( X_n \) can be quite complex depending on the relative importance of the various terms in Eq. 3-108. For the case where chain transfer to compound S is controlling (Eq. 3-119), one obtains

\[
-\ln \left( \frac{|M|}{|S|} \right) \left( \frac{1}{X_n} - \frac{1}{(X_n)_0} \right) = \ln \left( \frac{k_p}{k_r S} \right) = \ln \left( \frac{A_p}{A_{r S}} \right) - \frac{(E_p - E_{r S})}{RT} \tag{3-172}
\]

The quantity \((E_p - E_{r S})\) is now \( E_{X_n} \) and can be obtained from a plot of either of the two forms of the left side of Eq. 3-172 versus \( 1/T \). \( E_{r S} \) usually exceeds \( E_p \) by 20–65 kJ mol\(^{-1}\), with the more active transfer agents having lower values. The term \((E_p - E_{r S})\) is usually \(-20\) to \(-65\) kJ mol\(^{-1}\) (Table 3-14) and the molecular weight decreases with temperature.

<table>
<thead>
<tr>
<th>Transfer Agent</th>
<th>(- (E_p - E_{r S}))</th>
<th>log ((A_{r S}/A_p))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cyclohexane</td>
<td>56.1</td>
<td>3.1</td>
</tr>
<tr>
<td>Benzene</td>
<td>62.0</td>
<td>3.9</td>
</tr>
<tr>
<td>Toluene</td>
<td>42.3</td>
<td>1.7</td>
</tr>
<tr>
<td>Ethylbenzene</td>
<td>23.0</td>
<td>(-0.55)</td>
</tr>
<tr>
<td>Isopropylbenzene</td>
<td>23.0</td>
<td>(-0.47)</td>
</tr>
<tr>
<td>t-Butylbenzene</td>
<td>57.4</td>
<td>3.8</td>
</tr>
<tr>
<td>n-Butyl chloride</td>
<td>58.6</td>
<td>4</td>
</tr>
<tr>
<td>n-Butyl bromide</td>
<td>46.1</td>
<td>2</td>
</tr>
<tr>
<td>n-Butyl iodide</td>
<td>29.3</td>
<td>1</td>
</tr>
<tr>
<td>Carbon tetrachloride</td>
<td>20.9</td>
<td>1</td>
</tr>
</tbody>
</table>

\(a\) Data from Gregg and Mayo [1948, 1953a,b].
increasing temperature. The frequency factors for transfer reactions are usually greater than those for propagations, and the low transfer constant of a particular transfer agent is a consequence only of the high activation energy.

3-9b Thermodynamics of Polymerization

3-9b-1 Significance of $\Delta G$, $\Delta H$, and $\Delta S$

The thermodynamic characteristics ($\Delta G$, $\Delta H$, $\Delta S$) of polymerization are important to an understanding of the effect of monomer structure on polymerization [Ivin, 2000]. Further, knowledge of $\Delta H$ allows one to maintain the desired $R_p$ and $X_n$ by appropriate thermal control of the process. The $\Delta G$, $\Delta H$, and $\Delta S$ for a polymerization are the differences in free energy, enthalpy, and entropy, respectively, between 1 mol of monomer and 1 mol of repeating units in the polymer product. The thermodynamic properties of a polymerization relate only to the propagation step, since polymerization consists of single acts of initiation and termination and a large number of propagation steps.

Chain polymerizations of alkenes are exothermic (negative $\Delta H$) and exoentropic (negative $\Delta S$). The exothermic nature of polymerization arises because the process involves the exothermic conversion of $\pi$-bonds in monomer molecules into $\sigma$-bonds in the polymer. The negative $\Delta S$ for polymerization arises from the decreased degrees of freedom (randomness) for the polymer relative to the monomer. Thus, polymerization is favorable from the enthalpy viewpoint but unfavorable from the entropy viewpoint. Table 3-15 shows the wide range of

<table>
<thead>
<tr>
<th>Monomer</th>
<th>$-\Delta H$</th>
<th>$-\Delta S$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ethylene</td>
<td>93</td>
<td>155</td>
</tr>
<tr>
<td>Propene</td>
<td>84</td>
<td>116</td>
</tr>
<tr>
<td>1-Butene</td>
<td>83.5</td>
<td>113</td>
</tr>
<tr>
<td>Isobutylene</td>
<td>48</td>
<td>121</td>
</tr>
<tr>
<td>1,3-Butadiene</td>
<td>73</td>
<td>89</td>
</tr>
<tr>
<td>Isoprene</td>
<td>75</td>
<td>101</td>
</tr>
<tr>
<td>Styrene</td>
<td>73</td>
<td>104</td>
</tr>
<tr>
<td>$\alpha$-Methylstyrene</td>
<td>35</td>
<td>110</td>
</tr>
<tr>
<td>Vinyl chloride</td>
<td>72</td>
<td>—</td>
</tr>
<tr>
<td>Vinylidene chloride</td>
<td>73</td>
<td>89</td>
</tr>
<tr>
<td>Tetrafluoroethylene</td>
<td>163</td>
<td>112</td>
</tr>
<tr>
<td>Acrylic acid</td>
<td>67</td>
<td>—</td>
</tr>
<tr>
<td>Acrylonitrile</td>
<td>76.5</td>
<td>109</td>
</tr>
<tr>
<td>Maleic anhydride</td>
<td>59</td>
<td>—</td>
</tr>
<tr>
<td>Vinyl acetate</td>
<td>88</td>
<td>110</td>
</tr>
<tr>
<td>Methyl acrylate</td>
<td>78</td>
<td>—</td>
</tr>
<tr>
<td>Methyl methacrylate</td>
<td>56</td>
<td>117</td>
</tr>
</tbody>
</table>

* Data from Brandrup and Immergut [1989]; Sawada [1976].

$\Delta H$ refers to the conversion of liquid monomer to amorphous or (slightly) crystalline polymer. $\Delta S$ refers to the conversion of monomer (at a concentration of 1 M) to amorphous or slightly crystalline polymer. The subscripts lc are often used with $\Delta H$ and $\Delta S$ to show the initial and final states (that is, $\Delta H_{lc}$ and $\Delta S_{lc}$). The units of $\Delta H$ are kJ mol$^{-1}$ of polymerized monomer; the units of $\Delta S$ are J K$^{-1}$ mol$^{-1}$.

* Data are for conversion of gaseous monomer to crystalline polymer.
$\Delta H$ values for various monomers. The $\Delta S$ values fall in a narrower range of values. The methods of evaluating $\Delta H$ and $\Delta S$ have been reviewed [Dainton and Ivin, 1950, 1958]. These include direct calorimetric measurements of $\Delta H$ for the polymerization, determination by the difference between the heats of combustion of monomer and polymer, and measurements of the equilibrium constant for the polymerization. The overall thermodynamics of the polymerization of alkenes is quite favorable. The value of $\Delta G$ given by

$$\Delta G = \Delta H - T \Delta S$$  (3-173)

is negative because the negative $T \Delta S$ term is outweighed by the negative $\Delta H$ term.

One should recall the earlier discussion (Sec. 3-1b) on the thermodynamic and kinetic feasibilities of polymerization. The data in Table 3-15 clearly show the general thermodynamic feasibility for any carbon–carbon double bond. Although the relative thermodynamic feasibility of any one monomer varies depending on the substituents present in the monomer, $\Delta G$ is negative in all cases and polymerization is favored. However, thermodynamic feasibility does not indicate the experimental conditions that may be required to bring about the polymerization. Thus Table 3-1 showed that the kinetic feasibility of polymerization varies considerably from one monomer to another in terms of whether radical, cationic, or anionic initiation can be used for the reaction. In some instances thermodynamically feasible polymerizations may require very specific catalyst systems. This is the case with the $\alpha$-olefins, which cannot be polymerized to high-molecular-weight polymers by any of the conventional radical or ionic initiators. The polymerization of these monomers was not achieved until the discovery of the Ziegler–Natta or coordination-type initiators (Chap. 8).

**3-9b-2 Effect of Monomer Structure**

Consider the effect of monomer structure on the enthalpy of polymerization. The $\Delta H$ values for ethylene, propene, and 1-buene are very close to the difference ($82-90 \text{ kJ mol}^{-1}$) between the bond energies of the $\pi$-bond in an alkene and the $\sigma$-bond in an alkane. The $\Delta H$ values for the other monomers vary considerably. The variations in $\Delta H$ for differently substituted ethylenes arise from any of the following effects:

1. Differences in the resonance stabilization of monomer and polymer due to differences in conjugation or hyperconjugation.

2. Steric strain differences in the monomer and polymer arising from bond angle deformation, bond stretching, or interactions between nonbonded atoms.

3. Differences in hydrogen bonding or dipole interactions in the monomer and polymer.

Many substituents stabilize the monomer but have no appreciable effect on polymer stability, since resonance is only possible with the former. The net effect is to decrease the exothermicity of the polymerization. Thus hyperconjugation of alkyl groups with the C=C lowers $\Delta H$ for propylene and 1-butene polymerizations. Conjugation of the C=C with substituents such as the benzene ring (styrene and $\alpha$-methylstyrene), and alkene double bond (butadiene and isoprene), the carbonyl linkage (acrylic acid, methyl acrylate, methyl methacrylate), and the nitrile group (acrylonitrile) similarly leads to stabilization of the monomer and decreases enthalpies of polymerization. When the substituent is poorly conjugating as in vinyl acetate, the $\Delta H$ is close to the value for ethylene.
The effect of 1,1-disubstitution manifests itself by decreased $\Delta H$ values. This is a consequence of steric strain in the polymer due to interactions between substituents on alternating carbon atoms of the polymer chain.

![1,3-Interactions](image)

In XXXV the polymer chain is drawn in the plane of the text with the H and Y substituents placed above and below the plane of the text. The dotted and triangular lines indicate substituents below and above this plane, respectively. Such interactions are referred to as 1,3-interactions and are responsible for the decreased $\Delta H$ values in monomers such as isobutylene, $\alpha$-methylstyrene, methyl methacrylate, and vinylidene chloride. The effect in $\alpha$-methylstyrene is especially significant. The $\Delta H$ value of $-35$ kJ mol$^{-1}$ is essentially the smallest heat of polymerization of any monomer.

A contributing factor to the lowering of $\Delta H$ in some cases is a decrease in hydrogen bonding or dipole interactions on polymerization. Monomers such as acrylic acid and acrylamide are significantly stabilized by strong intermolecular associations. The intermolecular associations are not as important in the polymer because its steric constraints prevent the required lining up of substituents.

The $\Delta H$ value for vinyl chloride is lowered relative to that for ethylene because of increased steric strain in the polymer and increased resonance stabilization of the monomer. However, it is not clear why $\Delta H$ for vinylidene chloride is not lower than that for vinyl chloride. The abnormally high $\Delta H$ for tetrafluoroethylene is difficult to understand. A possible explanation may involve increased stabilization of the polymer due to the presence of intermolecular association (dipole interaction).

While the $\Delta H$ values vary over a wide range for different monomers, the $\Delta S$ values are less sensitive to monomer structure, being relatively constant within the range of 100–120 J K$^{-1}$ mol$^{-1}$. The $T \Delta S$ contribution to the $\Delta G$ of polymerization will be small as indicated earlier and will vary only within a narrow range. Thus the variation in the $T \Delta S$ term at 50°C for all monomers is in the narrow range 30–40 kJ mol$^{-1}$. The entropy changes that occur on polymerization have been analyzed for several monomers [Dainton and Ivin, 1950, 1958]. The $\Delta S$ of polymerization arises primarily from the loss of the translational entropy of the monomer. Losses in the rotational and vibrational entropies of the monomer are essentially balanced by gains in the rotational and vibrational entropies of the polymer. Thus $\Delta S$ for polymerization is essentially the translational entropy of the monomer, which is relatively insensitive to the structure of the monomer.

### 3-9b-3 Polymerization of 1,2-Disubstituted Ethylenes

With some exceptions, 1,2-disubstituted ethylenes containing substituents larger than fluorine such as maleic anhydride, stilbene, and 1,2-dichloroethylene exhibit little or no tendency
Maleic anhydride, stilbene, 1,2-dichloroethylene, and other similar compounds undergo polymerization [Bacsik, 1976; Kellou and Jenner, 1976; Seno et al., 1976]. Steric inhibition is the cause of this behavior, but the effect is different from that responsible for the low reactivity of 1,1-disubstituted ethylenes.

Polymers from 1,2-disubstituted ethylenes (**XXXVI**) possess 1,3-interactions, but the steric strain is not as severe as in **XXXV**. Both **XXXV** and **XXXVI** possess the same number of 1,3-interactions but the distribution of the interactions is different. For **XXXV**, pairs of 1,3-carbons each have a pair of 1,3-interactions. No pair of 1,3-carbons in **XXXVI** has more than a single 1,3-interaction. Thus the $\Delta H$ value for maleic anhydride is $-59 \text{ kJ mol}^{-1}$, which is favorable for polymerization compared to the value for some 1,1-disubstituted ethylenes.

The low tendency of 1,2-disubstituted ethylenes to polymerize is due to kinetic considerations superimposed on the thermodynamic factor. The approach of the propagating radical to a monomer molecule is sterically hindered. The propagation step is extremely slow because of steric interactions between the $\beta$-substituent of the propagating species and the two substituents of the incoming monomer molecule:

**XXXVII**

Some success has been achieved in polymerizing 1,2-disubstituted ethylenes, although the molecular weights are generally low. Maleic anhydride is very sluggish in polymerization. Only low-molecular-weight polymers are produced even when high initiator concentrations are used and the reaction proceeds in a complex manner with some loss of carbon dioxide [Culbertson, 1987; Gaylord, 1975; Gaylord and Mehta, 1988]. Various $N$-substituted maleimides, dialkyl fumarates (and fumaramides), and vinylene carbonate have been polymerized.
to higher molecular weights, many in the $10^3$–$10^4$ range with a few as high as $10^5$ [Field and Schaefgen, 1962; Matsumoto and Kimura, 1996; Matsumoto and Otsu, 1995; Matsumoto et al., 1990, 1993; Reimschussel and Creasy, 1978]. Dialkyl maleates have not been successfully polymerized, except when a base such as morpholine is present to isomerize the maleate ester to fumarate ester prior to polymerization [Matsumoto et al., 1996; Otsu et al., 1993; Yoshioka et al., 1991]. The lack of polymerization for the maleate esters is a consequence of the cis placement of the substituents, which maximizes the steric problem. Steric hindrance is lowered when the cis substituents are part of a cyclic structure, as in maleic anhydride, maleimides, and vinylene carbonate. Fumarate esters polymerize because there is less steric hindrance when the substituents are trans. Both $k_p$ and $k_d$ are lowered in fumarate esters compared to monomers such as methyl acrylate or methyl methacrylate, but the decrease in $k_i$ is much greater than the decrease in $k_p$, and polymerization is facilitated. The effect of decreased $k_i$ relative to $k_p$ and increased $R_p$ is enhanced for larger sterically hindered groups such as $t$-butyl. Similar effects have been observed for dialkyl itaconates [Otsu et al., 1993].

### 3-9c Polymerization–Depolymerization Equilibria

#### 3-9c-1 Ceiling Temperature

For most chain polymerizations there is some temperature at which the reaction becomes a reversible one, that is, the propagation step (Eq. 3-15) should be written as an equilibrium reaction [Joshi and Zwolinski, 1967; Sawada, 1976],

$$
M_n \cdot + M \xrightarrow{k_p} M_{n+1} \cdot \quad \text{(3-174)}
$$

where $k_{dp}$ is the rate constant of the reverse reaction—termed depolymerization or depropagation. The overall effect of temperature on polymerization is complex, due to the presence of this propagation–depropagation equilibrium. When the temperature is initially increased for the polymerization of a monomer the polymerization rate increases as $k_p$ increases (Sec. 3-9a-1). However, at higher temperatures the depropagation rate constant $k_{dp}$, which was initially zero, increases and becomes significant with increasing temperature. Finally, a temperature—the ceiling temperature $T_c$—is reached at which the propagation and depropagation rates are equal. These effects are shown in Fig. 3-14 for styrene. At the ceiling temperature the net rate of polymer production is zero.

The equilibrium position for the monomer–polymer equilibrium in Eq. 3-174 will be dependent on the temperature with increased temperature, resulting in a shift to the left, since the forward reaction is exothermic. The reaction isotherm

$$
\Delta G = \Delta G^\circ + RT \ln Q \quad \text{(3-175)}
$$

is applicable to an analysis of polymerization–depolymerization equilibria. $\Delta G^\circ$ is the $\Delta G$ of polymerization for the monomer and polymer in the appropriate standard states [Dainton and Ivin, 1950, 1958; Ivin, 2000]. The standard state for monomer is often taken as the pure monomer or a 1 M solution. The standard state for the polymer is usually the solid amorphous or slightly crystalline polymer or a solution that is 1 M in the repeat unit of the
polymer. For an equilibrium situation $\Delta G = 0$, $Q = K$ and Eq. 3-175 may be combined with Eq. 3-173 to yield

$$\Delta G^\circ = \Delta H^\circ - T \Delta S^\circ = -RT \ln K \quad (3-176)$$

The equilibrium constant is defined by $k_p/k_{dp}$ or more conveniently by

$$K = \frac{[M_{n+1}]}{[M_n][M]} = \frac{1}{[M]} \quad (3-177)$$

Combination of Eqs. 3-176 and 3-177 yields

$$T_c = \frac{\Delta H^\circ}{\Delta S^\circ + R \ln [M]_c} \quad (3-178a)$$

or

$$\ln [M]_c = \frac{\Delta H^\circ}{RT_c} - \frac{\Delta S^\circ}{R} \quad (3-178b)$$

Equation 3-178b shows the equilibrium monomer concentration $[M]_c$ as a function of the reaction or ceiling temperature $T_c$. (Note that $\Delta H^\circ$ in Eq. 3-178 can be replaced by $\Delta H$ because the enthalpy change is independent of [M]. This is not the case for $\Delta S^\circ$ since the entropy change is dependent on [M].) Since $\Delta H^\circ$ is a negative quantity, the monomer concentration in equilibrium with polymer increases with increasing temperature, that is, a plot of $[M]_c$ versus $1/T$ is linear with a negative slope of $\Delta H^\circ/R$ and intercept of $-\Delta S^\circ/R$. This means that there is a series of ceiling temperatures corresponding to different equilibrium monomer concentrations. For any monomer solution of concentration $[M]_c$, there is a temperature $T_c$ at which polymerization does not occur. (For each $[M]_c$, there is a corresponding plot analogous to Fig. 3-14, in which $k_{dp} = k_p[M]$ at its $T_c$.) Stated another way, the polymerization of a particular monomer solution at a particular temperature proceeds until
equilibrium is established, that is, until the monomer concentration decreases to the $[M]_0$ value corresponding to that $T_c$ temperature. Thus higher initial monomer concentrations are required with increasing temperature in order to observe a net production of polymer before equilibrium is established. There is an upper temperature limit above which polymer cannot be obtained even from pure monomer. The reader is cautioned to note that the literature often appears to refer only to a singular $T_c$ value—''the ceiling temperature.'' It is clear from the discussion above that each monomer concentration has its own $T_c$ value. The apparent designation of a singular $T_c$ value usually refers to the $T_c$ for the pure monomer or in some cases to that for the monomer at unit molarity.

For many of the alkene monomers, the equilibrium position for the propagation–depropagation equilibrium is far to the right under the usual reaction temperatures employed, that is, there is essentially complete conversion of monomer to polymer for all practical purposes. Table 3-16 shows the monomer concentrations at 25°C for a few monomers [Cook et al., 1958; McCormick, 1957; Wall, 1960; Worsfold and Bywater, 1957]. Data are also shown for the ceiling temperatures of the pure monomers. The data do indicate that the polymer obtained in any polymerization will contain some concentration of residual monomer as determined by Eq. 3-178. Further, there are some monomers for which the equilibrium is not particularly favorable for polymerization, for example, $\alpha$-methylstyrene. Thus at 25°C a 2.2-$M$ solution of $\alpha$-methylstyrene will not undergo polymerization. Pure $\alpha$-methylstyrene will not polymerize at 61°C. Methyl methacrylate is a borderline case in that the pure monomer can be polymerized below 220°C, but the conversion will be appreciably less than complete. For example, the value of $[M]_c$ at 110°C is 0.14 $M$ [Brandrup and Immergut, 1989]. Equation 3-178 applies equally well to ionic chain and ring-opening polymerizations as will be seen in subsequent chapters. The lower temperatures of ionic polymerizations offer a useful route to the polymerization of many monomers that cannot be polymerized by radical initiation because of their low ceiling temperatures. The successful polymerization of a previously unpolymerizable monomer is often simply a matter of carrying out the reaction at a temperature below its ceiling temperature.

Interestingly, it should not be assumed that a polymer will be useless above its ceiling temperature. A dead polymer that has been removed from the reaction media will be stable and will not depolymerize unless an active end is produced by bond cleavage of an end group or at some point along the polymer chain. When such an active site is produced by thermal, chemical, photolytic, or other means, depolymerization will follow until the monomer concentration becomes equal to $[M]_c$ for the particular temperature. The thermal behavior of many polymers, however, is much more complex. Degradative reactions other than depolymerization will often occur at temperatures below the ceiling temperature.
3-9c-2  Floor Temperature

The ceiling temperature phenomenon is observed because $\Delta H$ is highly exothermic, while $\Delta S$ is mildly exoentropic. The opposite type of phenomenon occurs in rare instances where $\Delta S$ is endoentropic ($\Delta S = +$) and $\Delta H$ is very small (either + or −) or zero. Under these conditions, there will be a floor temperature $T_f$ below which polymerization is not possible. This behavior has been observed in only three cases—the polymerizations of cyclic sulfur and selenium octamers and octamethylcyclotetrasiloxane to the corresponding linear polymers (Secs. 7-11a). $\Delta H$ is 9.5, 13.5, and 6.4 kJ mol$^{-1}$, respectively, and $\Delta S$ is 27, 31, and 190 J K$^{-1}$ mol$^{-1}$, respectively [Brandrup et al., 1999; Lee and Johannson, 1966, 1976].

3-10  AUTOACCELERATION

3-10a  Course of Polymerization

Radical chain polymerizations are characterized by the presence of an autoacceleration in the polymerization rate as the reaction proceeds [North, 1974]. One would normally expect a reaction rate to fall with time (i.e., the extent of conversion), since the monomer and initiator concentrations decrease with time. However, the exact opposite behavior is observed in many polymerizations—the reaction rate increases with conversion. A typical example is shown in Fig. 3-15 for the polymerization of methyl methacrylate in benzene solution [Schulz and Haborth, 1948]. The plot for the 10% methyl methacrylate solution shows the behavior that would generally be expected. The plot for neat (pure) monomer shows a dramatic autoacceleration in the polymerization rate. Such behavior is referred to as the gel effect. (The term gel as used here is different from its usage in Sec. 2-10; it does not refer to the formation of a crosslinked polymer.) The terms Trommsdorff effect and Norrish–Smith effect are also used in recognition of the early workers in the field. Similar behavior has been observed for a variety of monomers, including styrene, vinyl acetate, and methyl methacrylate [Balke and Hamielec, 1973; Cardenas and O’Driscoll, 1976, 1977; Small, 1975; Turner, 1977; Yamamoto and Sugimoto, 1979]. It turns out that the gel effect is the “normal”
behavior for most polymerizations. The gel effect should not be confused with the autoacceleration that would be observed if a polymerization were carried out under nonisothermal conditions such that the reaction temperature increased with conversion (since $\Delta H$ is negative). The gel effect is observed under isothermal reaction conditions.

A more critical analysis of accurate polymerization data indicates that the situation is complicated; three stages can be distinguished in some polymerizations when $R_p/[M][I]^{1/2}$ is plotted against time (or conversion) (Fig. 3-16) [Dionisio et al., 1979; Dionisio and O’Driscoll, 1980; Sack et al., 1988]. Plotting $R_p/[M][I]^{1/2}$ instead of percent conversion takes into account the concentration changes in monomer and initiator with time. Stage I involves either a constant rate (IA) or declining rate (IB) with time. Stage II constitutes the autoaccelerative gel effect region. Stage III involves either a constant (IIIA) or declining (IIIB) rate.

### 3-10b Diffusion-Controlled Termination

An understanding of this behavior requires that we appreciate termination is a diffusion-controlled reaction best described as proceeding by the three-step process [Mahabadi and O’Driscoll, 1977a,b; North, 1974]:

1. **Translational diffusion** of two propagating radicals (i.e., movement of the whole radicals) until they are in close proximity to each other:

   
   \[
   M_n^\cdot + M_m^\cdot \xrightleftharpoons[k_2]{k_1} \left[ M_n^\cdot \cdots M_m^\cdot \right]
   \]

   \(3-179\)

XXXVIII
2. Rearrangement of the two chains so that the two radical ends are sufficiently close for chemical reaction, which occurs by segmental diffusion of the chains, that is, by the movement of segments of a polymer chain relative to other segments

\[ [M_n \cdots - M_m] \xrightarrow{k_3} [M_n^*/M_m^*] \]

\[ \text{XXXVIII} \quad \text{XXXIX} \]

\[ k_3 \]

3. Chemical reaction of two radical ends

\[ [M_n^*/M_m^*] \xrightarrow{k_c} \text{dead polymer} \]

\[ \text{XXXIX} \]

Theoretical considerations indicate that \( k_c \) would be very large, about \( 8 \times 10^9 \text{ L mol}^{-1} \text{ s}^{-1} \), in low-viscosity media (such as bulk monomer) for the reaction between two radicals. The rate constants for reactions of small radicals (e.g., methyl, ethyl, propyl) are close to this value (being about \( 2 \times 10^9 \text{ L mol} \cdot \text{s}^{-1} \)) [Ingold, 1973]. Experimentally determined \( k_t \) values for radical polymerizations, however, are considerably lower, usually by two orders of magnitude or more (see Table 3-11). Thus diffusion is the rate-determining process for termination, \( k_c \gg k_4 \), and one obtains

\[ R_t = \frac{k_1 k_3 [M]^2}{k_2 + k_3} \]  

(3-182)

by assuming steady-state concentrations of both \text{XXXVIII} and \text{XXXIX}. Two limiting cases of termination arise. For the case of slow translational diffusion, \( k_3 \gg k_2 \), and

\[ R_t = k_1 [M]^2 \]  

(3-183)

For the case of slow segmental diffusion, \( k_2 \gg k_3 \), and

\[ R_t = \frac{k_1 k_3 [M]^2}{k_2} \]  

(3-184)

Thus the experimentally observed termination rate constant \( k_t \) corresponds to \( k_1 \) and \( k_1 k_3/k_2 \), respectively, for the two limiting situations.

Segmental diffusion and translational diffusion are expected to be affected differently with conversion [Dionisio and O’Driscoll, 1980; Mahabadi and O’Driscoll, 1977a,b; Mahabadi and Rudin, 1979]. With increasing conversion the polymerization medium becomes a poorer solvent because of the increased polymer concentration. The size of the randomly coiled up propagating radical in solution (referred to as coil) becomes smaller and there is an effective higher concentration gradient across the coil. Segmental diffusion of the radical end out of the coil to encounter another radical is increased. Simultaneously, the increasing polymer concentration decreases translational diffusion as the reaction medium becomes more viscous and, at sufficiently high concentrations, the polymer radicals become more crowded and entangled with each other. Chain entanglement leads to a faster decrease in translational diffusion relative to the decrease with increasing viscosity. Stage IA behavior corresponds to the situation observed for many monomers where the increase in segmental diffusion is apparently exactly counterbalanced by the decrease in translational diffusion (i.e., \( k_t \) remains constant). When the initial increase in segmental diffusion is greater than...
the decrease in translational diffusion, $k_t$ increases and the polymerization rate decreases (stage IB). Moderate stage IB behavior has been observed in several polymerizations (styrene, methyl methacrylate [Abuin et al., 1978; High et al., 1979]). At this time, no system has been observed with more than a moderate decrease in $R_p/[M][t]^{1/2}$ with conversion.

At some point, translational diffusion decreases faster than the increase in segmental diffusion and rapid autoacceleration occurs (stage II): the gel effect. Increased conversion results in increased polymer chain entanglements because of two effects: increased viscosity and increased polymer chain length [Lachinov, 1979]. The quantitative effects of polymer chain length on $k_t$ (and also $k_p$) have been discussed [Beuermann, 2002; Beuermann and Buback, 2002; Buback et al., 2000, 2002; O’Shaughnessy and Yu, 1994, 1998; Smith et al., 2003]. Termination becomes increasingly slower. Although propagation is also hindered, the effect is much smaller, since $k_p$ values are smaller than $k_t$ values by a factor of $10^4$–$10^5$. Termination involves the reaction of two large polymer radicals, while propagation involves the reaction of small monomer molecules and only one large radical. High viscosity affects the former much more than the latter. Therefore, the quantity $k_p/k_t^{1/2}$ increases and the result in accordance with Eq. 3-25 is an increase in $R_p$ with conversion. A second consequence of this effect is an increase in molecular weight with conversion as required by Eq. 3-95. These conclusions have been verified by the quantitative evaluation of the $k_p$ and $k_t$ values as a function of the percent conversion. Thus, Table 3-17 shows data on the polymerization of methyl methacrylate [Hayden and Melville, 1960]. It is seen that $k_p$ is relatively unaffected until 50% conversion (of monomer to polymer) has been reached, whereas $k_t$ has decreased by almost 2 orders of magnitude in the same span. The $k_p/k_t^{1/2}$ ratio and the polymerization rate simultaneously increase rapidly at first and then taper off as $k_p$ is also affected in the later stages of reaction. The attention of the reader is also directed to the data showing the increase in the radical lifetime with increasing conversion.

At very high conversion (e.g., above 50% for the system in Table 3-17), $k_p$ becomes sufficiently affected that the $R_p/[M][t]^{1/2}$ begins to level off (stage IIIA behavior) or decrease (stage IIIB behavior). Stage IIIB behavior is much more common than stage IIIA. The decrease in rate during stage IIIB, sometimes referred to as the glass or vitrification effect, can be extremely pronounced depending on the reaction temperature. The glass transition temperature of a polymerization reaction mixture increases with conversion of monomer to polymer. Polymerization can stop appreciably short of full conversion if the reaction system has a percent conversion whose glass transition temperature exceeds the reaction temperature [Friis and Hamielec, 1976; Mita and Horie, 1987; Sundberg and James, 1978]. For example, this occurs in the polymerization of pure methyl methacrylate in Fig. 3-15 since the

<table>
<thead>
<tr>
<th>% Conversion</th>
<th>Rate (%/h)</th>
<th>$\tau$ (s)</th>
<th>$k_p$</th>
<th>$k_t \times 10^{-5}$</th>
<th>$(k_p/k_t^{1/2}) \times 10^2$</th>
</tr>
</thead>
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<tr>
<td>0</td>
<td>3.5</td>
<td>0.89</td>
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<td>442</td>
<td>5.78</td>
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<tr>
<td>10</td>
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<td>1.14</td>
<td>234</td>
<td>273</td>
<td>4.58</td>
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<td>8.81</td>
</tr>
<tr>
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<td>15.4</td>
<td>5.0</td>
<td>303</td>
<td>14.2</td>
<td>25.5</td>
</tr>
<tr>
<td>40</td>
<td>23.4</td>
<td>6.3</td>
<td>368</td>
<td>8.93</td>
<td>38.9</td>
</tr>
<tr>
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<td>9.4</td>
<td>258</td>
<td>4.03</td>
<td>40.6</td>
</tr>
<tr>
<td>60</td>
<td>20.0</td>
<td>26.7</td>
<td>74</td>
<td>0.498</td>
<td>33.2</td>
</tr>
<tr>
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<td>79.3</td>
<td>16</td>
<td>0.0564</td>
<td>21.3</td>
</tr>
<tr>
<td>80</td>
<td>2.8</td>
<td>216</td>
<td>1</td>
<td>0.0076</td>
<td>3.59</td>
</tr>
</tbody>
</table>

aData from Hayden and Melville [1960].

TABLE 3-17 Effect of Conversion on the Polymerization of Methyl Methacrylate (22.5°C)
polymerization temperature \((50^\circ C)\) is considerably below the glass transition temperature of poly(methyl methacrylate) \((105^\circ C)\).

More recent work indicates that variations in initiator efficiency \(f\) are also important in understanding the effect of conversion on rate and degree of polymerization. The calculations of \(k_p\) and \(k_t\) in Table 3-17 were carried out with the assumption of a constant \(f\) independent of conversion, but it is known that \(f\) varies with conversion. The initiator efficiency decreases slowly with conversion until the high conversions of the stage IIIB region are reached; thereafter, there is a very steep drop in \(f\) with conversion [Russel et al., 1988; Sack et al., 1988]. For example, \(f\) for dimethyl 2,2-azobisisobutyrate in styrene polymerization at \(70^\circ C\) decreases from an initial value of 0.65 to about 0.50 at 75% conversion and then falls by several orders of magnitude over the remainder of the reaction [Zetterlund et al., 2001].

Thus, the behavior in Stage IIIB is a consequence of decreases in both \(k_p\) and \(f\), not just a decrease in \(k_p\). If one corrects the calculations of rate constants in previous work for the variation in \(f\) with conversion, the trends for \(k_t\) and \(k_p\) are essentially unchanged.

### 3-10c Effect of Reaction Conditions

The rate of segmental diffusion is predicted to increase (with a corresponding increase in \(k_t\) and decreases in rate and degree of polymerization) by any factor that decreases the coil size of the propagating radical. Thus segmental diffusion will increase with decreasing polymer molecular weight and goodness of reaction solvent and with increasing conversion [Mahabadi, 1987; Olaj and Zifferer, 1987]. The various factors affecting segmental diffusion are interrelated. At zero or very low conversion, \(k_t\) is larger in a poor solvent compared to \(k_t\) in a good solvent. It is possible to observe a “crossover” at somewhat higher conversion whereby the \(k_t\) in the good solvent is larger than \(k_t\) in the poor solvent. This occurs because coil size decreases with increasing polymer concentration, but the decrease is steeper in better solvents [Mahabadi and Rudin, 1979]. Many of these predictions for the course of polymerization in stage I have been verified [Abuin et al., 1978; Dionisio and O’Driscoll, 1980; Ludwico and Rosen, 1975, 1976].

The behavior in stage II is dominated by the decreased rate of translational diffusion caused by the increasing viscosity of the reaction system. Viscosity increases with increasing polymer molecular weight and solvent goodness. Increased polymer molecular weight also leads to earlier chain entanglements. These expectations have been verified in a number of studies. Lower polymer molecular weights moderate the gel effect (stage II behavior) by shifting the conversion at which the gel effect begins and the steepness of the subsequent increase in rate [Abuin and Lissi, 1977; Cardenas and O’Driscoll, 1976, 1977]. Vinyl acetate yields a lower-molecular-weight polymer, due to chain transfer to monomer and does not show as dramatic a gel effect as styrene or methyl methacrylate. Temperature also plays a large role—higher temperatures decrease the viscosity of the reaction medium. This delays the gel effect and the autoacceleration may not be as pronounced. Similar effects are observed in the presence of solvents and chain-transfer agents. Solvents lower the viscosity of the medium directly, while chain-transfer agents do so by lowering the polymer molecular weight. The effect of solvent in methyl methacrylate polymerization is seen in Fig. 3-15. The effect of viscosity on the gel effect has also been examined by adding polymer to a monomer prior to initiating polymerization; \(R_p\) increases with viscosity (which increases with polymer concentration) [Kulkarni et al., 1979].

The percent conversion for the onset of the gel effect varies considerably depending on the monomer and the reaction conditions (which determine coil size, viscosity, entanglements). In some systems the gel effect has been reported as occurring at only a few percent
conversion, in others, not until 60–70% conversion. Further, there is considerable difficulty in obtaining sufficiently accurate data to allow a precise evaluation of the onset of the gel effect, especially if the onset occurs gradually.

3-10d Related Phenomena

3-10d-1 Occlusion (Heterogeneous) Polymerization

Autoacceleration of the gel effect type is observed for the polymerization of monomers whose polymers are insoluble or weakly soluble in their own monomers. Examples of this type of behavior are acrylonitrile, vinyl chloride, trifluorochloroethylene, and vinylidene chloride [Billingham and Jenkins, 1976; Gromov et al., 1980a,b; Guyot, 1987; Jenkins, 1967; Olaj et al., 1977a,b; Talamini and Peggion, 1967]. Similar effects are observed in other polymerizations when one uses solvents that are nonsolvents for the polymer [e.g., methanol for polystyrene, hexane for poly(methyl methacrylate)]. The accelerative effects observed in these instances of heterogeneous polymerization are similar to the gel effect and are caused by a decrease in $k_r$ relative to $k_p$. The growing polymeric radicals become coiled up, since they are essentially insoluble or on the verge of insolubility in the solvent or in their own monomer. Termination between radicals again becomes progressively more difficult, while propagation may still proceed reasonably well. The reason for the decrease in occlusion or heterogeneous polymerization is probably due more to a decrease in segmental diffusion than to decreased translational diffusion. Although the propagating radical coil size is decreased in the poor reaction medium, unlike homogeneous systems, segmental diffusion is not enhanced, since diffusion must take place in a poor medium.

3-10d-2 Template Polymerization

Template (matrix) polymerization involves the polymerization of a monomer in the presence of a polymer, often a polymer derived from a different monomer [Ciardelli et al., 2001a,b; Gons et al., 1978; Matuszewska-Czerwik and Polowinski, 1990; Polowinski, 2002; Srivstava et al., 1987; Tan and Challa, 1987, 1988; Tewari and Srivastava, 1989; van de Grampel et al., 1988]. The original polymer and formed polymer are often referred to as parent and daughter polymers, respectively. Examples include acrylic acid with polyethyleneimine or poly(N-vinylpyrrolidinone), N-vinylimidazole with poly(methacrylic acid), acrylonitrile with poly(vinyl acetate), and methyl methacrylate with poly(methyl methacrylate). Many of these polymerizations proceed with rate enhancements relative to the corresponding polymerizations in the absence of polymer. The rate enhancements are typically by a factor no larger than 2–5, although a few larger enhancements have been observed. Two types of mechanisms appear to be operative depending on how strongly monomer is absorbed to polymer. A zip mechanism occurs when monomer is strongly complexed with the parent polymer. The complexed monomer molecules are lined up next to each other, which facilitates rapid propagation when an initiating radical from the surrounding solution adds to one of the absorbed monomer molecules. The stereochemistry of the template polymer has an effect on the rate enhancement. For example, the polymerization rate for N-vinylimidazolone with poly(methyl methacrylate) template increases in the order: isotactic, syndiotactic, atactic [van de Grampel et al., 1992]. (The meanings of the terms isotactic, syndiotactic, and atactic are discussed in Chap. 8.) The effect of template stereochemistry on polymerization rate varies with the monomer, template polymer, and temperature.
For monomers that only weakly complex with the parent polymer, polymerization occurs by a pickup mechanism. Initiation occurs in the surrounding solution to form a propagating oligomer that then complexes with the parent polymer. Subsequent propagation proceeds as monomer is picked up at the propagating center. Rate enhancement for zip propagation probably results from an increase in $k_p$ due to alignment of monomer molecules on the parent polymer coupled with a decrease in $k_t$ due to slower translational and segmental diffusion of propagating radicals. Only the latter effect is operative for template polymerizations involving the pickup mechanism. Template polymerizations have been of interest from the viewpoint of synthesizing stereoregular polymers (Chap. 8) by using a stereoregular parent polymer but this approach has been successful in very few instances.

3-10e Dependence of Polymerization Rate on Initiator and Monomer

The occurrence of the three stages of homogeneous polymerization and the occlusion and template polymerizations give rise to observed deviations of the usual kinetic expressions (e.g., Eqs. 3-32 and 3-98). It is not unusual to observe $R_p$ dependence on [M] of greater than first-order and $R_p$ dependence on [I] of either less than or greater than $\frac{1}{2}$-order. (A difficulty in evaluating literature data is that it is not always clear what reaction conditions (stage I, II, or III, occlusion, template?) exist in a particular study.) Such results are almost always artifacts. For both homogeneous and heterogeneous polymerizations, one may observe a higher than first-order dependence on [M] due to the $k_p/(2k_t)^{1/2}$ ratio varying with [M] to some power, which coupled with the normal first-order monomer dependence of propagation gives a higher than first-order dependence of $R_p$ on [M]. The $k_p/(2k_t)^{1/2}$ may vary with [M] because changing [M] may change the viscosity and/or goodness of the solvent (which effect the rates of segmental and/or translational diffusion). An increased dependence of $R_p$ on [M] may also result from the second step (Eq. 3-14a) of the initiation sequence becoming the rate-determining step, due to decreased mobility of the primary radicals.

A lower than $\frac{1}{2}$-order dependence of $R_p$ on [I] may be the indirect result of the corresponding change in polymer molecular weight. The termination rate constant would decrease with polymer molecular weight, which in turn decreases with initiator concentration, leading to a dependence of $R_p$ on [I] less than $\frac{1}{2}$-order, even 0-order in some instances. One the other hand, the dependence of $R_p$ on [I] becomes close to first-order in some heterogeneous polymerizations because the propagating radicals become so coiled up and inaccessible as to be incapable of undergoing termination under the usual reaction conditions [Ueda et al., 1984]. Termination becomes first-order in radical concentration. The presence of buried or trapped nonterminated radicals has been shown by ESR and the ability of photochemically produced reaction mixtures to continue polymerizing for days after the discontinuation of illumination [Sato et al., 1984]. Such long-lived radicals have been studied as a means of producing block copolymers [Sato et al., 1983; Seymour and Stahl, 1977]. Thus, vinyl acetate has been polymerized in a poor and/or viscous solvent to produce occluded macro-radicals, which then initiate the polymerization of methyl methacrylate, acrylic acid, acrylonitrile, styrene, and N-vinylpyrrolidinone to produce various block copolymers.

Under conditions where bimolecular termination between propagating radicals becomes difficult because of the increased viscosity or heterogeneity, primary termination may become important or even the only mode of termination. The latter leads to $R_p$ being second-order in [M] and zero-order in [I].
3-10f Other Accelerative Phenomena

Various other rate and molecular weight accelerations have been observed. The polymerizations of acrylonitrile, N-vinylpyrrolidinone, and acrylic acid are faster in the presence of water or hydrogen-bonding solvents even though the reaction medium becomes homogeneous instead of heterogeneous as in nonpolar solvents [Burillo et al., 1980; Chapiro and Dulieu, 1977; Laborie, 1977; Olive and Olive, 1978; Senogles and Thomas, 1978]. The rate acceleration is due to an increase in the propagation step. The effect is very large in some cases; for example, $k_p$ for acrylonitrile at $25^\circ$C is $2.8 \times 10^4$ L mol$^{-1}$ s$^{-1}$ in water compared to 400 L mol$^{-1}$ s$^{-1}$ in dimethylformamide. Water simultaneously hydrogen-bonds with both monomer and the propagating radical chain end (through the CN group) to increase the effective local monomer concentration at the radical site and also to increase the reactivity of the monomer and/or radical by a polar effect. This effect of water has been referred to as a template effect. (This template effect is different from that discussed in Sec. 3-10d-2.) An alternate mechanism proposes that the solvent binds monomer molecules into linear aggregates, which undergo faster propagation due to a favorable orientation (referred to as zip propagation). This autoacceleration sometimes occurs only after some polymer has formed, the formed polymer assisting in stabilizing the linear monomer aggregates (similar to template polymerization).

Carboxylic acid monomers such as acrylic and methacrylic acids and trans-butadiene-1-carboxylic acid have lower polymerization rates in good solvents and/or at higher pH where monomer exists in ionized form. Repulsions between the carboxylate anion groups of the propagating chain end and monomer result in lowered reactivity in the propagation step [Bando and Minoura, 1976; Ponratnam and Kapur, 1977]. Monomers containing $\beta$-diketone and $\beta$-ketoester groups (e.g., ethyl 4-methyl-3-oxo-4-pentenoate) exhibit higher reaction rates in benzene compared to acetonitrile. The enol tautomer, more plentiful in the less polar solvent, is more reactive than the keto tautomer [Masuda et al., 1987, 1989].

The addition of Lewis acids such as ZnCl$_2$ and AlCl$_3$ often increases the polymerization rate of monomers with electron-withdrawing substituents, such as acrylamide, methyl methacrylate, and acrylonitrile [Gromov et al., 1980a,b; Haeringer and Reiss, 1978; Kabanov, 1987; Liaw and Chung, 1983; Madruga and Sanroman, 1981; Maekawa et al., 1978; Sugiyama and Lee, 1977]. The mechanism of acceleration is not well established. In some instances the metal salt increases the initiation rate by complexing with the initiator. Increased reactivity toward propagation by complexation of the propagating radical and/or monomer with the Lewis acid appears to be the predominant effect in other systems. Simultaneous effects on both initiation and propagation (and possibly also termination) are indicated in many systems, since the polymer molecular weight often shows a maximum and a minimum with increasing concentration of Lewis acid. Some reports of complexation between a monomer or propagating radical with solvent—leading to changes in reactivity—have also been reported [Ghosh and Mukhopadhyay, 1980; Kamachi et al., 1979]. Some effects of solvent on reactivity have been observed in copolymerization (Sec. 6-3a-1).

3-11 MOLECULAR WEIGHT DISTRIBUTION

3-11a Low-Conversion Polymerization

The molecular weight distribution in radical chain polymerizations is more complex than those in step polymerization. Radical chain polymerization involves several possible modes
by which propagation is terminated—disproportionation, coupling, and various transfer reactions. The situation is further complicated, since the molecular weight of the polymer produced at any instant varies with the overall percent conversion because of changes in the monomer and catalyst concentrations and the propagation and termination rate constants. Molecular weight distributions can be easily calculated for polymerizations restricted to low conversions where all the kinetic parameters ([M], [I], $k_d$, $k_p$, $k_t$) are approximately constant [Clay and Gilbert, 1995; Flory, 1953; Macosko and Miller, 1976; Peebles, 1971; Tobita, 1995; Tompa, 1976; Vollmert, 1973]. Under these conditions, the polymer molecular weight does not change with conversion.

Consider the situation where one polymer molecule is produced from each kinetic chain. This is the case for termination by disproportionation or chain transfer or a combination of the two, but without combination. The molecular weight distributions are derived in this case in exactly the same manner as for linear step polymerization (Sec. 2-7). Equations 2-86, 2-88, 2-89, 2-27, 2-96, and 2-97 describe the number-fraction, number, and weight-fraction

$$N_x = (1-p)p^{x-1}$$  \hspace{1cm} (2-86)

$$N_x = N_0(1-p)^2p^{x-1}$$  \hspace{1cm} (2-88)

$$w_x = x(1-p)^2p^{x-1}$$  \hspace{1cm} (2-89)

$$\bar{X}_n = \frac{1}{(1-p)}$$  \hspace{1cm} (2-27)

$$\bar{X}_w = \frac{(1+p)}{(1-p)}$$  \hspace{1cm} (2-96)

$$\bar{X}_w/\bar{X}_n = (1+p)$$  \hspace{1cm} (2-97)

distributions, the number- and weight-average degrees of polymerization, and the breadth of the distribution, respectively.

One difference in the use of these equations for radical chain polymerizations compared to step polymerizations is the redefinition of $p$ as the probability that a propagating radical will continue to propagate instead of terminating. The value of $p$ is given as the rate of propagation divided by the sum of the rates of all reactions that a propagating radical may undergo

$$p = \frac{R_p}{R_p + R_t + R_{tr}}$$  \hspace{1cm} (3-185)

where $R_p$, $R_t$, and $R_{tr}$ are the rates of propagation, termination by disproportionation, and chain transfer, respectively. There is a very important second difference in the use of the equations above for radical chain polymerization compared to step polymerizations. The equations apply to the whole reaction mixture for a step polymerization but only to the polymer fraction of the reaction mixture for a radical chain polymerization.

A consideration of the preceding equations indicates that high polymer (i.e., large values of $\bar{X}_n$ and $\bar{X}_w$) will be produced only if $p$ is close to unity. This is certainly what one expects from the previous discussions in Sec. 3-5. The distributions described by Eqs. 2-86, 2-88, and 2-89 have been shown in Figs. 2-9 and 2-10. The breadth of the size distribution $\bar{X}_w/\bar{X}_n$ [also referred to as the polydispersity index (PDI)] has a limiting value of two as $p$ approaches unity.

For termination by coupling ($R_{tr} = 0$ and $R_t$ is the rate of coupling) where a polymer arises from the combination of two kinetic chains, the size distribution is narrower. The
situation is analogous to that for step polymerizations with branching (Sec. 2-9). Polymer molecules of sizes much different from the average are less likely, since the probability for coupling between same-sized propagating radicals is the same as that between different-sized propagating radicals. The size distributions can be derived in a manner analogous to that used in Sec. 2-7a. Consider the probability \( N_{x+z} \) of formation of an \( x \)-sized polymer molecule by the coupling of \( y \)- and \( z \)-sized propagating radicals. \( N_{y+z} \) is the product of the probabilities, \( N_y \) and \( N_z \), of forming the \( y \)- and \( z \)-sized propagating radicals. \( N_y \) and \( N_z \) are given by

\[
N_y = (1-p)p^{r-1} \\
N_z = (1-p)p^{r-1}
\]

which are obtained in the same manner as Eq. 2-86. Equation 3-187 can be rewritten as

\[
N_y = (1-p)p^{r-y-1}
\]

since \( y + z = x \) and \( N_{y+z} \) is then given by

\[
N_{y+z} = (1-p)^2p^{r-2}
\]

Equation 3-189 gives the probability of forming an \( x \)-sized polymer molecule by only one of many equally probable pathways. An \( x \)-sized polymer molecule can be obtained by couplings of \( y \)- and \( z \)-sized radicals, \( z \)- and \( y \)-sized radicals, \((y+1)-\) and \((z-1)-\) sized radicals, \((z-1)-\) and \((y+1)-\) sized radicals, \((y+2)-\) and \((z-2)-\) sized radicals, \((z-2)-\) and \((y+2)-\) sized radicals, \((y-1)-\) and \((z+1)-\) sized radicals, \((z+1)-\) and \((y-1)-\) sized radicals, and so on. There are \((x-1)\) possible pathways of producing an \( x \)-sized polymer molecule when \( x \) is an even number. Each pathway has the same probability—that given by Eq. 3-189—and the total probability \( N_x \) for forming an \( x \)-sized polymer molecule is given by

\[
N_x = (x-1)(1-p)^2p^{r-2}
\]

\( N_x \) is synonymous with the mole- or number-fraction distribution. When \( x \) is an odd number, there are \( x \) pathways and the \((x-1)\) term in Eq. 3-190 should be replaced by \( x \). For polymerizations yielding high polymer, the difference between \( x \) and \((x+1)\) is negligible and can be ignored. [Some derivations of size distributions show exponents \( y \) and \( z \), respectively, in Eqs. 3-186 and 3-187 instead of \((y-1)\) and \((z-1)\), which results in an exponent of \( x \) instead of \((x-1)\) in Eqs. 3-189 and 3-190. The differences are, again, unimportant for systems that yield high polymer.]

Using the same approach as in Secs. 2-7a and 2-7b, the following equations are derived for the weight-fraction distribution, number- and weight-average degrees of polymerization, and \( X_x/X_n \):

\[
w_x = \frac{1}{2x}(1-p)^3(x-1)p^{r-2}
\]

\[
X_n = \frac{2}{1-p}
\]

\[
X_w = \frac{2p}{1-p}
\]

\[
\frac{X_w}{X_n} = \frac{2p}{2}
\]
For polymerizations where termination occurs by a combination of coupling, disproportionation, and chain transfer, one can obtain the size distribution by a weighted combination of the two sets of distribution functions presented above. Thus the weight distribution can be obtained as

\[ w_x = A x(1 - p)^2 p^{x-1} + \frac{1}{2} (1 - A) x(1 - p)^3 (x - 1)p^{x-2} \]  

(3-195)

where \( A \) is the fraction of polymer molecules formed by disproportionation and chain-transfer reactions [Smith et al., 1966].

### 3-11b High-Conversion Polymerization

For many practical radical chain polymerizations, the reaction is carried out to high or complete conversion. The size distributions for high-conversion polymerizations become much broader than those described above or those in step polymerizations. Both the monomer and initiator concentrations decrease as a polymerization proceeds. The polymer molecular weight depends on the ratio \([M]/[I]^{1/2}\) according to Eq. 3-98. In the usual situation \([I]\) decreases faster than \([M]\) and the molecular weight of the polymer produced at any instant increases with the conversion. The overall molecular-weight distributions for high or complete conversion polymerizations are quite broad, with the \(X_w/X_n\) ratio being in the range 2-5. Broad molecular weight distributions are usually not desirable from the practical viewpoint, since most polymer properties show optimum values at specific molecular weights. Commercial polymerization processes often involve the addition of multiple charges of initiator and/or monomer during the course of the reaction to minimize the molecular weight broadening.

When autoacceleration occurs in polymerization there is even larger broadening of the size distribution. The large increases in the \(k_p/k_i^{1/2}\) ratio (Table 3-17) that accompany the gel effect lead to large increases in the sizes of the polymers being produced as the polymerization proceeds. \(X_w/X_n\) values as high as 5–10 may be observed when the gel effect is present. Excessive molecular-weight broadening occurs when branched polymers are produced by chain transfer to polymer. Chain transfer to polymer can lead to \(X_w/X_n\) ratios as high as 20–50. This very extensive size broadening occurs because chain transfer to polymer increases as the polymer size increases. Thus branching leads to even more branching as a polymerization proceeds. One usually attempts to minimize the molecular weight broadening due to the gel effect and chain transfer to polymer, but it is quite difficult to do so successfully. Thus, for example, low temperatures minimize chain transfer to polymer but maximize the gel effect (Sec. 3-10a).

### 3-12 EFFECT OF PRESSURE

The effect of pressure on polymerization, although not extensively studied, is important from the practical viewpoint since several monomers are polymerized at pressures above atmospheric. Pressure affects polymerization through changes in concentrations, rate constants, and equilibrium constants [Ogo, 1984; Weale, 1974; Zutty and Burkhart, 1962]. The commercial polymerizations of most gaseous monomers (e.g., vinyl chloride, vinylidene chloride, tetrafluoroethylene, vinyl fluoride) are carried out at very moderate pressures of about 5–10 MPa (1 MPa = 145 psi), where the primary effect is one of increased
concentration (often in a solvent) leading to increased rates. Significant changes in rate and equilibrium constants occur only at higher pressures such as the 100–300-MPa pressures used to produce the large-volume polymer—low-density polyethylene (Sec. 3-13b-1).

3-12a Effect on Rate Constants

High pressure can have appreciable effects on polymerization rates and polymer molecular weights. Increased pressure usually results in increased polymerization rates and molecular weights. Figure 3-17 shows these effects for the radiation-initiated polymerization of styrene [Moore et al., 1977].

3-12a-1 Volume of Activation

The effect of pressure on $R_p$ and $X_n$, like that of temperature, manifests itself by changes in the three rate constants—initiation, propagation, and termination. The quantitative effect of $P$ (at constant temperature) on a rate constant is given by

$$\frac{d \ln k}{dP} = \frac{-\Delta V^\dagger}{RT}$$  \hspace{1cm} (3-196)

where $\Delta V^\dagger$ is the volume of activation, that is, the change in volume (cm$^3$ mol$^{-1}$) in going from the reactant(s) to the transition state [Asano and LeNoble, 1978]. A negative value of

![Graph showing the effect of pressure on polymerization rate and molecular weight.](image)

Fig. 3-17 Effect of pressure on the polymerization rate ($\bigcirc$) and polymer molecular weight ($\triangle$) of radiation-initiated polymerization of styrene at 25°C. After Moore et al. [1977] (by permission of Wiley-Interscience, New York.)
\( \Delta V^f \) corresponds to the volume of the transition state being smaller than that of the reactants; the result is that increased pressure leads to an increase in the reaction rate constant. A \( \Delta V^f \) of \(-10 \text{ cm}^3 \text{ mol}^{-1} \) corresponds to 1.5- and 60-fold increases in rate constant at 100 and 1000 MPa, respectively, at 25\(^\circ\)C. The increases are 2.2- and 3500-fold if \( \Delta V^f \) is \(-20 \text{ cm}^3 \text{ mol}^{-1} \). Positive values of \( \Delta V^f \) correspond to a decrease in the reaction rate constant with increasing pressure as the volume of the transition state is larger than that of the reactants.

The \( \Delta V^f \) term for initiation by the thermal decomposition of an initiator \( \Delta V^f_d \) is positive, since the reaction is a unimolecular decomposition involving a volume expansion for the initiator going to the transition state. The initiation rate decreases with increasing pressure. \( \Delta V^f_d \) is in the range of \(+4 \) to \(+13 \text{ cm}^3 \text{ mol}^{-1} \), with most initiators being in the narrower range of \(+5 \) to \(+10 \text{ cm}^3 \text{ mol}^{-1} \) [Luft et al., 1978; Neumann, 1972; Walling and Metzger, 1959]. The measured \( \Delta V^f_d \) for a particular initiator often varies with solvent viscosity indicating that a large portion of \( \Delta V^f_d \) is due to increased pressure decreasing the ability of radicals to diffuse from the solvent cage. This is further verified by the observation that \( \Delta V^f_d \) determined by the disappearance of initiator is lower than that measured using radical scavengers, which detect radicals only outside the solvent cage. It is estimated that \( \Delta V^f_d \) would be \(+4 \) to \(+5 \text{ cm}^3 \text{ mol}^{-1} \) for most initiators if there were no cage effect [Martin, 1973]. The volume of activation for propagation \( \Delta V^f_p \) is negative, since the reaction involves two species coming together (i.e., a volume decrease occurs) in going to the transition state. \( \Delta V^f_p \) is in the range \( -15 \) to \(-24 \text{ cm}^3 \text{ mol}^{-1} \) for most monomers [Beuermann and Buback, 2002; Brandrup et al., 1999; Ogo, 1984; Rzayev and Penelle, 2002; Weale, 1974]. The volume of activation for bimolecular termination \( \Delta V^f_t \) is positive with values that are generally in the range \(+13 \) to \(+25 \text{ cm}^3 \text{ mol}^{-1} \) for most monomers. At first glance one would expect \( \Delta V^f_t \) to be negative, since termination involves a decrease in volume when two radicals come together in the transition state. However, since the termination step is diffusion-controlled, increased pressure decreases \( k_t \) by increasing the viscosity of the reaction medium [Nicholson and Norrish, 1956; O’Driscoll, 1977, 1979]. (Another result of the increased viscosity is that the gel effect is observed at lower conversions at higher pressures.)

### 3-12a-2 Rate of Polymerization

The variation of the polymerization rate with pressure will depend on the variation of the ratio \( k_p (k_d/k_t)^{1/2} \) with pressure in accordance with Eqs. 3-32 and 3-196. This latter variation will be given by

\[
\frac{d \ln [k_p (k_d/k_t)^{1/2}]}{dP} = \frac{-\Delta V^f_R}{RT} \tag{3-197}
\]

where \( \Delta V^f_R \) is the overall volume of activation for the rate of polymerization and is given by

\[
\Delta V^f_R = \frac{\Delta V^f_d}{2} + \Delta V^f_p - \frac{\Delta V^f_t}{2} \tag{3-198}
\]

The various terms are such that the value of \( \Delta V^f_R \) is negative by 15–20 \text{ cm}^3 \text{ mol}^{-1} \) for most monomers (as high as 25 \text{ cm}^3 \text{ mol}^{-1} \) in some cases) and the rate of polymerization is increased by high pressures (see Fig. 3-17). Thus, \( \Delta V^f_R \) is \(-17.1, -17.2, -15.6, -26.3, \) and \(-17.5 \text{ cm}^3 \text{ mol}^{-1} \), respectively, for styrene, vinyl acetate, methyl methacrylate, butyl methacrylate, and ethylene [Buback and Lendle, 1983; Ogo, 1984]. It is worth noting that
the relative effect of pressure on $R_p$ is less than that of temperature from the practical viewpoint. For a polymerization with $\Delta V^i_R = -25$ cm$^3$ mol$^{-1}$ and $E_R = 80$ kJ mol$^{-1}$ an increase in pressure from 0.1 to 400 MPa at 50°C yields about the same increase in $R_p$ as does an increase in temperature from 50 to 105°C. The increase in temperature is considerably easier to achieve than the pressure increase. Commercial high-pressure polymerization is usually carried out only when the polymerization temperature is relatively high to begin with (see the discussion on ethylene polymerization in Sec. 3-14a.

3-12a-3 Degree of Polymerization

The variation of the degree of polymerization with pressure depends on the variation of the ratio $k_p/(k_d k_t)^{1/2}$ with pressure and is given by

$$\frac{d \ln \left[ k_p/(k_d k_t)^{1/2} \right]}{dP} = -\frac{\Delta V^i_p}{RT}$$

where $\Delta V^i_p$ is the overall volume of activation for the degree of polymerization defined by

$$\Delta V^i_p = \Delta V^i_p - \frac{\Delta V^i_d}{2} - \frac{\Delta V^i_t}{2}$$

$\Delta V^i_p$ is negative by about 20–25 cm$^3$ mol$^{-1}$ in most cases and the polymer molecular weight increases with increasing pressure (Fig. 3-17). $\Delta V^i_p$ is more negative than $\Delta V^i_R$, since $\Delta V^i_d$ appears as $-\Delta V^i_d/2$ in the former. Thus $X_n$ changes more steeply with pressure than does $R_p$. However, one often observes as in Fig. 3-20 that the increase in molecular weight with pressure is not continuous but reaches a limiting value at some pressure. The explanation for this effect is that chain transfer to monomer becomes progressively more important compared to bimolecular termination with increasing pressure. At the highest pressures bimolecular termination becomes insignificant, and chain transfer to monomer is the major determinant of molecular weight.

Chain-transfer reactions would be expected to increase in rate with increasing pressure since transfer is a bimolecular reaction with a negative volume of activation. The variation of chain-transfer constants with pressure, however, differ depending on the relative effects of pressure on the propagation and transfer rate constants. For the case where only transfer to chain-transfer agent S is important, $C_S$ varies with pressure according to

$$\frac{d \ln C_S}{dP} = \frac{d \ln (k_{p,S}/k_p)}{dP} = -\frac{(\Delta V^i_{p,S} - \Delta V^i_p)}{RT}$$

where $\Delta V^i_{p,S}$ is the volume of activation for chain transfer. For some transfer agents, $\Delta V^i_{p,S}$ is smaller than $\Delta V^i_p$, and $C_S$ increases with pressure; the opposite occurs with other transfer agents. However, the difference in activation volumes for propagation and transfer is generally small (1–7 cm$^3$ mol$^{-1}$) and the change in $C_S$ with pressure is generally small. Thus, $C_S$ for carbon tetrachloride in styrene polymerization is decreased by only 15% in going from 0.1 to 440 MPa [Toohey and Weale, 1962]. An interesting observation is that the extent of the backbiting self-transfer reaction in polyethylene decreases with increasing pressure [Woodbrey and Ehrlich, 1963]. This means that the amount of branching in polyethylene decreases as the polymerization pressure increases.
**3-12b Thermodynamics of Polymerization**

The variation of the equilibrium constant for a reaction with pressure (at constant temperature) takes the same form as for the variation of a rate constant

\[
\frac{d \ln K}{dP} = -\frac{\Delta V}{RT}
\]  

(3-202)

where \(\Delta V\) is the reaction volume (the difference in volume between reactants and products). \(K\) increases with increasing pressure since \(\Delta V\) is negative. \(\Delta V\) values are generally in the range \(-15\) to \(-25\) cm\(^3\) mol\(^{-1}\). Polymerization is thermodynamically more favored at high pressure. Analysis shows that the effect of high pressure is exerted primarily through the change in \(\Delta S\). Increased pressure makes both \(\Delta H\) and \(\Delta S\) less negative, but the quantitative effect is much greater on \(\Delta S\), resulting in a more favorable (more negative) \(\Delta G\) with increasing pressure. (The changes in \(\Delta H\) and \(T\Delta S\) are \(\sim 5\) and \(25\) kJ mol\(^{-1}\), respectively, at 1000 MPa relative to 0.1 MPa at 25°C [Allen and Patrick, 1974].

Increased pressure increases the ceiling temperature and decreases the equilibrium monomer concentration according to

\[
\frac{dT_c}{dP} = \frac{T_c \Delta V}{\Delta H}
\]  

(3-203)

\[
\frac{d \ln [M]_{ic}}{dP} = \frac{\Delta V}{RT}
\]  

(3-204)

The strong dependence of \(T_c\) and \([M]_{ic}\) on pressure can lead to the observation of a *threshold pressure*—a pressure below which polymerization does not occur for a particular monomer concentration at a particular temperature.

**3-12c Other Effects of Pressure**

High pressures also affect the course of polymerization through changes in the physical properties of a reaction system. (The effect of increased viscosity has previously been mentioned.) The freezing point of a liquid usually rises with increasing pressure, about 15–25°C per 100 MPa. Thus increasing pressure may result in changing the state of a reaction system from liquid to solid or the exact nature of the liquid state with corresponding complications in the rate and/or thermodynamics of polymerization [Sasuga and Takehisa, 1978; Weale, 1974]. Dielectric constant also increases with increasing pressure [Ogo et al., 1978]. These changes often lead to discontinuities or changes in the quantitative effect of pressure on rate and degree of polymerization and/or equilibrium constant.

**3-13 PROCESS CONDITIONS**

The conditions under which radical polymerizations are carried out are of both the homogeneous and heterogeneous types. This classification is usually based on whether the initial reaction mixture is homogeneous or heterogeneous. Some homogeneous systems may become heterogeneous as polymerization proceeds as a result of insolubility of the polymer in the reaction media. Mass and solution polymerizations are homogeneous processes; suspension and emulsion polymerizations are heterogeneous processes. Emulsion polymerization will be discussed separately in Chap. 4. The other processes will be considered
here. All monomers can be polymerized by any of the various processes. However, it is usually found that the commercial polymerization of any one monomer is best carried out by one or two of the processes. The laboratory techniques for carrying out polymerizations have been discussed [Sandler and Karo, 1992, 1993, 1998; Sorenson et al., 2001]. Up-to-date technological details of commercial polymerizations are difficult to ascertain, although general descriptions are available [Arpe, 2002; Brydson, 1999; Grulke, 1989; Matsumoto et al., 1977; Menikheim, 1988; Munzer and Trommsdorff, 1977; Salamone, 1996; Saunders, 1988; Schildknecht, 1977].

3-13a Bulk (Mass) Polymerization

_Bulk or mass polymerization_ of a pure monomer offers the simplest process with a minimum of contamination of the product. However, bulk polymerization is difficult to control because of the characteristics of radical chain polymerization. Their highly exothermic nature, the high activation energies involved, and the tendency toward the gel effect combine to make heat dissipation difficult. Bulk polymerization requires careful temperature control. Further, there is also the need for strong and elaborate stirring equipment since the viscosity of the reaction system increases rapidly at relatively low conversion. The viscosity and exotherm effects make temperature control difficult. Local hot spots may occur, resulting in degradation and discoloration of the polymer product and a broadened molecular weight distribution due to chain transfer to polymer. In the extreme case, uncontrolled acceleration of the polymerization rate can lead to disastrous “runaway” reactions [Sebastian and Biesenberger, 1979]. Bulk polymerization is not used commercially for chain polymerizations nearly as much as for step polymerizations because of the difficulties indicated. It is, however, used in the polymerizations of ethylene, styrene, and methyl methacrylate. The heat dissipation and viscosity problems are circumvented by carrying out the polymerizations to low conversions with separation and recycling of unreacted monomer. An alternative is to carry out polymerization in stages—to low conversion in a large reactor and to final conversion in thin layers (either on supports or free-falling streams).

3-13b Solution Polymerization

Polymerization of a monomer in a solvent overcomes many of the disadvantages of the bulk process. The solvent acts as diluent and aids in the transfer of the heat of polymerization. The solvent also allows easier stirring, since the viscosity of the reaction mixture is decreased. Thermal control is much easier in _solution polymerization_ compared to bulk polymerization. On the other hand, the presence of solvent may present new difficulties. Unless the solvent is chosen with appropriate consideration, chain transfer to solvent can become a problem. Further, the purity of the polymer may be affected if there are difficulties in removal of the solvent. Vinyl acetate, acrylonitrile, and esters of acrylic acid are polymerized in solution.

3-13c Heterogeneous Polymerization

_Heterogeneous polymerization_ is used extensively to control the thermal and viscosity problems. There are three types of heterogeneous polymerization: _precipitation, suspension, and emulsion_. Emulsion polymerization is discussed in Chap. 4. Precipitation polymerizations begin
as homogeneous polymerizations but are quickly converted to heterogeneous polymerizations. This occurs in polymerization of a monomer either in bulk or in solution (usually aqueous but sometimes organic) where the polymer formed is insoluble in the reaction medium. Bulk polymerization of vinyl chloride and solution polymerization of acrylonitrile in water are examples of precipitation polymerization. Precipitation polymerizations are often referred to as powder or granular polymerizations because of the forms in which the final polymer products are obtained. The initiators used in precipitation polymerization are soluble in the initial reaction medium. Polymerization proceeds after precipitation by absorption of monomer and initiator (and/or initiating radicals) into the polymer particles.

Suspension polymerization (also referred to as bead or pearl polymerization) is carried out by suspending the monomer (discontinuous phase) as droplets (50–500 µm in diameter) in water (continuous phase). Styrene, acrylic and methacrylic esters, vinyl chloride, vinyl acetate, and tetrafluoroethylene are polymerized by the suspension method. The water: monomer weight ratio varies from 1:1 to 4:1 in most polymerizations. The monomer droplets (subsequently converted to polymer particles) are prevented from coalescing by agitation and the presence of suspension stabilizers (also referred to as dispersants or surfactants). Two types of stabilizers are used—water-soluble polymers (often in the presence of electrolyte or buffer) and water-insoluble inorganic compounds. The former type includes poly (vinyl alcohol), hydroxypropyl cellulose, sodium poly(styrene sulfonate), and sodium salt of acrylic acid–acrylate ester copolymer; the latter type includes talc, hydroxyapatite, barium sulfate, kaolin, magnesium carbonate and hydroxide, calcium phosphate, and aluminum hydroxide. The levels of suspension stabilizers are typically less than 0.1 weight percent (wt%) of the aqueous phase (although the water-soluble polymers are sometimes used at higher concentrations). This is much lower than the surfactant concentrations used in emulsion polymerizations (typically as high as 1–5%) (Chap. 4) and accounts for the higher monomer droplet sizes in suspension polymerization. Also, unlike emulsion polymerization, the two-phase system cannot be maintained in suspension polymerization without agitation. Another difference is that the dispersants used in suspension polymerization seldom form colloidal micelles as in emulsion polymerization.

The initiators used in suspension polymerization are soluble in the monomer droplets. Such initiators are often referred to as oil-soluble initiators. Each monomer droplet in a suspension polymerization is considered to be a miniature bulk polymerization system. The kinetics of polymerization within each droplet are the same as those for the corresponding bulk polymerization.

An inverse suspension polymerization involves an organic solvent as the continuous phase with droplets of a water-soluble monomer (e.g., acrylamide), either neat or dissolved in water. Microsuspension polymerizations are suspension polymerizations in which the size of monomer droplets is about 1 µm.

Dispersion polymerization involves an initially homogeneous system of monomer, organic solvent, initiator, and particle stabilizer (usually uncharged polymers such as poly(N-vinylpyrrolidinone) and hydroxypropyl cellulose). The system becomes heterogeneous on polymerization because the polymer is insoluble in the solvent. Polymer particles are stabilized by adsorption of the particle stabilizer [Yasuda et al., 2001]. Polymerization proceeds in the polymer particles as they absorb monomer from the continuous phase. Dispersion polymerization usually yields polymer particles with sizes in between those obtained by emulsion and suspension polymerizations—about 1–10 µm in diameter. For the larger particle sizes, the reaction characteristics are the same as in suspension polymerization. For the smallest particle sizes, suspension polymerization may exhibit the compartmentalized kinetics of emulsion polymerization.
Several other techniques for carrying out radical chain polymerizations have been studied. Polymerization of clathrate (or inclusion or canal) complexes of monomer (guest molecule) with host molecules such as urea, thiourea, perhydrotriphenylene, apocholic and deoxycholic acids, or β-cyclodextrin offers the possibility of obtaining stereoregular polymers (Chap. 8) or polymers with extended-chain morphology by the proper choice of the host–guest pair and reaction conditions [Bernhardt et al., 2001; Farina and DiSilvestro, 1987; Miyata et al., 1988]. (Clathrates differ from other adducts such as hydrates and coordination complexes in that the latter involve significant secondary attractive interactions, such as hydrogen-bonding, ion-dipole, while the former involve much weaker forces that are related to the steric fit between host and guest molecules.) Radical polymerizations have also been carried out with monomers in the solid state [Chapiro, 1962; Chatani, 1974].

Polymerization in β-cyclodextrin (CD) complexes with monomer offers a route to polymerization, as well as other organic reactions, in water without the need for organic solvents [Ritter and Tabatabai, 2002]. β-Cyclodextrins are torus-shaped, cyclic oligosaccharides obtained by degradation of starch. The hydroxyl groups of the glucose repeat unit of CD are located on the outer surface. This makes the outer surface hydrophilic, whereas the inner surface and cavity are hydrophobic. Water-insoluble monomers become solubilized in water when mixed with CD or CD derivatives because the monomers are absorbed into the cavity. This allows polymerization in aqueous, not organic media, with water-soluble initiators.

There is a significant effort to construct unique polymer architectures that form well-defined nanostructures. One approach is to use monomers with structures that self-assemble into nanostructures; that is, the monomers aggregate together in a specific manner through secondary attractive forces [Day and Ringsdorf, 1979; Gin et al., 2001; Hsu and Blumstein, 1977; Jung et al., 2000; Ohno et al., 1989]. An example is an amphiphatic monomer with a long hydrophobic tail and a short hydrophilic head, such as XL, where \((m + n)\) is large, e.g., 15. In aqueous media, the monomer undergoes self-assembly so that its hydrophobic tails aggregate together and out of contact with the aqueous medium, whereas its hydrophilic heads are together and in contact with the aqueous medium. (In biological systems, amphipathic molecules—the glycerophospholipids and sphingolipids—aggregate together to form the cell membranes that surround and contain individual cells [Blei and Odian, 2000].)

Depending on the specific amphiphatic monomer used, self-assembly forms different structures, including micelles, vesicles, microtubules (cylinder-like aggregate). These structures many also aggregate at a higher level; For instance, several microtubules may assemble together along their lengths to form a columnar bundle. it is then possible to “lock in” the self-assembled structure of the monomer by photopolymerization.

Template polymerization (Sec. 3-10d-2) also involves self-assembly.
About 110 billion pounds of polymers were produced in the United States in 2001. Close to 40 billion pounds of this total are produced by radical chain polymerization.

3-14a Polyethylene

Radical chain polymerization of ethylene to polyethylene is carried out at high pressures of 120–300 MPa (17,000–43,000 psi) and at temperatures above the $T_m$ of polyethylene (Fig. 3-18) [Doak, 1986]. Batch processes are not useful since the long residence time gives relatively poor control of product properties. Long-chain branching due to intermolecular chain transfer becomes excessive with deleterious effects on the physical properties. Continuous processes allow better control of the polymerization.

\[
\text{CH}_2=\text{CH}_2 \xrightarrow{\text{radical}} \left(\text{CH}_2\text{CH}_2\right)_n
\]  

(3-205)

Tubular reactors are most often used, although autoclave reactors are also employed. Tubular reactors consist of a number of sections, each with an inner diameter of 2–6 cm and length of 0.5–1.5 km, arranged in the shape of an elongated coil. The polymerization mixture has very high linear velocities (>10 m s\(^{-1}\)) with short reaction times (0.25–2 min). Trace amounts of oxygen (≤300 ppm) are typically used as the initiator, often in combination with other substances. 

Fig. 3-18 Flow diagram of high-pressure polyethylene process. After Doak [1986] (by permission of Wiley-Interscience, New York).
with an alkyl or acyl peroxide or hydroperoxide. Ethylene is compressed in stages with cooling between stages and introduced into the reactor. Initiator and chain-transfer agent are added during a late stage of compression or simultaneously with the introduction of monomer into the reactor. Propane, butane, cyclohexane, propene, 1-butene, isobutylene, acetone, 2-propanol, and propionaldehyde have been used as chain-transfer agents. The initial reaction temperature is typically 140–180°C, but this increases along the length of the reactor to peak temperatures as high as 300–325°C before decreasing to about 250–275°C, due to the presence of cooling jackets. Polymerization occurs in the highly compressed gaseous state where ethylene behaves much as a liquid (even though ethylene is above its critical temperature). The reaction system after the start of polymerization is homogeneous (polymer swollen by monomer) if the pressure is above 200 MPa. Some processes involve multizone reactors where there are multiple injections of initiator (and, often, monomer and chain-transfer agent) along the length of the tubular reactor.

The conversion per pass is usually 15–20% and 20–30% per pass for single-zone (no additional injections of reactants) and multizone reactors, respectively. After leaving the reactor, polyethylene is removed from the reaction mixture by reducing the pressure, usually in two stages in series at 20–30 MPa and 0.5 MPa or less. Molten polyethylene is extruded, pelletized, and cooled. The recovered ethylene is cooled to allow waxes and oils (i.e., very-low-molecular-weight polymer) to be separated prior to recycling of ethylene to the reactor. Overall, ethylene polymerization is carried out as a bulk polymerization (i.e., no added solvent or diluent) in spite of the inherent thermal and viscosity problems. Control is achieved by limiting conversion to no more than 30% per pass. The polymerization is effectively carried out as a solution or suspension process (with unreacted monomer acting as solvent or diluent) depending on whether the pressure is above or below 200 MPa.

Autoclave reactors differ from tubular reactors in two respects. Autoclave reactors have much smaller length-to-diameter ratios (2–4 for single-zone and up to 15–18 for multizone reactors) and operate at a much narrower reaction temperature range.

The polyethylene produced by radical polymerization is referred to as low-density polyethylene (LDPE) or high-pressure polyethylene to distinguish it from the polyethylene synthesized using coordination catalysts (Sec. 8-11b). The latter polyethylene is referred to as high-density polyethylene (HDPE) or low-pressure polyethylene. Low-density polyethylene is more highly branched (both short and long branches) than high-density polyethylene and is therefore lower in crystallinity (40–60% vs. 70–90%) and density (0.91–0.93 g cm\(^{-3}\) vs. 0.94–0.96 g cm\(^{-3}\)).

Low-density polyethylene has a wide range and combination of desirable properties. Its very low \( T_g \) of about –120°C and moderately high crystallinity and \( T_m \) of 105–115°C give it flexibility and utility over a wide temperature range. It has a good combination of strength, flexibility, impact resistance, and melt flow behavior. The alkane nature of polyethylene imparts a very good combination of properties. Polyethylene is highly resistant to water and many aqueous solutions even at high temperatures. It has good solvent, chemical, and oxidation resistance, although it is slowly attacked by oxidizing agents and swollen by hydrocarbon and chlorinated solvents at room temperature. Polyethylene is a very good electrical insulator. Commercial low-density polyethylenes have number-average molecular weights in the range 20,000–100,000, with \( X_w/X_n \) in the range 3–20. A wide range of LDPE products are produced with different molecular weights, molecular-weight distributions, and extents of branching (which affects crystallinity, density, and strength properties), depending on the polymerization temperature, pressure (i.e., ethylene concentration), and reactor type. Long-chain branching increases with increasing temperature and conversion but decreases with increasing pressure. Short-chain branching decreases with increasing temperature and
conversion but increases with pressure. Autoclave processes generally yield polyethylenes with narrower molecular weight distributions but increased long-chain branching compared to tubular processes.

The wide range and combination of properties, including the ease of fabrication by a variety of techniques, makes LDPE a large-volume polymer. Over 8 billion pounds were produced in 2001 in the United States; worldwide production was more than 3 times that amount. These amounts are especially significant when one realizes that commercial quantities of polyethylene did not become available until after World War II in 1945. Polyethylene was discovered in the early 1930s at the ICI laboratories in England and played an important role in the outcome of World War II. The combination of good electrical properties, mechanical strength, and processability made possible the development of radar, which was critical to turning back Germany’s submarine threat and air attacks over England.

Film applications account for over 60% of polyethylene consumption. Most of this is extrusion-blown film for packaging and household uses (bags, pouches, and wrap for food, clothes, trash, and dry cleaning) and agricultural and construction applications (greenhouses, industrial tank and other liners, moisture and protective barriers). Injection molding of toys, housewares, paint-can lids, and containers accounts for another 10–15%. About 5% of the LDPE produced is used as electrical wire and cable insulation (extrusion coating and jacketing) for power transmission and communication. Extrusion coating of paper to produce milk, juice, and other food cartons and multiwall bags accounts for another 10%. Other applications include blow-molded squeeze bottles for glue and personal-care products.

Trade names for polyethylene include Alathon, Alkathene, Fertene, Grex, Hostalen, Marlex, Nipolon, and Petrothene.

Low- and high-density polyethylene, polypropene, and polymers of other alkene (olefin) monomers constitute the polyolefin family of polymers. All except LDPE are produced by coordination catalysts. Coordination catalysts are also used to produce linear low-density polyethylene (LLDPE), which is essentially equivalent to LDPE in structure, properties, and applications (Sec. 8-11c). The production figures given above for LDPE do not include LLDPE. The production of LLDPE now exceeds that of LDPE, with about 10 billion pounds produced in 2001 in the United States. (Copolymers constitute about one-quarter of all low density polyethylenes; see Sec. 6-8b.)

### 3-14b Polystyrene

Continuous solution polymerization is the most important method for the commercial production of polystyrene although suspension polymerization is also used [Moore, 1989].

\[
\text{CH}_2\text{CH} \quad \xrightarrow{\text{φ}} \quad \left\{\text{CH}_2\text{CH} \right\}_n
\]  

(3-206)

Emulsion polymerization is important for ABS production (Chap. 4) but not for polystyrene itself.

Figure 3-19 shows a generalized solution process for polymerization of styrene. Actual processes may have up to five reactors in series; processes with only one reactor are sometimes used. Styrene, solvent (usually ethylbenzene in amounts of 2–30%), and occasionally initiator are fed to the first reactor. Solvent is used primarily for viscosity control with the amount determined by the exact configuration of the reactor and the polymer molecular weight desired. A secondary function of solvent is control of molecular weight by chain
transfer, although more effective chain-transfer agents are also used. The reactors are run at successively increasing temperatures with 180°C in the last reactor. For thermal, self-initiated polymerization, the first reactor is run at 120°C. The temperature in the first reactor is 90°C when initiators are used. Both single- and two-initiator systems are used. Final conversions of 60–90% are achieved in the last reactor. The reaction mixture is passed through a vacuum devolatilizer to remove solvent and unreacted monomer that are condensed and recycled to the first reactor. The devolatilized polystyrene (at 220–260°C) is fed to an extruder and pelletized. Control of the heat dissipation and viscosity problems is achieved by the use of a solvent, limiting conversion to less than 100%, and the sequential increasing of reaction temperature.

Commercial polystyrenes (PS) have number-average molecular weights in the range 50,000–150,000 with $\bar{X}_w/\bar{X}_n$ values of 2–4. Although completely amorphous ($T_g = 85°C$), its bulky rigid chains (due to phenyl–phenyl interactions) impart good strength with high-dimensional stability (only 1–3% elongation); polystyrene is a typical rigid plastic. PS is a very good electrical insulator, has excellent optical clarity due to the lack of crystallinity, possesses good resistance to aqueous acids and bases, and is easy to fabricate into products since only $T_g$ must be exceeded for the polymer to flow. However, polystyrene has some limitations. It is attacked by hydrocarbon solvents, has poor weatherability (UV, oxygen, and ozone attack) due to the labile benzylic hydrogens, is somewhat brittle, and has poor impact strength due to the stiff polymer chains. The upper temperature limit for using poly-styrene is low because of the lack of crystallinity and low $T_g$. In spite of these problems, styrene polymers are used extensively with almost 10 billion pounds of plastics and about 1 billion pounds of elastomers produced in 2001 in the United States. Weathering problems of styrene products are significantly decreased by compounding with appropriate stabilizers (UV absorbers and/or antioxidants). Solvent resistance can be improved somewhat by compounding with glass fiber and other reinforcing agents. Copolymerization and polymer blends are used extensively to increase the utility of styrene products. Copolymerization involves polymerizing a mixture of two monomers. The product, referred to as a copolymer,

![Diagram of continuous solution polymerization of styrene.](image-url)
contains both monomers in the polymer chain—in the alternating, statistical, block, or graft arrangement depending on the detailed chemistry of the specific monomers and reactions conditions (Chap. 6). Polymer blends are physical mixtures of two different materials (either homopolymers or copolymers). All the elastomeric styrene products are copolymers or blends; none are homopolystyrene. No more than about one-third of the styrene plastic products are homopolystyrene. The structural details of the copolymers and blends will be considered in Sec. 6-8a.

About 2 billion pounds of styrene homopolymer are produced annually in the United States in the form of a product referred to as crystal polystryene. Although the term crystal is used to describe the great optical clarity of the product, crystal polystyrene is not crystalline; it is completely amorphous. A variety of products are formed by injection molding, including tumblers, dining utensils, hairbrush handles, housewares, toys, cosmetic containers, camera parts, audiotape cassettes, computer disk reels, stereo dust covers, and office fixtures. Medical applications include various items sterilized by ionizing radiation (pipettes, Petri dishes, medicine containers). Extruded sheet is used for lighting and decoration applications. Biaxially oriented sheet is thermoformed into various shapes, such as blister packaging and food-packaging trays. Expandable polystyrene, either crystal polystyrene or styrene copolymers impregnated with a blowing agent (usually pentane), is used to produce various foamed products. Among the products are disposable drinking cups (especially coffee cups), cushioned packaging, and thermal insulation used in the construction industry. Extruded foam sheets are converted by thermoforming into egg cartons, meat and poultry trays, and packaging for fast-food takeouts. The production of expandable polystyrene and styrene copolymers probably exceeds one billion pounds annually in the United States.

Trade names for PS include Carinex, Cellofoam, Dylene, Fostarene, Hostyren, Lustrex, Styron, and Styrofoam.

3-14c Vinyl Family

The vinyl family of polymers consists of poly(vinyl chloride), poly(vinylidene chloride), poly(vinyl acetate), and their copolymers and derived polymers.

3-14c-1 Poly(vinyl chloride)

Most poly(vinyl chloride) (PVC) is commercially produced by suspension polymerization [Brydson, 1999; Endo, 2002; Saeki and Emura, 2002; Tornell, 1988]. Bulk and emulsion polymerizations are used to a much lesser extent, and solution polymerization is seldom used. Suspension polymerization of vinyl chloride is generally carried out in a batch reactor such as that shown in Fig. 3-20. A typical recipe includes 180 parts water and 100 parts vinyl chloride plus small amounts of dispersants (<1 part), monomer-soluble initiator, and chain-transfer agent (trichloroethylene). All components except monomer are charged into the reactor, which is then partially evacuated. Vinyl chloride is drawn in, sometimes by using pressurized oxygen-free nitrogen to force monomer into the reactor. The reactants are then heated in the closed system to about 50°C and the pressure rises to about 0.5 MPa. The temperature is maintained at about 50°C as polymerization proceeds. When the pressure is about
0.05 MPa, corresponding to about 90% conversion, excess monomer is vented off to be recycled. Removal of residual monomer typically involves passing the reaction mixture through a countercurrent of steam. The reaction mixture is then cooled, and the polymer separated, dried in hot air at about 100°C, sieved to remove any oversized particles, and stored. Typical number-average molecular weights for commercial PVC are in the range 30,000–80,000.

Poly(vinyl chloride) has very low crystallinity but achieves strength because of the bulky polymer chains (a consequence of the large Cl groups on every other carbon). This is apparent in the high $T_g$ of 81°C, although $T_g$ is not so high that processing by a variety of techniques (injection molding, extrusion, blow molding, calendering) is impaired. Poly(vinyl chloride) is relatively unstable to light and heat with the evolution of hydrogen chloride, which can have deleterious effects on the properties of nearby objects (e.g., electrical components) as well as physiological effects on humans. The commercial importance of PVC would be greatly reduced were it not for the fact that this instability can be controlled by blending with appropriate additives such as metal oxides and carbonates as well as fatty acid salts. These additives stabilize PVC by slowing down the dehydrochlorination reaction and absorption of the evolved hydrogen chloride.

Poly(vinyl chloride) is a very tough and rigid material with extensive applications. Its range of utilization is significantly expanded by plasticization, which converts rigid PVC,
to flexible PVC. Plasticization involves blending PVC with plasticizers (e.g., diisooctyl phthalate, tritolyl phosphate, epoxidized oils). The plasticizer imparts flexibility by acting effectively as an “internal lubricant” between PVC chains. (Plasticization accomplishes for PVC what copolymerization and polymer blending accomplishes for polystyrene—changing a rigid material into a flexible one. The plasticization route is not useful for polystyrene as PS is not so compatible with plasticizers.) Blending of PVC with rubbery polymers to improve impact strength is also practiced. More than 14 billion pounds of PVC products, about evenly divided between rigid and flexible grades, were produced in 2001 in the United States. Rigid pipe for home and other construction accounts for more than 40% of the total PVC market. Vinyl siding, window frames, rain gutters, and downspouts account for another 10–15%. Packaging applications (bottles, box lids, blister packaging) account for about 8%. More than 10% of PVC is used for flooring (large sheet and tile). Other applications include wire and cable insulation for buildings, telecommunications and appliance wiring, garden hose, surgical and other protective gloves, and coated products.

Trade names for PVC include Carina, Corvic, Darvic, Geon, Koroseal, Marvinol, Nipeon, Opalon, and Vygen. The generic term vinyl is often used for PVC products.

3-14c-2 Other Members of Vinyl Family

More than 500 million pounds of poly(vinyl acetate) (PVAc), poly(vinylidene chloride), and their copolymers and polymers derived from them are produced annually in the United States. PVAc does not have sufficient strength for producing the types of products obtained from polyethylene, polystyrene, and poly(vinyl chloride) since it is noncrystalline and has a $T_g$ of only 28°C. However, poly(vinyl acetate) (XLI) and its copolymers find uses as water-based paints; as adhesives for paper, textiles, and wood (labeling, spackling compound, white glue); and as a sizing or coating compound for paper and textiles. Emulsion polymerization is the predominant commercial process with the resulting latices used directly for most applications. PVAc is also used to produce poly(vinyl alcohol) and acetals of the latter (Sec. 9-4). Poly(vinyl alcohol) (PVA) is used as thickening agents, coatings, adhesives, and for water-soluble packages for bath salts, bleaches, detergents, and other materials. The formal and butyral derivatives of PVA are used, respectively, as heat-resistant wire enamel insulation and the interlayer in safety glass laminates.

Poly(vinylidene chloride) (XLII) and its copolymers with vinyl chloride, acrylonitrile, and acrylates, usually produced by the suspension or emulsion process, are useful as oil, fat, oxygen, and moisture-resistant packaging films (Saran wrap), containers, coatings, tank liners, and monofilaments in drapery fabrics and industrial filter cloths.
3-14d  Acrylic Family

The acrylic family of polymers includes polymers and copolymers of acrylic and methacrylic acids and esters, acrylonitrile, and acrylamide [Kine and Novak, 1985; Nemec and Bauer, 1985; Peng, 1985; Thomas and Wang, 1985].

3-14d-1  Acrylate and Methacrylate Products

Close to 2 billion pounds of polymeric products based on acrylic and methacrylic esters are produced annually in the United States, about evenly divided between acrylates and methacrylates. A substantial fraction of the methacrylate products are copolymers. Most of the acrylate products are copolymers. The copolymers contain various combinations of acrylate and/or methacrylate monomers, including combinations of ester and acid monomers. Methyl methacrylate (MMA) is by far the most important methacrylate ester monomer, accounting for 90% of the volume of methacrylic ester monomers. Ethyl and n-butyl acrylates account for about 80% of the total volume of acrylate ester monomers.

Poly(methyl methacrylate) (PMMA) is polymerized by solution, suspension, and emulsion processes. PMMA is completely amorphous but has high strength and excellent dimensional stability due to the rigid polymer chains \( T_g = 105^\circ C \). It has exceptional optical clarity, very good weatherability, and impact resistance (can be machined) and is resistant to many chemicals, although attacked by organic solvents. Polycrylates differ considerably from the polymethacrylates. They are much softer since the polymer chains are not nearly as rigid [e.g., poly(ethyl acrylate), \( T_g = -24^\circ C \)], due to the absence of the methyl groups on alternating carbons of the polymer chains. Polymethacrylates tend to be used as shaped objects, while polyacrylates find applications requiring flexibility and extensibility.

![Chemical structure of PMMA]

Various rigid PMMA products, such as sheet, rod, and tube, are produced by bulk polymerization in a casting process. Polymerization is carried out in stages to allow easier dissipation of heat and control of product dimensions since there is a very large (21%) volume contraction on polymerization. Partially polymerized monomer (about 20% conversion) is produced by heating for about 10 min at 90°C with a peroxide. [Uncatalyzed thermal polymerization for much longer periods (about 2 hr) is also used to achieve greater control.] The syrup is cooled to ambient temperature and poured into a mold, and then the assembly is heated in a water or air bath to progressively higher temperatures. The maximum temperature used is 90°C, since higher temperatures can lead to bubble formation in the product as the boiling point of methyl methacrylate is 100.5°C. The mold often involves spacer units, which, together with clamps, exert pressure on the polymerizing system to accommodate shrinkage during polymerization. Continuous cast polymerization processes are also used extensively. Bulk polymerization and suspension polymerization are used to produce polymethacrylate molding powders.

Applications for rigid methacrylate polymer products include signs and glazing substitute for safety glass and to prevent vandalism (school, home, and factory windows, patio window doors, aircraft windows and canopies, panels around hockey rinks, bank-teller windows, bath and shower enclosures, skylights), indoor and outdoor lighting, lenses, diffusers, and louvers, architectural structures (domes over pools and stadia, archways between buildings), bathtubs.
and sanitary fixtures, optical fibers for light transmission, plastic eyeglass lenses, dentures and dental filling materials, and contact lenses (hard and soft).

Solution and emulsion polymerizations are used to produce acrylate and methacrylate polymer products for nonrigid applications. These applications include coatings (interior and exterior paints, including automotive paints), textiles (finishes for improving abrasion resistance, binding pigments, reducing shrinkage of wool, drapery and carpet backing), additives for engine oils and fluids, and caulks and sealants.

Trade names for acrylate and methacrylate polymer products include Acrylite, Dicalite, Lucite, Plexiglas, and Rhoplex.

### 3-14d-2 Polyacrylonitrile

The most important commercial processes for polyacrylonitrile (XLIII) are solution and suspension polymerizations. Almost all the products containing acrylonitrile are copolymers. Styrene-acrylonitrile (SAN) copolymers are useful as plastics (Sec. 6-8a).

\[
\text{CN} \quad \text{CH}_2\text{CH} \quad \text{CH}_2\text{CH}_2\text{CN} \quad n_{\text{XLIII}}
\]

More than 300 million pounds of modacrylic and acrylic fibers are produced annually in the United States [trade names: Acratlon (now Monsanto fiber), Dynel, Orlon, Verel]. Acrylic fibers contain at least 85% by weight of acrylonitrile, while modacrylic fibers contain less than 85% acrylonitrile but no less than 35%. Halogen-containing monomers, such as vinyl chloride, vinylidene chloride, and vinyl bromide, are copolymerized with acrylonitrile to impart flame retardancy. Methyl acrylate and vinyl acetate are used to increase the solubility of the polymer in solvents used for spinning of fibers. Monomers with acidic or basic groups are used to improve dyeability with basic and acid dyes, respectively. Acrylic and modacrylic fibers are the only fibers made from a monomer with a carbon–carbon double bond. Acrylonitrile is the only such monomer with a sufficiently polar group (nitrile) to yield a polymer with the high secondary forces required in a fiber. All other fibers are made from condensation polymers such as polyesters and polyamides. (The only other exception to this generalization is polypropene; see Sec. 8-11d).

Acrylic and modacrylic fibers have a wool-like appearance and feel, and excellent resistance to heat, ultraviolet radiation, and chemicals [Bajaj and Kumari, 1987]. These fibers have replaced wool in many applications, such as socks, pullovers, sweaters, and craft yarns. Other applications include tenting, awning fabric, and sandbags for rivershore stabilization. The use of acrylic and modacrylic fibers in carpets is low since these materials do not hold up well to recycling through hot–humid conditions. This also prevents its use in the easy-care garment market.

### 3-14d-3 Other Members of Acrylic Family

From the viewpoint of sales volume, all other members of the acrylic family constitute a small fraction of the total. However, many of them are useful specialty products. Polycrylamide (XLIV), poly(acrylic acid) (XLV), and poly(methacrylic acid) (XLVI) and some of their copolymers are used in various applications that take advantage of their solubility in water. Poly(acrylic acid) and poly(methacrylic acid) are used as thickening agents (water
used in secondary recovery of oil, rubber emulsions applied to fabrics to produce nonslip backing for floor covering), adhesives, dispersants for inorganic pigments in paints, flocculants (to aggregate suspended particles in metal recovery, clarification of waste and potable waters), and crosslinked ion-exchange resins. Polyacrylamides, often containing ionic comonomers, are used as flocculants in industrial waste and municipal drinking water treatments, papermaking, and mining; crosslinked polyacrylamide is used in gel electrophoresis.

3-14e Fluoropolymers

The fluoropolymer family consists of polymers produced from alkenes in which one or more hydrogens have been replaced by fluorine. The most important members of this family are polytetrafluoroethylene (PTFE) (XLVII), polychlorotrifluoroethylene (PCTFE) (XLVIII), poly(vinyl fluoride) (PVF) (XLIX), poly(vinylidene fluoride) (PVDF) (L); copolymers of tetrafluoroethylene with ethylene, perfluoropropyl vinyl ether, and perfluoropropene; and the copolymer of ethylene and chlorotrifluoroethylene. The fluoropolymers are obtained mainly by suspension polymerization; emulsion polymerization is also practiced. Commercial polymerization in supercritical carbon dioxide (scCO₂) (Sec. 2-17b) was achieved by DuPont in 2002 for the copolymerization of tetrafluoroethylene with hexafluoropropene and a perfluoroalkyl vinyl ether. The molecular weights of the polymers are high, ranging up to $10^5$-$10^6$ for PTFE, apparently due to the lack of appreciable chain-transfer reactions and the precipitation of growing radicals (leading to greatly decreased termination).

The commercial production of fluoropolymers is very small compared to commodity polymers such as polyethylene or PVC. But the production is still significant on an absolute basis, about 20 million pounds annually in the United States, and it finds a wide range of important specialized applications [Gangal, 1989]. PTFE is the largest-volume fluoropolymer. This family of polymers offer unique performance. Within the fluoropolymers are polymers that withstand a wide variety of chemical environments and are useful at temperatures as low as $-200^°C$ and as high as $260^°C$. Most fluoropolymers are totally insoluble in common organic solvents and unaffected by hot concentrated acids and bases. They have outstanding electrical resistance and low coefficient of friction (self-lubricating and nonstick parts), and will not support combustion. The properties of polytetrafluoroethylene, high crystallinity, $T_m$ of $327^°C$, and very high melt viscosity, preclude its processing by the usual techniques for plastics. Fabrication requires the powder and cold extrusion techniques of metal forming. The various copolymers of tetrafluoroethylene and the other fluoropolymers, possessing lower $T_m$ and crystallinity, were developed to overcome the lack of melt processability of PTFE.
Fluoropolymer applications include electrical (coaxial cable, tape, spaghetti tubing), mechanical (seals, piston rings, bearings, antistick coatings for cookware, self-lubricating parts), chemical (pipe liners, overbraided hose liners, gaskets, thread sealant tapes), and micropowders used in plastics, inks, lubricants, and lacquer finishes. A unique application of fluoropolymers is protection of the Statue of Liberty against corrosion.

Trade names for fluoropolymers include Aflon, Fluon, Halar, Hostaflon, Kel-F, Kynar, Polyflon, Tedlar, Teflon, and Tefzel.

3-14f Polymerization of Dienes

The polymerization of dienes (i.e., monomers with two double bonds per molecule) can proceed in a variety of ways depending on the chemical structure of the diene. Dienes are classified as conjugated or nonconjugated dienes depending on whether the two double bonds are conjugated with each other. Conjugated dienes are also referred to as 1,3-dienes. The polymerization of nonconjugated dienes often yields branched and crosslinked products. Nonconjugated dienes are often used to bring about crosslinking in other alkene monomers by the technique of copolymerization (Sec. 6-6a). Certain nonconjugated dienes undergo a special type of cyclization polymerization (cyclopolymerization) by an alternating intramolecular reaction mechanism (Sec. 6-6b).

The polymerization of conjugated dienes is of special interest. Two different types of polymerization reactions occur with 1,3-dienes such as 1,3-butadiene, isoprene(2-methyl-1,3-butadiene), and chloroprene (2-chloro-1,3-butadiene)

\[
\begin{align*}
\text{CH}_2=\text{CH} &= \text{CH} \equiv \text{CH}_2 \\
\text{CH}_3 &= \text{C} \equiv \text{CH} \equiv \text{CH}_2 \\
\text{Cl} &= \text{C} \equiv \text{CH} \equiv \text{CH}_2
\end{align*}
\]

One of the polymerization routes involves polymerization of one or the other of the double bounds in the usual manner. The other route involves the two double bonds acting in a unique and concerted manner. Thus addition of an initiating radical to a 1,3-diene such as 1,3-butadiene yields an allylic radical with the two equivalent resonance forms LI and LII

\[
\begin{align*}
\text{R} \cdot + \text{CH}_2=\text{CH} &= \text{CH} \equiv \text{CH}_2 & \Rightarrow & \text{LI} \\
\text{R} \cdot + \text{CH}_2=\text{CH} &= \text{CH} \equiv \text{CH}_2 & \Rightarrow & \text{LII}
\end{align*}
\]

Propagation may then occur by attachment of the successive monomer units either at carbon 2 (propagation via LI) or at carbon 4 (propagation via LII). The two modes of polymerization are referred to as 1,2-polymerization and 1,4-polymerization, respectively. The polymers obtained have the repeating structures

\[
\begin{align*}
\text{CH}_2=\text{CH} \equiv \text{CH} \equiv \text{CH}_2 & \quad \text{1,2-Polymerization} \\
\text{CH}_2=\text{CH} \equiv \text{CH} \equiv \text{CH}_2 & \quad \text{1,4-Polymerization}
\end{align*}
\]
and are named 1,2-poly-1,3-butadiene and 1,4-poly-1,3-butadiene, respectively. Both polymers are unsaturated—the 1,2-polymer has pendant unsaturation while there is unsaturation along the polymer chain in the 1,4-polymer. The polymerization of 1,3-dienes is considered in greater detail in Sec. 8-6.

The polymerization and copolymerization of 1,3-dienes is of commercial importance in the annual production of over 4 billion pounds of elastomers and about 2 billion pounds of plastics in the United States (Secs. 6-8 and 8-10).

3-14g Miscellaneous Polymers

3-14g-1 Poly(p-xylylene)

Pyrolysis of p-xylene yields poly(p-xylylene) [IUPAC: poly(1,4-phenyleneethylene)] [Errede and Szwarc, 1958; Humphrey, 1984; Itoh, 2001; Lee, 1977–1978; Lee and Wunderlich, 1975; Surendran et al., 1987]. The reaction is carried out by pyrolyzing p-xylene at temperatures of up to 950°C (in the absence of oxygen) to yield di-p-xylylene (LIII) (also named [2,2]-paracyclophane), which is isolated as a stable solid. Subsequent polymerization of di-p-xylylene to poly(p-xylylene) involves vaporization of di-p-xylylene by heating to about 160°C at 1 torr (1.3 × 10^2 Pa) followed by cleavage to p-xylylene diradical (LIV) by heating at 680°C at 0.5 torr. The diradical nature of p-xylylene was shown by ESR and trapping of α,α′-diiodo-p-xylylene with iodine. p-Xylylene is very reactive and can be trapped only in dilute solution at low temperature; the half-life at −78°C and 0.12 M is about 21 h. p-Xylylene spontaneously polymerized with crystallization when condensed on surfaces kept at temperatures below ~30°C at 0.1 torr. The reaction is extremely fast; quantitative conversion of di-p-xylylene to poly(p-xylylene) takes place in a fraction of a second. The overall polymerization process, often referred to as transport polymerization, involves transport of the monomer (p-xylylene) in the gas phase under vacuum from its place of synthesis to the solid surface on which it polymerizes. This physical process makes poly(p-xylylene) useful
commercially for forming thin coatings on objects with true conformality of the coating to all surfaces, including deep penetration into small spaces. Poly(p-xylene) (trade name: Parylene N; IUPAC name: poly[1,4-phenyleneethylene]) and the corresponding polymers derived from 2-chloro-p-xylene and 2,5-dichloro-p-xylene (Parylenes C and D) have a modest but growing importance in the electronics industry for coating and encapsulating delicate microcircuitry for protection from hostile environments. The polymers are crystalline ($T_m$ near or above 400°C) with excellent mechanical and electrical insulating characteristics at temperatures as low as −200°C and as high as 200°C. Other potential uses include coating of orthopedic parts (bone pins and joint prosthesis) to make them biocompatible and conservation of archival and artifact objects.

Polymerization is initiated by coupling of two $p$-xylylene radicals to form a diradical ($LV$), which then grows by the addition of $p$-xylylene at both of its radical centers:

\[
\begin{array}{ccccc}
\cdot\text{CH}_2-\text{CH}_2 & \rightarrow & \cdot\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}_2-
\end{array}
\]

Whether the formation of poly($p$-xyylene) should be included in this chapter is not clear. Decisive data are not available to indicate the classification of this polymerization as a step or chain reaction. The formation of high polymer occurs instantaneously when $p$-xylylene contacts the cool surface, precluding the evaluation of polymer molecular weight versus conversion. Also, the mode of termination for this reaction is unknown.

One aspect of the polymerization that is well established is the initiation step when di-$p$-xylylene is pyrolyzed. An alternate initiation mode involving the direct formation of the diradical $LV$ from $LIII$ by cleavage of only one of the two CH$_2$–CH$_2$ bonds is ruled out from experiments with monosubstituted di-$p$-xylenes. When acetyl-di-$p$-xylylene is pyrolyzed and the pyrolysis vapor led through successive condensation surfaces at temperatures of 90 and 25°C, respectively, the result is the formation of two different polymers neither of which is poly(acetyl-di-$p$-xylylene). Pyrolysis yields acetyl-$p$-xylylene and $p$-xylylene

\[
\begin{array}{ccccc}
\text{CH}_2-\text{CH}_2 & \rightarrow & \text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}_2-
\end{array}
\]

which undergo separate polymerizations at different condensation temperatures. Poly(acetyl-$p$-xylylene) is produced at the 90°C surface and poly($p$-xylylene) at the 25°C surface.
Transport polymerization has also been studied with other monomers, including methylene and other carbenes (phenylcarbene, 1,4-phenylenecarbene), silylenes such as :SiF₂ and germynes such as :GeCl₂ and :GeF₂ [Lee, 1977–1978; Lee and Wunderlich, 1978].

\[
\text{CH}_2=\text{CO} \text{ or } \text{CH}_2=\text{NN} \xrightarrow{-\text{CO or N}_2} \cdot \text{CH}_2 \xrightarrow{} \left( \text{CH}_2 \right)_n \tag{3-214}
\]

3-14g-2 Poly(N-vinylcarbazole)

Poly(N-vinylcarbazole) (PVK) is produced by the polymerization of \( N \)-vinylcarbazole (LVII). PVK has been used as a capacitor dielectric since it has good electrical resistance over a range of temperatures and frequencies. Other applications include electrical switch parts, coaxial cable separators, and electroluminescent devices. It is also used in electrostatic dry copying (xerography) machines, a consequence of its photoconductivity.

3-14g-3 Poly(N-vinylpyrrolidinone)

Poly(N-vinylpyrrolidinone) (PVP) is obtained by polymerization of \( N \)-vinylpyrrolidinone (LVII). The largest use is in hair sprays and wave sets because of its property as a film former, with good adhesion to hair, film luster, and ease of removal by washing with water. PVP is also used in hand creams and liquid makeup. Aqueous solutions of PVP complexed with iodine (Betadine) are useful in the management of wounds and incisions for preventing infections. PVP also finds applications in the textile industry because of its affinity for many dyestuffs; it is used for dye stripping and in the formulation of sizes and finishes. PVP has also been considered as a blood plasma substitute.

3-15 LIVING RADICAL POLYMERIZATION

3-15a General Considerations

Typical chain polymerization systems, both radical and ionic, proceed with accompanying chain-breaking reactions because of the type of propagating centers and/or the reagents

[Figure: LVII]
present. Bimolecular termination and chain transfer are ever present in radical chain polymerization and limit the lifetime of propagating radicals. Chain polymerizations without chain-breaking reactions, referred to as living polymerizations, would be highly desirable because they would allow the synthesis of block copolymers by the sequential addition of different monomers (Eq. 3-215). A reactive species $I^\ast$ initiates polymerization of monomer A.

$$I^\ast \xrightarrow{A} I-A_n^\ast \xrightarrow{B} I-A_n^\ast-B_m^\ast \quad (3-215)$$

When the polymerization of monomer A is complete, the reactive centers are intact because of the absence of chain-breaking reactions. Addition of a second monomer B results in the formation of a block copolymer containing a long block of A repeat units followed by a long block of B repeat units. It is possible to continue the sequential propagation by adding a third batch of monomer, or one can terminate the process by the addition of a reagent to terminate the propagating centers.

Block copolymers have commercial potential for obtaining products that can incorporate the desirable properties of two or more homopolymers. This potential has led to an intense effort to find reaction systems that proceed as living polymerizations. Some anionic chain polymerizations proceed as living polymerizations under conditions where no viable chain-breaking reactions occur, and this has resulted in useful block copolymers (Sec. 5-4).

The situation is very different for conventional (nonliving) radical polymerizations since the lifetime of propagating radicals in these systems is very short (typically less than a second or, at most, a few seconds) because of the ever-present occurrence of normal bimolecular termination (coupling and/or disproportionation). Living radical polymerizations have been achieved by minimizing normal bimolecular termination and prolonging the lifetime of living polymers into hours or longer through the introduction of dormant states for the propagating species. This is achieved through alternate modes of reaction for the propagating radicals, specifically, by either reversible termination or reversible transfer. Living radical polymerizations have good commercial potential for materials synthesis because many more monomers undergo radical polymerization compared to ionic polymerization (Sec. 3-1b).

Living radical polymerization (LRP) with reversible termination generally proceeds as follows:

$$R-Z \xrightarrow{R^\ast Z} R^\ast + Z^\ast \quad (3-216)$$

Reactive radical Stable radical

$$\xrightarrow{M}$$

$$RM_n^\ast \quad \text{Propagating radical} \quad (3-217)$$

Bimolecular termination

$$RM_n^\ast - Z \quad \text{Dormant species} \quad (3-218)$$

The initiator $RZ$ undergoes homolytic bond breakage, either simply by heating or by a more complex process of activation by some added reagent, to produce one reactive and one stable free radical (Eq. 3-216). The reactive radicals quickly initiate polymerization (Eq. 3-217), but the stable radicals are too stable to initiate polymerization. The technologically important
living systems are those in which all the initiator decomposes at once or in a very short time period so that all propagating radicals grow for very close to the same time. Fast initiation is important, but it is the fast equilibrium between the propagating radical and dormant species with an appropriate equilibrium constant that determine the living characteristics of these reaction systems. The equilibrium constant must be low but not too low; that is, the concentration of propagating radical must be sufficient to achieve a reasonable propagation rate but not so high that normal bimolecular termination becomes important.

The concentrations of propagating and stable radicals are equal at the start, but there is a rapid and drastic change in concentration. The most important feature of living radical polymerization is a buildup in the concentration of the stable radicals because of their stability, the normal termination of initiating and propagating radicals in the early stage of polymerization, and the irreversible addition of monomer to the initiating radicals. The equilibria in Eqs. 3-216 and 3-218 are shifted to the right—toward the dormant species. Overall, the concentration of stable radicals increases to at least 4 orders of magnitude greater than the concentration of propagating radicals. The concentration of propagating radicals is about the same or somewhat lower than that in traditional (i.e., nonliving) radical polymerizations.

The stable radical acts as a controlling or mediating agent because it is sufficiently reactive to couple rapidly with propagating chains to convert them reversibly into dormant, nonpropagating species. The dormant species are in equilibrium with propagating radicals. The equilibrium favors the dormant species by several orders of magnitude. The concentration of dormant species is about 6 orders of magnitude greater than the concentration of propagating radicals. The concentration of dormant species is about 6 orders of magnitude greater than the concentration of propagating radicals. Typically, the propagating radical concentrations are $10^{-7} - 10^{-9} \text{M}$ while the concentration of dormant species is $10^{-1} - 10^{-3} \text{M}$. The overall result is that, with the introduction of the dormant state for living polymers, the bimolecular termination of living polymers is suppressed, and the average lifetime for living polymers is increased by at least 4 orders of magnitude. The stable radical is often called the persistent radical, and its suppression of bimolecular termination between living polymers is called the persistent radical effect (PRE). The persistent radical effect with its suppression of bimolecular termination of living polymers coupled with the reversible reaction of propagating radicals with the persistent radicals form the basis for living radical polymerization. Otsu and coworkers [Otsu, 2000; Otsu et al., 1982] were the first to suggest this idea. Fischer and coworkers have described some of the quantitative aspects of PRE [Fischer, 1999, 2001; Souaille and Fischer, 2000, 2002].

When monomer conversion is complete, a second batch of a different monomer can be added to form a block copolymer. If the second batch of monomer is not added quickly and the reaction conditions not altered to preserve the dormant species, there will be a continuous deterioration of the reaction system’s ability to form block copolymers because of bimolecular termination between propagating radicals since no other competitive reaction is possible in the absence of monomer. The equilibrium between dormant species and radicals will be pushed toward the propagating radicals and their subsequent irreversible bimolecular termination.

There has been considerable debate on the correct terminology to use for these systems because the propagating radicals do not have a significant lifetime in the absence of monomer as do the anionic living systems. Terms such as controlled, “living,” and pseudoliving have been used instead of living to distinguish these radical systems from the anionic living systems. This proliferation of terms adds confusion, not clarity [Darling et al., 2000; Penczek, 2000]. It seems simpler and reasonable to define living polymerizations as those systems where irreversible terminations and transfers are sufficiently suppressed so that block copolymers can be synthesized by sequential addition of monomers.
Living radical polymerizations include *atom-transfer radical polymerization* (ATRP) and *stable free-radical polymerization* (SFRP), which proceed with reversible termination, and *reversible addition–fragmentation transfer* (RAFT), which proceeds with reversible chain transfer. Until the extensive exploration of these living polymerizations starting in the mid-1990s, radical polymerization was thought to be a mature process with relatively little left to discover. There is an ongoing effort to exploit the synthetic possibilities of living radical polymerization. Much of the driving force for the effort derives from the belief that well-defined materials from living radical polymerization will offer substantial advantages to build nanostructures for microelectronics, biotechnology, and other areas.

### 3-15b Atom Transfer Radical Polymerization (ATRP)

#### 3-15b-1 Polymerization Mechanism

ATRP, SFRP, and RAFT differ in the method of radical generation. Radical generation in atom-transfer radical polymerization involves an organic halide undergoing a reversible redox process catalyzed by a transition metal compound such as cuprous halide [Kamigaito et al., 2001; Lutz and Matyjaszewski, 2002; Matyjaszewski, 1998a,b, 2002; Matyjaszewski and Xia, 2001; Nanda and Matyjaszewski, 2003; Patten and Matyjaszewski, 1998, 1999; Wang and Matyjaszewski, 1995a; Yoshikawa et al., 2003]. ATRP proceeds as described in Eqs. 3-219 through 3-221:

\[
R\text{Br} + CuBr(L) \xrightarrow{k_a} R\cdot + CuBr_2(L) + Cu(L) (3-219)
\]

\[
RM_n^* + CuBr_2(L) \xrightarrow{k_d} RM_nBr + CuBr(L) (3-220)
\]

where \( L \) is a ligand that complexes with the cuprous salt and helps to solubilize it in the organic reaction system. \( k_a \) are \( k_d \) are rate constants for activation and deactivation of the halide initiator, with \( K = k_a/k_d \). Activation of the initiator involves the CuBr metal center undergoing an electron transfer with simultaneous halogen atom abstraction and expansion of its coordination sphere. \( R\cdot \) is the reactive radical that initiates polymerization. \( CuBr_2(L) \) is the persistent (metallo)radical that reduces the steady-state concentration of propagating radicals and minimizes normal termination of living polymers. The initiator and persistent (metallo)radical are also called the *activator* and *deactivator*, respectively.

The free-radical nature of ATRP is well established through a number of studies [Matyjaszewski et al., 2001]. The effects of inhibitors and retarders, solvents, and chain-transfer agents are the same in ATRP as in conventional radical polymerization. The regioselectivity, stereoselectivity, and copolymerization behaviors are also the same.

The concentration of propagating radicals in ATRP is obtained as

\[
[R\cdot] = \frac{K[I][Cu^{+}]}{[Cu^{2+}]} (3-222)
\]
from the equilibrium expression for Eq. 3-219. Combination with the expression for propagation (Eq. 3-22) yields the polymerization rate as

$$R_p = \frac{k_pK[M][I]}{[Cu^{+}]} \left(\frac{M}{C_1^{38}}\right)^{\frac{1}{2}} \left(\frac{I}{C_1^{38}}\right)^{\frac{1}{2}} \frac{Cu^+/C_1^{38}}{Cu^{2+}/C_1^{38}}$$

(3-223)

where I is the initiator, RBr in this case.

The polymerization rate is expressed as the change in monomer concentration with time:

$$\ln \left(\frac{[M]}{[M]_0}\right) = \frac{k_pK[I]}{[Cu^{+}]} t$$

(3-224)

A successful ATRP requires fast and quantitative initiation (activation of RBr) so that all propagating species begin growth at the same time, which results in a narrow molecular weight distribution. Rapid reversible deactivation of propagating radicals is needed to maintain low radical concentrations and minimize normal termination of living polymers. This further ensures a narrow molecular weight distribution because all propagating chains grow at the same rate and for the same length of time. The number-average degree of polymerization for a living polymerization under these conditions is given by

$$\overline{X}_n = \frac{[M]_0 - [M]}{[I]_0} = \frac{p[M]_0}{[I]_0}$$

(3-225)

where $[M]_0$ and $[I]_0$ are initial concentrations of monomer and initiator, respectively. $[M]$ and $p$ are the monomer concentration and fractional conversion of monomer at any time in the reaction. The number-average degree of polymerization is $[M]_0/[I]_0$ at complete conversion.

Fig. 3-21  Plots of $\ln([M]_0/[M])$ versus time for ATRP polymerizations of styrene at 110°C with CuBr, 1-phenylethyl bromide (I), and 4,4-di-5-nonyl-2,2'-bipyridine (L). Bulk polymerization (●): $[M] = 8.7\, M$, $[CuBr]_0 = [L]_0/2 = [I] = 0.087\, M$; Solution polymerization in diphenyl ether (○): $[M] = 4.3\, M$, $[CuBr]_0 = [L]_0/2 = [I] = 0.045\, M$. After Matyjaszewski et al. [1997] (by permission of American Chemical Society, Washington, DC); an original plot, from which this figure was drawn, was kindly supplied by Dr. K. Matyjaszewski.
Figures 3-21 and 3-22 show results in the ATRP polymerization of styrene using 1-phenylethyl bromide as the initiator, CuBr as catalyst (activator), and 4,4-di-5-nonyl-2,2'-bipyridine as ligand [Matyjaszewski et al., 1997]. Figure 3-21 shows the decrease in monomer concentration to be first-order in monomer, as required by Eq. 3-223. The linearity over time indicates that the concentration of propagating radicals is constant throughout the polymerization. The first-order dependencies of $R_p$ on monomer, activator, and initiator and the inverse first-order dependence on deactivator have been verified in many ATRP reactions [Davis et al., 1999; Patten and Matyjaszewski, 1998; Wang et al., 1997].

The number-average molecular weight increased linearly with conversion as required by Eq. 3-224. This behavior defines a living polymerization in which all (or nearly all) propagating chains have the same lifetime, starting at essentially the same time (i.e., fast initiation) and growing with negligible occurrence of chain-breaking reactions until high conversion of monomer is reached. The polymer should be approximately monodisperse (i.e., $X_w \simeq X_n$) under certain conditions. The polydispersity index (PDI) ($X_w/X_n$) is given by

$$
\frac{X_w}{X_n} = 1 + \left\{ \frac{[I]}{k_p} \right\} \left\{ \frac{2}{k_d[D]} \right\} \left\{ \frac{1}{p} - 1 \right\}
$$

(3-226)

where $D$ is the deactivating agent, namely, the persistent radical, which is CuBr$_2$ in this system [Gromada and Matyjaszewski, 2001, 2002; Litvinenko and Muller, 1997; Matyjaszewski and Xia, 2001]. The molecular weight distributions are narrower with lower initiator concentrations, higher conversions, rapid deactivation (higher values of $k_d$ and $[D]$), and lower $k_p$ values. When these conditions are fulfilled the molecular weight distribution follows the Poisson distribution [Flory, 1940; Peebles, 1971]

$$
\frac{X_w}{X_n} = 1 + \frac{X_n}{(X_n + 1)^2}
$$

(3-227)

![Fig. 3-22](image-url) Dependence of number-average molecular weight ($\bullet$) and polydisperisty index ($\triangle$) on monomer conversion for ATRP polymerization of bulk styrene at 110°C with CuBr, 1-phenylethyl bromide (I), and 4,4-di-5-nonyl-2,2'-bipyridine (L). $[M] = 0.087 \, M$; $[CuBr]_0 = [L]_0/2 = [I] = 0.087 \, M$. After Matyjaszewski et al. [1997] (by permission of American Chemical Society, Washington, DC); an original plot, from which this figure was drawn, was kindly supplied by Dr. K. Matyjaszewski.
which can be approximated by

\[
\frac{X_w}{X_n} = 1 + \frac{1}{X_n}
\]  (3-228)

Equation 3-227 shows that for any except a very-low-molecular-weight polymer, the size distribution will be very narrow with \(\frac{X_w}{X_n}\) being close to unity. For a polymer of number-average degree of polymerization of 50 having a Poisson distribution, the PDI would be 1.02. For the ATRP polymerization in Figure 3-22, PDI is about 1.05, very close to the theoretical value. Many ATRP polymerizations have somewhat broader distributions (PDI ≤ 1.2–1.3) for two reasons. First, there is the very initial period (as much as 5% conversion) before the persistent radical (deactivator) concentration has grown sufficiently large to suppress normal termination. Most of this problem can be avoided by initially adding CuBr₂ (~10 mol% of CuBr). Second, at very high conversion (~90%), the polymerization rate decreases significantly such that normal termination is not sufficiently suppressed. For the successful synthesis of block copolymers, the second monomer should be added no later than ~90–95% conversion, not at 100% conversion.

3-15b-2 Effects of Components of Reaction System

A variety of monomers, including styrene, acrylonitrile, (meth) acrylates, (meth) acrylamides, 1,3-dienes, and 4-vinylpyridine, undergo ATRP. ATRP involves a multicomponent system of initiator, an activator catalyst (a transition metal in its lower oxidation state), a deactivator (the transition state metal in its higher oxidation state) either formed spontaneously or deliberately added, ligands, and solvent. Successful ATRP of a specific monomer requires matching the various components so that the dormant species concentration exceeds the propagating radical concentration by a factor of \(~10^6\).

Various organic halides are used, including alkyl halides such as CHCl₃ and CCl₄, allyl and benzyl halides, α-haloesters, α-halo ketones, α-halonitriles, and sulfonyl halides. Fast and quantitative initiation is needed to achieve narrow molecular weight distributions, but an initiator that decomposes too rapidly results in increased normal bimolecular termination of propagating radicals. Bromides are more reactive than chlorides, iodides are highly reactive but undergo light-induced side reactions, and fluorides are unreactive. The initiator reactivity should be matched to the monomer reactivity. In general, this is achieved by using a halide with an organic group similar in structure to the propagating radical, for example, benzyl halide, α-haloester, and α-halonitrile for styrene, acrylate, and acrylonitrile polymerizations, respectively.

The metal catalyst must have two oxidation states easily accessed by a one electron transfer, an affinity for halogen, an expandable coordination sphere to accommodate the halogen, and a strong complexation with the ligand. The catalyst is the key to ATRP since it determines the position of equilibrium (value of \(K\)) and rate of exchange between dormant and propagating species. Various middle and late transition metals (groups 6–11) have been investigated. Catalysts based on copper are the most studied and have found the greatest utility, as they are useful irrespective of the monomer. Proper functioning of a metal catalyst requires appropriate ligands. Ligands solubilize the transition metal salt in organic media and adjust the redox potential of the metal center for appropriate activity. For copper catalysts, bidentate and multidentate, but not monodentate, nitrogen ligands work best. Bridged and cyclic ligands as well as branched aliphatic polyamines yield more active catalysts than do simple linear ligands. 4,4-Dialkyl-2,2'-bipyridines and tris-(2-dimethylaminoethyl)amine
are examples of active ligands. Longer alkyl chains in 4,4-dialkyl-2,2'-bipyridine are useful for achieving solubility of the catalyst in the less polar monomers such as styrene. Phosphorus ligands such as triphenyl phosphine are useful for most other transition metals, but not for copper. The optimum ligand to Cu\(^{2+}\) ratio depends in a complex manner on the ligand and counterion. For complex anions such as triflate and hexafluorophosphate, two bidentate or one tetradeutate ligands are needed per Cu\(^{+}\). For bromide counterion, one bidentate ligand or one-half tetradeutate ligand is needed per Cu\(^{+}\). The optimal ratio may change with temperature and solvent. Polymerization rates are lower below the optimum ratio and constant above.

It was noted previously that the addition of some Cu\(^{2+}\) at the beginning of ATRP decreases the amount of normal termination. The initial addition of metallic copper is sometimes advantageous for achieving a faster polymerization as excess Cu\(^{2+}\) undergoes redox reaction with Cu to form Cu\(^{+}\).

ATRP has been carried out in bulk, solution, suspension, and aqueous emulsion. A range of solvents have been used for solution polymerization, including toluene, ethyl acetate, alcohols, water, ethylene carbonate, DMF, and supercritical carbon dioxide. Apart from the usual considerations, one needs to consider if a solvent interacts with and affects the catalyst system, such as by displacement of ligands. Some polymer end groups (e.g., polystyryl halide) can undergo substitution or elimination in polar solvents at polymerization temperatures. ATRP can be carried out in aqueous heterogeneous systems (suspension and emulsion) with proper choice of the components of the reaction system (initiator, activator, deactivator). The components need to be chosen so that they are stable in the presence of water and soluble in the organic phase with minimal solubility in the aqueous phase. In addition to copper catalyst systems [Perrier and Haddleton, 2002], various Ru(II) and Fe(II) halide complexes with triphenylphosphine and cyclopentadienyl or indenyl ligands have been studied [Sawamoto and Kamigaito, 2002].

Temperatures for ATRP are generally in the range 60–120°C, with some polymerizations proceeding at lower temperatures. The polymerization rate increases with increased temperature because both \(k_p\) and \(K (= k_a/k_d)\) increase with increasing temperature. \(K\) increases since the equilibrium process is endothermic in the forward direction (toward propagating radicals). For example, \(\Delta H^0 = 20.1\) kJ mol\(^{-1}\) for styrene polymerization with RBr/CuBr (\(\Delta S^0 = -22\) J K\(^{-1}\) mol\(^{-1}\)). The tendency toward a living polymerization is enhanced at higher temperature since \(E_p > E_t\) and \(k_p/k_d\) increases with temperature. However, an excessively high temperature is counterproductive because chain transfer increases with increasing temperature. There is an optimum temperature for any specific ATRP reaction system. Temperature has other effects on ATRP, such as catalyst solubility, changes in catalyst structure, and changes in the equilibrium constant between dormant species and propagating radicals, which need to be considered.

Depending on the monomer, one needs to adjust the components of the system as well as reaction conditions so that radical concentrations are sufficiently low to effectively suppress normal termination. The less reactive monomers, such as ethylene, vinyl chloride, and vinyl acetate, have not been polymerized by ATRP. Acidic monomers such as acrylic acid are not polymerized because they interfere with the initiator by protonation of the ligands. The carboxylate salts of acidic monomers are polymerized without difficulty. New ATRP initiators and catalysts together with modification of reaction conditions may broaden the range of polymerizable monomers in the future.

ATRP as discussed to this point is normal ATRP which uses RX and a transition metal in its lower oxidation state to establish the equilibrium between dormant and propagating species. Reverse ATRP involves generating the same ATRP system by using a combination of a
conventional radical initiator such as AIBN and a transition metal in its higher oxidation state (e.g., Cu$^{2+}$) [Wang and Matyjaszewski, 1995b]. The initiator generates radicals which react with Cu$^{2+}$ to establish the equilibrium with RX and Cu$^+$. Simultaneous reverse and normal ATRP, using a mixture of radical initiator, RX, Cu$^{2+}$, and Cu$^+$, has also been successful. Reverse ATRP and reverse plus normal ATRP may allow a finer control to obtain high polymerization rate without loss of narrow polydispersity [Gromada and Matyjaszewski, 2001]. Thermal self-initiation is also present for styrene (Sec. 3-4e) in all ATRP processes. ATRP allows the synthesis of well-defined polymers with molecular weights up to \(\sim 150,000\)–200,000. At higher molecular weights normal bimolecular termination becomes significant especially at very high conversion and results in a loss of control. There also appears to be slow termination reactions of Cu$^{2+}$ with both the propagating radicals and polymeric halide [Matyjaszewski and Xia, 2001].

**3-15b-3 Complex Kinetics**

The kinetics described in Sec. 3-15b-1 apply for conditions in which propagating radical concentrations are sufficiently low that normal bimolecular termination is negligible. This corresponds to a quasi-steady-state condition for propagating radicals. It is not quite a true steady state, but the change in radical concentration over the course of the polymerization is small, sufficiently small to escape detection. This condition also corresponds to a quasi-steady-state high concentration of deactivator. To simplify matters, the term *steady state* is used in subsequent discussions. Theoretical considerations as well as experimental studies show that deviations occur when this steady-state condition is not met [Fischer, 1999; Shipp and Matyjaszewski, 1999, 2000; Souaille and Fischer, 2002; Yoshikawa et al., 2002; Zhang et al., 2001, 2002]. The polymerization rate under non-steady-state conditions, specifically, conditions far from steady state, is given by

\[
\ln \frac{[M]_0}{[M]} = \frac{3k_p}{2 \left( \frac{K[I]_0[Cu^+]_0}{3k_t} \right)^{1/3}} t^{2/3}
\]  

(3-229)

Compare Eq. 3-229 with 3-224. The decay in monomer concentration depends on the \(\frac{1}{3}\)-orders of both initiator and activator initial concentrations with no dependence on deactivator concentration and varies with \(t^{2/3}\) under non-steady-state conditions. For steady-state conditions, there are first-order dependencies on initiator and activator and inverse first-order dependence on deactivator and the time dependence is linear. Note that Eq. 3-229 describes the non-steady-state polymerization rate in terms of initial concentrations of initiator and activator. Equation 3-224 describes the steady-state polymerization rate in terms of concentrations at any point in the reaction as long as only short reaction intervals are considered so that concentration changes are small.

Whether steady-state or non-steady-state conditions apply depends on the reaction system. Higher concentrations of deactivator decrease normal bimolecular termination by decreasing the concentration of propagating radicals. Steady-state low concentrations of radicals occur when the deactivator/activator ratio is about equal to or greater than 0.1. Non-steady-state conditions occur when the ratio is lower than 0.1. Non-steady-state means non-steady-state conditions for both propagating radicals and deactivator. Under steady-state conditions, both radical and deactivator concentrations are at steady-state, where the radical concentration is lower and the deactivator concentration is higher than for non-steady-state conditions.
The time needed to suppress normal bimolecular termination is shortened by deliberately adding the deactivator at the start of polymerization, instead of waiting until its concentration builds up from the reaction of initiator and activator. Reaction variables that yield faster rates (e.g., higher initiator and activator concentrations and higher temperatures) increase normal bimolecular termination because the radical concentrations are higher. Another consideration is the suppression of normal bimolecular termination by the decrease in $k_t$ with conversion (increasing molecular weight).

Certain experimental considerations can complicate the kinetics. Cu$^+$ is difficult to obtain and maintain in pure form. Only a few percent of Cu$^{2+}$ present initially or formed as a result of insufficient deoxygenation in the polymerization can alter the process. Reaction systems may be heterogeneous or become heterogeneous with conversion as the medium changes.

3-15b-4 Block Copolymers

A number of different types of copolymers are possible with ATRP—statistical (random), gradient, block, and graft copolymers [Matyjaszewski, 2001]. Other polymer architectures are also possible—hyperbranched, star, and brush polymers, and functionalized polymers. Statistical and gradient copolymers are discussed in Chap. 6. Functionalized polymers are discussed in Sec. 3-16b.

3-15b-4-a All Blocks via ATRP. Block copolymers are synthesized via ATRP by two methods: the one-pot sequential and isolated macroinitiator methods [Davis and Matyjaszewski, 2001; Kamigaito et al., 2001; Matyjaszewski, 1998, 2000; Matyjaszewski and Xia, 2001]. An AB diblock copolymer is produced in the one-pot sequential method by polymerizing monomer A. Monomer B is then added when most of A has reacted (Eq. 3-230). In the isolated macroinitiator method, the halogen-terminated polyA (RA$n$X) is isolated and then used as an initiator (the macroinitiator) together with CuX to polymerize monomer B. RA$n$X is usually isolated by precipitation with a nonsolvent or some other technique. The halogen-terminated macroinitiator is typically quite stable and can be stored for long periods prior to use in forming the second block.

Both methods require that the polymerization of the first monomer not be carried to completion, usually 90% conversion is the maximum conversion, because the extent of normal bimolecular termination increases as the monomer concentration decreases. This would result in loss of polymer chains with halogen end groups and a corresponding loss of the ability to propagate when the second monomer is added. The final product would be a block copolymer contaminated with homopolymer A. Similarly, the isolated macroinitiator method requires isolation of RA$n$X prior to complete conversion so that there is a minimum loss of functional groups for initiation. Loss of functionality is also minimized by adjusting the choice and amount of the components of the reaction system (activator, deactivator, ligand, solvent) and other reaction conditions (concentration, temperature) to minimize normal termination.

The one-pot sequential method has the disadvantage that the propagation of the second monomer involves a mixture of the second monomer plus unreacted first monomer. The second block is actually a random copolymer. The isolated macroinitiator method is the method of choice to avoid this “contamination” of the second block. The isolated macroinitiator
method often stops the conversion of the first monomer at much less than 90%, sometimes as low as 50%, to save time. To go to the higher conversion, one needs to have more deactivator present to completely minimize normal termination, but this results in slower polymerization rates. Isolation of the macroinitiator at lower conversions allows the use of lower deactivator concentrations and faster polymerizations.

Tri- and higher block copolymers, such as ABA, ABC, ABCB, can be synthesized by a continuation of the processes with the successive additions of the appropriate monomers. A symmetric block copolymer such as ABA or CABAC can be made efficiently by using a difunctional initiator, such as, α, α-dichloro-p-xylene or dimethyl 2,6-dibromoheptanedioate, instead of the monofunctional initiator. For the ABA block copolymer only two, instead of three, monomer charges are needed:

\[
\begin{align*}
A & \xrightarrow{\text{XRX}} XA_nRA_mX \\
 & \xrightarrow{\text{B}} XB_m-\text{A}_n\text{R}_m-\text{B}_mX
\end{align*}
\] (3-231)

The exact sequence of monomer addition may be critical to success in producing the desired block copolymer. For example, does one add A first or B first to produce an AB block copolymer? The answer depends on the reactivity of an AX chain end toward monomer B compared to the reactivity of a BX chain end toward monomer A:

\[
\begin{align*}
\text{AX} & \xrightarrow{\text{B}} \text{BX} \\
\text{BX} & \xrightarrow{\text{A}} \text{AX}
\end{align*}
\] (3-232)

Either addition sequence works if the two monomers are in the same family (e.g., methyl acrylate and butyl acrylate or methyl methacrylate and butyl methacrylate or styrene and 4-acetoxystyrene), because the equilibrium constants (for activation) for both types of chain ends have about the same value. The situation is usually quite different for pairs of monomers from different families. Chain ends from monomers with large equilibrium constants can initiate the polymerization of monomers with lower equilibrium constants; thus, cross-propagation is efficient. Methacrylate works well as the first monomer to form methacrylate–acrylate and methacrylate–styrene blocks.

However, styrene or acrylate monomers are inefficient as the first monomer to form those block copolymers. The problem is that there is a slow activation of styrene or acrylate chain ends, cross-propagation is fast (because methacrylate is very reactive), and subsequent activation of methacrylate chain ends is fast, resulting in considerable conversion of the second monomer before all the styrene or acrylate chain ends are activated—all of which leads to increased polydispersity in methacrylate block lengths and molecular weight. If styrene or acrylate first is the desired sequence for some reason, for instance, as the prelude to some other block sequence, it may be possible to achieve it by employing a halogen exchange. One starts polymerization of the acrylate or styrene monomer with a bromo initiator and CuBr. Prior to the addition of methacrylate, CuCl is added to convert bromo-terminated chain ends to chloro-terminated chain ends. The equilibrium constant for the latter is lower, activation and cross-propagation are slowed sufficiently that complete activation and cross-propagation are achieved before significant conversion of methacrylate occurs.

Styrene—acrylate block copolymers can be synthesized with either monomer as the first monomer because the equilibrium constants for acrylate and styrene chain ends are similar.
Block copolymers have also been synthesized via transformation reactions in which not all blocks are produced by ATRP [Kamigaito et al., 2001; Matyjaszewski, 1998b; Matyjaszewski and Xia, 2001]. One approach is to use an appropriate initiator in the non-ATRP polymerization to produce a polymer with a halogenated end group either through initiation or termination. The halogen-terminated polymer is then used as a macroinitiator in ATRP. For example, polymers with halogenated end groups are obtained in the cationic polymerization of styrene with 1-phenylethyl chloride and SnCl₄, the anionic ring-opening polymerization of caprolactone with 2,2,2-tribromoethanol and triethyl aluminum, and the conventional radical polymerization of vinyl acetate with a halogen-containing azo compound.

Another approach is to use an initiator for ATRP that produces a polymer with a functional group capable of initiating a non-ATRP polymerization. ATRP polymerization of methyl methacrylate with 2,2,2-tribromoethanol produces an HO-terminated poly(methyl methacrylate). The hydroxyl group acts as an initiator in the presence of triethyl aluminum for the ring-opening polymerization of caprolactone.

Macroinitiators for ATRP can be produced from polymers obtained from non-ATRP polymerization by appropriate conversion of their end groups. For example, hydroxyl-capped polymers obtained by cationic or anionic chain polymerization or even step polymerization can be esterified with 2-bromopropanoyl bromide to yield Br-capped polymers that are ATRP macroinitiators.

Other Polymer Architectures

A star polymer contains polymer chains as arms emanating from a branch point. Star polymers can be synthesized via ATRP by using an initiator containing three or more halogens, for example, a 3-arm star polymer is obtained by using a tribromo initiator:

\[
\begin{align*}
\text{Br} & \quad \text{Br} \\
\text{Br} & \quad \text{R} \quad \text{Br} \\
& \quad \text{CuX} \\
\end{align*}
\]

\[
\begin{align*}
\text{BrA} & \quad \text{R} \quad \text{A}_n \quad \text{Br} \\
& \quad \text{BrA}_n \\
\end{align*}
\]

A graft copolymer is a branched polymer containing a polymer chain derived from one monomer to which are attached one or more polymer side chains of another monomer. ATRP produces a graft copolymer when the initiator is a polymer with one or more halogen-containing side groups:

\[
\begin{align*}
\text{X} & \quad \text{CuX} \\
& \quad \text{A}_n \quad \text{X} \\
\end{align*}
\]

When the polymeric initiator contains many halogens, there will be many grafted side chains, and the product is called a comb or brush polymer. A variety of polymers can be used as the polymeric initiator, including polymers containing vinyl chloride and 4-chloromethylstyrene units, and halogenated natural and butyl rubbers. Graft copolymers are discussed further in Chaps. 5, 6, and 9.

Hyperbranched polymers (see structure LXII in Sec. 2-16a) are produced from monomers that contain both a polymerizable double bond and an initiating function, such as \(p\)-(chloro-methyl)styrene. The product is highly branched with one double bond end group and many
chloromethyl end groups; the number of chloromethyl end groups equals the degree of polymerization. This polymerization has been called self-condensing vinyl polymerization (SCVP). Partial dendrimer structures have also been described.

The synthesis of complex polymer architectures by ATRP (or other living radical polymerizations) is useful but relatively restricted because the occurrence of bimolecular termination increases with the number of initiator sites on a polymeric species.

### 3-15c Stable Free-Radical Polymerization (SFRP)

Various stable radicals such as nitroxide, triazolinyl, trityl, and dithiocarbamate have been used as the mediating or persistent radical (deactivator) for SFRP. Nitroxides are generally more efficient than the others. Cyclic nitroxide radicals such as 2,2,6,6-tetramethyl-1-piperidinoxyl (TEMPO) have been extensively studied. SFRP with nitroxides is called nitroxide-mediated polymerization (NMP). Polymerization is carried out by two methods that parallel those used in ATRP [Bertin et al., 1998; Georges, 1993; Hawker, 1997; Hawker et al., 2001]. One method involves the thermal decomposition of an alkoxyamine such as 2,2,6,6-tetramethyl-1-(1-phenylethoxy)piperidine into a reactive radical and a stable radical (Eq. 3-236). The other method involves a mixture of a conventional radical initiator such as AIBN or benzoyl peroxide and the nitroxide radical. Nitroxide radicals are sufficiently stable (due to steric hindrance) that they can be stored at ambient temperatures without change and some are available for purchase from chemical vendors.

The reactive radical initiates polymerization while the stable radical mediates the reaction by reacting with propagating radicals to lower their concentration. The overall process (Eqs. 3-237–3-239) is analogous to ATRP. The nitroxide radical, although unreactive with

\[
R^1 - \text{ONR}^2 R^3 \xrightleftharpoons[\kappa_d]{\kappa_a} R^1 \cdot + \cdot \text{ONR}^2 R^3 \\
\xrightarrow{M} R^1 M_n \cdot \\
\xrightarrow{\cdot \text{ONR}^2 R^3} R^1 M_n - \text{ONR}^2 R^3
\]
itself, reacts rapidly with the propagating radical to decrease the concentration of propagating radicals sufficiently that conventional bimolecular termination is negligible. The propagating radical concentration is much lower than that of the dormant species; specifically, $K$ is small, and this results in living radical polymerization with control of molecular weight and molecular weight distribution. The general characteristics of ATRP described in Sec. 3-15b apply to NMP, that is, reaction variables control polymerization rate, molecular weight, and PDI in the same way [Ananchenko and Fischer, 2001; Greszta and Matyjaszewski, 1996; Lacroix-Desmazes et al., 2000, 2001; Lutz et al., 2001; Yoshikawa et al., 2002].

NMP with TEMPO generally requires higher temperatures ($125–145^\circ$C) and longer reaction times (1–3 days) compared to ATRP, and only styrene and 4-vinylpyridine polymerizations proceed with good control of molecular weight and polydispersity. Narrow molecular weight distributions with PDI below 1.1–1.2 are difficult to achieve with other monomers. The sluggishness of TEMPO systems is ascribed to $K$ values being too low. $K$ values are lower than in ATRP. Various techniques have been used to increase $R_p$. Adding a conventional initiator with a long half-life (slowly decomposing) to continuously generate reactive radicals throughout the reaction works well. Another technique is the addition of an acylating agents to reduce the concentration of nitroxide radicals via their acylation [Bauermann and Schmidt-Naake, 2001]. Self-initiation in styrene polymerization also enhances the reaction rate. However, it is not easy to increase reaction rates and maintain narrow PDI.

Some improvements occurred by changing to nitroxides with a hydrogen on at least one of the $\alpha$-carbons of the piperidine ring, in contrast to TEMPO, which has no hydrogens on $\alpha$-carbons. However, the major breakthrough came by using sterically hindered alicyclic nitroxides with a hydrogen on one of the $\alpha$-carbons. $t$-Butyl 2-methyl-1-phenylpropyl nitroxide (LVIII) and $t$-butyl 1-diethylphosphono-2,2-dimethylpropyl nitroxide (LIX) are examples of nitroxides that yield considerably faster polymerizations with control of molecular weight and polydispersity [Benoit et al., 2000a,b; Farcet et al., 2002; Grimaldi et al., 2000; Le Mercier et al., 2002]. These nitroxides and their corresponding alkoxyamines have allowed NMP of styrenes at lower temperatures and also extended NMP to monomers other than styrene. Acrylates, acrylamides, 1,3-dienes, and acrylonitrile polymerizations proceed with good molecular weight and PDI control, especially when fine-tuned in terms of the relative amounts of nitroxide radical, alkoxyamine, and conventional initiator and the reaction conditions (temperature, concentrations). The upper molecular weight limit of NMP is about 150,000–200,000, similar to the situation for ATRP.

NMP has not been extended to methacrylate monomers, in contrast to ATRP, which is successful with methacrylates. Many attempts to polymerize methacrylates by NMP have been unsuccessful, resulting in low conversions and/or broad PDI [Hawker et al., 2001]. This is generally ascribed to degradation of propagating radicals via $\beta$-hydrogen abstraction.
by nitroxide (Eq. 3-240) followed by the formed hydroxylamine acting as a chain-transfer
agent to terminate another propagating chain. There is one report of successful NMP of
methacrylate monomers [Yousi et al., 2000], but many other workers using very similar reac-
tion conditions were unsuccessful [Burguiere et al., 1999; Cheng and Yang, 2003].

Statistical, gradient, and block copolymers as well as other polymer architectures (graft,
star, comb, hyperbranched) can be synthesized by NMP following the approaches described
for ATRP (Secs. 3-15b-4, 3-15b-5) [Hawker et al., 2001]. Block copolymers can be synthe-
sized via NMP using the one-pot sequential or isolated macromonomer methods. The order of
addition of monomer is often important, such as styrene first for styrene-isoprene, acrylate first
for acrylate-styrene and acrylate-isoprene [Benoit et al., 2000a,b; Tang et al., 2003]. Differ-
ent methods are available to produce block copolymers in which the two blocks are formed
by different polymerization mechanisms:

1. A dual-function alkoxyamine with an appropriate functional group, such as the
hydroxyl-containing alkoxyamine $LX$, can initiate anionic polymerization (in the presence of

![LX]

aluminum isopropoxide) and NMP through the alcohol and nitroxide functions, respectively,
and the sequence is not critical.

2. An alkoxyamine with an appropriate functional group can be used to terminate a non-
NMP polymerization to yield a polymer with an alkoxyamine end group, which subsequently
initiates NMP of the second monomer, such as termination of a cationic polymerization by
$LX$.

3. An existing polymer with an appropriate end group can be reacted with an
alkoxyamine; for instance, alkoxide polymerization of ethylene oxide yields a hydroxyl-
terminated polymer that undergoes substitution (in the presence of sodium hydride) with a
halogen-containing alkoxyamine.

Star polymers are produced by using a core molecule that contains three or more alkoxy-
amine functions [Hawker, 1995; Miura and Yoshida, 2002]. Graft and comb (brush) polymers
are obtained by using a polymer containing alkoxyamine groups. For example, a chlorine-
containing polymer (from vinyl chloride or $p$-chlorostyrene units) could be reacted with the
sodium salt of $LX$ to place alkoxyamine groups on the polymer for subsequent initiation of
NMP. Or an alkoxyamine with a vinyl group can be polymerized or copolymerized to yield
the alkoxyamine-containing polymer.
NMP has some advantages and disadvantages compared to ATRP. A wide range of initiators (organic halides) are readily available for ATRP. Relatively few initiators for NMP, either nitroxides or alkoxyamines, are commercially available. The initiators need to be synthesized. $K$ is generally larger for ATRP compared to NMP and is more easily adjusted by changing the initiator, transition metal, and ligands. Larger $K$ values mean faster polymerization and milder reaction conditions. On the other hand, ATRP requires a relatively large amount of metal (0.1–1% of the reaction mixture) that needs to be removed from the final polymer product. In both NMP and ATRP, control of the reaction through establishment of a steady-state concentration of radicals is achieved by the balance between activation and deactivation. Conventional radical polymerization involves a balance between the rates of initiation and termination.

### 3-15d Radical Addition–Fragmentation Transfer (RAFT)

ATRP and NMP control chain growth by reversible termination. RAFT living polymerizations control chain growth through reversible chain transfer [Barner-Kowollik et al., 2001, 2003; Chiefari and Rizzardo, 2002; Cunningham, 2002; D’Agosto et al., 2003; Goto et al., 2001; Kwak et al., 2002; Moad et al., 2002; Monteiro and de Brouwer, 2001; Stenzel et al., 2003]. A chain-transfer agent such as cumyl dithiobenzoate reversibly transfers a labile end group (a dithioester end group) to a propagating chain (Eq. 3-241).

\[
\begin{align*}
\text{M}_n^+ + \text{R}' \text{S}\text{SR} & \rightleftharpoons \text{R}' \text{S}\text{SM}_n \rightarrow \text{R}' \text{S}\text{SM}_n + \text{R}^+ \\
\text{M}_n^+ + \text{R}' \text{S}\text{SM}_n & \rightleftharpoons \text{R}' \text{S}\text{SM}_n \rightarrow \text{R}' \text{S}\text{SM}_n + \text{M}_n^+ 
\end{align*}
\] (3-242)

The polymerization is carried out with a conventional initiator such as a peroxide or AIBN in the presence of the chain-transfer agent. The key that makes RAFT a living polymerization is the choice of the RAFT transfer agent. Living polymerization occurs with dithioesters because the transferred end group in the polymeric dithioester is as labile as the dithioester group in $\text{R}'\text{CSSR}$. This results in an equilibrium between dormant polymer chains and propagating radicals (Eq. 3-242 with $K = 1$), which controls the living polymerization. An end-group originating from the chain-transfer agent is reversibly exchanged between different propagating chains. The transfer reaction in RAFT is not a one-step transfer of the labile end group, but involves radical addition to the thiocarbonyl group of the dithioester to form an intermediate radical that fragments to yield a new dithioester and new radical.
The kinetics of RAFT are not established [Barner-Kowollik et al., 2003; Goto et al., 2001]. The RAFT agent generally acts in much the same way as a conventional transfer agent, but retardation is observed in some polymerizations because of coupling between the intermediate dithioester radical and a propagating radical [Perrier et al., 2002]. This radical coupling makes it very difficult to synthesize polymers with complex architectures such as stars (which lead to crosslinking). Retardation may also be due to slow fragmentation in the transfer reactions. The synthesis of complex architectures is also difficult because it requires radical initiators with complex structures, which are difficult to obtain.

The RAFT agent affects the number of polymer chains formed. The number of chains is determined by the amount of RAFT agent consumed and the amount of conventional initiator decomposed. The degree of polymerization depends on the monomer conversion and the number of polymer chains according to

$$X_n = \frac{p[M]_0}{\left(p'[RAFT]_0 + 2p''[I]_0\right)}$$

where $[M]_0$, $[RAFT]_0$, and $[I]_0$ are the initial concentrations of monomer, RAFT transfer agent, and initiator. $p$, $p'$, and $p''$ are the fractional conversions of monomer, RAFT agent, and initiator, respectively.

The fraction of polymer molecules with dithioester end groups is maximized (compared to chains terminated by normal bimolecular termination) by maximizing the amount of chain transfer. This is accomplished by using high concentrations of RAFT agents relative to initiator and RAFT agents with large chain-transfer constants. Many dithioesters have chain-transfer constants exceeding 1000. Under these conditions, the RAFT agent is consumed within the first few percent of monomer conversion ($p' = 1$) and the number of polymer chains due to initiator decomposition is small ($p'[RAFT]_0 \gg 2p''[I]_0$). The degree of polymerization is given by

$$X_n = \frac{p[M]_0}{[RAFT]_0}$$

RAFT polymerization proceeds with narrow molecular weight distributions as long as the fraction of chains terminated by normal bimolecular termination is small. This occurs when a RAFT agent with high transfer constant is used and the initiator concentration decreases faster than does the monomer concentration. PDI broadens when new chains are initiated over a longer time period.

Block copolymers have been synthesized by RAFT [Gaillard et al., 2003]. The use of RAFT for other polymer architectures has been studied, but not as extensively as ATRP and NMP [Mayadunne et al., 2003; Moad et al., 2003]. A significant advantage of RAFT is that it works with a wider range of monomers than NMP and ATRP. RAFT does not produce polymers with copper or other metal present. RAFT has some disadvantages. RAFT agents are not commercially available and must be synthesized. RAFT produces polymers with dithioester groups, which have some associated odors and colors (pink/red to yellow). Converting the dithioester end groups to thiol end groups by hydrolysis with base might be useful in decreasing the color and odor problems. ATRP polymers have a green color, which can be removed by extraction with water if the the ligands impart water solubility to Cu$^{2+}$. Cu$^{2+}$ can also be removed by treatment of the polymerization reaction system with alumina.

There are limitations for all types of LRP. The occurrence of irreversible bimolecular termination of propagating radicals becomes considerable under certain conditions: high monomer conversion, polyfunctional initiators, high initiator concentration, and high targeted molecular weight (about $>100,000$).
3-15e Other Living Radical Polymerizations

Xanthates have also been used as RAFT agents. RAFT polymerization has been observed for methacrylate monomers using double bond end-capped methacrylate oligomers [Gridnev and Ittel, 2001].

RAFT is actually a specialized form of degenerative transfer (DT). In DT using alkyl iodides as the transfer agent, there is a direct transfer of iodide between dormant polymer chains and propagating radicals instead of the addition–fragmentation sequence [Goto et al., 1998]. The method works primarily with styrene, but narrow molecular weight distributions are not achieved with other monomers. The chain transfer constants for alkyl iodides are not sufficiently high, which results in slow consumption of the DT agent, broad PDI, and much normal termination.

The presence of 1,1-diphenylethene (DPE) in the polymerization of a monomer results in a living polymerization [Raether et al., 2002; Wieland et al., 2002]. DPE adds reversibly to a propagating chain to form a dormant stable radical with no (or very low) reactivity to add monomer. This sets up an equilibrium between propagating chains (active species) and dormant DPE-terminal radicals.

Other systems include organotellurium and boroxyl-based initiators [Chung et al., 1996; Yamago et al., 2002].

3-16 OTHER POLYMERIZATIONS

3-16a Organometallic Polymers

Organometallic compounds containing polymerizable carbon–carbon double bonds have been synthesized and their polymerization studied [Archer, 2001; Pittman et al., 1987]. Among the organometallic monomers studied are vinylferrocene and trialkyltin methacrylate. Much of the interest in these polymerizations has been to obtain polymers with improved thermal stability or electrical (semi)conductivity, but these objectives have not been realized. Trialkyltin methacrylate polymers have been studied for formulating antifouling marine paints to prevent growth of barnacles and fungi on shore installations and ship bottoms [Yaeger and Castelli, 1978].

3-16b Functional Polymers

A functional polymer is a polymer that contains a functional group, such as a carboxyl or hydroxyl group. Functional polymers are of interest because the functional group has a desired property or can be used to attach some moiety with the desired property [Patil et al., 1998]. For example, a medication such as chloroamphenicol, a broad-spectrum antibiotic,
contains a hydroxyl group and can be bonded to COOH-containing polymers by esterification to produce a polymeric drug. The polymeric drug has the potential for a constant in vivo concentration of the medication via the slow in vivo release of chloroamphenicol by ester hydrolysis [Meslard et al., 1986].

There are two types of functional polymers: pendant-functionalized and end-functionalized polymers. Pendant-functionalized polymers have functional groups as side groups on the polymer chain. End-functionalized polymers, also called telechelic polymers (Sec. 2-13b-3), have functional groups that are the end groups of a polymer. There is interest in synthesizing functional polymers by both conventional and living radical polymerizations, but the research effort is greater in living polymerizations since the potential products have better defined structures. Most but not all methods of synthesizing functional polymers are possible with both conventional and living polymerizations. Radical polymerization offers an advantage over ionic polymerization for synthesizing functional polymers. Radical polymerization is more tolerant of polar functionalities; for instance, groups such as hydroxyl and amino can be present during a radical polymerization but not an ionic polymerization. Polymers with such functional groups are possible by an ionic polymerization, but the functional group needs to be protected during polymerization. For example, a hydroxyl group cannot be present during an anionic polymerization because the hydroxyl group terminates the propagating center by proton transfer. However, the hydroxyl group can be protected during polymerization by conversion to the trimethylsilyl derivative; hydrolysis subsequent to polymerization regenerates the hydroxyl group. The protection–deprotection sequence is unnecessary for the corresponding radical polymerization.

Pendant-functionalized polymers are obtained by polymerization of a monomer containing the desired functional group. Conventional and living radical polymerization are both useful. ATRP, NMP, and RAFT have been studied, but RAFT much less than NMP, and NMP less than ATRP at this time [Coessens et al., 2001; Harth et al., 2001; Patil et al., 1998].

End-functionalized polymers are obtained in both conventional and living radical polymerization by using initiators that contain the desired functional group. For example, a telechelic polymer with hydroxyl end groups at both ends is obtained in conventional radical polymerization using either H2O2 or 4,4′-azobis(4-cyanopentanol) as the initiator. If extensive chain transfer occurs, e.g., in the presence of a deliberately added strong chain transfer agent, the polymer has one end group from the initiator and one from the chain transfer agent. Choice of the chain-transfer agent offers an additional mode for attaching a desired functional group at the polymer chain end.

A telechelic polymer with one COOH and one Br end group is obtained in ATRP by using p-(1-bromoethyl)benzoic acid as the initiator. Similarly, NMP and RAFT can be used to attach different functional groups to the two ends of a polymer chain by the proper choice of functionalized alkoxyamine, nitroxides, and dithioesters.

Some functional groups can be introduced into polymers by conversion of one functional group to another. For example, pendant or end-group halogens can be displaced by nucleophilic substitution to yield hydroxyl or amino functional groups.
Acetylenic Monomers

The polymerization of acetylene (alkyne) monomers has received attention in terms of the potential for producing conjugated polymers with electrical conductivity. Simple alkynes such as phenylacetylene do undergo radical polymerization but the molecular weights are low ($\bar{X}_n < 25$) [Amdur et al., 1978]. Ionic and coordination polymerizations of alkynes result in high-molecular-weight polymers (Secs. 5-7d and 8-6c).

$$\phi\text{C}≡\text{CH} \rightarrow (\phi\text{C}≡\text{CH})_n \ (3-245)$$

The radical 1,4-polymerization of certain diacetylenes (conjugated dialkynes) proceeds to yield high-molecular-weight polymer ($10^5$) when carried out in the solid state. Diacetylene itself has not been successfully polymerized; it is too reactive to be polymerized in a controlled manner. 1,4-Disubstituted diacetylenes are polymerized by ionizing radiation, UV, or heat [Chance, 1986; Hoofman et al., 2001]. The reaction proceeds via a dicarbene propagating species (LXI) with the final product possessing an alternating ene-yne-conjugated structure (LXII). Among the diacetylenes studied are those in which $R$ is $-\text{CH}_2\text{OSO}_2\phi\text{CH}_3$, $-(\text{CH}_2)_4\text{OCONHCH}_2\text{COOC}_4\text{H}_9$, and $-(\text{CH}_2)_4\text{OCONH}\phi$. High-molecular-weight polymer is obtained only when the reaction proceeds as a lattice-controlled (topochemical) solid-state polymerization. This occurs only when the $R$ groups have the appropriate bulk such that the diacetylene monomer and corresponding polymer have essentially the same crystal structure. The topochemical reaction transforms a monomer crystal to a polymer crystal with similar dimensions. Polymer single crystals of macroscopic dimensions, several centimeters in some cases, have been synthesized. The conjugated $\pi$-electron system of the polydiacetylenes imparts intense light absorption in the visible region as well as interesting (photo)conductivity and nonlinear optical properties.

REFERENCES


REFERENCES


REFERENCES


PROBLEMS

3-1 When one considers the various polymers produced from carbon–carbon double bond monomers, the following generalizations are apparent:

a. The polymers are produced almost exclusively from ethylene, monomers that have one substituent on the double bond, or monomers that have two substituents on the same carbon atom of the double bond. Monomers containing one substituent on each carbon of the double bond seldom polymerize.

b. Most of the chain polymerizations are carried out by radical initiation; relatively few are produced by ionic initiation.

Why? Are there good reasons for these generalizations or are they simply a matter of chance? Discuss.

3-2 Show by chemical equations the polymerization of acrylonitrile initiated by the thermal decomposition of cumyl hydroperoxide.

3-3 Using ¹⁴C-labeled AIBN as an initiator, a sample of styrene is polymerized to an number-average degree of polymerization of 1.52 × 10⁴. The AIBN has an activity of 9.81 × 10⁷ counts min⁻¹ mol⁻¹ in a scintillation counter. If 3.22 g of the polystyrene has an activity of 203 counts min⁻¹, what is the mode of termination?

3-4 Poly(vinyl acetate) of number-average molecular weight 100,000 is hydrolyzed to poly(vinyl alcohol). Oxidation of the latter with periodic acid to cleave 1,2-diol linkages yields a poly(vinyl alcohol) with $X_n = 200$. Calculate the percentages of head-to-tail and head-to-head linkages in the poly(vinyl acetate).

3-5 The benzoyl peroxide–initiated polymerization of a monomer follows the simplest kinetic scheme, that is, $R_p = k_p[M]^1[(f_{kd}I)/k_i]^{1/2}$ with all rate constants and $f$ being independent of conversion. For a polymerization system with $[M]_0 = 2M$ and $[I]_0 = 10^{-2}M$, the limiting conversion $p_\infty$ is 10%. To increase $p_\infty$ to 20%:

a. Would you increase or decrease $[M]_0$ and by what factor?

b. Would you increase or decrease $[I]_0$ and by what factor? How would the rate and degree of polymerization be affected by the proposed changes in $[I]_0$?

c. Would you increase or decrease the reaction temperature for the case of thermal initiated polymerization? For the case of photopolymerization (assuming that an increase in temperature does not cause thermal decomposition of initiator)?

$E_d$, $E_p$, and $E_i$ are 124, 32, and 8 kJ mol⁻¹, respectively.

3-6 For a radical polymerization with bimolecular termination, the polymer produced contains 1.30 initiator fragments per polymer molecule. Calculate the relative extents of termination by disproportionation and coupling, assuming that no chain-transfer reactions occur.
3-7 A solution 0.20 M in monomer and $4.0 \times 10^{-3} M$ in a peroxide initiator is heated at 60°C. How long will it take to achieve 50% conversion? $k_p = 145$ L mol$^{-1}$ s$^{-1}$, $k_i = 7.0 \times 10^{7}$ L mol$^{-1}$ s$^{-1}$, $f = 1$, and the initiator half-life is 44 h.

3-8 Show that a plot of the fraction of monomer polymerized versus time $t$ yields a straight line for $t \gg \tau_s$ and that the extension of this line cuts the time axis at $t = \tau_s \ln 2$.

Hint: Use $[M^\cdot] = [M^\cdot]_s \tanh \left( t/\tau_s \right)$ as a starting point and assume low conversion.

3-9 The following data were obtained in the thermal initiated bulk polymerization of monomer $Z$ ([M] = 8.3 M) using radical initiator $W$ at 60°C:

<table>
<thead>
<tr>
<th>$R_p \times 10^3$ (mol L$^{-1}$ s$^{-1}$)</th>
<th>$\overline{X}_n$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.0050</td>
<td>8350</td>
</tr>
<tr>
<td>0.010</td>
<td>5550</td>
</tr>
<tr>
<td>0.020</td>
<td>3330</td>
</tr>
<tr>
<td>0.050</td>
<td>1317</td>
</tr>
<tr>
<td>0.10</td>
<td>592</td>
</tr>
<tr>
<td>0.15</td>
<td>358</td>
</tr>
</tbody>
</table>

Calculate $C_M$, $k_p/k_i^{1/2}$, and $f_{kd}$ in this polymerization if it is experimentally observed that $R_p = 4.0 \times 10^{-4} [l]^{1/2}$. Is chain transfer to initiator important? If it is, describe how to calculate $C_I$.

3-10 Consider the polymerization of styrene initiated by di-$t$-butyl peroxide at 60°C. For a solution of 0.01 M peroxide and 1.0 M styrene in benzene, the initial rates of initiation and polymerization are $4.0 \times 10^{-11}$ and $1.5 \times 10^{-7}$ mol L$^{-1}$ s$^{-1}$, respectively. Calculate the values of $(f_{kd})$, the initial kinetic chain length, and the initial degree of polymerization. Indicate how often on the average chain transfer occurs per each initiating radical from the peroxide. What is the breadth of the molecular weight distribution that is expected, that is, what is the value of $\overline{X}_w/?\overline{X}_n$? Use the following chain-transfer constants:

$C_M = 8.0 \times 10^{-5}$
$C_I = 3.2 \times 10^{-4}$
$C_P = 1.9 \times 10^{-4}$
$C_S = 2.3 \times 10^{-6}$

3-11 For a particular application the molecular weight of the polystyrene obtained in Problem 3-10 is too high. What concentration of $n$-butyl mercaptan should be used to lower the molecular weight to 85,000? What will be the polymerization rate for the reaction in the presence of the mercaptan?

3-12 Consider the polymerization reaction in Problem 3-10. Aside from increasing the monomer concentration, what means are available for increasing the polymerization rate? Compare the alternate possibilities with respect to any changes that are expected in the molecular weight of the product.

3-13 Show by chemical equations the reactions involved in chain transfer by hexane, benzene, isopropylbenzene, propanol, butyl iodide, carbon tetrabromide, $n$-butyl
mercaptan, and di-\(n\)-butyl sulfide. Compare and discuss the differences in the transfer constants of these agents for vinyl acetate polymerization (Table 3-7).

3-14 The polymerization of methyl acrylate (one molar in benzene) is carried out using a photosensitizer and 3130 Å light from a filtered mercury arc lamp. Light is absorbed by the system at the rate of \(1.0 \times 10^5\) erg L\(^{-1}\) s\(^{-1}\). Assuming that the quantum yield for radical production in this system is 0.50, calculate the rates of initiation and polymerization.

3-15 Consider the bulk polymerization of neat styrene by ultraviolet irradiation. The initial polymerization rate and degree of polymerization are \(1.0 \times 10^{-3}\) mol L\(^{-1}\) s\(^{-1}\) and 200, respectively, at 27°C. What will be the corresponding values for polymerization at 77°C?

3-16 The same initial polymerization rate and degree of polymerization as in Problem 3-15 are obtained at 27°C for a particular AIBN thermal-initiated polymerization of styrene. Calculate the \(R_p\) and \(X_n\) values at 77°C.

3-17 A radical chain polymerization following \(R_p = [M]k_p(fK_d[I]/k_i)^{1/2}\) shows the indicated conversions for specified initial monomer and initiator concentrations and reaction times:

<table>
<thead>
<tr>
<th>Experiment</th>
<th>Temperature (°C)</th>
<th>[M] mol L(^{-1})</th>
<th>[I] (\times 10^3) mol L(^{-1})</th>
<th>Reaction Time (min)</th>
<th>Conversion (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>60</td>
<td>1.00</td>
<td>2.5</td>
<td>500</td>
<td>50</td>
</tr>
<tr>
<td>2</td>
<td>80</td>
<td>0.50</td>
<td>1.0</td>
<td>700</td>
<td>75</td>
</tr>
<tr>
<td>3</td>
<td>60</td>
<td>0.80</td>
<td>1.0</td>
<td>600</td>
<td>40</td>
</tr>
<tr>
<td>4</td>
<td>60</td>
<td>0.25</td>
<td>10.0</td>
<td>?</td>
<td>50</td>
</tr>
</tbody>
</table>

Calculate the reaction time for 50% conversion in experiment 4. Calculate the overall activation energy for the rate of polymerization.

3-18 Calculate the equilibrium monomer concentration \([M]_e\) for radical polymerization of 1,3-butadiene at 27°C, assuming that \(\Delta H^0\) and \(\Delta S^0\) are given by the values in Table 3-14. Repeat the calculations for 77°C and 127°C.

3-19 Most radical chain polymerizations show a one-half-order dependence of the polymerization rate on the initiation rate \(R_i\) (or the initiator concentration [I]). Describe and explain under what reaction conditions [i.e., what type(s) of initiation and/or termination] radical chain polymerizations will show the following dependencies:

a. First-order

b. Zero-order

Explain clearly the polymerization mechanisms that give rise to these different kinetic orders. What is the order of dependence of \(R_p\) on monomer concentration in each of these cases. Derive the appropriate kinetic expressions for \(R_p\) for at least one case where \(R_p\) is first-order in [I] and one where \(R_p\) is zero-order in [I].

3-20 What is the breadth of the size distribution to be expected for a low conversion polymerization where termination is entirely by coupling. Discuss the manner in which each of the following situations alters the size distribution:
a. Chain transfer to $n$-butyl mercaptan

b. High conversion

c. Chain transfer to polymer

d. Autoacceleration

For those situations where there is a tendency toward a broadening of the size distribution, discuss the possible process conditions that may be used to decrease this tendency.

3-21 Calculate the rate and degree of polymerization of methyl methacrylate initiated by AIBN at 50°C at 2500 atm relative to the corresponding quantities at 1 atm if $\Delta V_R^1 = -19.0 \text{ cm}^3 \text{ mol}^{-1}$ and $\Delta V_d^1 = 3.8 \text{ cm}^3 \text{ mol}^{-1}$.

3-22 ATRP of 5.0 $M$ styrene is carried out at 110°C using 1-phenylethyl bromide (0.050 $M$) and CuBr (0.050 $M$) in the presence of 4,4'-di(5-nonyl)-2,2'-bipyridine (0.10 $M$). The number-average molecular weight at 72% conversion is 7150. Compare the observed molecular weight to the theoretical value expected for this polymerization.

3-23 The living character of LRP is limited under certain conditions, such as high monomer conversion, high initiator concentration, and high targeted molecular weight (>100,000). Explain why these conditions result in broadening of PDI and some difficulty in producing block copolymers with well-defined block lengths of the different monomers.

3-24 Describe how NMP is used to synthesize a block copolymer of styrene and 4-vinylpyridine.

3-25 Describe how ATRP is used to graft styrene onto a vinyl chloride–vinylchloroacetate copolymer.
EMULSION POLYMERIZATION

Emulsion polymerization refers to a unique process employed for some radical chain polymerizations. It involves the polymerization of monomers in the form of emulsions (i.e., colloidal dispersions). The process bears a superficial resemblance to suspension polymerization (Sec. 3-13c) but is quite different in mechanism and reaction characteristics. Emulsion polymerization differs from suspension polymerization in the type and smaller size of the particles in which polymerization occurs, in the kind of initiator employed, and in the dependence of polymer molecular weight on reaction parameters.

4-1 DESCRIPTION OF PROCESS

4-1a Utility

Emulsion polymerization was first employed during World War II for producing synthetic rubbers from 1,3-butadiene and styrene. This was the start of the synthetic rubber industry in the United States. It was a dramatic development because the Japanese naval forces threatened access to the southeast Asian natural-rubber (NR) sources, which were necessary for the war effort. Synthetic rubber has advanced significantly from the first days of “balloon” tires, which had a useful life of 5000 mi to present-day tires, which are good for 40,000 mi or more. Emulsion polymerization is presently the predominant process for the commercial polymerizations of vinyl acetate, chloroprene, various acrylate copolymerizations, and copolymerizations of butadiene with styrene and acrylonitrile. It is also used for methacrylates, vinyl chloride, acrylamide, and some fluorinated ethylenes.
The emulsion polymerization process has several distinct advantages. The physical state of the emulsion (colloidal) system makes it easy to control the process. Thermal and viscosity problems are much less significant than in bulk polymerization. The product of an emulsion polymerization, referred to as a latex, can in many instances be used directly without further separations. (However, there may be the need for appropriate blending operations, e.g., for the addition of pigments.) Such applications include paints, coating, finishes, and floor polishes. Aside from the physical difference between the emulsion and other polymerization processes, there is one very significant kinetic difference. For the other processes there is an inverse relationship (Eq. 3-97) between the polymerization rate and the polymer molecular weight. This drastically limits one’s ability to make large changes in the molecular weight of a polymer, from 25,000 to 100,000 or from 100,000 to 25,000. Large decreases in the molecular weight of a polymer can be made without altering the polymerization rate by using chain-transfer agents. However, large increases in molecular weight can be made only by decreasing the polymerization rate by lowering the initiator concentration or lowering the reaction temperature. Emulsion polymerization is a unique process in that it affords the means of increasing the polymer molecular weight without decreasing the polymerization rate. Because of a different reaction mechanism, emulsion polymerization has the advantage of being able to simultaneously attain both high molecular weights and high reaction rates.

4-1b Qualitative Picture

4-1b-1 Components and Their Locations

The physical picture of emulsion polymerization is based on the original qualitative picture of Harkins [1947] and the quantitative treatment of Smith and Ewart [1948] with subsequent contributions by other workers [Blackley, 1975; Casey et al., 1990; Gao and Penlidis, 2002; Gardon, 1977; Gilbert, 1995, 2003; Hawkett et al., 1977; Piirma, 1982; Poehlein, 1986; Ugelstad and Hansen, 1976]. Table 4-1 shows a typical recipe for an emulsion polymerization [Vandenberg and Hulse, 1948]. This formulation, one of the early ones employed for the production of styrene-1,3-butadiene rubber (trade name: GR-S), is typical of all emulsion polymerization systems. The main components are the monomer(s), dispersing medium, emulsifier, and water-soluble initiator. The dispersing medium is the liquid, usually water,

<table>
<thead>
<tr>
<th>Component</th>
<th>Parts by Weight</th>
</tr>
</thead>
<tbody>
<tr>
<td>Styrene</td>
<td>25</td>
</tr>
<tr>
<td>Butadiene</td>
<td>75</td>
</tr>
<tr>
<td>Water</td>
<td>180</td>
</tr>
<tr>
<td>Emulsifier (Dresinate 731)</td>
<td>5</td>
</tr>
<tr>
<td>(n)-Dodecyl mercaptan</td>
<td>0.5</td>
</tr>
<tr>
<td>NaOH</td>
<td>0.061</td>
</tr>
<tr>
<td>Cumene hydroperoxide</td>
<td>0.17</td>
</tr>
<tr>
<td>FeSO(_4)</td>
<td>0.017</td>
</tr>
<tr>
<td>Na(_4)P(_2)O(_7)\cdot10\ H(_2)O</td>
<td>1.5</td>
</tr>
<tr>
<td>Fructose</td>
<td>0.5</td>
</tr>
</tbody>
</table>

*Data from Vandenberg and Hulse [1948].
in which the various components are dispersed by means of the emulsifier. The ratio of water to monomer(s) is generally in the range 70/30 to 40/60 (by weight). The action of the emulsifier (also referred to as surfactant or soap) is due to its molecules having both hydrophilic and hydrophobic segments. Various other components may also be present in the emulsion system. Thus, a mercaptan is used in the above formulation as a chain-transfer agent to control the polymer molecular weight. The initiator is the hydroperoxide–ferrous ion redox system and the function of fructose is probably to regenerate ferrous ion by reducing the ferric ion produced in the initiation reaction (Eq. 3-36c). The sodium pyrophosphate acts to solubilize the iron salts in the strongly alkaline reaction medium. The emulsion system is usually kept in a well-agitated state during reaction.

The locations of the various components in an emulsion system will now be considered. When the concentration of a surfactant exceeds its critical micelle concentration (CMC), the excess surfactant molecules aggregate together to form small colloidal clusters referred to as micelles. The transformation of a solution to the colloidal state as the surfactant concentration exceeds the CMC occurs to minimize the free energy of solution (heat is liberated) and is accompanied by a sharp drop in the surface tension of the solution. Electrical conductivity, ion activities, viscosity, and other solution properties also show marked changes at CMC. CMC values are in the range 0.001–0.1 mol L\(^{-1}\), with most surfactants having values in the lower end of the range. Since surfactant concentrations in most emulsion polymerizations (0.1–3 wt% based on the aqueous phase) exceed CMC by one or more orders of magnitude, the bulk of the surfactant is in the micelles. Typical micelles have dimensions of 2–10 nm (1nm = 10 Å = 10\(^{-3}\) μm), with each micelle containing 50–150 surfactant molecules. Most authors show the shape of micelles as being spherical, but this is not always the case. Both spherical and rodlike micelles are observed depending on the surfactant and its concentration. The surfactant molecules are arranged in a micelle with their hydrocarbon portion pointed toward the interior of the micelle and their ionic ends outward toward the aqueous phase. The number of micelles and their size depends on the amount of emulsifier. Large amounts of emulsifier yield larger numbers of smaller-sized micelles.

When a water-insoluble or slightly water-soluble monomer is added, a very small fraction dissolves in the continuous aqueous phase. The water solubilities of most monomers are quite low, although the spread is large; for example, styrene, butadiene, vinyl chloride, methyl methacrylate, and vinyl acetate are soluble to the extent of 0.07, 0.8, 7, 16, and 25 g L\(^{-1}\), respectively, at 25°C [Gardon, 1977]. An additional but still small portion of the monomer enters the interior hydrocarbon portions of the micelles. This is evidenced by X-ray and light-scattering measurements showing that the micelles increase in size as monomer is added. The amount of monomer in micelles compared to that in solution is much greater for the water-insoluble, nonpolar monomers. For example, the amount of micellar monomer is 2-, 5-, and 40-fold larger for methyl methacrylate, butadiene, and styrene, respectively, than the amount in solution [Bovey et al., 1955]. For vinyl acetate, the amount of micellar monomer is only a few percent of that in solution [Dunn, 1985].

The largest portion of the monomer (>95%) is dispersed as monomer droplets whose size depends on the stirring rate. The monomer droplets are stabilized by surfactant molecules absorbed on their surfaces. Monomer droplets have diameters in the range 1–100 μm (10\(^3\)–10\(^5\) nm). Thus, in a typical emulsion polymerization system, the monomer droplets are much larger than the monomer-containing micelles. Consequently, while the concentration of micelles is 10\(^{19}\)–10\(^{21}\) L\(^{-1}\), the concentration of monomer droplets is at most 10\(^{12}\)–10\(^{14}\) L\(^{-1}\). A further difference between micelles and monomer droplets is that the total surface area of the micelles is larger than that of the droplets by more than two orders of magnitude. The size, shape, and concentration of each of the various types of particles in the
emulsion system are obtained from electron microscopy, light scattering, ultracentrifugation, photon correlation spectroscopy, and other techniques [Debye and Anacker, 1951; Kratohvil, 1964; Munro et al., 1979].

4-1b-2 Site of Polymerization

The initiator is present in the water phase, and this is where the initiating radicals are produced. The rate of radical production $R_i$ is typically of the order of $10^{13}$ radicals $L^{-1} s^{-1}$. (The symbol $\rho$ is often used instead of $R_i$ in emulsion polymerization terminology.) The locus of polymerization is now of prime concern. The site of polymerization is not the monomer droplets since the initiators employed are insoluble in the organic monomer. Such initiators are referred to as *oil-insoluble initiators*. This situation distinguishes emulsion polymerization from suspension polymerization. Oil-soluble initiators are used in suspension polymerization and reaction occurs in the monomer droplets. The absence of polymerization in the monomer droplets in emulsion polymerization has been experimentally verified. If one halts an emulsion polymerization at an appropriate point before complete conversion is achieved, the monomer droplets can be separated and analyzed. An insignificant amount (approximately <0.1%) of polymer is found in the monomer droplets in such experiments. Polymerization takes place almost exclusively in the micelles. Monomer droplets do not compete effectively with micelles in capturing radicals produced in solution because of the much smaller total surface area of the droplets.

Polymerization of the monomer in solution undoubtedly takes place but does not contribute significantly, since the monomer concentration is low and propagating radicals would precipitate out of aqueous solution at very small (oligomeric) size. The micelles act as a meeting place for the organic (oil-soluble) monomer and the water-soluble initiator. The micelles are favored as the reaction site because of their high monomer concentration (similar to bulk monomer concentration) compared to the monomer in solution. As polymerization proceeds, the micelles grow by the addition of monomer from the aqueous solution whose concentration is replenished by dissolution of monomer from the monomer droplets. A simplified schematic representation of an emulsion polymerization system is shown in Fig. 4-1. The system consists of three types of particles: monomer droplets, inactive micelles in which
polymerization is not occurring, and active micelles in which polymerization is occurring. The latter are no longer considered as micelles but are referred to as polymer particles. An emulsifier molecule is shown as $\sigma$– to indicate one end ($\sigma$) is polar or ionic and the other end ($-$) nonpolar.

Two mechanisms for particle nucleation (i.e., formation of polymer particles) have been discussed. The process described above, called micellar particle nucleation, occurs when radicals from the aqueous phase enter the micelles. (The term heterogeneous particle nucleation has been proposed as an alternative to the term micellar particle nucleation.) The radicals may be primary radicals or, much more likely, oligomeric radicals formed by solution polymerization with degrees of polymerization of $\sim 2-5$ [De Bruyn et al., 2002; Dong and Sundberg, 2002]. Homogeneous particle nucleation involves solution-polymerized oligomeric radicals becoming insoluble and precipitating onto themselves (or onto dead oligomer in solution) [Fitch et al., 1969; Hansen and Ugelstad, 1978]. The precipitated species become stabilized by absorbing surfactant (from solution, monomer droplets, and micelles) and on subsequent absorption of monomer are the equivalent of polymer particles formed by micellar nucleation. The relative extents of micellar and homogeneous nucleation are expected to vary with the surfactant concentration and the solubility of monomer in water.

Micellar nucleation is the predominant nucleation process when the surfactant concentration is well above CMC. For styrene and methyl methacrylate, more than 99% of particle nucleation occurs by micellar nucleation [Herrera-Ordonez and Olayo, 2000, 2001; Saldivar et al., 1998]. Since MMA is much more water-soluble than styrene (16 vs. 0.07 g L$^{-1}$), solubility in water is not important in determining the mechanism for nucleation well above CMC. Whether this is the case for vinyl acetate and other monomers more water-soluble than MMA is unclear. Around CMC, micellation nucleation is still the predominant mode of nucleation, but homogeneous nucleation is present—more for vinyl acetate and methyl methacrylate and less for styrene. The situation is much different for all monomers when the surfactant concentration is well below CMC. Micelles are absent below CMC and only homogeneous nucleation occurs. In fact, the occurrence of emulsion polymerization in the absence of micelles is evidence for the homogeneous nucleation mechanism.

It has been suggested that an important growth process for the first-formed polymer particles, sometimes called precursor particles, is coagulation with other particles and not polymerization of monomer. This coagulation, called coagulative nucleation, is then considered as part of the overall nucleation process for the formation of mature polymer particles whose subsequent growth occurs entirely by polymerization [Feeney et al., 1984]. Coagulative nucleation is probably important below CMC. The driving force for coagulation of precursor particles is their relative instability compared to larger particles, that is, there is insufficient surfactant to stabilize a larger number of smaller-sized particles. Once the particles reach a larger size, sufficiently large to be stabilized by the available surfactant, there is no longer a driving force for further coagulation and further growth occurs only by polymerization. Coagulative nucleation is much less important, if at all, above CMC since there is sufficient surfactant to stabilize smaller-sized particles.

4-1b-3 Progress of Polymerization

A variety of behaviors are observed for the polymerization rate versus conversion depending on the relative rates of initiation, propagation, and termination, which are in turn dependent on the monomer and reaction conditions (Fig. 4-2). Irrespective of the particular behavior observed, three intervals (I, II, III) can be discerned in all emulsion polymerizations based on the particle number $N$ (the concentration of polymer particles in units of number of
particles per liter) and the existence of a separate monomer phase (i.e., monomer droplets). There is a separate monomer phase in intervals I and II but not in III. The particle number increases with time in interval I and then remains constant during intervals II and III. Particle nucleation occurs in interval I, with the polymerization rate increasing with time as the particle number builds up. Monomer diffuses into the polymer particles to replace that which has reacted. The reaction system undergoes a very significant change during interval I. The particle number stabilizes at some value which is only a small fraction, typically about 0.1%, of the concentration of micelles initially present. $N$ is the range $10^{16} - 10^{18}$ particles L$^{-1}$. As the polymer particles grow in size and contain polymer as well as monomer, they absorb more and more surfactant (in order to maintain stability) from that in solution. The point is quickly reached at which the surfactant concentration in solution falls below its CMC, the inactive micelles become unstable and disappear with dissolution of micellar surfactant. By the end of interval I or very early in interval II all or almost all of the surfactant in the system has been absorbed by the polymer particles. As a consequence, the monomer droplets are relatively unstable and will coalesce if agitation is stopped. Interval I is generally the shortest of the three intervals, its duration varying in the range 2–15% conversion. Interval I is longer for low initiation rates as more time is needed to attain the steady-state particle number. The more water-soluble monomers such as vinyl acetate tend to complete interval I faster than do the less water-soluble monomers. This is probably a consequence of the significant extent of homogeneous nucleation occurring simultaneously with micellar nucleation, resulting in achieving the steady-state particle number sooner. The predicted maximum in Fig. 4-2 (curve $AB$), arising from a transient high particle number and/or high proportion of particles containing propagating radicals, is seldom distinguishable experimentally, since it is not a high maximum. The maximum is observed for many monomers when the initiation rates are sufficiently high.

Polymerization proceeds in the polymer particles as the monomer concentration in the particles is maintained at the equilibrium (saturation) level by diffusion of monomer from solution, which in turn is maintained at the saturation level by dissolution of monomer.
from the monomer droplets. The monomer concentration in the polymer particles is high; the volume fraction of monomer $\phi_m$ is 0.2, 0.3, 0.5, 0.6, 0.71, and 0.85 for ethylene, vinyl chloride, butadiene, styrene, methyl methacrylate, and vinyl acetate, respectively [Gardon, 1977]. The polymerization rate either is constant (behavior $D$) or increases slightly with time ($E$) during interval II. The latter behavior, which may begin immediately as shown in Fig. 4-2 or after a constant rate period, is a consequence of the gel or Trommsdorff effect (Sec. 3-10a). The polymer particles increase in size as the monomer droplets decrease. Interval II ends when the monomer droplets disappear. The transition from interval II to interval III occurs at lower conversions as the water solubility of the monomer increases and the extent of swelling of the polymer particles by monomer increases. For monomers (e.g., vinyl chloride) with low water solubility and low $\phi_m$, the transition occurs at about 70–80% conversion. The transition occurs at progressively lower conversion as the proportion of the total monomer in the system that is contained in the droplets decreases: styrene and butadiene at 40–50% conversion, methyl methacrylate at 25%, and vinyl acetate at 15% [Zollars, 1979].

The particle number remains the same in interval III as in interval II, but the monomer concentration decreases with time, since monomer droplets are no longer present. The decrease in $\phi_m$ is slower with the more water-soluble monomers as the monomer in solution acts as a reservoir. The presence of a gel effect continues in interval III. The quantitative interplay of a decreasing monomer concentration with the gel effect determines the exact behavior observed in this interval ($GF$ or $H$). Polymerization continues at a steadily decreasing rate as the monomer concentration in the polymer particles decreases. Final conversions of essentially 100% are usually achieved. The final polymer particles, spherical in shape, usually have diameters of 50–300 nm, which places them intermediate in size between the initial micelles and monomer droplets.

### 4-2 QUANTITATIVE ASPECTS

#### 4-2a Rate of Polymerization

An expression for the rate of polymerization is obtained by considering first the rate in a single polymer particle in which propagation is occurring (i.e., a particle containing a radical) and then the number of such particles. At the start of polymerization in a typical system where the concentration of micelles is $10^{21} \text{L}^{-1}$ and the initiation rate for the formation of radicals is $10^{16} \text{L}^{-1} \text{s}^{-1}$, a radical diffuses into a micelle every $10^5 \text{s}$ at the start of interval I. As the system progresses through interval I, this time period decreases sharply, since the concentration of micelles is decreasing. A radical enters each polymer particle on an average of every 10 s during intervals II and III, where $N$ is typically $10^{17} \text{L}^{-1}$. Once inside the micelle or polymer particle, a radical propagates in the usual manner at a rate $r_p$ dependent on the propagation rate constant $k_p$ and the monomer concentration $[M]$ in the particle.

$$r_p = k_p [M]$$

The monomer concentration is usually quite high since in many cases the equilibrium swelling of the particle by monomer is of the order 50–85% by volume. Values of $[M]$ as high a 5 $M$ are common. $[M]$ varies only weakly with the size of the polymer particles.

Consider now what occurs on the entry of a radical into a particle that already has a radical. For most reaction systems, the radical concentration in a polymer particle is $10^{-6} M$ or higher. This is a higher radical concentration than in the homogeneous polymerization systems and the radical lifetime here is only a few thousandths of a second. The entry of
A second radical into the polymer particle results in immediate bimolecular termination. Thus the polymer particle will have either one or zero radicals. The presence of two radicals in one particle is synonymous with zero radicals, since termination occurs so quickly. The particle is then dormant until another (the third) radical arrives. The particle is again activated and propagation proceeds until the next radical. The cycle of alternate growth and inactivity of the polymer particle continues until the monomer conversion is essentially complete.

Compartmentalization (or segregation) of a propagating radical in a polymer particle isolates it from other propagating radicals and allows growth to higher molecular weight than might be achieved in solution polymerization, provided that the rate of entry of another radical from the aqueous phase is sufficiently slow.

The rate of polymerization \( R_p \) at any instant is given by the product of the concentration of active particles \([P]\) and the rate of propagation in a particle.

\[
R_p = k_p[M][P]
\]  
\( (4-2) \)

\([P]\) is conveniently expressed by

\[
[P] = \frac{N'\bar{n}}{N_A}
\]  
\( (4-3) \)

where \( N' \) is the concentration of micelles plus particles, \( \bar{n} \) is the average number of radicals per micelle plus particle, and \( N_A \) is the Avogadro number. The use of \( N_A \) in Eq. 4-3 and in subsequent equations expresses \([P]\) in mol L\(^{-1}\) and \( R_p \) in mol L\(^{-1}\) s\(^{-1}\). Combination of Eqs. 4-2 and 4-3 yields the polymerization rate as

\[
R_p = \frac{N'\bar{n}k_p[M]}{N_A}
\]  
\( (4-4) \)

\( N'\bar{n} \) is zero at the start of interval I, since \( \bar{n} = 0 \). \( N' \) decreases, \( \bar{n} \) increases, and the product \( N'\bar{n} \) increases with time during interval I. At the start of interval II, \( N' \) has reached its steady-state value \( N \). \( \bar{n} \) may or may not reach an absolutely constant value. Behavior D in interval II usually involves a steady-state \( \bar{n} \) value, while behavior E usually involves a slow increase in \( \bar{n} \) with conversion. \( \bar{n} \) will remain approximately constant or increase in interval III although a decrease will occur if the initiation rate decreases sharply on exhaustion of the initiator concentration. Most texts show Eq. 4-5 for the polymerization rate instead of the more general Eq. 4-4. Equation 4-5 applies to intervals II and III where only polymer particles exist (no micelles). It is during intervals II and III that the overwhelming percent of monomer conversion to polymer takes place. In the remainder of Sec. 4-2, the discussions will be concerned only with these intervals.

\[
R_p = \frac{N\bar{n}k_p[M]}{N_A}
\]  
\( (4-5) \)

The value of \( \bar{n} \) during intervals II and III is of critical importance in determining \( R_p \) and has been the subject of much theoretical and experimental work. Three cases can be distinguished—cases 1, 2, and 3. The major differences between the three cases are the occurrence of radical diffusion out of the polymer particles (desorption), the particle size, modes of termination, and the rates of initiation and termination relative to each other and to the other reaction parameters. The quantitative interplay of these factors leading to case 1, 2, or 3 behavior has been discussed [Gao and Penlidis, 2002; Gilbert, 1995; Nomura, 1982;
Our discussion will be in qualitative terms.

Case 2: $\bar{n} = 0.5$. This is the case usually described in texts as applicable to most emulsion polymerizations. It occurs when desorption of radicals does not occur or is negligible compared to the rate of radicals entering particles (absorption) and the particle size is too small, relative to the bimolecular termination rate constant, to accommodate more than one radical. Under these conditions, a radical entering a polymer particle is trapped within that particle and undergoes propagation until another radical enters, at which point there is essentially instantaneous termination. Any polymer particle will be active half of the time and dormant the other half of the time. In other words, at any given moment half of the polymer particles contain one radical and are growing while the other half are dormant. The number of radicals per particle $\bar{n}$ averaged over the particles is 0.5. Case 2 behavior also requires the initiation rate not be excessively low and negligible termination of radicals in the aqueous phase. Systems exhibiting case 2 behavior are often referred to as zero–one systems to indicate that a polymer particle contains either zero or one radical at any given moment.

Case 1: $\bar{n} < 0.5$. The average number of radicals per particle can drop below 0.5 if radical desorption from particles and termination in the aqueous phase are not negligible. The decrease in $\bar{n}$ is larger for small particle sizes and low initiation rates.

Case 3: $\bar{n} > 0.5$. Some fraction of the polymer particles must contain two or more radicals per particle in order for $\bar{n}$ to be larger than 0.5, since there will always be a fraction (a very significant fraction) that has zero radical per particle. This occurs if the particle size is large or the termination rate constant is low while termination in the aqueous phase and desorption are not important and the initiation rate is not too low.

Although many texts indicate that case 2 is the predominant behavior for all monomers, this is not true. Monomers with high water solubility and significant desorption of radicals from polymer, such as vinyl acetate, vinyl chloride, and vinylidene chloride, follow case 1 behavior under a variety of reaction conditions [Blackley, 1975; Nomura and Harada, 1981; Sakai et al., 2001]. For example, $\bar{n}$ is approximately 0.1 or lower for vinyl acetate and vinyl chloride [Gilbert and Napper, 1974; Litt et al., 1970]. Values of $\bar{n}$ are calculated from Eq. 4-5 using the $k_p$ value from bulk polymerization at the appropriate percent conversion, that is, at the conversion corresponding to the volume fraction of monomer in the polymer particles. The monomers that show strong case 1 behavior are those with high monomer chain-transfer constants. Chain transfer to monomer results in a small-sized monomer radical that can desorb from the polymer particle much more readily than the large-sized propagating radical. This was verified by carrying out emulsion polymerizations with intermittent ionizing radiation. The polymerization rate decays to zero after irradiation ceases but before all of the monomer has polymerized [Lansdowne et al., 1980; Ley et al., 1969; Sundari, 1979]. If desorption of monomer radicals did not occur, polymerization should continue until monomer would be exhausted. The polymerization rate decays for all monomers but at very different rates. The decay rate, which follows the desorption rate, increased as the monomer chain transfer constant increased.

The effect of reaction conditions on $\bar{n}$ (and $R_p$, of course) can be observed even with styrene, which shows a very strong tendency toward case 2 behavior under a wide range of reaction conditions [Brooks and Qureshi, 1976; Hawkett et al., 1980]. Seed polymerization
[Hayashi et al., 1989], involving the addition of monomer and initiator to a previously prepared emulsion of polymer particles, is especially useful for this purpose since it allows the variation of certain reaction parameters while holding \( N \) constant. Thus, \( \bar{n} \) in seeded styrene polymerization drops from 0.5 to 0.2 when the initiator concentration decreases from \( 10^{-2} \) to \( 10^{-5} \) \( M \). At sufficiently low \( R_i \), the rate of radical absorption is not sufficiently high to counterbalance the rate of desorption. One also observes that above a particular initiation rate \( ([I] = 10^{-2} M \text{ in this case}) \), the system maintains case 2 behavior with \( \bar{n} \) constant at 0.5 and \( R_p \) independent of \( R_i \). A change in \( R_i \) simply results in an increased rate of alternation of activity and inactivity in each polymer particle. Similar experiments show that \( \bar{n} \) drops below 0.5 for styrene when the particle size becomes sufficiently small. The extent of radical desorption increases with decreasing particle size since the travel distance for radical diffusion from a particle decreases.

Case 3 behavior occurs when the particle size is sufficiently large (about 0.1–1 \( \mu m \)) relative to \( k_t \) such that two or more radicals can coexist in a polymer particle without instantaneous termination. This effect is more pronounced as the particle size and percent conversion increase. At high conversion the particle size increases and \( k_t \) decreases, leading to an increase in \( \bar{n} \). The increase in \( \bar{n} \) occurs at lower conversions for the larger-sized particles. Thus for styrene polymerization \( \bar{n} \) increases from 0.5 to only 0.6 at 90% conversion for 0.7-\( \mu m \) particles. On the other hand, for 1.4-\( \mu m \) particles, \( \bar{n} \) increases to about 1 at 80% conversion and more than 2 at 90% conversion [Chatterjee et al., 1979; Gerrens, 1959]. Much higher values of \( \bar{n} \) have been reported in other emulsion polymerizations [Ballard et al., 1986; Mallya and Plamthottam, 1989]. Methyl methacrylate has a more pronounced Trommsdorff effect than styrene and vinyl acetate, and this results in a more exaggerated tendency toward case 3 behavior for methyl methacrylate.

Consider now the implications of Eq. 4-5. The values of \( k_p \), [M] and, to a large extent, \( \bar{n} \) are specified for any particular monomer. The polymerization rate is then determined by the value of \( N \). Increasing the surfactant concentration and increasing \( R_i \) increases \( N \) (Sec. 4-2c) and, therefore, \( R_p \). These trends are shown in Figs. 4-3 and 4-4 [Hansen and Ugelstad, 1979a,b; Vidotto et al., 1970]. It should be noted that the polymerization rate is unaffected by change in \( R_i \) once particle nucleation has ceased at the end of interval I. Such changes would result only in changing the rate of alternation of activity and inactivity in each polymer particle.

![Fig. 4-3](image_url)  
**Fig. 4-3** Plot of percent conversion versus time for emulsion polymerizations of styrene with different concentrations of potassium laurate at 60°C. The moles of emulsifier per polymerization charge (containing 180 g H2O, 100 g styrene, 0.5 g K2S2O8) are 0.0035 (plot 1), 0.007 (plot 2), and 0.014 (plot 3). After Williams and Bobalek [1966] (by permission of Wiley-Interscience, New York).
The number-average degree of polymerization in an emulsion polymerization can be obtained by considering what occurs in a single polymer particle. The rate \( r_i \) at which primary radicals enter a polymer particle is given by

\[
ri = \frac{R_i}{N} \tag{4-6}
\]

This is the same as the rate of termination \( r_t \) of a polymer chain for case 2 behavior, since termination occurs immediately on the entry of a radical into a polymer particle in which a polymer chain is propagating. The degree of polymerization is then the rate of growth of a polymer chain divided by the rate at which primary radicals enter the polymer particle, that is, Eq. 4-1 divided by Eq. 4-5:

\[
\bar{X}_n = \frac{r_p}{r_i} = \frac{Nk_p[M]}{R_i} \tag{4-7}
\]

Figure 4-5 shows the viscosity-average molecular weights in the emulsion polymerizations of styrene of Fig. 4-3. The results are in line with Eq. 4-7 in that the polymer size increases with the emulsifier concentration.

It should be noted that the degree of polymerization in an emulsion polymerization is synonymous with the kinetic chain length. Although termination is by bimolecular coupling, one of the radicals is a primary (or oligomeric) radical, which does not significantly contribute to the size of a dead polymer molecule. The derivation of Eq. 4-7 assumes the absence
of any termination by chain transfer. If chain transfer occurs the degree of polymerization will be given by

$$X_n = \frac{r_p}{r_i + \sum r_{tr}}$$  \hspace{2cm} (4-8)

where $\sum r_{tr}$ is the sum of the rates of all transfer reactions. The rate of a chain-transfer reaction in a polymer particle would be given by an equation of the type

$$r_{tr} = k_{tr} [X^A] \frac{C_{138}}{C_3}$$  \hspace{2cm} (4-9)

analogous to the case of transfer in homogeneous polymerization (Eq. 3-102).

The degree of polymerization, like the polymerization rate, varies directly with $N$, but the degree of polymerization also varies indirectly with $R_i$. A consideration of Eqs. 4-5 and 4-7 with their analogs for homogeneous, radical chain polymerization (Eqs. 3-25 and 3-99) shows the significant characteristic of the emulsion process. In homogeneous polymerization, one can increase the polymerization rate by increasing the rate of initiation, but the result is a simultaneous lowering of the polymer molecular weight. No experimental variable is available to increase $R_p$ without decreasing $X_n$. The situation is quite different in emulsion polymerization. The rate and degree of polymerization can be simultaneously increased by increasing the number of polymer particles at a constant initiation rate. This important reaction characteristic results from compartmentalization of the propagating radicals, which reduces the rate of termination.

Equations 4-7 and 4-8 require modification to be applicable to case 3 behavior where a significant fraction of the polymer particles have 2 or more radicals per particle. For such particles, one still has $r_i = r_t$ (assuming a steady-state $\dot{n}$) but the degree of polymerization will be twice that for case 2, since termination is by coupling between propagating radicals instead of propagating and primary (or oligomeric) radicals. Thus, the overall degree of polymerization for case 3 behavior will be between $X_n$ as calculated from Eq. 4-7 and twice that value, the exact value being the average between the two weighted in proportion to the fraction of particles that contain more than one propagating radical.
4-2c Number of Polymer Particles

The number of polymer particles is the prime determinant of the rate and degree of polymerization since it appears as the first power in both Eqs. 4-5 and 4-7. The formation (and stabilization) of polymer particles by both micellar nucleation and homogeneous nucleation involves the adsorption of surfactant from the micelles, solution, and monomer droplets. The number of polymer particles that can be stabilized is dependent on the total surface area of surfactant present in the system $a_s S$, where $a_s$ is the interfacial surface area occupied by a surfactant molecule and $S$ is the total concentration of surfactant in the system (micelles, solution, monomer droplets). However, $N$ is also directly dependent on the rate of radical generation. The quantitative dependence of $N$ on $a_s S$ and $R_i$ has been derived as

$$N = k \left( \frac{R_i}{\mu} \right)^{2/5} (a_s S)^{3/5}$$

(4-10)

where $\mu$ is the rate of volume increase of polymer particle (which can be determined from $r_p$ and geometric considerations). The same result has been derived for both micellar and homogeneous nucleations—each in the absence of coagulative nucleation [Roe, 1968; Smith and Ewart, 1948]. The value of $k$ is between 0.37 and 0.53 depending on the assumptions made regarding the relative efficiencies of radical capture by micelles versus polymer particles and which geometric parameter of the particle (radius, surface area or volume) determines the rate at which polymer particles capture radicals. We should note that high particle numbers are associated with small particle size and low particle numbers with large particle size. Equation 4-10 leads to the prediction that the particle radius will be inversely dependent on the 0.20- and 0.13- order of $S$ and $R_i$, respectively.

A consideration of Eq. 4-10 together with Eqs. 4-5 and 4-7 shows that both $R_p$ and $\bar{X}_n$ depend on the $1/3$-power of the total surfactant concentrations. The polymerization rate varies with the $2/3$-power of $R_i$ while the degree of polymerization varies inversely with the $1/3$-power of $R_i$. The dependence of $R_p$ on $R_i$ does not contradict the earlier conclusion regarding the independence of the polymerization rate on the rate of radical production. The rate of radical generation affects the number of polymer particles formed, which in turn determines the polymerization rate. However, once an emulsion polymerization system has reached a steady state with regard to $N$, the rate of radical generation no longer has any effect on the polymerization rate as long as initiation is taking place. Further and very significantly, it should be noted that the number of polymer particles can be increased by increasing the emulsifier concentration while maintaining a constant rate of radical generation. Thus, from the practical viewpoint, one can simultaneously increase $R_p$ and $\bar{X}_n$ by increasing $N$. Increasing $N$ by increasing $R_i$ increases $R_p$ but at the expense of decreasing $\bar{X}_n$.

The predicted dependence of $N$ on $S$ and $R_i$ for the formation of polymer particles by micellar and homogeneous nucleation followed by coagulative nucleation is given by Eq. 4-11 [Feeney et al., 1984]:

$$N \propto R_i^{2/5} S^{0.4-1.2}$$

(4-11)

The occurrence of coagulative nucleation does not alter the $2/3$-power dependence of $N$ on $R_i$. However, the coagulative nucleation mechanism indicates a more complex dependence of $N$ on $S$. The exponent of $S$ decreases monotonically from 1.2 to 0.4 with increasing $S$. The concentration of polymer particles is higher and the nucleation time is longer for systems with high surfactant concentrations. Polymer particle formation becomes less efficient at longer
times as there is a greater tendency for capture of precursor particles by polymer particles when the latter concentrations are high. Within the overall behavior predicted by Eq. 4-11, there is compatibility with the $\frac{1}{3}$-power dependence of $N$ on $R_i$ predicted by Eq. 4-10.

Nonpolar monomers such as styrene, with little tendency toward radical desorption, generally show $\frac{1}{2}$- and $\frac{1}{5}$-power dependencies of $N$ on $S$ and $R_i$, respectively. This result, however, cannot be taken to exclude coagulative nucleation since one cannot preclude the exponent of the dependence of $N$ on $S$ being larger and smaller, respectively, than $\frac{1}{2}$ at lower and higher concentrations of surfactant than those studied. Monomers such as vinyl acetate and vinyl chloride, which show case 1 behavior, tend to show a dependence of $N$ on $S$ in line with that predicted by Eq. 4-11, indicating the presence of coagulative nucleation. Simultaneously, the dependence of $N$ on $R_i$ deviates markedly from that expressed by Eq. 4-11. When extensive radical desorption occurs, the large fraction of nucleation is initiated by desorbed radicals with the result that $N$ is little affected by $R_i$. Thus, the order of dependence of $N$ on $S$ is 0.64 for styrene, 0.86 for methyl methacrylate, 1.0 for vinyl chloride, and 1.0 for vinyl acetate, while the orders of dependence on $R_i$ are 0.36, 0.20, 0, and 0, respectively [Hansen and Ugelstad, 1979a,b]. The emulsion copolymerization of acrylonitrile and butyl acrylate shows a decrease in the exponent of the dependence of $N$ and $S$ from 0.67 to 0.40 with increasing surfactant concentration when an anionic surfactant was used [Capek et al., 1988]. The exponent was close to one for polymerization in the presence of a cationic surfactant.

Anomalous results have been observed in some emulsion polymerizations—inverse dependencies of $N$, $R_p$, and $\overline{X}_n$ on surfactant concentration. Some surfactants act as inhibitors or retarders of polymerization, especially of the more highly reactive radicals from vinyl acetate and vinyl chloride [Okamura and Motoyama, 1962; Stryker et al., 1967]. This is most apparent with surfactants possessing unsaturation (e.g., certain fatty acid soaps). Degradative chain transfer through allyl hydrogens is probably quite extensive.

The polymer particles decrease in stability during intervals II and III since the total polymer particle surface area increases and the coverage of the surface with surfactant decreases. The relative decrease in particle stability appears to be insufficient to cause coalescence as long as stirring is maintained since $N$ is generally observed to be constant. In some systems, however, the stability decreases sufficiently to cause the particles to coalesce and $N$ decreases with conversion [Blackley, 1975].

4-3 OTHER CHARACTERISTICS OF EMULSION POLYMERIZATION

4-3a Initiators

The initiators used in emulsion polymerization are water-soluble initiators such as potassium or ammonium persulfate, hydrogen peroxide, and 2,2'-azobis(2-amidinopropane) dihydrochloride. Partially water-soluble peroxides such as succinic acid peroxide and $t$-butyl hydroperoxide and azo compounds such as 4,4'-azobis(4-cyanopentanoic acid) have also been used. Redox systems such as persulfate with ferrous ion (Eq. 3-38a) are commonly used. Redox systems are advantageous in yielding desirable initiation rates at temperatures below 50°C. Other useful redox systems include cumyl hydroperoxide or hydrogen peroxide with ferrous, sulfite, or bisulfite ion.

4-3b Surfactants

Anionic surfactants are the most commonly used surfactants in emulsion polymerization [Blackley, 1975; Gardon, 1977]. These include fatty acid soaps (sodium or potassium
stearate, laurate, palmitate), sulfates, and sulfonates (sodium lauryl sulfate and sodium dodecylbenzene sulfonate). The sulfates and sulfonates are useful for polymerization in acidic medium where fatty acid soaps are unstable or where the final product must be stable toward either acid or heavy-metal ions. Nonionic surfactants such as poly(ethylene oxide), poly (vinyl alcohol) and hydroxyethyl cellulose are sometimes used in conjunction with anionic surfactants for improving the freeze–thaw and shear stability of the polymer or to aid in controlling particle size and size distribution. The presence of the nonionic surfactant imparts a second mode of colloidal stabilization, in addition to electrostatic stabilization by the anionic surfactant, via steric interference with the van der Waals attraction between polymer particles. Non-ionic surfactants are also of use where the final polymer latex should be insensitive to changes in pH over a wide range. Nonionic surfactants are only infrequently used alone, since their efficiency in producing stable emulsions is less than that of the anionic surfactants. Anionic surfactants are generally used at a level of 0.2–3 wt% based on the amount of water; nonionic surfactants are used at the 2–10% level. Cationic surfactants such as dodecylammonium chloride and cetyltrimethylammonium bromide are much less frequently used than anionic surfactants because of their inefficient emulsifying action or adverse effects on initiator decomposition. Also, cationic surfactants are more expensive than anionic surfactants.

Surfactants increase particle number and decrease particle size as their concentration in the initial reaction charge is increased. However, one can use delayed addition of surfactant after nucleation is complete to improve particle stability, without affecting the particle number, size, and size distribution.

4-3c Other Components

The quality of the water used in emulsion polymerization is important. Deionized water may be used since the presence of foreign ions or ions in uncontrolled concentrations can interfere with both the initiation process and the action of the emulsifier. Antifreeze additives are used to allow polymerization at temperatures below 0°C. These include inorganic electrolytes as well as organics such as ethylene glycol, glycerol, methanol, and monoalkyl ethers of ethylene glycol. The addition of inorganic electrolytes often affects the polymerization rate and stability of the emulsion. Sequestering agents such as ethylenediamine tetraacetic acid or its alkali metal salts may be added to help solubilize a component of the initiator system or to deactivate traces of calcium and magnesium ions present in the water. Buffers such as phosphate or citrate salts may be used to stabilize the latex toward pH changes.

4-3d Propagation and Termination Rate Constants

Emulsion polymerization proceeds in a polymer particle where the concentration of polymer is quite high throughout the reaction. This type of system is similar to a bulk polymerization in the later stages of reaction where there is a strong Trommsdorff effect. The propagation rate constant for an emulsion polymerization can be obtained for case 2 systems from the polymerization rate using Eq. 4-5, where $n = 0.5$. One can ascertain that case 2 behavior is present by observing whether the polymerization rate in interval II is insensitive to changes in the initiation rate. The value of $k_p$ can also be obtained from the degree of polymerization using Eq. 4-7. This is often a more reliable measure of $k_p$ since there is no need to make any assumption on the value of $n$. The propagation rate constant is generally found to have the same value in emulsion polymerization as in the corresponding bulk polymerization at high conversion—more specifically, at a conversion corresponding to the volume fraction of polymer in monomer that exists in the emulsion system.
4-3e Energetics

The heat of an emulsion polymerization is the same as that for the corresponding bulk or solution polymerization, since $\Delta H$ is essentially the enthalpy change of the propagation step. Thus, the heats of emulsion polymerization for acrylic acid, methyl acrylate, and methyl methacrylate are $-67$, $-77$, and $-58$ kJ mol$^{-1}$, respectively [McCurdy and Laidler, 1964], in excellent agreement with the $\Delta H$ values for the corresponding homogeneous polymerizations (Table 3-14).

The effect of temperature on the rate of emulsion polymerization, although not extensively studied, is generally similar to that on homogeneous polymerization with a few modifications. The overall rate of polymerization increases with an increase in temperature. Temperature increases the rate by increasing both $k_p$ and $N$. The increase in $N$ is due to the increased rate of radical generation at higher temperatures. Opposing this trend to a slight extent is the small decrease in the concentration of monomer in the particles at higher temperatures. Thus, the value of [M] for styrene decreases $\sim$15% in going from 30 to 90°C [Smith and Ewart, 1948]. The overall activation energy for emulsion polymerization is, thus, a combination of the activation energies for propagation, radical production, and [M]. For the few systems studied, the overall activation energies for emulsion polymerization are approximately the same as or less than those for the corresponding homogeneous polymerization [Stavrova et al., 1965].

Carrying out an emulsion polymerization requires an awareness of the krafft point of an ionic surfactant and the cloud point of a nonionic surfactant. Micelles are formed only at temperatures above the Krafft point of an ionic surfactant. For a nonionic surfactant, micelles are formed only at temperatures below the cloud point. Emulsion polymerization is carried out below the cloud temperature of a nonionic surfactant and above the Krafft temperature of an ionic surfactant.

4-3f Molecular Weight and Particle Size Distributions

Theoretical considerations indicate that compartmentalization of radicals in polymer particles does not change the polydispersity index $PDI (= \bar{X}_w/\bar{X}_n)$ in emulsion polymerization from its value of 2 in homogeneous polymerization when termination takes place by transfer to monomer, chain-transfer agent, or other substance [Butte et al., 2002a,b; Giannetti et al., 1988; Gilbert, 1995; Lichti et al., 1980, 1982; Mendizabal et al., 2000]. However, emulsion polymerization results in molecular weight broadening when termination involves bimolecular reaction between radicals. While short propagating chains are likely to couple or disproportionate with longer chains in homogeneous polymerization (PDI = 1.5 and 2 for coupling and disproportionation, respectively) (Sec. 3-11), any two chains that undergo bimolecular termination in emulsion polymerization are not random. The broadening of PDI in emulsion polymerization is greater for disproportionation than for coupling. For case 2 behavior, coupling of the propagating chain in a polymer particle with the low-molecular-weight entering radical does not greatly affect PDI. Such coupling is equivalent to termination by chain transfer and PDI has a value of 2 compared to 1.5 for homogeneous polymerization. When termination is by disproportionation, PDI has a value of 4 at $n = 0.5$ compared to 2 for homogeneous polymerization [Butte et al., 2002a,b]. Low-molecular-weight radicals entering the polymer particles disproportionate with propagating radicals and increase the number of low-molecular-weight molecules; $\bar{X}_n$ is decreased while $\bar{X}_w$ is essentially unchanged and $\bar{X}_w/\bar{X}_n$ increases. When $n > 0.5$ (case 3), the tendency toward molecular weight broadening decreases as the size of the radicals undergoing coupling or disproportionation
become more nearly the same size. PDI tends toward the values in homogeneous polymerization (1.5 and 2 for coupling and disproportionation, respectively) as \( \bar{n} \) increases from 0.5 to 2.

The preceding discussion relates primarily to polymerization in stage II of an emulsion polymerization. Since this constitutes the major portion of an emulsion polymerization and the reaction conditions (\( N, R, k_p, [M] \)) are relatively constant during stage II, the molecular weight distribution is considerable narrower than in homogeneous polymerization [Cooper, 1974; Lin and Chiu, 1979]. However, there is molecular weight broadening with conversion as reaction proceeds through stage III where various reaction parameters are no longer constant. Also, the molecular weights produced during stage I are not the same as in stage II. The PDI for a batch polymerization taken to complete conversion can be as high as 5–7 [Butte et al., 2002a,b], which is still lower than for a typical homogeneous polymerization.

In addition to the molecular-weight distribution, there is a particle size distribution in emulsion polymerization [Chen and Wu, 1988; Gardon, 1977; Lichti et al., 1982]. The particle size distribution (PSD) is expressed, analogously to the molecular weight distribution, as the ratio of the weight-average particle size to number-average particle size. (Different particle sizes are calculated depending on whether one uses the particle radius, diameter, or volume as the measure of particle size.) The particle size distribution is a consequence of the distribution of times at which different polymer particles are nucleated. The polydispersity is maximum during interval I and narrows considerably during the subsequent period. There has been an effort to produce narrow-particle-size distributions (PSD) by controlling the nucleation process, choice and amount of surfactant, temperature and other reaction variables, and the use of seed emulsion polymerization. Narrow particle size distributions are useful in applications such as calibration of electron microscope, ultracentrifuge, aerosol counting, and light-scattering instruments and the measurement of pore sizes of filters and membranes. Narrow particle distributions, with PSD values of 1.1 and lower, have been obtained by choosing reaction conditions with short nucleation times (short interval I relative to intervals II and III), increased latex stability (to prevent coagulation), and decreased interval III times.

4-3g Surfactant-Free Emulsion Polymerization

The presence of surfactant is a disadvantage for certain applications of emulsion polymers such as those involving instrument calibration and pore size determination. The presence of adsorbed surfactant gives rise to somewhat variable properties since the amount of adsorbed surfactant can vary with the polymerization and application conditions. Removal of the surfactant, either directly or by desorption, can lead to coagulation or flocculation of the destabilized latex. Surfactant-free emulsion polymerization, involving no added surfactant, is a useful approach to solving this problem [Chainey et al., 1987; Li and Salovey, 2000; Ni et al., 2001]. The process uses an initiator yielding initiator radicals that impart surface-active properties to the polymer particles. Persulfate is a useful initiator for this purpose. Latexes prepared by the surfactant-free technique are stabilized by chemically bound sulfate groups of the \( \text{SO}_4^- \)-initiating species derived from persulfate ion. Since the surface-active groups are chemically bound, the latexes can be purified (freed of unreacted monomer, initiator, etc.) without loss of stability, and their stability is retained over a wider range of use conditions than the corresponding latices produced using surfactants. A characteristic of surfactant-free emulsion polymerization is that the particle number is generally lower by up to about 2 orders of magnitude compared to the typical emulsion polymerization, typically \( 10^{12} \) versus \( 10^{14} \) particles per milliliter. This is a consequence of the lower total particle surface area.
that can be stabilized by the sulfate groups alone relative to that when added surfactant is present.

Another approach to producing latexes with chemically bound surface-active groups is to use a reactive surfactant—a surfactant with a polymerizable double bond, such as sodium dodecyl allyl sulfosuccinate [Wang et al., 2001a,b,c]. Copolymerization of the reactive surfactant with the monomer of interest binds the surface active groups into the polymer chains.

4-3h Other Emulsion Polymerization Systems

In the conventional emulsion polymerization, a hydrophobic monomer is emulsified in water and polymerization initiated with a water-soluble initiator. Emulsion polymerization can also be carried out as an inverse emulsion polymerization [Poehlein, 1986]. Here, an aqueous solution of a hydrophobic monomer is emulsified in a nonpolar organic solvent such as xylene or paraffin and polymerization initiated with an oil-soluble initiator. The two types of emulsion polymerizations are referred to as oil-in-water (o/w) and water-in-oil (w/o) emulsions, respectively. Inverse emulsion polymerization is used in various commercial polymerizations and copolymerizations of acrylamide as well as other water-soluble monomers. The end use of the reverse latexes often involves their addition to water at the point of application. The polymer dissolves readily in water, and the aqueous solution is used in applications such as secondary oil recovery and flocculation (clarification of wastewater, metal recovery).

Nonionic surfactants such as sorbitan monooleate yield more stable emulsions than do ionic surfactants. However, the latexes from inverse emulsion polymerizations are generally less stable than those from conventional emulsion polymerizations, and flocculation is a problem.

Miniemulsion polymerization involves systems with monomer droplets in water with much smaller droplets than in emulsion polymerization, about 50–1000 nm compared to 1–100 µm in diameter [Antonietti and Landfester, 2002; Asua, 2002; Bechthold and Landfester, 2000; Landfester, 2001]. Micelles are usually not present because surfactant concentrations are generally below CMC. Water-insoluble costabilizers such as hexadecane and cetyl alcohol are present along with the surfactant to stabilize the monomer droplets against diffusional degradation (coagulation), referred to as Ostwald ripening. The droplet size depends not only on the amount of surfactant and costabilizer but also on the amount of energy used in the homogenization process. The final polymer particle size is similar to the monomer droplet size. Both water-soluble and oil-soluble initiators have been used in miniemulsion polymerization. The reaction approximates an emulsion or suspension polymerization depending on the monomer droplet size. Larger droplet sizes (>500 nm) lead to suspension polymerization; smaller droplet sizes lead to emulsion polymerization. Miniemulsion polymerizations are useful for producing high-solids-content latexes. Inverse miniemulsion polymerizations have also been studied [Landfester et al., 2001].

Microemulsion polymerization is an emulsion polymerization with very much smaller monomer droplets, about 10–100 nm compared to 1–100 µm. Micelles are present because the surfactant concentration is above CMC. The final polymer particles generally have diameters of 10–50 nm. Although many of the characteristics of microemulsion polymerization parallel those of emulsion polymerization, the details are not exactly the same [Co et al., 2001; de Vries et al., 2001; Lopez et al., 2000; Medizabal et al., 2000]. Water-soluble initiators are commonly used, but there are many reports of microemulsion polymerization with oil-soluble initiators. Nucleation in emulsion polymerization occurs almost exclusively in the early portion of the process (interval I). Nucleation occurs over a larger portion of the process in microemulsion polymerization because of the large amount of surfactant present. Nucleation
may extend over most of the process. The result is that interval II with an approximately constant polymerization rate is not observed. Unlike emulsion polymerizations, only two intervals are observed in most microemulsion polymerizations. The polymerization rate increases with time, reaches a maximum, and then decreases.

### 4-3i Living Radical Polymerization

The emulsion process has been studied for ATRP, NMP, RAFT, and other living radical polymerizations [Antonietti and Landfester, 2002; Asua, 2002; Cunningham, 2002; Farcet and Charleaux, 2002; Prescott et al., 2002; Qui et al., 2001]. Living polymerizations with the ability to produce block copolymers and functionalized polymers have been observed, although fast polymerizations with good control of molecular weight and PDI are not easily achieved. More work is needed to fully understand the kinetic and other characteristics of the processes, which are not necessarily the same as conventional (nonliving) radical polymerization under emulsion conditions.

The components of the reaction system (initiator, transfer agent, catalyst, deactivating agent, surfactant) need to be carefully chosen to avoid undesirable interactions at the temperatures and concentrations used in emulsion systems. Among the possible undesirable interactions is decreased stability of micelles and polymer particles. Another consideration is partitioning of the reaction components between the aqueous and organic phases. Controlled polymerization requires that the various components have the appropriate relative solubilities in the droplets, micelles, and polymer particles. The components also need to be water-soluble so that they can be transported from the monomer droplets through the aqueous phase to the micelles and polymer particles. With appropriate choices, the conditions needed for living polymerization can be achieved.

Nonliving and living polymerizations differ in the nucleation process. In nonliving polymerization, propagating radicals undergo fast growth in polymer particles in an irreversible process without desorption of propagating chains. In living polymerization, polymer chain growth is slow and proceeds with reversible activation/deactivation (ATRP, NMP) or transfer (RAFT). Short polymer chains are not irreversibly trapped in polymer particles and desorption occurs with a distribution between the aqueous phase and the polymer particles. Nucleation with well-defined polymer particles is delayed and not easy to achieve. Colloid stability and well-controlled polymerization (with good control of molecular weight, PDI, and PSD) are a challenge. Miniemulsion polymerization simplifies the nucleation process and the choice of the various components of the system. It allows the use of hydrophobic initiators, transfer agents, activators, and other components, which are soluble in the monomer droplets, instead of requiring a balance between hydrophobic and hydrophilic characteristics as required for particle nucleation in emulsion polymerization. Living miniemulsion polymerizations are more easily controlled than living emulsion polymerizations.

The kinetics of living emulsion polymerization follow a different course depending on whether there is reversible termination or reversible transfer. For reversible termination living systems (ATRP, NMP), the overall radical concentration is lowered relative to the nonliving systems, the average number of radicals per polymer particle is usually far below 1, while the average number of deactivator species is much larger than 1. The compartmentalization effect of emulsion polymerization is absent, and the polymerization essentially follows bulk polymerization behavior. The polymerization rates are generally similar to or lower than those in homogeneous polymerization. There is less control of molecular weight, and the PSD is broader for living emulsion polymerization. For reversible transfer systems (RAFT), there is continuous radical generation, and the radical concentrations in emulsion
polymerization are similar to those in homogeneous polymerization. The compartmentaliza-
tion effect of emulsion polymerization is present for living polymerizations. The overall rate
and kinetics are similar to those in nonliving emulsion polymerization, but retardation is
often observed for dithioesters, most likely due to desorption of radicals from polymer
particles.

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PROBLEMS

4-1 Describe the components of an emulsion polymerization system on a macroscopic level. Compare the pros and cons of emulsion polymerization as a process condition in comparison to bulk and solution polymerization.

4-2 Describe the microscopic picture of emulsion polymerization according to Harkins, Smith, and Ewart. Where are the monomer, initiator, and emulsifier located? Describe the changes that take place as the reaction proceeds to 100% conversion.

4-3 What are the characteristic overall features that distinguish emulsion polymerization from homogeneous polymerization? Compare the two with regard to the heat of polymerization and the effect of temperature on the polymerization rate.

4-4 Quantitatively compare the rate and degree of polymerization of styrene polymerized in bulk at 60°C with an emulsion polymerization (case 2 behavior: \( n = 0.5 \)) containing \( 1.0 \times 10^{15} \) polymer particles per milliliter. Assume that \([M] = 5.0\) molar, \( R_i = 5.0 \times 10^{12} \) radicals per milliliter per second, and all rate constants are the same for both systems. For each polymerization system, indicate the various ways (if any) by which the polymerization rate can be affected without affecting the degree of polymerization.

4-5 Describe the reaction conditions under which deviations from case 2 behavior are observed; that is, when does \( n > 0.5 \) (case 3) and \( n < 0.5 \) (case 1)?
The ionic chain polymerization of unsaturated linkages is considered in this chapter, primarily the polymerization of the carbon–carbon double bond by cationic and anionic initiators (Secs. 5-2 and 5-3). The last part of the chapter considers the polymerization of other unsaturated linkages. Polymerizations initiated by coordination and metal oxide initiators are usually also ionic in nature. These are called coordination polymerizations and are considered separately in Chap. 8. Ionic polymerizations of cyclic monomers is discussed in Chap. 7. The polymerization of conjugated dienes is considered in Chap. 8. Cyclopolymerization of nonconjugated dienes is discussed in Chap. 6.

5-1 COMPARISON OF RADICAL AND IONIC POLYMERIZATIONS

Almost all monomers containing the carbon–carbon double bond undergo radical polymerization, while ionic polymerizations are highly selective (Table 3-1). Cationic polymerization is essentially limited to those monomers with electron-releasing substituents such as alkoxy, phenyl, vinyl, and 1,1-dialkyl. Anionic polymerization takes place with monomers possessing electron-withdrawing groups such as nitrile, carbonyl, phenyl, and vinyl. The selectivity of ionic polymerization is due to the very strict requirements for stabilization of anionic and cationic propagating species (Sec. 3-1b-2). The commercial utilization of cationic and anionic polymerizations is rather limited because of this high selectivity of ionic polymerizations compared to radical polymerization (and the greater importance of coordination polymerization compared to ionic polymerization).
Ionic polymerizations, especially cationic polymerizations, are not as well understood as radical polymerizations because of experimental difficulties involved in their study. The nature of the reaction media in ionic polymerizations is often not clear since heterogeneous inorganic initiators are often involved. Further, it is extremely difficult in most instances to obtain reproducible kinetic data because ionic polymerizations proceed at very rapid rates and are extremely sensitive to the presence of small concentrations of impurities and other adventitious materials. The rates of ionic polymerizations are usually greater than those of radical polymerizations. These comments generally apply more to cationic than anionic polymerizations. Anionic systems are more reproducible because the reaction components are better defined and more easily purified.

Cationic and anionic polymerizations have many similar characteristics. Both depend on the formation and propagation of ionic species, a positive one in one case and a negative one in the other. The formation of ions with sufficiently long lifetimes for propagation to yield high-molecular-weight products generally requires stabilization of the propagating centers by solvation. Relatively low or moderate temperatures are also needed to suppress termination, transfer, and other chain-breaking reactions which destroy propagating centers.

Although solvents of high polarity are desirable to solvate the ions, they cannot be employed for several reasons. The highly polar hydroxylic solvents (water, alcohols) react with and destroy most ionic initiators. Other polar solvents such as ketones prevent initiation of polymerization by forming highly stable complexes with the initiators. Ionic polymerizations are, therefore, usually carried out in solvents of low or moderate polarity such as tetrahydrofuran, ethylene dichloride, and pentane, although moderately high polarity solvents such as nitrobenzene are also used. In such solvents one usually does not have only a single type of propagating species. For any propagating species such as ~~~BA in cationic polymerization, one can visualize the range of behaviors from one extreme of a completely covalent species (I) to the other of a completely free (and highly solvated) ion (IV)

\[
\begin{align*}
\sim\sim\sim BA & \quad \sim\sim B^+ A^- & \quad \sim\sim B^+ || A^- & \quad \sim\sim B^+ + A^- \\
I & \quad II & \quad III & \quad IV
\end{align*}
\]

The intermediate species include the tight or contact ion pair (II) (also referred to as the intimate ion pair) and the solvent-separated or loose ion pair (III). The intimate ion pair has a counter- or gegenion of opposite charge close to the propagating center (unseparated by solvent), the solvent-separated ion pair involves ions that are partially separated by solvent molecules. The propagating cationic chain end has a negative counterion. For an anionic polymerization the charges in species II-IV are reversed; that is, B carries the negative charge and A the positive charge. There is a propagating anionic chain end with a positive counterion. Alternate terms used for free ion and ion pair are unpaired ion and paired ion, respectively.

Most ionic polymerizations involve two types of propagating species, an ion pair and a free ion IV, coexisting in equilibrium with each other. The identity of the ion pair (i.e., whether the ion pair is best described as species II or III) depends on the particular reaction conditions, especially the solvent employed. Increased solvent polarity favors the loose ion pair while the tight ion pair predominates in solvents of low polarity. The ion pairs in cationic polymerization tend to be loose ion pairs even in solvent of low or moderate polarity since the counterions (e.g., bisulfate, SbCl$_5^-$, perchlorate) are typically large ions. The lower charge density of a large counterion results in smaller electrostatic attractive forces between the propagating center and counterion. The nature of the ion pairs is much more solvent-dependent
in anionic polymerizations where the typical counterion (e.g., Li\(^+\), Na\(^+\)) is small. The covalent species I is generally ignored since it is usually unreactive (or much lower in reactivity) compared to the other species. Free-ion concentrations are generally much smaller than ion-pair concentrations but the relative concentrations are greatly affected by the reaction conditions. Increased solvent polarity results in a shift from ion pairs to free ions. The nature of the solvent has a large effect in ionic polymerization since the different types of propagating species have different reactivities. Loose ion pairs are more reactive than tight ion pairs. Free ions are orders of magnitude higher in reactivity than ion pairs in anionic polymerization. Ion pairs are generally no more than an order of magnitude lower in reactivity compared to free ions in cationic polymerization.

Ionic polymerizations are characterized by a wide variety of modes of initiation and termination. Unlike radical polymerization, termination in ionic polymerization never involves the bimolecular reaction between two propagating polymer chains of like charge. Termination of a propagating chain occurs by its reaction with the counterion, solvent, or other species present in the reaction system.

5-2 CATIONIC POLYMERIZATION OF THE CARBON–CARBON DOUBLE BOND

5-2a Initiation

Various initiators can be used to bring about the polymerization of monomers with electron-releasing substituents [Faust and Shaffer, 1997; Gandini and Cheradame, 1980, 1985; Kennedy and Marechal, 1982; Matyjaszewski and Pugh, 1996; Sauvet and Sigwalt, 1989]. Additional information on cationic initiators is described in Chap. 7.

5-2a-1 Protonic Acids

Protonic (Brønsted) acids initiate cationic polymerization by protonation of the olefin. The method depends on the use of an acid that is strong enough to produce a reasonable concentration of the protonated species

\[
\text{HA} + \text{RR'C} = \text{CH}_2 \rightarrow \text{RR'}^{+}\text{C}(\text{A})^{-} \quad \text{CH}_3 \tag{5-1}
\]

but the anion of the acid should not be highly nucleophilic; otherwise it will terminate the protonated olefin by combination (i.e., by covalent bond formation)

\[
\text{RR'}^{+}\text{C}(\text{A})^{-} \rightarrow \text{RR'}\text{C} = \text{CH}_3 \tag{5-2}
\]

The method used in drawing the ionic species in these two equations and throughout this chapter is meant to show that the ionic species usually do not exist as free ions but as ion pairs. The parentheses around the anionic fragment is used to indicate that the negative counterion remains close to the positive fragment. (Even when the counterion is not shown, one should understand it is present.) However, keep in mind that free ions coexist with the ion pairs, and it is the relative concentrations that determine the overall polymerization rate.
The nomenclature for positively charged organic ions has undergone some change. The older term, no longer used, for the trivalent, trigonal sp\(^2\)-hybridized species such as those in Eqs. 5-1 and 5-2 is carbonium ion. Olah [1972, 1988] proposed that carbenium ion be used instead with the term carbonium ion being reserved for pentavalent charged carbon ions (e.g., nonclassical ions) and the term carboxation encompassing both carbenium and carbonium ions. The term carbenium ion for the trivalent carbon ion has not taken firm hold. Most text and journal references use the term carbocation, and so will this text. The term carbocation polymerization is used synonymously with cationic polymerization in the literature.

The requirement for the anion not to be excessively nucleophilic generally limits the utility of most strong acids as cationic initiators. Hydrogen halides are ineffective as initiators of cationic polymerization because of the highly nucleophilic character of halide ions. One forms only the 1:1 addition product of alkene and hydrogen halide under most conditions. Hydrogen iodide shows some tendency to initiate polymerization of the most reactive monomers, such as vinyl ethers and N-vinylcarbazole (Sec. 5-2g-3). Other strong acids with less nucleophilic anions, such as perchloric, sulfuric, phosphoric, fluoro- and chlorosulfonic, methanesulfonic, and trifluoromethanesulfonic (triflic) acids, initiate polymerization, but the polymer molecular weights rarely exceed a few thousand.

**5-2a-2 Lewis Acids**

Various Lewis acids are used to initiate cationic polymerization, generally at low temperatures, with the formation of high-molecular-weight polymers in high yield. These include metal halides (e.g., AlCl\(_3\), BF\(_3\), SnCl\(_4\), SbCl\(_5\), ZnCl\(_2\), TiCl\(_4\)) and their organometallic derivatives (e.g., RAICl\(_2\), R\(_2\)AlCl, R\(_3\)Cl). Lewis acids are the most important means of initiating cationic polymerization. Aluminium, boron, tin, and titanium halides are the most frequently used Lewis acids.

Initiation by Lewis acids almost always requires and/or proceeds much faster in the presence of either a proton donor (protogen) such as water, hydrogen halide, alcohol, and carboxylic acid, or a carbocation donor (cationogen) such as an alkyl halide (e.g., \textit{t}-butyl chloride and triphenylmethyl chloride), ester, ether, or anhydride. Thus, dry isobutylene is unaffected by dry boron trifluoride but polymerization occurs immediately when trace amounts of water are added [Evans and Meadows, 1950]. The terminology of Kennedy and Marechal [1982] is used in this book; the protogen or cationogen is referred to as the \textit{initiator}, while the Lewis acid is the \textit{coinitiator}. The reader is cautioned that much of the published literature until 1990 or so used the reverse terminology. The protogen or cationogen is referred to as the initiator since it supplies the proton or cation that ultimately adds to monomer to initiate polymerization. The initiator and coinitiator, representing an \textit{initiating system}, react to form an \textit{initiator–coinitiator complex} (or \textit{syncatalyst system}), which then proceeds to donate a proton or carbocation to monomer and, thus, to initiate propagation [Dunn, 1979; Kennedy, 1976].

The initiation process for boron trifluoride and water is

\[
\text{BF}_3 + \text{H}_2\text{O} \rightleftharpoons \text{BF}_3\cdot\text{OH}_2 \quad (5-3a)
\]

\[
\text{BF}_3\cdot\text{OH}_2 + (\text{CH}_3)_2\text{C}==\text{CH}_2 \rightarrow (\text{CH}_3)_3\text{C}^+\!(\text{BF}_3\text{OH})^- \quad (5-4a)
\]

The initiator–coinitiator complex BF\(_3\cdot\text{OH}_2\) is often shown as H\(^+\)(BF\(_3\text{OH}\))\(^-\). Initiation by aluminum chloride and \textit{t}-butyl chloride is described by

\[
\text{AlCl}_3 + (\text{CH}_3)_2\text{CCl} \rightleftharpoons (\text{CH}_3)_3\text{C}^+\!(\text{AlCl}_4)^- \quad (5-3b)
\]

\[
(\text{CH}_3)_3\text{C}^+\!(\text{AlCl}_4)^- + \phi\text{CH}==\text{CH}_2 \rightarrow (\text{CH}_3)_3\text{C}\phi\text{CH}==\text{CH}_2\phi(\text{AlCl}_4)^- \quad (5-4b)
\]
The initiation process can be generalized as

\[
\begin{align*}
I + ZY & \overset{K}{\longrightarrow} Y^+(IZ)^- \\
Y^+(IZ)^- + M & \overset{k_i}{\longrightarrow} YM^+(IZ)^-
\end{align*}
\]  

(5-3c)  

(5-4c)

where I, ZY, and M represent the coinitiator, initiator, and monomer, respectively. Initiation by the combination of a Lewis acid and protogen or cationogen has the advantage over initiation by a Brønsted acid that the anion \(IZ^-\) is far less nucleophilic than \(A^-\). This prolongs the life of the propagating carbocation and allows propagation to proceed to higher molecular weight.

Initiation by the combination of an alkyl halide and Lewis acid can be achieved by using a hydrogen halide and a Lewis acid. The alkyl halide is produced in situ by addition of hydrogen halide to monomer, followed by reaction with the Lewis acid.

There is evidence that Lewis acids initiate a slow polymerization in some (but not most) systems by a self-ionization process in addition to the coinitiation process [Balogh et al., 1994; Grattan and Plesch, 1980; Masure et al., 1978, 1980]. Two mechanisms are possible for self-initiation. One involves bimolecular ionization

\[
2\text{AlBr}_3 \overset{\text{K}}{\longrightarrow} \text{AlBr}_2^2(\text{AlBr}_4)^-
\]  

(5-3d)

followed by reaction with monomer:

\[
\text{AlBr}_2^2(\text{AlBr}_4)^- + M \rightarrow \text{AlBr}_2M^+(\text{AlBr}_4)^-
\]  

(5-4d)

The Lewis acid acts as both initiator and coinitiator. The second mechanism involves the addition of Lewis acid to monomer followed by reaction of the adduct with another molecule of Lewis acid:

\[
\text{BF}_2 + M \overset{\text{K}}{\longrightarrow} \text{BF}_2M \overset{\text{K}}{\longrightarrow} \text{BF}_2M^+ \text{BF}_4^-
\]  

(5-5)

Most of the evidence to support the self-ionization process is indirect, consisting of kinetic, conductance, and spectrophotometric data for polymerization at different levels of dryness and purity. One concludes that self-ionization occurs if polymerization is achieved in systems subjected to the most stringent purification and drying procedures. The major problem in ascertaining whether self-initiation occurs—and, if it does, its extent relative to the initiation process involving a coinitiator—is the large effect exerted by small amount of protogens or cationogens. Thus water concentrations of \(10^{-3} M\) are sufficient to increase the initiation rate by a factor of \(10^3\) for TiCl_4 and AlCl_3 in CH_2Cl_2 [Masure et al., 1978, 1980; Sauvet et al., 1978]. Polymerizations in the presence of sterically hindered pyridines such as 2,6-di-t-butylpyridine and 2,4,6-tri-t-butylpyridine offer further evidence for the presence of a self-ionization initiation process [Gandini and Martinez, 1988]. Sterically hindered pyridines (SHP) are generally active proton scavengers but do not react with Lewis acids or carbocations; in other words, steric hindrance cuts down on the reactivity of the nitrogen toward electrophilic species larger than protons. The presence of SHP results in complete inhibition of polymerization in some systems but only lowered reaction rates in other systems. For the latter, one observes a continuous decrease in polymerization rate with increasing concentration of SHP up to some critical SHP concentration. Thereafter, there is a residual (self-initiation) polymerization rate that is unaffected by increasing SHP concentration. The
SHP method is not completely without ambiguity since SHP may not scavenge protons efficiently in a heterogeneous reaction system or in systems where protons never appear as such but are transferred in a concerted process. The strongest evidence to support self-ionization is the detection of one boron end group per polymer molecule in the BI₃ polymerization of α-methylstyrene in the presence of SHP [Koroskenyi et al., 1997]. When self-ionization occurs, its contribution to the overall initiation process is generally small in the presence of a protogen or cationogen. For many polymerizations, the moisture content (and/or level of other protogen or cationogen) is often sufficient so that self-ionization constitutes only a minor proportion of the total initiation process. (Conventional “dry box” conditions usually do not involve moisture levels lower than 10⁻³ M [Kennedy, 1976].)

The activity of an initiator–coinitiator complex is dependent on its ability to donate a proton or carboxylation to the monomer, which, in turn, depends on the initiator, coinitiator, solvent, and monomer. The extent of formation of the initiator–coinitiator complex (i.e., the value of K in Eq. 5-3c) and its rate of addition to monomer (i.e., the value of kᵢ in Eq. 5-4c) generally increase with increasing acidity of the Lewis acid coinitiator. Lewis acidity for different metals generally increases with increasing atomic number in each group (vertical row of periodic table): Ti > Al > B; Sn > Si; Sb > As [Matyjaszewski and Pugh, 1996]. For any metal, Lewis acidity increases with increasing oxidation state, for example, TiCl₄ > TiCl₂. Ligands increase Lewis acidity in the order: F > Cl > Br > I > RO > RCOO > R, Ar. The strongest Lewis acids (e.g., SbF₅) are not always the most useful since the result may be excessively fast and uncontrolled polymerization or the reverse—low rates due to the formation of excessively stable and inactive complexes between the Lewis acid and some other component of the reaction system.

The activity of the initiator–coinitiator complex also increases with increasing acidity of the initiator, for example, hydrogen chloride > acetic acid > nitroethane > phenol > water > methanol > acetone in the polymerization of isobutylene with tin(IV) chloride [Kennedy, 1968; Plesch, 1963]. A word of caution regarding these generalizations—the order of activity of a series of initiators or coinitiators may differ depending on the identity of the other component, monomer, solvent, or the presence of competing reactions. For example, the activity of boron halides in isobutylene polymerization, BF₃ > BCl₃ > BBr₃, with water as the initiator is the opposite of their acidities. Hydrolysis of the boron halides to inactive products, increasing in the order BBr₃ > BCl₃ > BF₃, is responsible for the observed polymerization results [Kennedy et al., 1977, Kennedy and Feinberg, 1978].

The reactivity of organic halide cationogens in initiation depends on carboxylation stability in a complex manner. Increased carboxylation stability results in the formation of higher concentrations of carboxylations from the cationogen but the carboxylations have lower reactivity. Differences in the stability of the carboxylation formed from the cationogen compared to the propagating carboxylation are also important in determining the effectiveness of a cationogen. Primary and secondary alkyl halides are generally ineffective as initiators of cationic polymerization. Primary and secondary carboxylations are formed too slowly and/or in extremely low concentrations. (There are a few reports of initiation by primary or secondary halides [Toman et al., 1989a,b], but initiation more likely involves self-ionization of the Lewis acid or the presence of adventitious water.) Tertiary carboxylations such as t-butyl and 2-phenyl-isopropyl (cumyl) are sufficiently stable to form but are not more stable than the carboxylations derived from their additions to monomers such as isobutylene, styrene, or N-vinylcarbazole, so that polymerizations of those monomers occur. Cumyl and t-butyl carboxylations have been generated from cumyl and t-butyl esters and ethers as well as from the halides [Faust and Kennedy, 1987; Mishra and Kennedy, 1987]. Highly stable carboxylations such as trityl, Ï₃C⁺ and cycloheptatrienyl (tropylium), C₇H₇⁺ are generally too...
stable to be very efficient in polymerizing the less reactive monomers such as isobutylene and styrene but polymerization of the more reactive monomers (\(p\)-methoxystyrene, vinyl ethers, indene, \(N\)-vinylcarbazole) proceeds rapidly [Ledwith, 1979a,b; Rooney, 1978]. (Tryptyl and tropylium carbocations are sufficiently stable that their salts with stable anions such as hexafluoroantimoniate, Sb\(\text{F}_6\), can be purchased in pure crystalline form from chemical vendors.) Acylium ions (oxacarbocations) have also been used to initiate cationic polymerization [Sawamoto et al., 1977, 1978]. These can be formed in situ or separately prepared as the solid salt, which is subsequently added to the monomer solution:

\[
\begin{align*}
\text{RC} & \quad \text{O} \quad \text{F} \quad \text{SbF}_3 \quad \text{R} \quad \text{C} \quad \text{O} \quad \text{F} \\
\text{H} & \quad \text{SbF}_3 \quad \rightarrow \quad \text{R} & \quad \text{C} \quad \text{(SbF}_6\text{)} & \quad \text{O} \\
\end{align*}
\]

(5-6)

Many polymerizations exhibit a maximum polymerization rate at some ratio of initiator to coinitiator [Biswas and Kabir, 1978, 1978; Colclough and Dainton, 1958; Taninaka and Minoura, 1976]. The polymerization rate increases with increasing [initiator]/[coinitiator], reaches a maximum, and then either decreases or levels off. Figure 5-1 shows this behavior for the polymerization of styrene initiated by tin(IV) chloride–water in carbon tetrachloride. The decrease in rate at higher initiator concentration is usually ascribed to inactivation of the coinitiator by initiator. The inactivation process in a system such as Sn\(\text{Cl}_4\)-H\(\text{2O}\) may involve hydrolysis of Sn—Cl bonds to Sn—OH. There is experimental evidence for such reactions when comparable concentrations of coinitiator and initiator are present. However, the rate maxima as in Fig. 5-1 are observed at quite low [initiator]/[coinitiator] ratios where corresponding experimental evidence is lacking. An alternate mechanism for the behavior in Fig. 5-1 is that initiator, above a particular concentration, competes successfully with monomer for the initiator–coinitiator complex (V) to yield the oxonium salt (VI), which

\[
\begin{align*}
\text{SnCl}_4 & \quad + \quad \text{H}_2\text{O} \quad \rightarrow \quad \text{SnCl}_4\cdot\text{OH}_2 \quad \rightarrow \quad (\text{H}_3\text{O}^+)(\text{SnCl}_4\text{OH}^-) \\
\end{align*}
\]

(5-7)

![Fig. 5-1](image-url)

Fig. 5-1  Effect of water concentration on the Sn\(\text{Cl}_4\)-initiated polymerization rate of styrene in carbon tetrachloride at 25°C. Symbols ○ and ● refer to initiator concentrations of 0.08 and 0.12 M, respectively. After Colclough and Dainton [1958] (by permission of the Faraday Society and Royal Society of Chemistry, London).
is too unreactive in protonating olefins because the basicity of the carbon–carbon double bond is far less than that of water [Ledwith and Sherrington, 1974] (see also Sec. 5-2c-4). The optimum initiator to coinitiator ratio varies considerably depending on the initiator, coinitiator, monomer, solvent, and temperature, since these factors affect the balance between the competing processes of initiation and inactivation.

Initiation by some organotransition metal complexes involves addition of a positive metallic site to monomer [Baird, 2000]. For example, the complex formed from cyclopentadienyltrimethyltitanium and triperfluorophenyl boron initiates polymerization by the sequence

\[
(C_5H_5)(CH_3)_3Ti + (C_6F_5)_3B \rightarrow (C_5H_5)(CH_3)_2Ti^+ (C_6F_5)_3(CH_3)B^- \quad (5-3e)
\]

\[
M \rightarrow (C_5H_5)(CH_3)_2TiM^+ (C_6F_5)_3(CH_3)B^- \quad (5-4e)
\]

5-2a-3 Halogen

Chlorine, bromine, and iodine act as cationogens in the presence of the more active Lewis acids such as trialkylaluminum or dialkylaluminum halide [DiMaina et al., 1977; Magagnini et al., 1977]. The initiating species is the halonium ion \( X^+ \) present in low concentration via the equilibrium reaction between Lewis acid and halogen.

Iodine is unique among the halogens in that it initiates polymerization of the more reactive monomers (styrene, vinyl ether, acenaphthylene, \( N \)-vinylcarbazole) even in the absence of a Lewis acid [Johnson and Young, 1976; Sauvet and Sigwalt, 1989]. Iodine is not the actual initiator in this system. Iodine adds to the double bond to form a diiodide that eliminates hydrogen iodide. The hydrogen iodide generated by this process acts as the cationogen with iodine acting as a Lewis acid to form the initiating system. It was noted earlier (Sec. 5-2a-1) that hydrogen iodide is not an efficient initiator because iodide ion is too nucleophilic. The presence of iodine “activates” (dissociates) the C–I bond sufficiently to allow propagation to proceed. (See Sec. 5-2g for details of the propagation mechanism.) This initiation route is more efficiently utilized by directly adding a mixture of hydrogen iodide and either iodine or a metal halide such as \( \text{ZnX}_2 \) or \( \text{SnX}_2 \) to the reaction system [Higashimura et al., 1988].

5-2a-4 Photoinitiation by Onium Salts

Aryldiazonium (\( \text{ArN}_2^+Z^- \)), diaryliodonium (\( \text{Ar}_2\text{I}^+Z^- \)), and triarylsulfonium (\( \text{Ar}_3\text{S}^+Z^- \)) salts, where \( Z^- \) is a nonnucleophilic and photostable anion such as tetrafluoroborate (\( \text{BF}_4^- \)), hexafluoroantimonate (\( \text{SbF}_6^- \)), and tetrafluorophenylborate \( [(\text{C}_6\text{F}_5)_3\text{B}]^- \), and
hexafluorophosphate (PF\textsubscript{6}), are effective photoinitiators of cationic polymerization [Crivello, 1999; Crivello et al., 1999; Crivello and Sangermano, 2001; Decker et al., 2001]. Aryldiazonium salts have limited practical utility because of their inherent thermal instability. Diarylidonium and triarylsulfonium salts are very stable—so stable that their mixtures with highly reactive monomers do not undergo polymerization on long-term storage. Some of these initiators have found commercial application in the photocrosslinking of epoxy resins through cationic polymerization.

Diarylidonium and triarylsulfonium salts act as photoinitiators of cationic polymerization. Photolytic cleavage of an Ar–I or Ar–S bond yields a radical–cation (Eq. 5-8) that reacts with HY to yield an initiator–coinitiator complex that acts as a proton donor to initiate cationic polymerization. HY may be solvent or some other deliberately added substance such as an alcohol (or adventitious impurity, including water) with a labile hydrogen. Overall, the process is a photolytically induced redox reaction between the cation–radical and HY. Interestingly, the same result has been achieved thermally without photolysis by coupling the appropriate reducing agent (e.g., ascorbic acid or copper(I) benzoate) with a diarylidonium salt [Crivello et al., 1983]. The spectral response (absorption wavelength, absorption coefficient, quantum yield, photosensitivity) and thermal stability of the onium salt photoinitiators can be altered by modifying the structure of the aromatic groups in the cation portion. The choice of anion in the onium salt alters its behavior in polymerization by altering the identity of the initiating species.

Cationic photoinitiators are used in coatings, printing inks, adhesives, sealants, and photoresist applications. Most of the applications involve vinyl ether polymerizations or ring-opening polymerizations of epoxy monomers (Sec. 7-2b).

Quantitative aspects of photopolymerization have been described in Sec. 3-4c. There are some differences between radical and cationic photopolymerizations. The dependence of \( R_p \) on light intensity is half-order for radical polymerization, but first-order for cationic polymerization. Radical photopolymerizations stop immediately on cessation of irradiation. Most cationic photopolymerizations, once initiated, continue in the absence of light because most of the reaction systems chosen are living polymerizations (Sec. 5-2g).

5-2a-5 Electroinitiation

Electrolytic or electroinitiated polymerization involves initiation by cations formed via electrolysis of some component of the reaction system (monomer, solvent, electrolyte, or other deliberately added substance) [Cerrai et al., 1976, 1979; Funt et al., 1976; Oberrauch et al.,
1978; Olaj, 1987]. Thus initiation in the presence of perchlorate ion proceeds by oxidation of perchlorate followed by hydrogen abstraction.

\[
\text{ClO}_4^- \xrightarrow{e^-} \text{ClO}_4^\cdot \quad \text{HY} \xrightarrow{\cdot} \text{HClO}_4^n
\]  

(5-10)

where HY is some hydrogen donor in the system. Perchloric acid is the actual initiating species.

Some electroinitiated polymerizations proceed via monomer radical–cations (VII) formed by electron transfer

\[
\begin{align*}
&\text{CH}_2=\text{CH} \xrightarrow{e^-} \text{CH}_2^+\text{CH} \quad \text{OR} \quad \text{OR} \\
&\text{CH}_2^+\text{CH}_2^+\text{CH} \quad \text{OR} \quad \text{OR}
\end{align*}
\]

(5-11)

VII

VIII

from monomer either to the anode or to a polynuclear aromatic compound. Propagation is proposed to proceed via the dicarbocation VIII formed by dimerization of VII.

### 5-2a-6 Ionizing Radiation

Ionizing radiations (Sec. 3-4d) initiate cationic polymerization [Deffieux et al., 1983; Plesch, 1993; Stannett, 1989]. The first event is the formation of a radical–cation such as VII by the ejection of a \(\pi\)-electron. The radical–cation can react to form other radical, anionic, and cationic species (Sec. 3-4d). Whether one observes radical, cationic, or anionic polymerization depends on the monomer and reaction conditions. Styrene can undergo polymerization by all three mechanisms. For superdry reaction systems at 25°C, the overwhelming mechanism for polymerization is cationic with about 2.5% anionic and negligible radical reaction. Radical polymerization becomes the dominant process with increasing reaction temperature. The presence of water or other protogens markedly decreases the extent of ionic polymerization relative to radical polymerization. Isobutylene shows negligible tendency to undergo any polymerization except cationic, and that occurs only at lower temperatures (usually considerably below 0°C). At higher temperatures, no polymerization occurs since the cationic reaction is not favored.

The actual species responsible for cationic polymerizations initiated by ionizing radiation is not established. The most frequently described mechanism postulates reaction between radical–cation and monomer to form separate cationic and radical species; subsequently, the cationic species propagates rapidly while the radical species propagates very slowly. The proposed mechanism for isobutylene involves transfer of a hydrogen radical from monomer to the radical–cation to form the \(t\)-butyl carbocation and an unreactive allyl-type radical:

\[
\begin{align*}
&(\text{CH}_3)_2\text{C}≡\text{CH}_2 \xrightarrow{\text{radiation}} (\text{CH}_3)_2\text{C}^\cdot\text{CH}_2 \\
&(\text{CH}_3)_3\text{C}^+ + \text{CH}_3=\text{C}≡\text{CH}_2
\end{align*}
\]

(5-12)

The evidence for this mechanism is based on mass spectroscopy of the gas-phase radiolysis of isobutylene, which may not be applicable to the typical liquid-phase polymerization system. Initiation in condensed systems may follow the same course as electroinitiation—coupling of radical–cations to form dicarbocations.
Cationic polymerization initiated by ionizing radiation is markedly different from other cationic polymerizations in that the propagating species is a free ion remote from a counterion. Overall electrical neutrality is maintained by electrons trapped by the monomer.

5-2b Propagation

The initiator ion pair (consisting of the carbocation and its negative counterion) produced in the initiation step (Eq. 5-4) proceeds to propagate by successive additions of monomer molecules

\[
\begin{align*}
&H^+\text{C}_2\text{H}_2\text{C}(\text{CH}_3)_2\text{BF}_3\text{OH}^- + (\text{CH}_3)_2\text{C} = \text{CH}_2 \\
\rightarrow \\
&H^+\text{C}_2\text{H}_2\text{C}(\text{CH}_3)_2\text{BF}_3\text{OH}^- + n\text{CH}_3\text{C}(\text{CH}_3)_2\text{CH}_2\text{C}(\text{CH}_3)_2\text{BF}_3\text{OH}^- \quad (5-13a)
\end{align*}
\]

or

\[
\begin{align*}
&HM^+_n(IZ)^- + M \\ &\rightarrow HM^+_nM^+(IZ)^- \quad (5-13b)
\end{align*}
\]

This addition proceeds by insertion of monomer between the carbocation and its negative counterion.

The propagation reaction can be complicated in some cases by the occurrence of intramolecular rearrangements due to 1,2-hydride ion (H:\text{C}-) or 1,2-methide (CH\text{3}:\text{C}) shifts. Polymerizations proceeding with rearrangement are referred to as isomerization polymerizations. The extent of rearrangement during cationic propagation will depend on the relative stabilities of the propagating and rearranged carbocations and the relative rates of propagation and rearrangement. Both factors favor propagation without rearrangement for monomers such as styrene, indene, acenaphthylene, coumarone, vinyl ethers, and isobutylene. Not only do these monomers propagate via reasonably stable carbocations such as tertiary, benzyl, and oxycarbocations; the carbocations have no routes available for rearrangement to more stable carbocations. Extensive rearrangement during propagation occurs for a variety of 1-alkenes (\(\alpha\)-olefins) [Cesca, 1985]. Propene, 1-butene, and higher 1-alkenes yield oligomers (DP no higher than 10–20) with highly irregular structures due to various combinations of 1,2-hydride and 1,2-methide shifts. For example, propene polymerization proceeds to give an extremely complicated oligomer structure with methyl, ethyl, n- and isopropyl, and other groups. (Hydride transfer to polymer is also involved; see Sec. 5-2c-3.) The propagating secondary carbocations are insufficiently stable to propagate without extensive rearrangement. Simultaneously, only oligomers are formed since none of the rearrangement pathways are favorable for rapid propagation (relative to a variety of chain-transfer and termination reactions).

Isomerization polymerizations yield high-molecular-weight products when reaction proceeds through relatively simple rearrangement routes involving stable carbocations. Thus
polymerization of 3-methyl-1-butene yields high polymer containing both the first-formed (IXa) and rearranged (IXb) repeating units in varying amounts depending on the temperature

\[
\begin{align*}
\text{IXa} & : \quad \begin{array}{c}
\text{CH}_2 = \text{CH} \\
\text{CH(CH}_3)_2
\end{array} \\
\text{IXb} & : \quad \begin{array}{c}
\text{CH}_2 = \text{CH}_2 - \text{C(CH}_3)_2 \\
\text{CH}_2 \text{CH}_2 \text{C(CH}_3)_2
\end{array}
\end{align*}
\]

[Kennedy et al., 1964]. Isomerism occurs by a 1,2-hydride shift in the first-formed carbocation (Xa) prior to the addition of the next monomer unit. The rearranged ion (Xb) is a tertiary carbocation and is more stable than the first-formed carbocation, which is a secondary carbocation. The product contains mostly the rearranged repeating unit, but some normal propagation occurs at higher temperatures as a result of kinetic factors. The product contains about 70 and 100% of the rearranged repeating unit at polymerization temperatures of \(-100\) and \(-130^\circ\text{C}\), respectively.

High resolution \(^1\text{H}\) and \(^{13}\text{C}\) NMR shows that there is great complexity to the rearrangements occurring for certain monomers. Five different repeating units, derived from carbocations XI–XV, are found in the polymer from 4-methyl-1-pentene [Ferraris et al., 1977; Kennedy and Johnston, 1975]. The first-formed carbocation XI undergoes hydride shift to form carbocations XII, XIII, and XIV; XIII rearranges to XV by a methide shift. The repeating unit derived from XIV, the most stable carbocation, is present in the greatest abundance (42–51%). The other carbocations are of comparable stability, and the repeating units derived from them are found in comparable amounts.

\[
\begin{align*}
\text{CH}_2\equiv\text{CH} & \quad \text{CH}_2\text{CH(CH}_3)_2 \\
\text{H: shift} & \quad \begin{array}{c}
\text{H} \\
\text{CH}_2\text{CH}(\text{CH}_3)_2
\end{array} \\
\text{XII} & : \quad \begin{array}{c}
\text{H} \quad \text{CH}_2\text{CH}(\text{CH}_3)_2
\end{array} \\
\text{XIV} & : \quad \begin{array}{c}
\text{H: shift} \\
\text{CH}_3
\end{array} \\
\text{XV} & : \quad \begin{array}{c}
\text{H: shift} \\
\text{CH}_3
\end{array}
\end{align*}
\]

The driving force in some isomerization polymerizations is relief of steric strain. Polymerization of \(\beta\)-pinene proceeds by the first-formed carbocation XVI rearranging to XVII

\[
\begin{align*}
\text{XI V I} & : \quad \begin{array}{c}
\text{CH}_3 \\
\text{CH}_2\text{CH}_2\text{CH}_2
\end{array} \\
\text{X V I I} & : \quad \begin{array}{c}
\text{CH}_3 \\
\text{CH}_2\text{CH}_2\text{CH}_2
\end{array}
\end{align*}
\]
via cleavage of the strained four-membered ring and migration of the resulting gem-dimethyl carbocation center [Kennedy and Marechal, 1982].

Other monomers that undergo isomerization polymerization include 5-methyl-1-hexene, 4,4-dimethyl-1-pentene, 6-methyl-1-heptene, α-pinene, and vinylcyclopropane [Cesca, 1985; Corno et al., 1979].

5-2c Chain Transfer and Termination

Various reactions lead to termination of chain growth in cationic polymerization [Allen and Bevington, 1990; Dunn, 1979; Gandini and Cheradame, 1985; Kennedy and Marechal, 1982; Matyjaszewski and Pugh, 1996]. Many of the reactions that terminate the growth of a propagating chain do not, however, terminate the kinetic chain because a new propagating species is generated in the process.

5-2c-1 β-Proton Transfer

Transfer of a β-proton from the propagating carbocation is the most important chain-breaking reaction. It occurs readily because much of the positive charge of the cationic propagating center resides not on carbon, but on the β-hydrogens because of hyperconjugation. Monomer, counterion or any other basic species in the reaction mixture can abstract a β-proton. Chain transfer to monomer involves transfer of a β-proton to monomer with the formation of terminal unsaturation in the polymer.

\[
H^+\text{CH}_2\text{C(CH}_3\text{)}_2\overset{+}{\overset{\text{CH}_2\text{C}}{\text{C}}(\text{CH}_3\text{)}_2(\text{BF}_3\text{OH})^-} + \text{CH}_2=\text{C}(\text{CH}_3\text{)}_2 \rightarrow \text{CH}_2=\text{C}(\text{CH}_3\text{)}_2
\]

(5-17a)

or

\[
\text{HM}_n\text{M}^+(\text{IZ})^- + M \xrightarrow{k_{\text{tr}, M}} M_{n+1} + \text{HM}^+(\text{IZ})^-
\]

(5-17b)

There are two different types of β-protons, and two different unsaturated end groups are possible for isobutylene as well as some other monomers such as indene and α-methylstyrene. The relative amounts of the two end groups depend on the counterion, identity of the propagating center, and other reaction conditions. Only one type of unsaturated end group (internal) is possible for other monomers such as styrene, ethyl vinyl ether, and coumarone.

It should be noted that the kinetic chain is not terminated by this reaction since a new propagating species is regenerated. Many polymer molecules are usually produced for each initiator–coinitiator species present. Chain transfer to monomer is on much more
favorable terms with propagation in many cationic polymerizations compared to radical polymerization. Since it is kinetically indistinguishable from propagation, the relative rates of transfer and propagation are given by the ratio $k_{tr,M}/k_p$, which is the chain-transfer constant for monomer $C_M$. The value of $C_M$ determines the molecular weight of the polymer if other chain-breaking processes are not significant. The larger the value of $C_M$ the lower will be the molecular weight.

Chain transfer to monomer is the principal reaction that limits polymer molecular weight for most monomers, especially at reaction temperatures higher than about 20°C. Since chain transfer to monomer generally has a higher activation energy than propagation, it is usually suppressed by working at lower reaction temperatures.

Another type of chain transfer to monomer reaction is that involving hydride ion transfer from monomer to the propagating center [Kennedy and Squires, 1967].

\[
\text{HC} \quad \text{H} \quad \text{2C}(\text{CH}_3)_2 \quad \text{CH}_2 \text{C}(\text{CH}_3)_2 (\text{BF}_3 \text{OH})^- + \text{CH}_2=\text{C}(\text{CH}_3)_2 \quad \rightarrow \quad \text{CH}_2=\text{C}(\text{CH}_3)_2 - \text{CH}_2 \text{BF}_3 \text{OHH}_2
\]

This reaction may account in part for the oligomers obtained in the polymerization of propene, 1-butene, and other 1-alkenes where the propagation reaction is not highly favorable (due to the low stability of the propagating carbocation). Unreactive 1-alkenes and 2-alkenes have been used to control polymer molecular weight in cationic polymerization of reactive monomers, presumably by hydride transfer to the unreactive monomer. The importance of hydride ion transfer from monomer to monomer is not established for the more reactive monomers. For example, hydride transfer by monomer is less likely a mode of chain termination compared to proton transfer to monomer for isobutylene polymerization since the tertiary carbocation formed by proton transfer is more stable than the allyl carbocation formed by hydride transfer. Similar considerations apply to the polymerizations of other reactive monomers. Hydride transfer is not a possibility for those monomers without easily transferable hydrogens, such as $N$-vinylcarbazole, styrene, vinyl ethers, and coumarone.

The two types of chain transfer to monomer are kinetically indistinguishable, but one (Eq. 5-17) results in unsaturated end groups, while the other (Eq. 5-18) results in saturated end groups.

Chain transfer to counterion, also called spontaneous termination, involves transfer of a $\beta$-proton to the counterion. The initiator–coinitiator is regenerated by its expulsion from the propagating species and, as in chain transfer to monomer, the polymer molecule has a terminal double bond

\[
\text{BF}_3 \cdot \text{OH}_2 + \text{H}^+ \text{CH}_2 \text{C}(\text{CH}_3)_2 - \frac{1}{n} \text{CH}_2 \text{C}(\text{CH}_3)_2 \text{C}(\text{CH}_3) \equiv \text{CH}_2 \quad \rightarrow \quad \text{H}^+ [\text{IZ}]^+ \quad \text{M}_{n+1} \quad [\text{IZ}]^- \quad \text{H}^+ [\text{IZ}]^+ \quad \text{M}_{n+1} \quad [\text{IZ}]^-
\]

or, in more general terms,

\[
\text{HM}_n \text{M}^+ [\text{IZ}]^- \quad \xrightarrow{k_n} \quad \text{M}_{n+1} \quad + \quad \text{H}^+ [\text{IZ}]^+ \quad \text{M}_{n+1} \quad [\text{IZ}]^-
\]

Chain transfer to counterion differs kinetically from chain transfer to monomer in that the rate of chain transfer to monomer has a first-order dependence on monomer while chain
transfer to counterion is zero-order in monomer. Chain transfer to monomer is usually the dominant termination reaction compared to chain transfer to counterion.

Chain transfer of a β-proton to other basic substances in the reaction mixture is also possible. The various β-proton transfer reactions limit polymer molecular weight, but do not terminate the kinetic chain.

5-2c-2 Combination with Counterion

Termination by combination of the propagating center with the counterion

\[
\text{HM}_n \text{M}^+ (\text{IZ})^- \xrightarrow{k_i} \text{HM}_n \text{MIZ}
\]

occurs, for example, in the trifluoroacetic acid initiated polymerization of styrene [Throssell et al., 1956]

\[
\text{H} + \text{CH}_2\text{CH} + \text{CH}_2\text{CH(OOCOCF}_3^- \rightarrow \text{H} + \text{CH}_2\text{CH} + \text{CH}_2\text{CH} - \text{OCOCF}_3 \quad (5-21)
\]

Alternately, the propagating ion may combine with an anionic fragment from the counterion, for example

\[
\text{H} + \text{CH}_2\text{C(CH}_3\text{)}_2 \rightarrow \text{CH}_2\text{C(CH}_3\text{)}_2\text{BF}_3\text{OH}^- \rightarrow \text{H} + \text{CH}_2\text{C(CH}_3\text{)}_2\text{OH} + \text{BF}_3 \quad (5-22)
\]

or

\[
\text{H} + \text{CH}_2\text{C(CH}_3\text{)}_2 \rightarrow \text{CH}_2\text{C(CH}_3\text{)}_2\text{BCl}_3\text{OH}^- \rightarrow \text{H} + \text{CH}_2\text{C(CH}_3\text{)}_2\text{Cl} + \text{BCl}_2\text{OH} \quad (5-23)
\]

Termination by combination differs from the other modes of termination in that the kinetic chain is usually terminated, since the concentration of the initiator–coinitiator complex decreases.

Equations 5-22 and 5-23 indicate the complexity of cationic polymerization even when seemingly similar initiators such as \(\text{BCl}_3\) and \(\text{BF}_3\) are used. Termination in the \(\text{BCl}_3\)-initiated polymerizations of isobutylene and styrene occurs almost exclusively by combination with chloride [Kennedy and Feinberg, 1978; Kennedy et al., 1977]. For \(\text{BF}_3\)-initiated polymerization, chain transfer to monomer is the major mode of chain breaking with a minor contribution by combination with OH. The differences are explained by the order of bond strengths: \(\text{B}–\text{F} > \text{B}–\text{O} > \text{B}–\text{Cl}\) [Jolly, 1984]. A similar situation is found in the polymerization of styrene by trityl salts. Polymerization occurs readily when the counterion is \(\text{SbF}_6^-\) but poorly with the corresponding hexachloroantimonate counterion [Johnson and Pearce, 1976]. Chloride ion easily transfers from the counterion to terminate the propagating center, while fluoride is inactive toward transfer.

Combination with counterion is also important when aluminum alkyl–alkyl halide-initiating systems are used [DiMaina et al., 1977; Kennedy, 1976; Reibel et al., 1979].
Termination occurs by either \textit{alkylation}

\[
\cdots \text{CH}_2 \text{C}^+(\text{CH}_3)_2\text{R}_3\text{AlCl}^- \quad \rightarrow \quad \cdots \text{CH}_2 \text{C}^-(\text{CH}_3)_2\text{R} + \text{R}_2\text{AlCl}^+ \quad (5-24)
\]

or \textit{hydridation}:

\[
\cdots \text{CH}_2 \text{C}^+(\text{CH}_3)_2\text{[(CH}_3\text{CH}_2)_3\text{AlCl}]^- \quad \rightarrow \quad \cdots \text{CH}_2\text{CH}(\text{CH}_3)_2 + \text{CH}_2=\text{CH}_2 + \text{(CH}_3\text{CH}_2)_2\text{AlCl}^+ \quad (5-25)
\]

Alkylation involves transfer of an alkyl anion to the propagating center. Hydridation involves transfer of a hydride ion from the alkyl anion to the propagating center. Hydridation occurs in preference to alkylation when the trialkylaluminum contains \(\beta\)-hydrogens.

\textbf{5-2c-3 \hspace{1em} Chain Transfer to Polymer}

Several \textit{chain transfer to polymer} reactions are possible in cationic polymerization. Transfer of the cationic propagating center can occur either by electrophilic aromatic substitution or hydride transfer. \textit{Intramolecular electrophilic aromatic substitution} (or \textit{backbiting}) occurs in the polymerization of styrene as well as other aromatic monomers with the formation of terminal indanyl structures and regeneration of the initiator–coinitiator complex [Mayr and Patz, 1994; Rooney, 1976, 1978].

Some branching has been detected in the polymerizations of styrene and anethole (\(\beta\)-methyl-\(p\)-methoxystyrene), indicating \textit{intermolecular aromatic substitution} by a propagating carbocation on the aromatic ring of another polymer chain [Hatada et al., 1980; Kennedy and Marechal, 1982].

\textit{Intermolecular hydride transfer} to polymer probably accounts for the short-chain branching found in the polymerizations of 1-alkenes such as propene. The propagating carbocations are reactive secondary carbocations that can abstract tertiary hydrogens from the polymer

\[
\cdots \text{CH}_2\text{CH}=\text{CH}_2\text{CH}^+\text{φ}(\text{IZ})^- \quad \rightarrow \quad \cdots \text{CH}_2\text{CH}=\text{CH}_2\text{φ} + \text{H}^+\text{(IZ)}^- \quad (5-26)
\]

[Plensch, 1953]. This reaction along with hydride transfer from monomer (Eq. 5-18) and intramolecular transfers (Sec. 5-2b) are responsible for the production of only low-molecular-weight products from ethylene and 1-alkenes.

\textbf{5-2c-4 \hspace{1em} Other Transfer and Termination Reactions}

Various transfer agents (denoted by \(S\) or \(XA\) as in Chap. 3), present as solvent, impurity, or deliberately added to the reaction system, can terminate the growing polymer chain by
Transfer of a negative fragment $A^-$

$$HM_nM^+(IZ)^- + XA \xrightarrow{k_{tr,S}} HM_nMA + X^+(IZ)^-$$ (5-28)

Water, alcohols, acids, anhydrides, and esters have varying chain-transfer properties [Mathieson, 1963]. The presence of any of these transfer agents in sufficient concentrations results in Reaction 5-28 becoming the dominant mode of termination. Termination by these compounds involves transfer of HO, RO, or RCOO anion to the propagating carbocation. Aromatics, ethers, and alkyl halides are relatively weak chain-transfer agents. Transfer to aromatics occurs by alkylation of the aromatic ring.

Although a chain-transfer agent decreases the degree of polymerization in proportion to its concentration (Sec. 5-2d), it is not expected to affect the polymerization rate since the initiator–coinitiator complex should be regenerated on transfer. However, one finds that the more active transfer agents such as water, alcohols, and acids do decrease the polymerization rate; that is, they function as inhibitors or retarders. The decrease in polymerization rate is caused by inactivation of the coinitiator by reaction with the chain-transfer agent, such as hydrolysis of SnCl$_4$. An alternate mechanism is inactivation of the proton or $X^+$ species (generated via Reaction 5-28) by solvation. For example, in the presence of considerable amounts of water, the preferred reaction for protons is probably not addition to alkene but reaction with water to form hydronium ion; thus, water is a stronger base than an alkene. As indicated in Sec. 5-2a-2, the polymerization rate is usually observed to increase with increasing initiator concentration (at constant coinitiator concentration), reach a maximum, and then decrease or level off.

Compounds such as amines, triaryl or trialkylphosphines, and thiophene act as inhibitors or retarders by converting propagating chains to stable cations that are unreactive to propagation [Biswa and Kamannarayana, 1976], for example

$$HM_nM^+(IZ)^- + \cdot NR_3 \xrightarrow{} HM_nMNR_3(IZ)^-$$ (5-29)

Phosphines have been advantageously used to convert propagating carbocations to highly stable phosphonium ions that can be studied with $^{31}$P NMR [Brzezinska et al., 1977].

$p$-Benzoquinone acts as an inhibitor in cationic polymerization by proton transfer from the propagating carbocation and/or initiator–coinitiator complex to form $p$-hydroquinone. For styrene polymerization, copolymerization between $p$-benzoquinone and styrene is also important in the inhibiting action of $p$-benzoquinone [Ragimov et al., 1980].

The most nucleophilic of the reagents discussed, such as water, alcohol (often with KOH), ammonia, and amines, are often used in excess to *quench* a cationic polymerization. This is typically carried out after complete (or at least maximum) conversion has been reached in order to inactivate the coinitiator by the process described above.

**5-2d Kinetics**

**5-2d-1 Different Kinetic Situations**

The overall kinetics vary considerably depending largely on the mode of termination in a particular system. Consider the case of termination exclusively by combination of the propagating center with the counterion (Eq. 5-21). The kinetic scheme of initiation, propagation, and termination consists of Eqs. 5-3, 5-4, 5-16, and 5-21, respectively. The derivation of the
rate expression for this polymerization under steady-state conditions \((R_i = R_t)\) follows in a manner analogous to the used in radical polymerization (Sec. 3-3b). The rates of initiation, propagation, and termination are given by

\[
R_i = k_i[I][Z]Y][M] \tag{5-30}
\]

\[
R_p = k_p[YM^+(IZ)^-][M] \tag{5-31}
\]

\[
R_t = k_t[YM^+(IZ^-)] \tag{5-32}
\]

where \([YM^+(IZ^-)]\) is the total concentration of all-sized propagating centers:

\[
[YM^+(IZ^-)] = \frac{Kk_i[I][Z]Y][M]}{k_t} \tag{5-33}
\]

Combining Eqs. 5-31 and 5-33 yields the rate of polymerization as

\[
R_p = \frac{R_i k_p[M]}{k_t} = \frac{Kk_i k_p[I][Z]Y][M]^2}{k_t} \tag{5-34}
\]

The number-average degree of polymerization is obtained as the propagation rate divided by the termination rate:

\[
\bar{X}_n = \frac{R_p}{R_t} = \frac{k_p[M]}{k_t} \tag{5-35}
\]

When chain breaking involves chain transfer to monomer (Eqs. 5-18 and 5-19), spontaneous termination (Eq. 5-20), and chain transfer to chain-transfer agent \(S\) in addition to combination with the counterion, the concentration of the propagating species remains unchanged (assuming relatively small amounts of \(S\) such that the coinitiator is not inactivated), and the polymerization rate is again given by Eq. 5-34. However, the degree of polymerization is decreased by these other chain-breaking reactions and is given by the polymerization rate divided by the sum of all chain-breaking reactions:

\[
\bar{X}_n = \frac{R_p}{R_t + R_{ts} + R_{tr,M} + R_{tr,S}} \tag{5-36}
\]

The rates of spontaneous termination and the two transfer reactions are given by

\[
R_{ts} = k_{ts}[YM^+(IZ^-)] \tag{5-37}
\]

\[
R_{tr,M} = k_{tr,M}[YM^+(IZ^-)][M] \tag{5-38}
\]

\[
R_{tr,S} = k_{tr,S}[YM^+(IZ^-)][S] \tag{5-39}
\]

Combination of Eq. 5-36 with Eqs. 5-31, 5-32, and 5-37 to 5-39 yields

\[
\bar{X}_n = \frac{k_p[M]}{k_t + k_{ts} + k_{tr,M}[M] + k_{tr,S}[S]} \tag{5-40}
\]

or

\[
\frac{1}{\bar{X}_n} = \frac{k_t}{k_p[M]} + \frac{k_{ts}}{k_p[M]} + c_M + c_S \frac{[S]}{[M]} \tag{5-41}
\]

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where \( C_M \) and \( C_S \) are the chain-transfer constants for monomer and chain-transfer agent \( S \) defined by \( k_{tr,M}/k_p \) and \( k_{tr,S}/k_p \), respectively. Equation 5-39 is the cationic polymerization equivalent of the previously described Mayo equation (Eq. 3-108) for radical polymerization.

For the case where chain transfer to \( S \) (Eq. 5-29) terminates the kinetic chain, the polymerization rate is decreased and is given by

\[
R_p = \frac{Kk_ip[1][ZY][M]^2}{k_i + k_{tr,S}[S]} \tag{5-42}
\]

The various rate expressions were derived on the assumption that the rate-determining step in the initiation process is Reaction 5-4. If this is not the situation, the forward reaction in Eq. 5-3 is rate-determining. The initiation rate becomes independent of monomer concentration and is expressed by

\[
R_i = k_i[1][ZY] \tag{5-43}
\]

The polymerization rate expressions (Eqs. 5-34 and 5-42) will then be modified by replacing \( Kk_i \) by \( k_i \), and there will be a one-order-lower dependence of \( R_p \) on \([M] \). The degree of polymerization is unchanged and still described by Eq. 5-41.

The expressions (Eqs. 5-34 and 5-42) for \( R_p \) in cationic polymerization point out one very significant difference between cationic and radical polymerizations. Radical polymerizations show a \( \frac{1}{2} \)-order dependence of \( R_p \) on \( R_i \), while cationic polymerizations show a first-order dependence of \( R_p \) on \( R_i \). The difference is a consequence of their different modes of termination. Termination is second-order in the propagating species in radical polymerization but only first-order in cationic polymerization. The one exception to this generalization is certain cationic polymerizations initiated by ionizing radiation (Secs. 5-2a-6, 3-4d). Initiation consists of the formation of radical–cations from monomer followed by dimerization to dicarbocations (Eq. 5-11). An alternate proposal is reaction of the radical–cation with monomer to form a monocarbocation species (Eq. 5-12). In either case, the carbocation centers propagate by successive additions of monomer with radical propagation not favored at low temperatures in superpure and dry systems.

In the usual situation the radiolytic reaction determines the rate of initiation and \( R_i \) is given by

\[
R_i = IG[M] \tag{5-44}
\]

where \( I \) is the radiation intensity and \( G \) is the number of radical–cations formed per 100 eV of energy absorbed. In sufficiently pure systems (concentrations of water and other terminating agents \(<10^{-7} - 10^{-10} \ M \)), termination of the propagating carbocation centers occurs by combination with a negative fragment \( Y^- \)

\[
\sim M^+ + Y^- \rightarrow \sim M \sim Y \tag{5-45}
\]

\( Y^- \) is either a solvated electron (displaced electron formed during the radiolytic reaction) or the product of the electron having reacted with some compound in the reaction system [Allen et al., 1974; Hayashi et al., 1967; Kubota et al., 1978; Williams et al., 1967]. If \( Y^- \) is an electron, the propagating carbocation centers are converted to radical centers that subsequently undergo reaction with some species in the reaction system to form molecular species. The termination rate is given by

\[
R_t = k_r[M^+][Y^-] = k_r[M^+]^2 \tag{5-46}
\]
where \([M^+] = [Y^-]\) due to the stoichiometry in the radiolytic reaction. Setting \(R_i = R_t\) and combining the result with Eq. 5-31 yields the polymerization rate as

\[
R_p = k_p[M^{1/2} (R_i/k_r) = k_p [M]^{3/2} (G/t)_{1/2} \]

(5-47)

which is quite different from other cationic polymerizations in that the polymerization rate is \(1/2\)-order in \(R_i\). The \(1/2\)-order dependence is then the same as observed in radical polymerization.

For cationic polymerization initiated by radiation in reaction systems where the major termination occurs by reaction with some species other than \(Y^-\), the termination process is first-order in propagating centers (not second-order as in Eq. 5-47) and the polymerization rate will show first-order dependence on \(R_i\).

### 5-2d-2 Validity of Steady-State Assumption

The assumption of a steady state for \([YM^+(IZ)^-]\) is not valid in many, if not most, cationic polymerizations, which proceed so rapidly that steady state is not achieved [Kennedy and Feinberg, 1978; Kennedy and Marechal, 1982]. Some of these reactions (e.g., isobutylene polymerization by \(\text{AlCl}_3\) at \(-100^\circ\text{C}\)) are essentially complete in a matter of seconds or minutes. Even in slower polymerizations, the steady state may not be achieved if \(R_i > R_t\) [Villesange et al., 1977]. The concentration of propagating centers slowly increases throughout the polymerization, reaching a maximum late in the reaction, and then decreases. When initiation is fast, steady state may still not be achieved if the termination rate is lower or higher. The expressions in Sec. 5-2d-1 for \(R_p\) can be employed only if there is assurance that steady-state conditions exist, at least during some portion of the overall reaction. The existence of a steady state can be ascertained by measuring \([YM^+(IZ)^-]\) as a function of time. Since this is relatively difficult in most systems, it is more convenient to observe the polymerization rate as a function of time. Steady state is implied if \(R_p\) is constant with conversion except for changes due to decreased monomer and initiator concentrations. A more rapid decline in \(R_p\) with time than indicated by the decreases in \([M]\) and \([ZY]\) signifies a non-steady state. The absence of a steady state would also be indicated by an increase in \(R_p\) with time. The reader is cautioned that many of the experimental expressions reported in the literature to describe the kinetics of specific cationic polymerizations are invalid, since they are based on data where steady-state conditions do not apply [e.g., Biswas and Kabir, 1978, 1979]. Contrary to these considerations for \(R_p\), the derivations of the expressions for \(X_n\) do not assume steady-state conditions.

Another consideration in the application of the various kinetic expressions is the uncertainty in some reaction systems as to whether the initiator–coinitiator complex is soluble. Failure of the usual kinetic expressions to describe a cationic polymerization may indicate that the reaction system is actually heterogeneous. The method of handling the kinetics of heterogeneous polymerizations is described in Sec. 8-4c.

### 5-2d-3 Molecular Weight Distribution

The theoretical molecular weight distributions for cationic chain polymerizations are the same as those described in Sec. 3-11 for radical chain polymerizations terminating by reactions in which each propagating chain is converted to one dead polymer molecule, that is, not including the formation of a dead polymer molecule by bimolecular coupling of two propagating chains. Equations 2-86 through 2-89, 2-27, 2-96, and 2-97 with \(p\) defined by Eq. 3-185
are applicable to cationic chain polymerizations carried out to low conversions. The polydispersity index \( \text{PDI} = \frac{X_w}{X_n} \) has a limit of 2. Many cationic polymerizations proceed with rapid initiation (in some cases, essentially instantaneous initiation), which narrows the molecular weight distribution. In the extreme case where termination and transfer reactions are very slow or nonexistent, this would yield a very narrow molecular weight distribution with PDI close to one (Secs. 5-2g-2, 5-3b-1). The polydispersity index is greater than one when chain-breaking reactions are operative with values generally between 1 and 2 but greater than 2 depending on the chain-breaking reactions and their rates relative to propagation [Cai et al., 1988; Yan and Yuan, 1986, 1987; Yuan and Yan, 1988].

For polymerizations carried out to high conversions where the concentrations of propagating centers, monomer, and transfer agent as well as rate constants change, the polydispersity index increases considerably. Relatively broad molecular-weight distributions are generally encountered in cationic polymerizations.

5-2e Absolute Rate Constants
5-2e-1 Experimental Methods

The determination of the various rate constants \( (k_i, k_p, k_{1s}, k_{tr}) \) for cationic chain polymerization is much more difficult than in radical polymerization (or in anionic polymerization). \( R_p \) data from experiments under steady-state conditions are convenient for calculating rate constants, since the concentration of propagating species is not required. \( R_p \) data from non-steady-state experiments can be used, but only when the concentration of the propagating species is known. Unfortunately, most cationic polymerizations proceed neither under steady-state conditions nor with a clear knowledge of the concentration of the propagating species. Because the expressions for \( \bar{X}_n \) do not depend on either steady-state reaction conditions or a knowledge of the concentration of propagating species, it is more convenient to calculate the ratios of various rate constant from \( \bar{X}_n \) data than from \( R_p \) data. The use of \( \bar{X}_n \) data, like the use of \( R_p \) data, does require that one employ data obtained at low conversions where rate constants and reactant concentrations have not changed appreciably. Further, the techniques used for measurement of \( \bar{X}_n \), size exclusion chromatography (SEC), membrane and vapor pressure osmometry, require careful utilization to avoid their inherent limitations.

The degree of polymerization under various reaction conditions is used to obtain the \( k_i/k_p, k_{1s}/k_p, k_{tr,M}/k_{tr} (= C_M) \), and \( k_{tr,S}/k_p (= C_S) \) ratios from Eq. 5-39. Experiments with varying \([M]\) in the absence of chain-transfer agents yield a linear plot of \( 1/\bar{X}_n \) versus \( 1/\text{[M]} \) with intercept equal to \( C_M \). The slope of the plot is given by \( (k_i/k_p + k_{1s}/k_p) \). The two ratios can be separated from each other by chemical analysis of the polymer end groups. Spontaneous termination and chain transfer to monomer both yield polymers with unsaturated end groups, while combination with counterion yields polymer end groups derived from the counterion. The end-group analysis combined with the calculated values of \( C_M \) and \( (k_i/k_p + k_{1s}/k_p) \) allow the separation of the latter two ratios. The value of \( C_S \) is obtained by carrying out experiments with varying amounts of chain-transfer agent. A plot of the data according to Eq. 3-119 as \( 1/\bar{X}_n \) versus \([S]/[M]\) is linear with a slope of \( C_S \). \( (1/\bar{X}_n)_0 \) represents the value of \( 1/\bar{X}_n \) in the absence of chain-transfer agent and is given by the sum of the first three terms on the right side of Eq. 5-39.

\[
1/\bar{X}_n = (1/\bar{X}_n)_0 + C_S \left( \frac{S}{M} \right)
\] (3-119)
The determination of the individual rate constants requires the determination of $k_p$, a difficult task and one that has not often been performed well [Dunn, 1979; Kennedy and Marechal, 1982; Plesch, 1971, 1984, 1988]. The value of $k_p$ is obtained directly from Eq. 5-31 from a determination of the polymerization rate. However, this requires critical evaluation of the concentration of propagating species. The literature contains too many instances where the propagating species concentration is taken as equal to the concentration of initiator without experimental verification. Such an assumption holds only if $R_p < R_i$ and all the initiator is active, that is, the initiator is not associated or consumed by side reactions.

There are two general methods for the experimental evaluation of the propagating species concentration, neither method being experimentally simply nor unambiguous [Matyjaszewski and Pugh, 1996; Matyjaszewski and Sawamoto, 1996]. One involves short-stopping a polymerizing system by adding a highly efficient terminating agent. All propagating centers are quickly terminated with incorporation into the polymer of an end group derived from the terminating agent. The end groups in the polymer are analyzed after separation of the polymer from the other components of the reaction system. This method is limited by the general difficulty of end-group analysis since the concentration of end groups can be quite low and by the need to assume that the terminating agent terminates all propagating centers. 2-Bromothiophene has been used to short-stop styrene polymerization with the bromine content of the polymer being analyzed by neutron activation [Higashimura et al., 1971]. Termination of isobutylene polymerization by 2,6-di-t-butylphenol involves aromatic alkylation in the para position of the phenol by the propagating carbocations. Analysis of the 2,6-di-t-butylphenol end groups is accomplished by UV spectroscopy [Russell and Vail, 1976].

The second method for determining the propagating species concentration involves direct UV–visible spectroscopic analysis of the propagating species during polymerization. The high extinction coefficients of some aromatic carbocation propagating species coupled with the availability of highly accurate spectrophotometers has resulted in extensive use of this method. Measurement of the UV absorbance of the polymerizing system as a function of time allows one to determine $k_i$, $R_i$, the concentration of propagating species, and $k_p$. The UV method has also been used to study very fast polymerizations. In stopped-flow, rapid-scan spectroscopy, separate monomer and initiator solutions are rapidly forced through a mixing chamber (where instantaneous mixing occurs) and then into a capillary tube located in a spectrophotometer, flow is stopped and the progress of reaction followed by measuring the change in absorbance with time [Chance, 1974; Givehchi et al., 2000; Sawamoto and Higashimura, 1979; Szwarc, 1968].

More recent advances in experimental techniques offer potential for improvements in our knowledge of the concentrations of propagating species and the values of propagation rate constants. Conductivity and spectroscopic methods have improved because of modern instrumentation, allowing a more reliable measurement of the propagating center concentration. A new method referred to as the diffusion clock method offers an alternate approach to obtain propagation rate constants. This involves polymerization in the presence of an highly active terminating agent, such as allyltrimethylsilane, specifically known to have a rate constant for reaction with carbocations at the diffusion-controlled reaction limit ($k \approx 3 \times 10^9$ L mol$^{-1}$ s$^{-1}$). The ratio of the rate constant for propagation to that for termination is obtained from measurements of the amounts of monomer and terminating agent consumed. This ratio multiplied by the diffusion-controlled reaction rate constant $k$ yields the propagation rate constant. The carbocation propagation rate constant for isobutylene is reported as $6 \times 10^8$ L mol$^{-1}$ s$^{-1}$ and $3 \times 10^8$ L mol$^{-1}$ s$^{-1}$ by two different laboratories using the diffusion clock method, values that are in good agreement with the values obtained by other methods (Table 5-3) [Roth and Mayr, 1996; Schlaad et al., 2000].
Most reported values of $k_p$ and other rate constants and kinetic parameters are questionable for several reasons. First, as discussed above, there is ambiguity about the concentration of propagating species. Second, the calculations of various rate constants and kinetic parameters are often based on inadequately substantiated reaction kinetics and mechanisms [Kennedy and Marechal, 1982; Plesch, 1971, 1990]. Even if the propagating species concentration is accurately known, the use of Eq. 5-31 without verification can lead to incorrect results. This occurs when the kinetics of cationic chain polymerization deviate from Eq. 5-31 and the scheme described in Sec. 5-2d-1 under certain reaction conditions (Sec. 5-2f). Third, there is the large question of how to interpret any obtained rate constants in view of the known multiplicity of propagating carboxylic propagating species. The kinetic expressions in Sec. 5-2d are written in terms of only one type of propagating species—usually shown as the ion pair. This is incorrect, since both ion pairs and free ions are simultaneously present in most polymerization systems, usually in equilibrium with each other (Sec. 5-1). Thus the correct expression for the rate of any step (initiation, propagation, termination, transfer) in the polymerization should include separate terms for the respective contributions of the two types of propagating species. As an example, the propagation rate should be written as

$$R_p = k_p^+ [YM^+] [M] + k_p^- [YM^+ (IZ)^-] [M] \tag{5-48}$$

where $[YM^+]$ and $[YM^+ (IZ)^-]$ are the concentrations of free ions and ion pairs, respectively, and $k_p^+$ and $k_p^-$ are the corresponding propagation rate constants. Most reported $k_p$ values are only apparent or pseudo or global rate constants, $k_p^{app}$, obtained from the polymerization rate using the expression

$$R_p = k_p^{app} [M^*] [M] \tag{5-49}$$

where $[M^*]$ is the total concentration of both types of propagating species. The apparent rate constant is thus not really a rate constant but a combination of rate constants and concentrations:

$$k_p^{app} = \frac{k_p^+ [YM^+] + k_p^- [YM^+ (IZ)^-]}{[YM^+] + [YM^+ (IZ)^-]} \tag{5-50}$$

There are two approaches to the separation of $k_p^{app}$ into the individual $k_p^+$ and $k_p^-$ values. One approach involves the experimental determination of the individual concentrations of free ions and ion pairs by a combination of conductivity with short-stop experiments or UV-visible spectroscopy. Conductivity directly yields the concentration of free ions; that is, only free ions conduct. Short-stop experiments yield the total of the ion-pair and free-ion concentrations. UV-visible spectroscopy for those monomers (mostly aromatic) where it is applicable is also used to obtain the total of the free-ion and ion-pair concentrations. It is usually assumed that ion pairs show the same UV-visible absorption as free ions since the ion pairs in cationic systems are loose ion pairs (due to the large size of the negative counter-ions; see Sec. 5-1). This approach is limited by the assumptions and/or experimental difficulties inherent in the various measurements. Conductivity measurements on systems containing low concentrations of ions are difficult to perform, and impurities can easily lead to erroneous results. The short-stop experiments do not distinguish between ion pairs and free ions, and the assumption of the equivalence of free ions and ion pairs in the spectroscopic method is not firmly established. The second approach involves determination of the
polymerization rate at various concentrations of coinitiator and initiator and in both presence and absence of an added common ion salt. The latter containing the counterion of the propagating carbocation, accentuates propagation by ion pairs by depressing their ionization to free ions. This approach, used extensively in anionic polymerization, is detailed in Sec. 5-3. It is equally applicable to cationic polymerization but has not been used extensively. In fact, neither approach has been used extensively in cationic polymerization.

One of the most often encountered errors in reported \( k_{p}^{\text{app}} \) values is their assignment as \( k_{p}^{\pm} \). This can be erroneous since relatively small concentrations of free ions can have a significant effect on \( k_{p}^{\text{app}} \). For the equilibrium between ion pairs and free ions

\[
\text{YM}^{+}(IZ)^{-} \rightleftharpoons \frac{K}{[\text{YM}^{+}(IZ)^{-}]} \text{YM}^{+} + IZ^{-}
\]  

(5-51)

it can be shown [Plesch, 1973, 1977, 1984] that the ratio of concentrations of free ions and ion pairs is

\[
\frac{[\text{YM}^{+}]}{[\text{YM}^{+}(IZ)^{-}]} = \frac{(1 + 4C/K)^{1/2} - 1}{2C/K + 1 - (1 + 4C/K)^{1/2}}
\]  

(5-52)

where \( C = [\text{YM}^{+}] + [\text{YM}^{+}(IZ)^{-}] \). The relative concentrations of free ions and ion pairs depend on the ratio \( C/K \) according to Eq. 5-52. Free ions constitute approximately 99, 90, 62, 27, 9, 2, 1, and 0.3% of the propagating species at \( C/K \) values of 0.01, 0.1, 1, 10, 10^2, 10^3, 10^4, and 10^5, respectively. Cationic polymerizations are carried out over a wide range of \( C/K \) values, typically anywhere from \( 10^{3} \) to \( 10^{-2} \), depending on the specifics of the reaction system. Consider styrene polymerization by triflic (trifluoromethanesulfonic) acid in 1,2-dichloroethane at 20°C where \( K \) is \( 2.8 \times 10^{-7} \) mol L^{-1} [Kunitake and Takarabe, 1979]. Experiments performed at acid concentrations of \( 2.8 \times 10^{-5} \) M(\( C/K = 10^{2} \)) would involve 91% propagation by ion pairs and 9% propagation by free ions. The relative contribution of free ions to the overall propagation increases for lower acid concentrations. There is considerable error if the \( k_{p}^{\text{app}} \) value is simply taken to be \( k_{p}^{\pm} \) (as is often done since \( K \) is typically unknown and one cannot make the appropriate corrections). The ratio \( k_{p}^{\pm}/k_{p} \) is probably in the range 5–20 for most systems. The calculated \( k_{p}^{\pm} \) value is high by a factor of 1.5 for \( k_{p}^{+}/k_{p}^{\pm} = 5 \). One can safely equate \( k_{p}^{\text{app}} \) with \( k_{p}^{\pm} \) only for systems where \( C/K = 10^{3} \) – \( 10^{4} \) or larger. This can be done by using higher concentrations of triflic acid as long as there are no solubility problems or the reaction rates are not excessively high.

For most of the systems reported in the literature, \( C/K \) is not known—very often, neither \( K \) nor \( C \) is known. For two-component initiator–coinitiator systems, \( C \) is usually taken to be the initiator concentration [YZ] when the coinitiator is in excess or the coinitiator concentration [I] when the initiator is in excess. \( C \) may be lower than [YZ] or [I] due to association; that is, only a fraction of [YZ] or [I] may be active in polymerization. This may also be the case for one-component initiators such as triflic acid. It would be prudent to determine the actual value of \( C \) in any polymerization system—usually a difficult task and seldom achieved. Experimental difficulties have also limited our knowledge of \( K \) values, which are obtained most directly from conductivity measurements or, indirectly, from kinetic data. A comparison of polymerization in the absence and presence of a common ion salt (e.g., tetra-n-butylammonium triflate for the triflic acid initiated polymerization) is useful for ascertaining whether significant amounts of free ions are present in a reaction system.

Polymerizations initiated by ionizing radiation or stable carbocation salts such as trityl or tropylidium hexachloroantimonate are useful for evaluating the free-ion propagation rate constant. Ionizing radiation yields free ions (in the absence of ion pairs) whose concentrations
can be obtained by conductivity measurements [Deffieux et al., 1980; Hayashi et al., 1971; Hsieh et al., 1980; Stannett et al., 1976]. Many carbocation salts are sufficiently stable to be isolated, purified, and characterized as crystalline products. Thus their concentration in a polymerization system is known, unlike the situation with other initiation systems such as boron trifluoride–water. It is often assumed that polymerizations initiated by these salts proceed with propagation carried entirely by free ions and the $k_p$ is taken to be $k_p + k_{p^+}$. This is a valid assumption only under certain conditions. $K$ is probably $10^{-4} - 10^{-5}$ for such system [Gandini and Cheradame, 1985; Subira et al., 1988]. If $C/K$ is no larger than 0.1 (e.g., $C$ no higher than $10^{-5}$ for $K = 10^{-4}$), the system consists of 90% free ions and 10% ion pairs. The presence of 10% of the less reactive (ion pair) propagating species results in no more than a 10% error in the value of $k_p$ obtained by equating $k_{pp}$ with $k_{p^+}$.

Throughout the remainder of the chapter it should be understood that any rate constants that are presented are apparent rate constants unless otherwise indicated to be those for the free ion or ion pair. In general, the available data are used to point out certain trends (e.g., the effect of solvent on reactivity) without necessarily accepting the exact value of any reported rate constant as that for the ion pair or free ion. Comparison of data from different investigators should be done with caution.

### 5-2e-3 Comparison of Rate Constants

Table 5-1 shows the various kinetic parameters, including $k_p$ and $k_{p^+}$, in the polymerization of styrene initiated by triflic acid in 1,2-dichloroethane at 20°C. Data for the polymerization of isobutyl vinyl ether initiated by trityl hexachloroantimonate in methylene chloride at 0°C are shown in Table 5-2. Table 5-3 shows $k_p$ values for several polymerizations initiated

#### TABLE 5-1 Kinetic Parameters in CF$_3$SO$_3$H
Polymerization of Styrene at 20°C in ClCH$_2$CH$_2$Cl$^a$

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>[Styrene]</td>
<td>0.27–0.40 M</td>
</tr>
<tr>
<td>[CF$_3$SO$_3$H]</td>
<td>3.8–7.1 × 10$^{-3}$ M</td>
</tr>
<tr>
<td>$k_i$</td>
<td>10–23 L mol$^{-1}$ s$^{-1}$</td>
</tr>
<tr>
<td>$K_d$</td>
<td>$4.2 \times 10^{-7}$ mol L$^{-1}$</td>
</tr>
<tr>
<td>$k_p^+$</td>
<td>$1.2 \times 10^6$ L mol$^{-1}$ s$^{-1}$</td>
</tr>
<tr>
<td>$k_p^-$</td>
<td>$1.0 \times 10^5$ L mol$^{-1}$ s$^{-1}$</td>
</tr>
<tr>
<td>$k_{ls}$</td>
<td>170–280 s$^{-1}$</td>
</tr>
<tr>
<td>$k_t$</td>
<td>&lt;0.01$s^{-1}$</td>
</tr>
<tr>
<td>$k_{tr,M}$</td>
<td>$1–4 \times 10^3$ L mol$^{-1}$ s$^{-1}$</td>
</tr>
</tbody>
</table>

$^a$Data from Kunitake and Takarabe [1979].

#### TABLE 5-2 Kinetic Parameters in φ$_3$C$^+$SbCl$_6$
Polymerization of Isobutyl Vinyl Ether in CH$_2$Cl$_2$ at 0°C$^a$

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$[φ_3C^+SbCl_6^-]$</td>
<td>$6.0 \times 10^{-5}$ M</td>
</tr>
<tr>
<td>$k_i$</td>
<td>5.4 L mol$^{-1}$ s$^{-1}$</td>
</tr>
<tr>
<td>$k_p^+$</td>
<td>$7.0 \times 10^3$ L mol$^{-1}$ s$^{-1}$</td>
</tr>
<tr>
<td>$k_{tr,M}$</td>
<td>$1.9 \times 10^2$ L mol$^{-1}$ s$^{-1}$</td>
</tr>
<tr>
<td>$k_{tr} + k_t$</td>
<td>0.2 s$^{-1}$</td>
</tr>
</tbody>
</table>

$^a$Data from Subira et al. [1976].
by ionizing radiation or trityl salts. Values of $k_p^+ / C_6 p$ for two of the reaction systems are also included. A comparison of the $k_p^+$ and $k_p^\pm$ values for the styrene, $p$-methoxystyrene, and $N$-vinylcarbazole polymerizations shows the free-ion propagation rate to be an order of magnitude higher than the ion-pair propagation rate constant. Although there are relatively few other systems in which reasonably accurate measures of both $k_p^+$ and $k_p^\pm$ are available, it is generally considered that the reactivity of free ions is no more than a factor of 5–20 greater than the reactivity of ion pairs in cationic polymerization [Gandini and Cheradame, 1985; Matyjaszewski, 1989; Mayr, 1990; Mayr et al., 1988; Sauvet and Sigwalt, 1989]. The counterion is typically quite large for cationic polymerization (e.g., SbCl$_6^-$, CF$_3$SO$_3^-$); the ion pair is a very loose ion pair with little difference in availability of the positive charge center for reaction compared to the free ion.

A comparison of Table 5-1 through 5-3 with corresponding data for radical chain polymerization (see Table 3-10 and 3-11) allows us to understand why cationic polymerizations are generally faster than radical polymerizations. The propagation rate constants in cationic polymerization are similar to or greater than those for radical polymerization. However, the termination rate constants are considerably lower in cationic polymerization. The polymerization rate is determined by the ratio of rate constants—$k_p / k_t$ in cationic polymerization and $k_p / k_t^{1/2}$ in radical polymerization. The former ratio is larger than the latter by up to 4 orders of magnitude depending on the monomers being compared. Cationic polymerization is further favored, since the concentration of propagating species is usually much higher than in a radical polymerization. The concentration of propagating species is typically $10^{-7} - 10^{-9} M$, much lower than that in cationic polymerization.

Table 5-3 shows the order of reactivity of monomers in propagation. It is not a simple matter to explain the order of propagation rate constants for a set of monomers because there are variables—the reactivity of the monomer and the reactivity of the carbocation. For example, carbocation stability is apparently the more important feature for isopropyl vinyl ether and results in decreasing its propagation reactivity compared to isobutylene.

### Table 5-3 Propagation Rate Constants

<table>
<thead>
<tr>
<th>Monomer</th>
<th>Initiator</th>
<th>Solvent</th>
<th>Temperature ($^\circ$C)</th>
<th>$k_p^+ \times 10^{-4}$ (L mol$^{-1}$ s$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Isobutylene$^a$</td>
<td>Radiation</td>
<td>Bulk</td>
<td>0</td>
<td>15000</td>
</tr>
<tr>
<td>Styrene$^b$</td>
<td>Radiation</td>
<td>Bulk</td>
<td>15</td>
<td>350</td>
</tr>
<tr>
<td>$p$-Methoxystyrene$^c$</td>
<td>Radiation</td>
<td>Bulk</td>
<td>0</td>
<td>300</td>
</tr>
<tr>
<td>$N$-Vinylcarbazole$^d$</td>
<td>$\phi_3 C^+ SbCl_6$</td>
<td>CH$_2$Cl$_2$</td>
<td>10</td>
<td>36$^e$</td>
</tr>
<tr>
<td>Isopropyl vinyl ether$^e$</td>
<td>$\phi_3 C^+ SbF_6^-$</td>
<td>CH$_2$Cl$_2$</td>
<td>20</td>
<td>60$^h$</td>
</tr>
<tr>
<td>Isoprene$^f$</td>
<td>Radiation</td>
<td>CH$_2$Cl$_2$</td>
<td>0</td>
<td>8.6</td>
</tr>
</tbody>
</table>

$^a$Data from Williams and Taylor [1969].
$^b$Data from Williams et al. [1967].
$^c$Data from Sauvet et al. [1986].
$^d$Data from Rooney [1976, 1978].
$^e$Data from Subira et al. [1988], Deffieux et al. [1983].
$^f$Data from Williams et al. [1976].
$^g k_p^+ = 4.1 \times 10^4$ L mol$^{-1}$ s$^{-1}$.
$^h k_p^+ = 5.0 \times 10^4$ L mol$^{-1}$ s$^{-1}$.
Monomer chain-transfer constants are shown in Tables 5-4 and 5-5 for various polymerizations of styrene and isobutylene. It is apparent that the $C_M$ values for styrene are, in general, larger than those for isobutylene by one to two orders of magnitude. This corresponds to the greater reactivity of isobutylene toward propagation. Although extensive data are not available, one generally observes that the monomers with the larger $k_p$ values usually possess lower $C_M$ values.

The values of $C_S$ for some compounds in the polymerization of styrene are shown in Table 5-6. The larger transfer constants are associated with transfer agents that possess a

### TABLE 5-4 Monomer Transfer Constant for Styrene

<table>
<thead>
<tr>
<th>Initiator</th>
<th>Solvent</th>
<th>Temperature ($^\circ$C)</th>
<th>$C_M \times 10^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>SnCl$_4$</td>
<td>$\phi$H</td>
<td>30</td>
<td>1.9$^a$</td>
</tr>
<tr>
<td>SnCl$_4$</td>
<td>CCl$_4$-$\phi$NO$_2$ (3 : 7)</td>
<td>0</td>
<td>0.51$^b$</td>
</tr>
<tr>
<td>SnCl$_4$</td>
<td>C$_2$H$_5$Br</td>
<td>−63</td>
<td>0.02$^c$</td>
</tr>
<tr>
<td>TiCl$_4$</td>
<td>$\phi$H</td>
<td>30</td>
<td>2.0$^d$</td>
</tr>
<tr>
<td>TiCl$_4$</td>
<td>(CH$_2$Cl)$_2$-$\phi$H (3 : 7)</td>
<td>30</td>
<td>1.5$^d$</td>
</tr>
<tr>
<td>TiCl$_4$</td>
<td>CH$_2$Cl$_2$</td>
<td>−60</td>
<td>0.04$^e$</td>
</tr>
<tr>
<td>TiCl$_4$</td>
<td>CH$_3$Cl</td>
<td>−90</td>
<td>&lt;0.005$^e$</td>
</tr>
<tr>
<td>FeCl$_3$</td>
<td>$\phi$H</td>
<td>30</td>
<td>1.2$^c$</td>
</tr>
<tr>
<td>BF$_3$</td>
<td>$\phi$H</td>
<td>30</td>
<td>0.82$^e$</td>
</tr>
<tr>
<td>BF$_3$</td>
<td>CH$_2$Cl$_2$</td>
<td>−50</td>
<td>0.057$^f$</td>
</tr>
<tr>
<td>CF$_3$SO$_3$H</td>
<td>CH$_2$Cl$_2$</td>
<td>20</td>
<td>1.5$^g$</td>
</tr>
</tbody>
</table>

$^a$Data from Okamura and Higashimura [1956a,b, 1960].
$^b$Data from Endres and Overberger [1955].
$^c$Data from Biddulph and Plesch [1960].
$^d$Data from Sakurda et al. [1958].
$^e$Data from Mathieson [1963].
$^f$Data from Imanishi et al. [1961].
$^g$Data from Kennedy and Feinberg [1978], Kennedy et al. [1977].

### TABLE 5-5 Monomer Transfer Constants in Cationic Polymerization of Isobutylene in CH$_2$Cl$_2$

<table>
<thead>
<tr>
<th>Cointitator–Initiator</th>
<th>Temperature ($^\circ$C)</th>
<th>$C_M \times 10^4$</th>
</tr>
</thead>
<tbody>
<tr>
<td>TiCl$_4$-H$_2$O$^a$</td>
<td>−20</td>
<td>21.2</td>
</tr>
<tr>
<td></td>
<td>−50</td>
<td>6.60</td>
</tr>
<tr>
<td></td>
<td>−78</td>
<td>1.52</td>
</tr>
<tr>
<td>TiCl$_4$-Cl$_3$CO$_2$H$^a$</td>
<td>−20</td>
<td>26.9</td>
</tr>
<tr>
<td></td>
<td>−50</td>
<td>5.68</td>
</tr>
<tr>
<td></td>
<td>−78</td>
<td>2.44</td>
</tr>
<tr>
<td>SnCl$_4$-Cl$_3$CO$_2$H$^a$</td>
<td>−20</td>
<td>60.0</td>
</tr>
<tr>
<td></td>
<td>−50</td>
<td>36.0</td>
</tr>
<tr>
<td></td>
<td>−78</td>
<td>5.7</td>
</tr>
<tr>
<td>BF$_3$-H$_2$O$^b$</td>
<td>−25</td>
<td>15</td>
</tr>
<tr>
<td></td>
<td>−50</td>
<td>3.9</td>
</tr>
</tbody>
</table>

$^a$Data from Imanishi et al. [1961].
$^b$Data from Kennedy and Feinberg [1978], Kennedy et al. [1977].
weakly bonded negative fragment (e.g., $\text{CH}_3\text{O}^-$ in $\text{CH}_3\text{OH}$) or are readily alkylated ($\text{CH}_3\text{O}^-$). However, the value of $C_S$ for a transfer agent is seen to vary considerably when the initiator, coinitiator, or solvent is changed.

### 5-2f Effect of Reaction Medium

The nature of the reaction medium can play a significant role in cationic polymerization. Changes in rate and/or degree of polymerization often occur when the solvent or counterion are changed. The effect of reaction medium can affect the reaction in several ways. The equilibrium between free ions and ion pairs will be shifted toward free ions by high-polarity solvents. This usually results in an increased polymerization rate since free ions propagate faster than ion pairs, but the effect is not huge since $k_p^+$ typically does not exceed $k_p^-$ by more than an order of magnitude. However, large solvent effects can be observed for systems in which the counterion has a significant tendency to form a covalent bond to the carbocation. Low-polarity solvents drive the reaction system toward the covalent species $I$, (see Sec. 5-1), which does not propagate, or at most, propagates much more slowly than does the free ion or ion pair. In addition, solvent can affect the rate and degree of polymerization by changing propagation rate constants.

#### 5-2f-1 Propagation by Covalent Species; Pseudocationic Polymerization

The major species in most cationic polymerization systems are covalent, including halides and esters. There has been considerable controversy as to whether covalent species undergo propagation by direct monomer insertion into a covalent bond or only through ionization to

<table>
<thead>
<tr>
<th>Initiator or Cointiator</th>
<th>Solvent</th>
<th>Temperature ($^\circ$C)</th>
<th>Transfer Agent</th>
<th>$C_M \times 10^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\text{SnCl}_4$</td>
<td>$\phi \text{H}$</td>
<td>30</td>
<td>$\phi \text{H}$</td>
<td>0.22$^a$</td>
</tr>
<tr>
<td>$\text{H}_2\text{SO}_4$</td>
<td>($\text{CH}_2\text{Cl})_2$</td>
<td>25</td>
<td>($\text{CH}_3)_2\text{CH}\phi$</td>
<td>4.5$^b$</td>
</tr>
<tr>
<td>$\text{SnCl}_4$</td>
<td>$\text{C}<em>6\text{H}</em>{12}$</td>
<td>0</td>
<td>($\text{CH}_3)_2\text{CH}\phi$</td>
<td>0.60$^c$</td>
</tr>
<tr>
<td>$\text{SnCl}_4$</td>
<td>$\text{CCl}_4$-$\phi\text{NO}_2(3 : 7)$</td>
<td>0</td>
<td>$\text{CH}_3\text{O}\phi$</td>
<td>162$^d$</td>
</tr>
<tr>
<td>$\text{SnCl}_4$</td>
<td>$\text{CCl}_4$</td>
<td>30</td>
<td>$\text{CCl}_4$</td>
<td>0.52$^e$</td>
</tr>
<tr>
<td>$\text{SnCl}_4$</td>
<td>$\phi \text{H}$</td>
<td>30</td>
<td>$\text{CH}_3\text{OH}$</td>
<td>312$^e$</td>
</tr>
<tr>
<td>$\text{SnCl}_4$</td>
<td>($\text{CH}_2\text{Cl})_2$</td>
<td>30</td>
<td>$\text{CH}_3\text{OH}$</td>
<td>90$^f$</td>
</tr>
<tr>
<td>$\text{SnCl}_4$</td>
<td>$\phi \text{H}$</td>
<td>30</td>
<td>$\text{CH}_3\text{COOH}$</td>
<td>350$^i$</td>
</tr>
<tr>
<td>$\text{SnCl}_4$</td>
<td>($\text{CH}_2\text{Cl})_2$</td>
<td>30</td>
<td>$\text{CH}_3\text{COOH}$</td>
<td>40$^i$</td>
</tr>
<tr>
<td>$\text{BF}_3$</td>
<td>$\phi \text{H}$</td>
<td>30</td>
<td>$\text{CH}_3\text{COOH}$</td>
<td>144$^i$</td>
</tr>
<tr>
<td>$\text{SnCl}_4$</td>
<td>$\phi \text{H}$</td>
<td>30</td>
<td>($\text{CH}_3\text{CO})_2\text{O}$</td>
<td>960$^i$</td>
</tr>
<tr>
<td>$\text{SnCl}_4$</td>
<td>$\phi \text{H}$</td>
<td>30</td>
<td>$\text{CH}_3\text{COOC}_2\text{H}_3$</td>
<td>12$^i$</td>
</tr>
<tr>
<td>$\text{H}_2\text{SO}_4$</td>
<td>($\text{CH}_2\text{Cl})_2$</td>
<td>25</td>
<td>($\text{C}_2\text{H}_3)_2\text{O}$</td>
<td>19$^i$</td>
</tr>
<tr>
<td>$\text{CCl}_3\text{COOH}$</td>
<td>None</td>
<td>25</td>
<td>Benzoquinone</td>
<td>24$^i$</td>
</tr>
</tbody>
</table>

---

$^a$Data from Biddulph and Plesch [1960].
$^b$Data from Jenkinson and Pepper [1961].
$^c$Data from Overberger et al. [1956].
$^d$Data from Endres and Overberger [1955].
$^e$Data from Okamura and Higashimura [1956a,b].
$^f$Data from Brown and Mathieson [1957, 1958].
ions (ion pairs and free ions). Polymerization proceeding through covalent propagating centers, called pseudocationic polymerization, was proposed to explain certain behavior in the perchloric acid polymerization of styrene [Dunn et al., 1976; Gandini and Cheradame, 1980; Plesch, 1971, 1988, 1993]. The polymerization proceeds in three stages, two very fast stages separated by a very slow stage, slower by 3–6 orders of magnitude. Conductivity and spectroscopy measurements showed that ions and/or ion pairs were present in the fast stages but absent in the slow stage. Thus, the slow stage reaction was attributed to pseudocationic (covalent) propagation involving a multicenter insertion of monomer into the C–O bond of a perchlorate ester:

\[
\begin{align*}
\phi & \quad \phi \\
\sim\text{CH}_2\text{CH} & \quad \text{CHOClO}_3 \\
\text{H}_2\text{C} & \quad \phi \\
\phi & \quad \phi
\end{align*}
\]

(5-53)

The pseudocationic mechanism is also consistent with the observation of a bimodal molecular weight distribution. A bimodal MWD consists of a mixture of two molecular weight distributions that are sufficiently different to be distinguished by SEC. The presence of a bimodal molecular weight distribution indicates that there are two different propagating species that are not in fast equilibrium with each other (fast relative to their propagation rates). There would be a unimodal MWD (with some broadening) if two different propagating species were interconverting at a rate greater than either of their propagation rates. This is what is observed in various polymerizations where only free ions and ion pairs are present; in other words, free ions and ion pairs interconvert faster than they propagate. The bimodal MWD observed in the perchloric acid polymerization of styrene is attributed to separate propagations by covalent ester and free ion/ion pair. Propagation by free ions–ion pairs yields polymers (molecular weight \(\sim 10^4\)), while covalent propagation yields oligomers (molecular weight 600–700). (The low molecular weight of the latter indicates that extensive transfer to monomer occurs in competition with the slow propagation of the ester.) The amount of the low-molecular-weight fraction relative to the high-molecular-weight fraction as observed in the SEC correlates with the fraction of the total reaction carried by the slow stage reaction as observed by rate measurements. The high-molecular-weight fraction can be suppressed by the addition of a common ion salt such as tetra-\(n\)-butylammonium perchlorate, which pushes the equilibrium between ionic and covalent species toward the ester. The extent of the slow stage reaction is dependent on both temperature and solvent. It is observed only at \(-20\) to \(30^\circ\text{C}\) and only in solvents that are no more polar than chlorinated hydrocarbons.

Similar results have been observed for a number of other polymerizations—styrene (\(\text{CH}_3\text{COCIO}_4\), \(\text{FSO}_3\text{H}\), \(\text{CISO}_3\text{H}\), \(\text{CH}_3\text{SO}_3\text{H}\), \(\text{CF}_3\text{SO}_3\text{H}\), \(\text{CF}_3\text{COOH}\)), \(\text{p}\)-methylstyrene (\(\text{CF}_3\text{SO}_3\text{H}\), \(\text{I}_2\), \(\text{CH}_3\text{COCIO}_4\)), \(\text{p}\)-methoxystyrene (\(\text{CF}_3\text{SO}_3\text{H}\), \(\text{I}_2\)), and \(\text{p}\)-chlorostyrene (\(\text{CH}_3\text{COCIO}_4\), \(\text{CF}_3\text{SO}_3\text{H}\)) [Higashimura et al., 1976; Sawamoto et al., 1977, 1978; Sawamoto and Higashimura, 1978, 1979; Tanizaki et al., 1986]. Polymerizations in low-polarity solvents yield bimodal molecular weight distributions that respond to changes in reaction conditions in the same manner as described for the styrene–perchloric acid system. Certain polymerizations of isobutylene, vinyl ethers, and \(N\)-vinylcarbazole, called living cationic polymerizations (sec. 5-2g), show similar behavior under some conditions. Lewis acid–initiating systems such as \(\text{BF}_3\) plus \(\text{H}_2\text{O}\) do not follow the same behavior since the counterions in these systems do not form covalent bonds to carbon.
There is now a general consensus, but not unanimity, that covalent propagation does not occur. The arguments against covalent propagation and for propagation by ions (specifically, most likely, by ion pairs) have been described [Matyjaszewski and Pugh, 1996; Matyjaszewski and Sawamoto, 1996]. (Plisch has presented the case for covalent propagation [1988, 1993, 2001, 2002].) There is no argument that the propagating species in fast cationic polymerizations (such as the fast stages described above for styrene–perchloric acid) are ions (ion pairs and/or free ions). The only uncertainty is the identity of the propagating species in the slow stage. The polymerizations previously ascribed to covalent propagation may simply be due to very small concentrations of ions, concentrations that cannot be detected by conductivity or spectroscopy. Very low concentrations of ions result in observed polymerization because of their very high reactivity (Table 5-1 through 5-3). Most of the experimental observations ascribed to covalent propagation can be rationalized in terms of ionic propagation. The bimodal MWD may be the result of simultaneous propagation by ions and ion pairs with significantly different lifetimes such that there is little interconversion during propagation [Kunkel et al., 1992; Matyjaszewski, 2001; Matyjaszewski et al., 1994; Szwarc and Van Beylen, 1993]. Changes in polymerization rate with reaction conditions can be rationalized in terms of changes in the concentrations of free ions versus ion pairs. Finally, an interesting experiment was the addition of optically active 1-phenylethyl trifluoroacetate to styrene. Complete racemization was observed before addition was complete, consistent with the formation of carbocationic species. The addition reaction should have occurred by a stereoselective route if it proceeded by a multicenter reaction.

**5-2f-2 Solvent Effects**

Polymerization rates and polymer molecular weights increase with increasing solvent polarity because there is a shift in concentrations from the unreactive (dormant) covalent species toward the ion pairs and free ions. For the perchloric acid polymerization of styrene, there is an increase in overall reaction rate by about 3 orders of magnitude when polymerization is carried out in 1,2-dichloroethane ($\epsilon = 9.72$) compared to carbon tetrachloride ($\epsilon = 2.24$) [Pepper and Reilly, 1962]. Table 5-7 shows data for the polymerization of $p$-methoxystyrene by iodine [Kanoh et al., 1965]. The apparent propagation rate constant increases by more than 2 orders of magnitude in going from carbon tetrachloride ($\epsilon = 2.24$) to methylene chloride ($\epsilon = 9.08$). (Although the dielectric constant $\epsilon$ is generally used as an indication of the solvating power of a solvent, it is not necessarily a quantitative measure. Specific solvation and polarization effects, which are not adequately described by $\epsilon$, may be important in a particular system.)

Similar effects are observed for reaction systems where covalent species are not present. Thus, BCl$_3$ + H$_2$O do not polymerize neat isobutylene, but polymerization occurs for

<table>
<thead>
<tr>
<th>Solvent</th>
<th>$k_{pp}^{app}$ (L mol$^{-1}$ s$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>CH$_2$Cl$_2$</td>
<td>17</td>
</tr>
<tr>
<td>CH$_2$Cl$_2$/CCl$_4$, 3/1</td>
<td>1.8</td>
</tr>
<tr>
<td>CH$_2$Cl$_2$/CCl$_4$, 1/1</td>
<td>0.31</td>
</tr>
<tr>
<td>CCl$_4$</td>
<td>0.12</td>
</tr>
</tbody>
</table>

aData from Kanoh et al. [1965].
solutions of isobutylene in solvents (e.g., CH₂Cl₂, CH₃Cl) more polar than isobutylene [Kennedy et al., 1977]. Ionic propagating species (either free ions or ion pairs) are not sufficiently stable and do not form unless the reaction medium possesses some minimum solvating ability.

The preceding discussion assumes that the effect of solvent polarity on reaction rate (and polymer molecular weight) manifests itself only by altering the concentration of propagating centers. However, solvent polarity is also expected to alter propagation rate constants, $k_\text{p}^+$ and $k_\text{p}^-$. One expects $k_\text{p}^+$ to decrease with increasing solvent polarity [Ledwith and Sherrington, 1974]. The transition state for propagation by a free ion involves charge dispersal, so that solvents of higher polarity stabilize the reactants more than the transition state [Reichardt, 1988]. The effect of solvent polarity on $k_\text{p}^-$ is more difficult to predict. Whether increased solvent polarity increases or decreases $k_\text{p}^-$ depends on whether the transition state has a higher or lower dipole moment than the ion pair. There are very few data available on the effect of solvents on the different propagation rate constants. A comparison of reported $k_\text{p}^+$ values for styrene, ethyl vinyl ether, and isopropyl vinyl ether in different solvents shows the expected decrease in propagation rate constant with increasing solvent polarity [Deffieux et al., 1983; Sawamoto and Higashimura, 1978, 1979]. Table 5-8 shows data for isopropyl vinyl ether in radiation polymerization at 30°C.

Table 5-8 Effect of Solvent on $k_\text{p}^+$ in Radiation Polymerization of Isopropyl Vinyl Ether at 30°C

<table>
<thead>
<tr>
<th>Solvent</th>
<th>$\varepsilon$</th>
<th>$k_\text{p}^+ \times 10^{-4}$ (L mol⁻¹ s⁻¹)</th>
</tr>
</thead>
<tbody>
<tr>
<td>φH</td>
<td>2.7</td>
<td>57</td>
</tr>
<tr>
<td>Bulk</td>
<td>3.0</td>
<td>130</td>
</tr>
<tr>
<td>(C₂H₅)₂O</td>
<td>3.7</td>
<td>34</td>
</tr>
<tr>
<td>CH₂Cl₂</td>
<td>6.0</td>
<td>1.5</td>
</tr>
<tr>
<td>CH₃NO₂</td>
<td>19.5</td>
<td>0.02</td>
</tr>
</tbody>
</table>

$^a$Data from Deffieux et al. [1983].
$^b$Calculated from $\varepsilon$ values of solvent and monomer assuming additivity of volumes and $\varepsilon$ of mixture to vary with volume fraction of solvent.

The need for solvation of ionic propagating species in cationic polymerization is evident when reaction is carried out in media of low dielectric constant. In addition to lowered polymerization rates in poorly solvating media, one frequently encounters increased kinetic orders in one of the reactants. The polymerization rate may show an increased order of dependence on the monomer, initiator, or coinitiator. Thus, the rate for the tin (IV) chloride polymerization of styrene depends on $[M]^2$ in benzene solution and $[M]^3$ in carbon tetrachloride solution [Okamura and Higashimura, 1956a,b, 1960]. Carbon tetrachloride is a poor solvating agent compared to benzene, and the higher order in styrene concentration is due to styrene taking part in solvation of propagating species. At high concentrations of styrene (and also in neat styrene) the order in styrene decreases to 2 as the reaction medium becomes equivalent to the benzene system. (That benzene is a better solvating medium than
carbon tetrachloride is not entirely clear from a consideration of dielectric constants since the values are quite close—2.28 and 2.24 for benzene and carbon tetrachloride, respectively. However, other measures of solvating power such as the $E_N$ scale show the difference between benzene and CCl$_4$. The $E_N$ value for a solvent is derived from the energy of UV excitation for a pyridinium-$N$-phenoxide betaine dye in the solvent. Benzene and CCl$_4$ have $E_N$ values of 0.111 and 0.052, respectively, with larger values being indicative of higher solvating power [Reichardt, 1988].

The polymerization of styrene by trichloroacetic acid without solvent and in 1,2-dichloroethane and nitroethane solutions illustrates the situation where the initiator solvates ionic propagating species [Brown and Mathieson, 1958]. The kinetic order in the concentration of trichloroacetic acid increases from 1 in the highly polar nitroethane to 2 in the less polar 1,2-dichloroethane to 3 in neat styrene.

Another effect of reaction medium on polymerization is the observation that the polymerization rate in some systems (e.g., styrene–triflic acid and $N$-vinylcarbazole–$n$-butylmagnesium bromide) becomes independent of or inversely proportional to the monomer concentration at higher monomer concentrations [Biswas and John, 1978; Chmelir and Schulz, 1979; Gandini and Cheradame, 1980; Hatada et al., 1980; Sawamoto et al., 1977, 1978]. The mechanism for this behavior may be different depending on the reaction system. Monomer may form an unreactive complex with initiator or coinitiator. Varying the monomer concentration may alter concentrations of ionic propagating species through a change in solvent polarity [Roth et al., 1997]. Plesch [1993, 2001, 2002] cautioned that propagation rate constants may be low by an order of magnitude if calculated on the assumption of a first-order dependence on monomer. However, data from isobutylene polymerization indicate that this complication is not present, propagation rate constants are independent of monomer concentration [Mayr et al., 2002].

5-2f-3 Counterion Effects

It is generally accepted that there is little effect of counterion on reactivity of ion pairs since the ion pairs in cationic polymerization are loose ion pairs. However, there is essentially no experimental data to unequivocally prove this point. There is no study where polymerizations of a monomer using different counterions have been performed under reaction conditions in which the identities and concentrations of propagating species are well established. (Contrary to the situation in cationic polymerization, such experiments have been performed in anionic polymerization and an effect of counterion on propagation is observed; see Sec. 5-3e-2.)

5-2g Living Cationic Polymerization

Living polymerizations are polymerizations without chain-breaking reactions (Sec. 3-15). For a highly purified reaction system devoid of impurities, the concentration of propagating species remains constant throughout the polymerization and even after 100% conversion. A plot of $M_n$ versus conversion is linear. Further, after 100% conversion, additional polymerization takes place by adding more monomer to the reaction system. The molecular weight of the polymer increases further since the propagating centers remain intact. The utility of living polymers for producing polymeric materials with different architectures and well-defined end groups was discussed in Sec. 3-15. The first living polymerizations were achieved in anionic polymerizations of styrenes and 1,3-dienes in the mid-1950s (Sec. 5-3b-1). Some of the potential of living anionic polymerization has been realized with commercial processes for block copolymers of styrene with butadiene and isoprene.
5-2g-1 General Requirements

Living anionic polymerization is relatively easy to achieve if one has a well-purified system without water or other adventitious agents that terminate anionic propagating centers by proton transfer. Anionic propagating systems do not have a “built-in” termination reaction, anionic centers are reasonably stable under a wide range of polymerization conditions. It has been much more difficult to achieve living cationic polymerizations (LCPs), even in well-purified systems and even when the components of the reaction system have been carefully chosen so that nucleophiles are not present to terminate the cationic centers. Cationic propagating centers have a facile built-in termination reaction—transfer of β-protons to monomer, counterion or some other basic species present. In spite of this formidable problem, LCP has been achieved starting with major advances in the early 1980s [Faust and Kennedy, 1987; Faust et al., 1986; Higashimura et al., 1988; Higashimura and Sawamoto, 1985; Kaszas et al., 1990; Kennedy, 1990, 1999; Kennedy and Ivan, 1992; Matyjaszewski and Sawamoto, 1996; Sawamoto, 1991; Sawamoto and Higashimura, 1986, 1990; Sawamoto et al., 1987].

To achieve LCP, one needs to start by choosing the initiator, coinitiator, and other components of a reaction so that there is no nucleophile present that can irreversibly terminate the propagating cationic species. Basic components also need to be avoided to minimize β-proton transfer. However, even with the most judicious choice of reaction system, β-proton transfer is still present because monomer itself is a base. One needs to minimize β-proton transfer to monomer to achieve LCP.

Both free ions and ion pairs are highly reactive species with very short lifetimes (less than several seconds), and both propagation and transfer are very fast. Very fast reactions result in uncontrolled exotherms, the reaction temperature increases, and transfer increases relative to propagation because the activation energy for transfer is greater than that for propagation. The result is a lack of control and a nonliving polymerization. LCP is achieved by slowing down the reaction, specifically, extending the lifetime of the propagating centers, so that significant propagation occurs prior to β-proton transfer to monomer. Lower temperature is one reaction parameter that is used to achieve this objective.

The major approach to extending the lifetime of propagating species involves reversible conversion of the active centers to dormant species such as covalent esters or halides by using initiation systems with Lewis acids that supply an appropriate nucleophilic counterion. The equilibrium between dormant covalent species and active ion pairs and free ions is driven further toward the dormant species by the common ion effect—by adding a salt that supplies the same counterion as supplied by the Lewis acid. Free ions are absent in most systems; most of the species present are dormant covalent species with much smaller amounts of active ion pairs. Further, the components of the reaction system are chosen so that there is a dynamic fast equilibrium between active and dormant species, as the rates of deactivation and activation are faster than the propagation and transfer rates. The overall result is a slower but more controlled reaction with the important features of living polymerization (Sec. 3-15).

In addition to the choice of Lewis acid, added common ion salt, and temperature, the fast equilibrium between active and dormant species can be fostered by including additional nucleophiles (separate from the nucleophilic counterion) in the reaction system and by variations in solvent polarity. Nucleophiles act by further driving of the dynamic equilibrium toward the covalent species and/or decreasing the reactivity of ion pairs. Nucleophilic counterions and added nucleophiles work best in nonpolar solvents such as toluene and hexane. Their action in polar solvents is weaker because the polar solvents interact with the nucleophiles and nucleophilic counterions, as well as the ion pairs. Polar solvents such as methylene.
chloride are not conducive to LCP because the equilibrium between active and dormant species is driven more toward the active species, which leads to faster and less controlled polymerization. Added salts are useful in polar solvents for driving the equilibrium back the other way, back to the dormant covalent species.

It is not an absolute necessity for LCP to have no free ions. If free ions are present, LCP is possible only if there are fast equilibria between free ions, ion pairs, and covalent species. If the equilibrium between free ions and ion pairs is slow, the result is a bimodal distribution. Further, to have any possibility of LCP with free ions present, the concentration and reactivity of the free ions should not be such that the reaction is too fast.

The specific combination of initiator, coinitiator, solvent temperature, and additives needed to achieve LCP varies with the monomer. The components of the reaction system need to be fine-tuned differently for different monomers (Sec. 5-2g-3).

5-2g-2 Rate and Degree of Polymerization

The rate of living cationic polymerization is expressed as the rate of propagation of ion pairs

\[ R_p = k_p^+ [Y^+ (IZ^-)] [M] \]  \hspace{1cm} (5-54)

in the absence of free ions and for the case where initiation is very fast (i.e., the concentration of propagating ion pairs equals the concentration of ion pairs derived from initiator and coinitiator). The concentration of ion pairs is rarely directly determined, but one can relate it to the concentration of initiator (ZY) and coinitiator (I). Two equilibria are involved

\[ I + ZY \xrightleftharpoons[K_1]{K_2} IZY \xrightarrow{K_1} Y^+(IZ^-) \]  \hspace{1cm} (5-55)

and the concentration of ion pairs is given by

\[ [Y^+ (IZ^-)] = K_1 K_2 [I] [ZY] \]  \hspace{1cm} (5-56)

Combination of Eqs. 5-54 and 5-56 yields the polymerization rate as

\[ R_p = k_p^+ K_1 K_2 [I] [ZY] [M] \]  \hspace{1cm} (5-57)

Some living polymerization show a greater than first-order dependence of \( R_p \) on [M] indicating that the initiation rate is slow and dependent on monomer.

The number-average degree of polymerization for a living cationic polymerization is defined as the concentration of monomer consumed divided by the total concentration of all propagating chains (dormant and active)

\[ X_n = \frac{p [M]_0}{[ZY]_0} \]  \hspace{1cm} (5-58)

where [M]_0 and [ZY]_0 are initial concentrations of monomer and initiator, respectively, and \( p \) is the fractional conversion of monomer at any time in the reaction. The number-average degree of polymerization is \([M]_0/[ZY]_0\) at complete conversion. Equation 5-58 is the LCP analog of Eq. 3-225 for ATRP living polymerization. The PDI for LCP is given by the
Poisson distribution [Flory, 1940; Peebles 1971; Szwarc, 1968], the same for ATRP and other living polymerizations

\[
\frac{X_w}{X_n} = 1 + \frac{1}{X_n} 
\]

(3-228)

5-2g-3 Specific Living Cationic Polymerization Systems

Vinyl ethers form more stable carbocations than most other monomers because the ether group is effective at resonance stabilization of positive charge. This means that the equilibrium between active and dormant species can be achieved using relatively weak initiators. LCP of isobutyl vinyl ether takes place using HI with I₂ or ZnI₂ in toluene or CH₂Cl₂ at −40 to 25°C. Lower temperatures are generally more useful for the more polar solvent. Figure 5-2 shows LCP for isobutyl vinyl ether with HI/I₂ [Sawamoto and Higashimura, 1986]. These data are typical of LCP. The plot of \( M_n \) versus conversion is linear over the complete conversion range for successive additions of two batches of monomer. The fact that the \( M_n \) values for both batches of monomer fall on the same line shows that polymerization proceeds throughout with a constant concentration of propagating species, with negligible termination and transfer. The presence of significant termination or transfer would result in the plot showing a downward curvature with conversion. Protonic acids such as RCO₂H and RSO₃H with a weak Lewis acid yield similar results.

Stronger Lewis acids such as SnCl₄, TiCl₄, and CH₃AlCl₂ yield fast but uncontrolled polymerization with broad PDI. LCP of vinyl ethers can be achieved if the other components and reaction parameters are appropriately adjusted by various combinations of lower reaction temperature, added nucleophile, added common salt, and solvent polarity. For example, polymerization of isobutyl vinyl ether using HCl as the initiator (or one can use the preformed adduct of monomer and HCl) with SnCl₄ or TiCl₄ in CH₂Cl₂ is non-LCP.

![Fig. 5-2](image-url)Dependence of \( M_n \) and \( M_w/M_n \) on conversion for the polymerization of isobutyl vinyl ether by HI/I₂ in CH₂Cl₂ at −15°C. \([M] = 0.38 \, M \) at beginning of each batch; \([HI] = 0.01 \, M \); \([I₂] = 0.02 \, M \) (Δ), 0.001 \( M \) (●), 0.005 \( M \) (○). After Sawamoto and Higashimura [1986] (by permission of Huthig and Wepf Verlag, Basel and Wiley-VCH, Weinheim).
(PDI = 1.5) when carried out at −15°C [Katayama et al., 2001]. The reaction converts to LCP with PDI < 1.2 when the polymerization temperature is lowered to −78°C or tetra-n-butylammonium chloride is added. Mild nucleophiles such as esters, ethers, sulfides, and pyridines are also useful to decelerate the reaction rate, narrow PDI, and yield LCP [Aoshima and Higashimura, 1989; Cho et al., 1990; Kishimoto et al., 1989].

Isobutylene, which forms a less stable carbocation than does vinyl ether, requires a stronger Lewis acid (BF₃, SnCl₄ and TiCl₄) [Kennedy, 1999; Storey and Donnalley, 2000]. Dialkylaluminum chloride has also been used [Bahadur et al., 2000]. Tertiary chlorides such as cumyl chloride and 2-chloro-2,4,4-termethylpentane or the corresponding esters are often used so that the initiating carbocation is of comparable stability to the propagating carbocation. Haloalkanes or mixtures of alkanes and haloalkanes are generally used as solvents to achieve reasonable reaction rates and prevent polymer precipitation before the desired molecular weight is achieved. Strong nucleophiles such as N,N-dimethylacetamide and dimethyl sulfoxide and/or salts such as tetra-n-butylammonium chloride are often used, and temperatures below −30°C are needed to achieve LCP.

N-Vinylcarbazole (NVC) forms a more stable carbocation than does a vinyl ether because of the electron-releasing nitrogen and conjugation of the positive charge with the π-electrons of the ring. This results in LCP using HI in the absence of a Lewis acid in toluene at −40°C. LCP converts to non-LCP by conditions that shift the equilibrium away from the covalent species and toward ion pairs and free ions, for example, by adding a Lewis acid such as zinc iodide or iodine or using the more polar solvent methylene chloride. LCP can be restored in the more polar solvent by the addition of tetra-n-butylammonium iodine. Highly nucleophilic counterions such as chloride often push the equilibrium so far toward the covalent species that neither living nor nonliving polymerization occurs.

The occurrence of a narrow size distribution is diagnostic of a living polymerization. In reaction systems where one passes from nonliving to living polymerization by changes in coinitiator, temperature, solvent, added nucleophile, or added salt, one observes a shift from a unimodal molecular weight distribution (PDI considerably above 1; theoretical PDI = 2 as per Sec. 3-11a and Eq. 2-97) for nonliving polymerization to a bimodal distribution for a mixture of living and nonliving polymerizations to a unimodal distribution (PDI close to 1) for living polymerization. The rates and molecular weights for the living polymerizations are lower than those for the nonliving polymerizations. The latter proceed by free-ion and ion-pair centers that are much more reactive than the propagating species in living systems. A range of molecular weights has been obtained in the various living systems. Some studies have concentrated on the synthesis of low-molecular-weight telechelic polymers with molecular weights of only a few thousand, while polymers of number-average molecular weights up to 50,000–100,000 have been synthesized in other studies.

The formation of Poisson distributions is corroboration of the fast equilibrium assumed between active and inactive propagating centers. For any propagating center, the fractions of its total lifetime spent as active and inactive centers are very close to those for other propagating centers.

None of the cationic living polymerization systems are as long-lived as the anionic systems to be described in Sec. 5-3b-1. The various cationic living systems show the characteristics of living systems as long as monomer is present, but decay of propagating species begins in the absence of monomer. The half-lives for propagating species in the absence of monomer vary from less than an hour to many hours at the higher temperatures but were as high as a day or more for lower temperatures depending on the particular system [Choi et al., 1990; Higashimura and Sawamoto, 1989]. The lifetimes for the isobutylene systems appear to be lower than those for other monomers, probably only minutes.
Cationic polymerizations, like their radical counterparts, are quite exothermic, since the reaction involves the conversion of \( \pi \)-bonds to \( \sigma \)-bonds. The heat of polymerization for any particular monomer is essentially the same irrespective of the mode of initiation (if the monomer can be polymerized by both radical and cationic initiators).

From a consideration of Eqs. 5-34 and 5-35, the composite activation energies \( E_R \) and \( E_{\bar{X}_n} \) for the rate and degree of polymerization, respectively, are obtained as

\[
E_R = E_i + E_p - E_t \tag{5-59}
\]
\[
E_{\bar{X}_n} = E_p - E_t \tag{5-60}
\]

where \( E_i \), \( E_p \), and \( E_t \) are the activation energies for the initiation, propagation, and chain termination steps, respectively. For the activation energy for \( \bar{X}_n \), \( E_t \) will be replaced by an \( E_{tr} \) term or terms when transfer occurs. Propagation involves the addition of an ion or ion pair to a monomer in a medium of low polarity and does not require a large activation energy (about <20–25 kJ mol\(^{-1}\)). The values of \( E_i \) and \( E_t \) are greater than \( E_p \) in most cases. The net interaction of the various activation energies leads to values of \( E_R \) in the range of \(-20 \) to \(+40 \) kJ mol\(^{-1}\). For many polymerization systems \( E_R \) is negative and one observes the rather unusual phenomenon of increasing polymerization rates with decreasing temperatures. The negative activation energy for the polymerization rate is not, however, a complete generalization. The sign and value of \( E_R \) vary from one monomer to another. Even for the same monomer, the value of \( E_R \) may vary considerably depending on the initiator, coinitiator, and solvent [Biswas and Kabir, 1978, 1979; Biswas and Kamannarayana, 1976; Brown and Mathieson, 1957, 1958; Plesch, 1953]. Table 5-9 shows that \( E_R \) may vary from \(-35.5 \) to \(+58.6 \) kJ mol\(^{-1}\) for styrene polymerization. The variations in \( E_R \) are a consequence of the differences in \( E_i \), \( E_p \), and \( E_t \) caused by the differences in the initiator, coinitiator, and the solvating power of the reaction medium. It should be noted that, irrespective of sign, the values of \( E_R \) are generally smaller than in radical polymerizations. The rates of most cationic polymerizations do not change with temperature as much as those of radical polymerizations.

A negative value of \( E_R \) does not mean a negative activation energy for some reactant(s) going to a transition state. No simple, single step in any reaction pathway will have a negative activation energy. A negative \( E_R \) is simply a consequence of \( E_t \) being larger than \( E_i + E_p \). Increased temperature decreases \( R_p \) because termination becomes more favored relative to initiation and propagation. What appears at first glance to be even more anomolous are negative values of \( E_p \) observed in a few polymerizations [Cotrel et al., 1976; Villesange et al., 1977]. The negative activation energy indicates that the measured \( E_p \) includes not only the

<table>
<thead>
<tr>
<th>Initiating System</th>
<th>Solvent</th>
<th>( E_R ) (kJ mol(^{-1}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>TiCl(_4)-H(_2)O (^a)</td>
<td>(CH(_2))(_2)</td>
<td>-35.5</td>
</tr>
<tr>
<td>TiCl(_4)-CCl(_3)CO(_2)H (^a)</td>
<td>( \phi )CH(_3)</td>
<td>-6.3</td>
</tr>
<tr>
<td>CCl(_3)CO(_2)H (_2)</td>
<td>C(_2)H(_4)Br</td>
<td>12.6</td>
</tr>
<tr>
<td>SnCl(_4)-H(_2)O</td>
<td>( \phi )H</td>
<td>23.0</td>
</tr>
<tr>
<td>CCl(_3)CO(_2)H</td>
<td>(CH(_3))(_2)</td>
<td>33.5</td>
</tr>
<tr>
<td>CCl(_3)CO(_2)H</td>
<td>CH(_3)NO(_2)</td>
<td>58.6</td>
</tr>
</tbody>
</table>

\(^a\)Data from Plesch [1953]; all other data from Brown and Mathieson [1957, 1958].
activation energy for propagation but also a term for some other process. Since increased temperature decreases the dielectric constant of a liquid, the negative $E_p$ may be indicative of a change in the relative concentrations of different propagating species (free ion, ion pair) or the effect of solvent polarity of $k_p$. The phenomenon may also be responsible for the changes in $E_R$ with temperature that are sometimes observed [Biswas and Kabir, 1978, 1979; Plesch, 1971].

The composite activation energy for the degree of polymerization $E_{X_n}$ is almost always negative because $E_t$ or $E_tr$ is generally greater than $E_p$ irrespective of the mode of termination or transfer [Biswas and Kabir 1978, 1979; DiMaina et al., 1977; Kennedy and Feinberg, 1978; Kennedy et al., 1977]. This means that the degree of polymerization decreases as the temperature increases. $E_{X_n}$ in more negative when transfer reactions predominate over termination by combination or spontaneous termination since the transfer reactions have larger activation energies. As the polymerization temperature is increased, the principal mode of chain breaking shifts from termination to transfer [Biswas and Kamannarayana, 1976; Kennedy and Squires, 1965]. Further, there may be a shift from one transfer mode to another as the temperature is changed. Figure 5-3 shows a plot of $\log E_{X_n}$ versus $1/T$ for the polymerization of isobutylene by AlCl$_3$ in methylene chloride solution. There is a change in the

![Fig. 5-3](image)

**Fig. 5-3** Temperature dependence of $X_n$ for the aluminum chloride polymerization of isobutylene. After Kennedy and Squires [1965] (by permission of Butterworth, London and Elsevier, Oxford).
slope of the plot at approximately $-100^\circ\text{C}$ from an $E_{X_n}$ value of $-23.4$ to $-3.1$ kJ mol$^{-1}$. This has been attributed to a change in the chain-breaking step from chain transfer to monomer below $-100^\circ\text{C}$ to chain transfer to solvent above $-100^\circ\text{C}$. The change in $E_{X_n}$ may also be (at least partially) due to the effect of temperature on the relative amounts of the different types of propagating species.

5-2i Commercial Applications of Cationic Polymerization

5-2i-1 Polyisobutylene Products

Various polymerizations and copolymerizations of isobutylene to produce polyisobutylene, polybutene, and butyl rubber constitute the most important commercial applications of cationic polymerization [Kennedy and Marechal, 1982; Kresge et al., 1987; Russell and Wilson, 1977; Vairon and Spassky, 1996]. The polybutenes are very-low-molecular-weight copolymers ($M_n < 3000$), containing about 80% isobutylene and 20% other butenes (mostly 1-butene), used in adhesives, caulking, sealants, lubricants, plasticizers, and additives for motor oils and transmission fluids (for viscosity improvements). Low-molecular-weight polyisobutylenes (up to $M_v 5–10 \times 10^5$) range from viscous liquids to tacky semisolids and are used for sealant and caulking applications. High-molecular-weight polyisobutylenes ($M_v > 10^5$) are rubbery solids used to make uncured (uncrosslinked) rubber products and as impact modifiers of thermoplastics. The molecular weights are controlled primarily by choice of polymerization temperature. Polymerization at $-40$ to $10^\circ\text{C}$ with AlCl$_3$ (BF$_3$ or TiCl$_4$ is used in some processes) produces the lower-molecular-weight products. The high-molecular-weight polyisobutylenes are obtained at considerably lower reaction temperatures ($-100$ to $-90^\circ\text{C}$) by using a process similar to that for butyl rubber.

Butyl rubber (BR) is a copolymer of isobutylene with small amounts of isoprene produced by aluminum chloride initiated polymerization. About 1 billion pounds of butyl rubber are produced annually in the United States. Polymerization is carried out in a continuous process using methyl chloride as diluent as shown in Fig. 5-4. Isobutylene and isoprene are purified and then mixed together in methyl chloride solution. The initiation system is produced by passing methyl chloride through beds of aluminum chloride at 30–45$^\circ\text{C}$ followed by dilution with methyl chloride and the addition of the initiator (protogen or cationogen). The initiation and monomer solutions are chilled separately to $-100$ to $-90^\circ\text{C}$ by using boiling ethylene and propene or propane as heat exchangers (referred to as C$_2$ and C$_3$ chillers in Fig. 5-4). The cold monomer and initiation solutions are injected rapidly and continuously into the reactor. Polymerization occurs almost instantaneously with the polymer precipitating as a fine slurry in methyl chloride. The slurry overflows into a flash tank containing steam and hot water. Solvent and unreacted monomers are vaporized and pass into a recovery system. Small amounts of zinc or aluminum stearate (to control the particle size of the butyl rubber latex) and antioxidant are added to the water in the flash tank. The aqueous slurry of butyl rubber passes into a stripping tank operating under vacuum to pull off residual amounts of methyl chloride and unreacted monomer. The stripped slurry is then pumped to a series of drying extruders to dewater the product and compressed into bales ready for shipment.
The isoprene incorporates double bonds into the polymer chains, which makes subsequent vulcanization (crosslinking) possible (Sec. 9-2b). The amount of isoprene is in the range of 0.5–2.5% of the amount of isobutylene, the exact amount depending on the extent of cross-linking that is desired. Molecular weights of at least 200,000 are needed to obtain products that are not tacky. Control of molecular weight is achieved by working at the lower reaction temperatures and regulating the amounts of transfer and terminating agents present. Butyl rubber, unlike natural rubber, does not crystallize on cooling and hence remains flexible down to \(-50^\circ\text{C}\). The low degree of unsaturation imparts good resistance to aging, moisture, chemicals, and ozone. The low gas permeability of butyl rubber makes it well suited for innerubes for tires (which are still used in most nonpassenger automobile tires). The high-damping behavior of butyl rubber makes it well suited for engine and auto-body mounts. Other uses include electrical cable insulation, protective gloves, chemical tank liners, and pharmaceutical stoppers.

**5-2i-2 Other Products**

*Hydrocarbon resins* comprise a range of low-molecular-weight products (\(M_n < 3000\)) used as adhesives, hot-melt coatings, tackifying agents, inks, and additives in rubber. These include products based on monomers derived from petroleum as well as plant sources. The petroleum-derived products include polymers produced from various alkenes, isoprene, piperylene, styrene, \(\alpha\)-methylstyrene, vinyltoluene, and dicyclopentadiene. The plant-derived products include *polyterpenes* obtained by the polymerization of dipentene, limonene,
α-pinene, and β-pinene. Low-molecular-weight coumarone–indene polymers, referred to as coal-tar resins, are used in surface coatings and floor tiles.

The polymerization of alkyl vinyl ethers is of some commercial importance. The homopolymers, which can be obtained only by cationic polymerization, are useful as plasticizers of other polymers, adhesives, and coatings. (The copolymerization of vinyl ethers with acrylates, vinyl acetate, maleic anhydride, and other monomers is achieved by radical polymerization but not the homopolymerizations of alkyl vinyl ethers.)

5-3 ANIONIC POLYMERIZATION OF THE CARBON–CARBON DOUBLE BOND

Anionic chain polymerizations show many of the same characteristics as cationic polymerizations, although there are some distinct differences. The propagating species are anionic ion pairs and free ions with relative concentrations that depend on the reaction media as in cationic polymerization. Unlike cationic polymerization, there is a large difference between the reactivities of ion pairs and free ions in anionic polymerization. Although anionic polymerizations generally proceed rapidly at low temperatures, they are seldom as temperature-sensitive as cationic polymerizations. Further, most anionic polymerizations possess positive $E_R$ values and proceed well at and somewhat above ambient temperatures. Many anionic polymerizations are easier to understand, since the identities of the initiating species and counterions are much better established. The range of solvents useful for anionic polymerization is limited to aliphatic and aromatic hydrocarbons and ethers. Halogenated solvents, suitable for cationic polymerization, cannot be used for anionic polymerization because of their facile nucleophilic substitution reactions with carbanions. Other polar solvents such as esters and ketones are also excluded as a result of reaction with carbanions.

Termination occurs by transfer of a positive fragment, usually a proton, from the solvent or some transfer agent (often deliberately added), although other modes of termination are also known. Many anionic polymerizations are living polymerizations when the reaction components are appropriately chosen.

5-3a Initiation

5-3a-1 Nucleophilic Initiators

A variety of basic (nucleophilic) initiators have been used to initiate anionic polymerization [Bywater, 1975, 1976, 1985; Fontanille, 1989; Hsieh and Quirk, 1996; Morton, 1983; Morton and Fetters, 1977; Quirk, 1995, 1998, 2002; Richards, 1979; Szwarc, 1983; Young et al., 1984]. These include covalent or ionic metal amides such as NaNH$_2$ and LiN(C$_2$H$_5$)$_2$, alkoxides, hydroxides, cyanides, phosphines, amines, and organometallic compounds such as $n$-C$_4$H$_9$Li and φMgBr. Initiation involves the addition to monomer of a nucleophile (base), either a neutral (B:) or negative (B:−) species.

Alkyl lithium compounds are probably the most useful of these initiators, employed commercially in the polymerizations of 1,3-butadiene and isoprene. Initiation proceeds by addition of the metal alkyl to monomer

$$
\text{C}_4\text{H}_9\text{Li} + \text{CH}_2=\text{CHY} \rightarrow \text{C}_4\text{H}_9-\text{CH}_2-\text{C}^-\text{Li}^+ (\text{Li}^+) \quad (5-61)
$$
followed by propagation:

$$
\text{C}_4\text{H}_9\text{CH}_2\text{C}^-\text{Li}^+ + n\text{CH}_2=\text{CHY} \rightarrow \text{C}_4\text{H}_9\{\text{CH}_2\text{CHY}\}_{n}\text{CH}_2\text{C}^-\text{Li}^+
$$

The extensive use of alkyllithium initiators is due to their solubility in hydrocarbon solvents. Alkyls or aryls of the heavier alkali metals are poorly soluble in hydrocarbons, a consequence of their more ionic nature. The heavier alkali metal compounds, as well as alkyllithiums, are soluble in more polar solvents such as ethers. The use of most of the alkali metal compounds, especially, the more ionic ones, in ether solvents is somewhat limited by their reactivity toward ethers. The problem is overcome by working below ambient temperatures and/or using less reactive (i.e., resonance-stabilized) anions as in benzylpotassium, cumylcesium and diphenylmethyllithium.

Alkyl derivatives of the alkaline-earth metals have also been used to initiate anionic polymerization. Organomagnesium compounds are considerably less active than organolithiums, as a result of the much less polarized metal–carbon bond. They can only initiate polymerization of monomers more reactive than styrene and 1,3-dienes, such as 2- and 4-vinylpyridines, and acrylic and methacrylic esters. Organostrontium and organobarium compounds, possessing more polar metal–carbon bonds, are able to polymerize styrene and 1,3-dienes as well as the more reactive monomers.

In the relatively few anionic polymerizations initiated by neutral nucleophiles such as tertiary amines or phosphines the proposed propagating species is a zwitterion [Cronin and Pepper, 1988; Eromosele et al., 1989; Klemarczyk, 2001; Pepper and Ryan, 1983]. Primary and secondary amines are much less effective than tertiary amines. The zwitterion propagating species has the glaring deficiency of requiring increasing charge separation as propagation proceeds. Stabilization of zwitterion species may involve the positive end of one zwitterion propagating chain acting as the counterion of the carbanion end of another zwitterion propagating chain. The need for a zwitterion propagating species is avoided if initiation is proposed as occurring via hydroxide ion formed by the reaction of amine with adventitious water [Donnelly et al., 1977; Ogawa and Romero, 1977].

The initiator required to polymerize a monomer depends on the reactivity of the monomer toward nucleophilic attack. Monomer reactivity increases with increasing ability to stabilize the carbanion charge. Very strong nucleophiles such as amide ion or alkyl carbanion are needed to polymerize monomers, such as styrene and 1,3-butadiene, with relatively weak electron-withdrawing substituents. Weaker nucleophiles, such as alkoxide and hydroxide
ions, can polymerize monomers with strongly electron-withdrawing substituents, such as acrylonitrile, methyl methacrylate, and methyl vinyl ketone, although the efficiency is lower than that of the stronger nucleophiles. A monomer, such as methyl-\(\alpha\)-cyanoacrylate, with two electron-withdrawing substituents can be polymerized with very mild nucleophiles such as \(\text{Br}^-\), \(\text{CN}^-\), tertiary amines, and phosphines. This monomer, used in many so-called super-glues, polymerizes on contact with many surfaces. Polymerization probably involves initiation by adventitious water (or \(\text{OH}^-\) from water) [Donnelly et al., 1977].

5-3a-2 Electron Transfer

Szwarc and coworker have studied the interesting and useful polymerizations initiated by aromatic radical-anions such as sodium naphthalene [Szwarc, 1968, 1974, 1983]. Initiation proceeds by the prior formation of the active initiator, the naphthalene radical–anion (XVIII)

\[
\text{Na}^+ + \text{Na}^- \Xrightarrow{} \text{XVIII}
\]

The reaction involves the transfer of an electron from the alkali metal to naphthalene. The radical nature of the anion–radical has been established from electron spin resonance spectroscopy and the carbanion nature by their reaction with carbon dioxide to form the carboxylic acid derivative. The equilibrium in Eq. 5-65 depends on the electron affinity of the hydrocarbon and the donor properties of the solvent. Biphenyl is less useful than naphthalene since its equilibrium is far less toward the anion–radical than for naphthalene. Anthracene is also less useful even though it easily forms the anion–radical. The anthracene anion–radical is too stable to initiate polymerization. Polar solvents are needed to stabilize the anion–radical, primarily via solvation of the cation. Sodium naphthalene is formed quantitatively in tetrahydrofuran (THF), but dilution with hydrocarbons results in precipitation of sodium and regeneration of naphthalene. For the less electropositive alkaline-earth metals, an even more polar solvent than THF [e.g., hexamethylphosphoramide (HMPA)] is needed.

The naphthalene anion–radical (which is colored greenish-blue) transfers an electron to a monomer such as styrene to form the styryl radical–anion (XIX)

\[
\left[\begin{array}{c}
\text{Na}^+ \\
\text{Na}^+
\end{array}\right] + \Phi\text{CH}=\text{CH}_2 
\]

\[
\Xrightarrow{} \text{XIX}
\]

The styryl radical–anion is shown as a resonance hybrid of the forms wherein the anion and radical centers are alternately on the \(\alpha\)- and \(\beta\)-carbon atoms. The styryl radical–anion dimerizes to form the dicarbanion (XX)

\[
2 [\Phi\text{CH}^-\text{CH}_2] \Xrightarrow{} \Phi\text{CH}^-\text{CH}_2\text{Na}^+ \Xrightarrow{} \text{XX}
\]
That this reaction occurs is shown by electron spin resonance measurements, which indicate
the complete disappearance of radicals in the system immediately after the addition
of monomer. The dimerization occurs to form the styryl dicarbanion instead of
\[ \text{C} - \text{CH}_2 - \text{CH} - \text{C}^\cdot \]
since the former is much more stable. The styryl dianions so-formed
are colored red (the same as styryl monocarbanions formed via initiators such as \text{n-butyl-lithium}). Anionic propagation occurs at both carbanion ends of the styryl dianion

\[
\text{Na}^+ \left[ \begin{array}{c}
\phi \\
H
\end{array} \right] \text{C} - \text{CH}_2 - \text{CH}_2 - \text{C}^\cdot \\
\text{Na}^+ + (n + m) \phi \text{CH} = \text{CH}_2 \rightarrow
\]

Although the suggestion that the styryl anion–radical adds a few monomer molecules prior to
dimerization has not been discounted, the reaction kinetics clearly show that better than 99%
of the propagation occurs through the dianion. Dimerization of radical centers is highly
favored by their high concentrations, typical \(10^{-3} - 10^{-2} \text{ M}\) (much higher than in a radical
polymerization) and the larger rate constants (\(10^6 - 10^8\ \text{L mol}^{-1} \text{ s}^{-1}\)) for radical coupling
[Wang et al., 1978, 1979].

Electron-transfer initiation from other radical-anions, such as those formed by reaction of
sodium with nonenolizable ketones, azomethines, nitriles, azo and azoxy compounds, has also
been studied. In addition to radical–anions, initiation by electron transfer has been observed
when one uses certain alkali metals in liquid ammonia. Polymerizations initiated by alkali
metals in liquid ammonia proceed by two different mechanisms. In some systems, such as the
polymerizations of styrene and methacrylonitrile by potassium, the initiation is due to amide
ion formed in the system [Overberger et al., 1960]. Such polymerizations are analogous to
those initiated by alkali amides. Polymerization in other systems cannot be due to amide ion.
Thus, polymerization of methacrylonitrile by lithium in liquid ammonia proceeds at a much
faster rate than that initiated by lithium amide in liquid ammonia [Overberger et al., 1959].
The mechanism of polymerization is considered to involve the formation of a \textit{solvated electron}:

\[
\text{Li} + \text{NH}_3 \rightarrow \text{Li}^+ (\text{NH}_3) + e^- (\text{NH}_3)
\]  

(5-69)

Such ammonia solutions are noted by their characteristic deep blue color. The solvated
electron is then transferred to the monomer to form a radical–anion,

\[
e^- (\text{NH}_3) + \text{CH}_3\equiv\text{CH}Y \rightarrow \left[ \dot{\text{CH}}_2\equiv\dot{\text{CH}}Y \leftrightarrow \dot{\text{CH}}_2\equiv\dot{\text{CH}}Y \right] (\text{NH}_3)
\]  

(5-70)

The radical–anion proceeds to propagate in the same manner as discussed above for initiation
by sodium naphthalene. (Polymerizations in liquid ammonia are very different from those in
organic solvents in that free ions probably constitute the major portion of propagating
species.)

Electron-transfer initiation also occurs in heterogeneous polymerizations involving dis-
persions of an alkali metal in monomer. Initiation involves electron transfer from the metal
to monomer followed by dimerization of the monomer radical–anion to form the propagating
dianion [Fontanille, 1989; Gaylord and Dixit, 1974; Morton and Fetters, 1977]. The rate of initiation is dependent on the surface area of the metal since the reaction is heterogeneous. Increased surface area of metal is achieved by condensing metal vapors directly into a reaction mixture or as a thin coating (mirror) of the metal on the inside walls of the reaction vessel or simply using small particle size of the metal.

Initiation by ionizing radiation occurs by electron transfer. Some component of the reaction system, either the solvent or monomer, undergoes radiolysis to yield a cation–radical and solvated electron [Stannett et al., 1989]. If a monomer with an electron-withdrawing substituent is present, polymerization occurs by addition of the electron to monomer followed by dimerization to the dicarbanion and propagation (Sec. 5-2a-6).

Electroinitiated polymerization proceeds by direct electron addition to monomer to generate the monomer anion–radical, although initiation in some systems may involve the formation of an anionic species by electrolytic reaction of some component of the reaction system (often the electrolyte) [Olaj, 1987].

5-3b Termination

5-3b-1 Polymerizations without Termination

Termination of a propagating carbanion by combination with the counterion occurs in only a few instances, such as in electroinitiated polymerization when the contents of the anode and cathode chambers are mixed and in initiation by ionizing radiation. Termination by combination of the anion with a metal counterion does not take place. Many anionic polymerizations, especially of nonpolar monomers such as styrene and 1,3-butadiene, take place under conditions in which there are no effective termination reactions. Propagation occurs with complete consumption of monomer to form living polymers. The propagating anionic centers remain intact because transfer of proton or other positive species from the solvent does not occur. Living polymers are produced as long as one employs solvents, such as benzene, tetrahydrofuran, and 1,2-dimethoxyethane, which are relatively inactive in chain transfer with carbanions. The polymerization of styrene by amide ion in liquid ammonia, one of the first anionic systems to be studied in detail, is one of the few anionic polymerizations where chain transfer to solvent is extensive [Higginson and Wooding, 1952].

The nonterminating character of living anionic polymerization (LAP) is apparent in several different ways. Many of the propagating carbanions are colored. If a reaction system is highly purified so that impurities are absent, the color of the carbanions is observed to persist throughout the polymerization and does not disappear or change at 100% conversion. Further, after 100% conversion is reached, additional polymerization can be effected by adding more monomer, either the same monomer or a different monomer. The added monomer is also polymerized quantitatively and the molecular weight of the living polymer is increased.

5-3b-2 Termination by Impurities and Deliberately Added Transfer Agents

Most anionic (as well as cationic) polymerizations are carried out in an inert atmosphere with rigorously cleaned reagents and glassware since trace impurities lead to termination [Hadjichristidis et al., 2000]. Moisture absorbed on the surface of glassware is usually removed by

\[
S \rightarrow S^+ + \epsilon_{\text{solv}} \tag{5-71}
\]
flaming under vacuum or washing with a living polymer solution. Oxygen and carbon di-
oxide from the atmosphere add to propagating carbanions to form peroxy and carboxyl
anions. These are normally not reactive enough to continue propagation. (The peroxy and
carboxyl anions usually are finally obtained as HO and HOOC groups when a proton donor
is subsequently added to the polymerization system.) Any moisture present terminates prop-
gagating carbanions by proton transfer:

\[
\begin{align*}
\phi \text{CH}_2 \text{C}^- \text{H} & + \text{H}_2\text{O} \rightarrow \phi \text{CH}_2 \text{CH}^- + \text{HO}^- \\
\end{align*}
\tag{5-72}
\]

The hydroxide ion is usually not sufficiently nucleophilic to reinitiate polymerization and the
kinetic chain is broken. Water has an especially negative effect on polymerization, since it is
an active chain-transfer agent. For example, \( C_{r,S} \) is approximately 10 in the polymerization
of styrene at 25°C with sodium naphthalene [Szwarc, 1960], and the presence of even small
concentrations of water can greatly limit the polymer molecular weight and polymerization
rate. The adventitious presence of other proton donors may not be as much of a problem.
Ethanol has a transfer constant of about \( 10^{-3} \). Its presence in small amounts would not pre-
vent the formation of high polymer because transfer would be slow, although the polymer
would not be living.

Living polymers are terminated by the deliberate addition of chain-transfer agent such as
water or alcohol to the reaction system after all of the monomer has reacted.

### 5-3b-3 Spontaneous Termination

Living polymers do not live forever. In the absence of terminating agents the concentration of
carbanion centers decays with time [Fontanille, 1989; Glasse, 1983; Wietelmann and Bauer,
2002]. Polystyryl carbanions are the most stable of living anionic systems; they are stable for
weeks in hydrocarbyl solvents. Stability is enhanced by storage below 0°C. (This is much
more stable than any of the living cationic systems; see Sec. 5-2g-3.) The mechanism for the
decay of polystyryl carbanions, referred to as spontaneous termination, is based on spectro-
scopy of the reaction system and final polymer after treatment with water and consists of

\[
\begin{align*}
\phi \text{CH}_2\text{CH}^-\text{CH} \rightarrow \phi \text{CH}_2\text{CH}^=\text{CH}^- + \text{H}^+ \text{Na}^- \\
\end{align*}
\tag{5-73}
\]

hydride elimination (Eq. 5-73) followed by abstraction of an allylic hydrogen from XXI
by a carbanion center to yield the unreactive 1,3-diphenylallyl anion (XXII) [Spach et al.,
1962]. The sodium hydride eliminated in Reaction 5-73 may also participate in hydrogen
abstraction from XXI. The order of stability of polystyryl carbanions depends on the alkali
metal in the order K > Na > Li.
The stability of polystyryl carbanions is greatly decreased in polar solvents such as ethers. In addition to hydride elimination, termination in ether solvents proceeds by nucleophilic displacement at the C–O bond of the ether. The decomposition rate of polystyryllithium in THF at 20°C is a few percent per minute, but stability is significantly enhanced by using temperatures below 0°C [Quirk, 2002]. Keep in mind that the stability of polymeric carbanions in the presence of monomers is usually sufficient to synthesize block copolymers because propagation rates are high. The living polymers of 1,3-butadiene and isoprene decay faster than do polystyryl carbanions.

5-3b-4 Termination and Side Reactions of Polar Monomers

Polar monomers, such as methyl (meth)acrylate, methyl vinyl ketone, and acrylonitrile, are more reactive than styrene and 1,3-dienes because the polar substituent stabilizes the carbanion propagating center by resonance interaction to form the enolate anion. However, the polymerizations are more complicated than those of the nonpolar monomers because the polar substituents (ester, ketone, nitrile) are reactive toward nucleophiles. This leads to termination and side reactions competitive with both initiation and propagation, resulting in complex polymer structures and major difficulties in achieving living polymerizations [Bywater, 1975, 1985; Hogen-Esch and Smid, 1987; Muller et al., 1986; Quirk, 1995, 1998, 2002; Vleck and Lochmann, 1999; Warzelhan et al., 1978; Zune and Jerome, 1999].

Several different nucleophilic substitution reactions have been observed in the polymerization of methyl methacrylate. Attack of initiator on monomer converts the active alkyl-lithium to the less active alkoxide initiator (Eq. 5-75). Further, methyl methacrylate (MMA) is converted to isopropenyl alkyl ketone to the extent that this reaction occurs.

\[
\begin{align*}
\text{CH}_3\text{O} & \\
\text{CH}_2=\text{C}=\text{C}=\text{OCH}_3 + \text{R}^+\text{Li}^+ & \rightarrow & \text{CH}_3\text{O} & \\
& & & \text{CH}_2=\text{C}=\text{C}=\text{R} + \text{CH}_3\text{O}^-\text{Li}^+ \\
\end{align*}
\]

(5-75)

The resulting polymerization is a copolymerization between the two monomers, not a homopolymerization of MMA. More importantly, this results in a slower reaction (and lower polymer molecular weight) since the carbanion derived from the ketone is not as reactive as the carbanion from MMA. Nucleophilic substitution by intramolecular backbiting attack of a propagating carbanion lowers the polymer molecular weight and decreases the polymerization rate since methoxide is a weak initiator. Other reactions have been proposed—nucleophilic attack by a propagating carbanion on monomer to displace methoxide and yield a polymer with an isopropenyl keto end group and the intermolecular analog of Reaction 5-76.

\[
\begin{align*}
\begin{array}{c}
\text{CH}_3\text{O} \\
\text{CH}_2=\text{C}=\text{C}=\text{OCH}_3 \\
\text{CH}_3\text{O} \\
\end{array} & \rightarrow & \begin{array}{c}
\text{CH}_3\text{O} \\
\text{CH}_2=\text{C}=\text{C}=\text{R} \\
\text{CH}_3\text{O}^- \\
\end{array} \\
\end{align*}
\]

(5-76)
to yield branched polymer. Acrylate monomers have an additional side reaction—abstraction of the α-hydrogen of monomer by the initiator.

The effort to minimize side reactions and achieve polymers with controlled structures as well as living anionic polymerization (LAP) has involved control of temperature, solvent, and the addition of ligands [Baskaran, 2003]. Side reactions are minimized by altering the reactivities of the propagating species (free ions and/or ion pairs) so that there is greater selectivity in favor of normal propagation. To achieve LAP with narrow PDI requires fast initiation and fast exchange among free-ion- and ion-pair-propagating species and dormant (and associated) covalent species. The side reactions predominate over normal polymerization in hydrocarbon solvents, yielding nonliving polymerization with lowered polymerization rate and polymer molecular weight. Reaction 5-75 is the major reaction when n-butyllithium is the initiator. Less than 1% of the initiator results in high-molecular-weight polymer in the polymerization of MMA in toluene at room temperature. Lower temperature has some effect, but even at −78°C half of the initiator attacks the carbonyl carbon to produce lithium methoxide. Reaction 5-75 can be significantly minimized but not completely eliminated by using a sterically hindered, less nucleophilic initiator such as 1,1-diphenylhexyllithium, cumyllithium, or polystyryl carbanions to which a few units of α-methylstyrene have been added [Wiles and Bywater, 1965]. However, Reaction 5-75 as well as the other side reactions are sufficiently minimized to achieve living anionic polymerization (LAP) of methacrylates, but not acrylates, by using the less nucleophilic initiator in a polar solvent such as THF at low temperatures (−20°C to −70°C).

A major strategy for achieving LAP of methacrylates and acrylates is via ligated anionic polymerization, which uses ligands to enhance the reactivity of the propagating species and the equilibria among the different active and dormant species [Fayt et al., 1987; Jerome et al., 1999; Quirk, 2002; Teyssie et al., 1990; Varshney et al., 1990; Vleck and Lochmann, 1999; Wang et al., 1995; Zune and Jerome, 1999]. Efficient ligands include metal alkoxides (LiOR), inorganic salts (LiCl), aluminium alkyls (R₃Al), and crown ethers. The ligand alters the propagating species by coordinating with either the propagating anionic center or its counterion. Some ligands such as polyether metal alkoxides [e.g., lithium 2-(2-methoxyethoxy) ethoxide] coordinate with both the anionic center and counterion. The use of appropriate ligands facilitates living anionic polymerizations of methacrylates and hindered acrylates (e.g., t-butyl acrylate) with high rates and molecular weights, narrow PDI, and the absence of side reactions at moderate temperatures (near 0°C or even higher) and even in toluene. Unhindered acrylates such as methyl acrylate are more difficult to control. LAP is achieved only at lower temperatures, usually −78°C, and often only in polar solvents.

Aluminum porphyrins (Z = Cl, OR, SR) also initiate living polymerizations of methacrylates and acrylates without the need for low temperatures [Aida and Inoue, 1996; Inoue, 2000;
Inoue et al., 1990; Sugimoto and Inoue, 1999. Polymerizations with narrow molecular weight distribution are achieved at temperatures as high as 35°C in methylene chloride. The polymerization rates are low unless a Lewis acid is present together with the aluminum porphyrin. The Lewis acid coordinates with the carbonyl group of the monomer, which results in suppression of the side reactions as well as activation of the carbon–carbon double bond to nucleophilic attack by the initiator. The Lewis acid must be sterically hindered to prevent attack by the nucleophilic initiator on the carbonyl group. Thus, aluminum ortho-substituted phenolates such as methylaluminum bis(2,6-di-t-butyl-4-methylphenolate) accelerate the polymerization by factors up to $10^3$–$10^4$ even at room temperature while maintaining the living character of the reaction. Less sterically hindered Lewis acids, including the aluminum phenolates without ortho substituents, result in loss of the living character and even complete lack of polymerization, unless the reaction temperature is lowered to about $-40^\circ$C. Steric crowding between the porphyrin structure and the Lewis acid is the key to minimizing side reactions and allowing living polymerization to proceed. The aluminum propyrin initiators are discussed further in Sec. 7-2a-1.

Polymerizations of vinyl ketones such as methyl vinyl ketone are also complicated by nucleophilic attack of the initiator and propagating carbanion at the carbonyl group although few details have been established [Dotcheva and Tsvetanov, 1985; Hrdlovic et al., 1979; Nasrallah and Baylouzian, 1977]. Nucleophilic attack in these polymers results in addition, while that at the ester carbonyl of acrylates and methacrylates yields substitution. The major side reaction is an intramolecular aldol-type condensation. Abstraction of an $\alpha$-hydrogen from a methyl group of the polymer by either initiator or propagating carbanion yields an $\alpha$-carbanion that attacks the carbonyl group of the adjacent repeat unit.

$$\overset{\sim}{\overset{\sim}{\text{CH}}}_2\text{CHCH}_2\text{CHCH}_2\overset{\sim}{\sim}\overset{\sim}{\sim}\text{O}=\overset{\sim}{\sim}\overset{\sim}{\sim}\overset{\sim}{\sim}\frac{\text{CH}_3}{\text{CO}}\overset{\sim}{\sim}\overset{\sim}{\sim}\overset{\sim}{\sim}\text{CH}_3\overset{\sim}{\sim}\overset{\sim}{\sim}\overset{\sim}{\sim}\overset{\sim}{\sim}\text{O}$$

Acrylonitrile polymerization is similarly complicated by addition reactions of the initiator and/or propagating nucleophiles with the nitrile group [Berger and Adler, 1986; Tsvetanov, 1979; Vankerckhoven and Van Beylen, 1978].

### 5-3c Group Transfer Polymerization

Group transfer polymerization offers another route to LAP of (meth)acrylates without resorting to low temperatures [Hertler, 1994, 1996; Muller, 1990; Quirk et al., 1993; Reetz, 1988; Schubert and Bandermann, 1989, Sogah et al., 1987, 1990; Webster, 1987, 1992, 2000]. The initiator is a silyl ketene acetal (XXIV) that is synthesized from an ester enolate:

$$\overset{\sim}{\overset{\sim}{\text{Me}}}_2\text{CHCOOMe} \xrightarrow{\text{OMe}} \overset{\sim}{\overset{\sim}{\text{Me}}}_2\text{C}=\overset{\sim}{\sim}\overset{\sim}{\sim}\overset{\sim}{\sim}\frac{\text{Me}}{\text{OLi}}\overset{\sim}{\sim}\overset{\sim}{\sim}\overset{\sim}{\sim}\text{OMe} \xrightarrow{\text{Me}_{2}\text{SiCl}} \overset{\sim}{\overset{\sim}{\text{Me}}}_2\text{C}=\overset{\sim}{\sim}\overset{\sim}{\sim}\overset{\sim}{\sim}\frac{\text{Me}}{\text{OSiMe}}_3$$

Group transfer polymerization (GTP) requires either a nucleophilic or Lewis acid catalyst. Bifluoride ($\text{HF}_2^-$) and fluoride ions, supplied by soluble reagents such as tris(dimethylamino)-sulfonium bifluoride, $[(\text{CH}_3)_3\text{N}]_3\text{HF}_2^-$, and $(n-\text{C}_4\text{H}_9)_4\text{NF}$, are the most effective nucleophilic catalysts, although other nucleophiles (CN$^-$, acetate, $p$-nitrophenolate) are also useful. Zinc
chloride, bromide, and iodide, and dialkylaluminum chloride have been used as Lewis acid (electrophilic) catalysts. Nucleophilic catalysts are effective at low concentrations (often 0.1 mol% relative to initiator). Much higher concentrations of Lewis acid catalysts are needed, 10 mol% or higher and this greatly limits the practical utility of electrophilic GTP. GTP requires the absence of materials such as water with active hydrogens, although GTP is not as sensitive to water as traditional anionic polymerization. Oxygen does not interfere with GTP. The range of solvents suitable for GTP is wider than for other anionic polymerizations. \(N, N\)-Dimethylformamide has been used with nucleophilic GTP, and chlorinated hydrocarbons as well as acetonitrile for electrophilic GTP, although ethers such as THF and aromatics such as toluene are the most commonly used solvents.

The mechanisms for nucleophilic GTP and electrophilic GTP are not the same. Electrophilic GTP proceeds by an associative or concerted mechanism that does not involve anionic propagating centers. Initiation involves a concerted addition of methyl trimethylsilyl dimethyl ketene acetal to monomer to form species XXV. The overall effect is to transfer the silyl ketene acetal center from initiator to monomer. Propagation proceeds in a similar manner, with the ketene acetal double bond acting as the propagating center. Both initiation and propagation involve nucleophilic attack of the \(\pi\)-electrons of the ketene acetal on monomer. Electrophilic catalysts probably function by coordination with the carbonyl oxygen of monomer to increase the electrophilicity of the double bond, rendering it more prone to nucleophilic attack.

Nucleophilic GTP proceeds by a dissociative mechanism in which the propagating centers are ionic—similar to other anionic polymerizations [Hertler, 1994, 1996; Quirk and Bidinger, 1989; Quirk et al., 1993; Webster, 1992, 2000]. The anionic propagating species XXVII is generated in low concentrations by nucleophilic displacement of the trimethylsilyl group by the nucleophilic catalyst (\(W^+\text{Nu}^-\)):
Control of the side reactions is achieved through two factors: (1) reversible complexation of the anionic propagating species XXVII by the silyl ketene acetal polymer chain ends XXVI maintains the concentration of the anionic propagating species at a low concentration; and (2) the bulky counterion $W^+$ (e.g., tetra-$n$-butylammonium, tris(dimethylamino)sulfonium) decreases the reactivity of the anionic propagating centers toward the terminating side reactions.

Living polymerizations of methacrylates with narrow PDI, generally 1.2–1.3 with some lower, are achieved by nucleophilic (dissociative) GTP at temperatures of 0–80°C. However, the maximum molecular weights that can be achieved with narrow PDI are limited to about 20,000–30,000. Two factors limit the molecular weights—termination by cyclization (Eq. 5-76), although suppressed, is always present and by complexation of silyl ketene acetal ended polymer. GTP of acrylates is not as successful. Lower temperatures are required and there is substantial PDI broadening even at 0°C. Better results for acrylates are achieved by electrophilic (associative) GTP using HgCl$_2$ and trimethylsilyl iodide at 20°C [Zhuang and Muller, 1995].

A variation of GTP, referred to as *aldol GTP*, involves polymerization of a silyl vinyl ether initiated by an aldehyde [Sogah and Webster, 1986; Webster, 1987]. Both initiation and propagation involve nucleophilic addition of the vinyl ether to the aldehyde carbonyl group with transfer of the trialkyl silyl group from vinyl ether to the carbonyl oxygen (Eq. 5-82). The reaction has similar characteristics as GTP. The product is a silated poly(vinyl alcohol) (PVA), which can be hydrolyzed by acid to PVA (Eq. 5-83).

\[
\begin{align*}
\phi \text{CH} + \text{CH}_2=\text{CH}^-\text{OSiR}_3 & \rightarrow \phi \text{C}^-\text{CH}_2=\text{CH}^-\text{OSiR}_3 \\
\phi \text{C}^-\text{CH}_2=\text{CH}^-\text{OSiR}_3 & \rightarrow \phi \text{C}^-\text{CH}_2=\text{CH}_2\text{OH}^-\text{OSiR}_3 \\
\phi \text{C}^-\text{CH}_2=\text{CH}_2\text{OH}^-\text{OSiR}_3 & \rightarrow \phi \text{C}^-\text{CH}_2=\text{CH}_2\text{OH}
\end{align*}
\]

(5-82) (5-83)

### 5-3d Kinetics of Living Polymerization

#### 5-3d-1 Polymerization Rate

The rate of polymerization in nonterminating systems can be expressed as the rate of propagation

\[
R_p = k_p^{app}[M^-][M]
\]

(5-84)

where $[M^-]$ is the total concentration of all types of living anionic propagating centers (free ions and ion pairs). $[M^-]$ can be determined by reacting the living polymer with a terminating agent such as methyl iodide, carbon dioxide, or other electrophilic substance followed by analysis of the amount of terminating agent incorporated into the polymer. The use of
isotopically labeled terminating agents can increase the analytical sensitivity. Ultraviolet-visible and NMR spectroscopy are also useful for determining the total concentration of propagating species. Since free ions constitute a very small percentage of \([M^-]/C_0\) for most systems, equating the concentration of ion pairs with \([M^-]/C_0\) may not introduce a significant error. The living ends are monoanions in polymerizations initiated by butyllithium and similar initiators and dianions in polymerizations initiated by electron transfer. The two types of anions are referred to as one-ended (monofunctional) and two-ended (bifunctional) living anions.

Equation 5-84 applies for the case where initiation is rapid relative to propagation. This condition is met for polymerizations in polar solvents. However, polymerizations in nonpolar solvent frequently proceed with an initiation rate that is of the same order of magnitude as or lower than propagation. More complex kinetic expressions analogous to those developed for radical and nonliving cationic polymerizations apply for such systems [Pepper, 1980; Szwarc et al., 1987].

As with certain cationic systems, many anionic living polymerizations proceed too rapidly to be followed by techniques such as dilatometry. The stopped-flow technique (Sec. 5-2e-1) is useful for studying these fast polymerizations. Ultraviolet-visible spectroscopy of the rapidly mixed reaction system contained in a capillary tube allows one to follow the initiation rate (observing the increase in optical density of propagating species) and/or the polymerization rate (by following loss of monomer). The polymerization rate can also be obtained by a modification of the apparatus in which polymerization is stopped by running the contents of the capillary tube into a solvent containing a terminating agent. The reaction time is given by the ratio of the capillary volume to the flow rate. Short reaction times of 0.005–2 s can be accurately studied in this manner. The conversion and, hence, \(R_p\) and apparent propagation rate constant are obtained by analyzing the quenched reaction mixture for either polymer or unreacted monomer.

It is useful to understand the reasons for the faster reaction rates encountered in many anionic polymerizations compared to their radical counterparts. This can be done by comparing the kinetic parameters in appropriate rate equations: Eq. 3-22 for radical polymerization and Eq. 5-84 for anionic polymerization. The \(k_p\) values in radical polymerization are similar to the \(k_{app}^p\) values in anionic polymerization. Anionic \(k_{app}^p\) values may be 10–100-fold lower than in radical polymerization for polymerization in hydrocarbon solvents, while they may be 10–100-fold higher for polymerizations in ether solvents. The major difference in the rates of anionic and radical polymerizations resides in the lack of termination in anionic polymerization and the larger difference in the concentrations of the propagating species. The concentration of propagating radicals is \(10^{-9}–10^{-7}\ \text{M}\), while that for propagating anions is often as high as \(10^{-4}–10^{-2}\ \text{M}\). Thus anionic polymerization rates are much higher than radical rates based only on the concentrations of propagating species.

5-3d-2 Effects of Reaction Media

The propagation rate constant and the polymerization rate for anionic polymerization are dramatically affected by the nature of both the solvent and the counterion. Thus the data in Table 5-10 show the pronounced effect of solvent in the polymerization of styrene by sodium naphthalene \((3 \times 10^{-3}\ \text{M})\) at \(25^\circ\text{C}\). The apparent propagation rate constant is increased by 2 and 3 orders of magnitude in tetrahydrofuran and 1,2-dimethoxyethane, respectively, compared to the rate constants in benzene and dioxane. The polymerization is much faster in the more polar solvents. That the dielectric constant is not a quantitative measure of solvating power is shown by the higher rate in 1,2-dimethoxyethane (DME) compared to tetrahydrofuran (THF). The faster rate in DME may be due to a specific solvation effect arising from the presence of two ether functions in the same molecule.
The increase in $k_{app}^p$ with increased solvating power of the reaction medium is due mainly to the increased fraction of free ions present relative to ion pairs. It would be more informative to obtain the individual propagation rate constants for the free ions and ion pairs as well as the relative amounts of the two types of propagating species.

### 5-3d-2-a Evaluation of Individual Propagation Rate Constants for Free Ions and Ion Pairs

The rate of polymerization is appropriately expressed as the sum of the rates for the free propagating anion $P^-$ and the ion pair $P^- (C^+)$:

$$ R_p = k_p^- [P^-][M] + k_p^+ [P^- (C^+)][M] \quad (5-85) $$

where $k_p^-$ and $k_p^+$ are the propagation rate constants for the free ion and ion pair, respectively, $[P^-]$ and $[P^- (C^+)]$ are the concentrations of the free ion and ion pair, and $[M]$ is the monomer concentration. $C^+$ in the above notation is the positive counterion. Comparison of Eqs. 5-84 and 5-85 yields the apparent $k_p$ as

$$ k_{app}^p = \frac{k_p^- [P^-] + k_p^+ [P^- (C^+)]}{[M]} \quad (5-86) $$

The two propagating species are in equilibrium according to

$$ P^-(C^+) \overset{K}{\underset{}{\rightleftharpoons}} P^- + C^+ \quad (5-87) $$

governed by the dissociation constant $K$ given by

$$ K = \frac{[P^-][C^+]}{[P^- (C^+)]} \quad (5-88) $$

For the case where $[P^-] = [C^+]$, that is, there is no source of either ion other than $P^- (C^+)$, the concentration of free ions is

$$ [P^-] = (K[P^- (C^+)])^{1/2} \quad (5-89) $$

The extent of dissociation is small under most conditions, the concentration of ion pairs is close to the total concentration of living ends and Eq. 5-89 can be rewritten as

$$ [P^-] = (K[M^-])^{1/2} \quad (5-90) $$

### TABLE 5-10 Effect of Solvent on Anionic Polymerization of Styrene

<table>
<thead>
<tr>
<th>Solvent</th>
<th>Dielectric Constant (ε)</th>
<th>$k_{app}^p$ (L mol$^{-1}$ s$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Benzene</td>
<td>2.2</td>
<td>2</td>
</tr>
<tr>
<td>Dioxane</td>
<td>2.2</td>
<td>5</td>
</tr>
<tr>
<td>Tetrahydrofuran</td>
<td>7.6</td>
<td>550</td>
</tr>
<tr>
<td>1,2-Dimethoxyethane</td>
<td>5.5</td>
<td>3,800</td>
</tr>
</tbody>
</table>

aData from Szwarc and Smid [1964].
The concentration of ion pairs is given by

$$[P^- (C^+)] = [M^-] - (K[M^-])^{1/2}$$  (5-91)

Combination of Eqs. 5-86, 5-90, and 5-91 yields $k_{p\text{ app}}$ as a function of $[M^-]$:

$$k_{p\text{ app}} = k_p^\pm + \frac{(k_p^- - k_p^\pm)K^{1/2}}{[M^-]^{1/2}}$$  (5-92)

Polymerizations can also be carried out in the presence of excess counterion by adding a strongly dissociating salt (e.g., NaBF$_4$ to supply excess Na$^+$. The concentration of free ions, depressed by the common ion effect, is given by

$$[P^-] = \frac{K[M^-]}{[C^-]}$$  (5-93)

When the added salt is strongly dissociated and the ion pairs slightly dissociated, the counterion concentration is very close to that of the added salt [CZ]:

$$[C^-] \approx [CZ]$$  (5-94)

The concentrations of free anions and ion pairs are given by

$$[P^-] = \frac{K[M^-]}{[CZ]}$$  (5-95)
$$[P^- (C^+)] = [M^-] - \frac{K[M^-]}{[CZ]}$$  (5-96)

which are combined with Eq. 5-86 to yield

$$k_{p\text{ app}} = k_p^\pm + \frac{(k_p^- - k_p^\pm)K}{[CZ]}$$  (5-97)

Equations 5-92 and 5-97 allow one to obtain $k_p^-$, $k_p^\pm$, and $K$ from $k_{p\text{ app}}$ values obtained in the absence and presence of added common ion. A plot of $k_{p\text{ app}}$ obtained in the absence of added common ion versus $[M^-]^{1/2}$ yields a straight line whose slope and intercept are $(k_p^- - k_p^\pm)K^{1/2}$ and $k_p^\pm$, respectively. A plot of $k_{p\text{ app}}$ obtained in the presence of added common ion versus $[CZ]^{-1}$ yields a straight line whose slope and intercept are $(k_p^- - k_p^\pm)K$ and $k_p^\pm$, respectively. Figures 5-5 and 5-6 show these plots for polystyryl sodium in 3-methyltetrahydrofuran at 20°C. The combination of the two slopes and two intercepts allows the individual calculation of $k_p^-$, $k_p^\pm$, and $K$. [Note: $K$ as well as $[P^-]$ and $[P^- (C^+)]$ can also be independently determined from conductivity measurements.]

5-3d-2-b Reactivity in Anionic Polymerization. Table 5-11 shows the values of $K$ and the propagation rate constants for free ions and ion pairs in styrene polymerization in THF at 25°C with various alkali metal counterions [Bhattacharyya et al., 1965a,b]. The corresponding $k_p^\pm$ values in dioxane are also presented. The values of $K$ and $k_p^-$ in dioxane could not be obtained as conductivity measurements indicated no detectable dissociation of ion pairs to free ions in dioxane. A consideration of the data in Table 5-11 allows an understanding of reactivity in anionic polymerization. The polymerization data show the much greater reactivity of the free ion compared to any of the ion pairs. The value of $k_p^-$ is $6.5 \times 10^4$ L mol$^{-1}$ s$^{-1}$ which is larger by a factor of $10^5$–$10^3$ than the $k_p^\pm$ values. Similar
differences between $k_p^-$ and $k_p^+$ have been observed in polymerizations of methyl methacrylate (MMA), 2-vinylpyridine (2VP), and isoprene (IP) [Bywater, 1985; Jeuk and Muller, 1982; Van Beylen et al., 1988]. For reference, $k_p^-$ has values of $3.8 \times 10^3$, $1.0 \times 10^4$, and $2.0 \times 10^5$ L mol$^{-1}$ s$^{-1}$ for IP ($25^\circ$C), 2VP ($25^\circ$C), MMA ($-98^\circ$C), respectively, all measured in THF [Bywater, 1985].

Fig. 5-5  Polymerization of styrene by sodium naphthalene in 3-methyltetrahydrofuran at 20°C. After Schmitt and Schulz [1975] (by permission of Pergamon Press and Elsevier, Oxford).

Fig. 5-6  Polymerization of styrene by sodium naphthalene in 3-methyltetrahydrofuran at 20°C in the presence of sodium tetraphenylborate. After Schmitt and Schulz [1975] (by permission of Pergamon Press and Elsevier, Oxford).
The $K$ values in Table 5-11 indicate that increased solvating power affects the reaction rate primarily through an increase in the concentration of free ions. When lithium is the counterion, one calculates from the equilibrium constant that 1.5% of the propagating centers are free ions in THF (for a system where the total concentration of all propagating centers is $10^{-3} \ M$) compared to zero in dioxane. Since free ions are so much more reactive than ion pairs, their small concentration has a very large effect on the observed polymerization rate. The majority of the propagation is carried by free ions; only about 10% of the observed reaction rate is due to ion pairs. It is worth mentioning that $K$ values independently measured by conductivity are in excellent agreement with those obtained from the kinetic measurements. The $K$ values from conductivity are 1.9, 1.5, 0.7, and $0.028 \times 10^{−7}$, respectively, for lithium, sodium, potassium, and cesium counterions [Geacintov et al., 1962; Shimomura et al., 1967a,b; Szwarc, 1969]. Table 5-11 shows that the dissociation constant for the ion pair decreases in going from lithium to cesium as the counterion. The order of increasing $K$ is the order of increasing solvation of the counterion. The smaller Li$^+$ is solvated to the greater extent and the larger Cs$^+$ is the least solvated. The decrease in $K$ has a very significant effect on the overall polymerization, since there is a very significant change in the concentration of the highly reactive free ions. Thus the free-ion concentration for polystyryl cesium ($K = 0.02 \times 10^{-7}$) is less than 10% that of polystyryl lithium ($K = 10^{-7}$).

The reactivities of the various ion pairs also increase in the same order as the $K$ values: Li $>$ Cs. The fraction of the ion pairs that are of the solvent-separated type increases with increasing solvation of the counterion. Solvent-separated ion pairs are much more reactive than contact ion pairs (Sec. 5-3d-4). The lower values of $k_p$ in dioxane relative to THF are also a consequence of the presence of a smaller fraction of the more reactive solvent-separated ion pairs. The order of reactivity for the different ion pairs in dioxane is the reverse of that in tetrahydrofuran. Solvation is not important in dioxane. The ion pair with the highest reactivity is that with the weakest bond between the carbanion center and counterion. The bond strength decreases and reactivity increases with increasing size of counterion. However, the effect of increasing counterion size levels off after K$^+$ as $k_p^+$ is approximately the same for potassium, rubidium, and cesium. The effect of counterion on ion-pair reactivity is different for methyl methacrylate (MMA) compared to styrene. The value of $k_p^+$ is 1 for lithium counterion and 30–33 for the larger alkali metal counterions for polymerization in tetrahydrofuran at −98°C [Jeuk and Muller, 1982; Szwarc, 1983]. The difference between lithium counterion and the larger counterions for MMA in THF is similar to that observed for styrene in dioxane. These results have been interpreted as indicating the absence of solvation by THF.
for MMA polymerization due to the presence of intramolecular solvation. Intramolecular solvation involves electron donation from the carbonyl oxygen of the penultimate unit (i.e., the unit just before the end unit of the propagating chain) as shown in XXVIII [Kraft et al., 1978, 1980]. This additional binding of the counterion to the polymer accounts for the low dissociation constant \( K < 10^{-9} \) for polymethyl methacrylate and also poly(2-vinylpyridine) ion pairs [Tardi and Sigwalt, 1972; Van Beylen et al., 1988]. Intramolecular solvation in poly(2-vinylpyridine) involves electron donation from the nitrogen of a penultimate pyridine ring. This effect may also be responsible for the decrease in dissociation constant of the poly(2-vinylpyridine) ion pair with decreasing size of counterion in THF. Thus \( K \) is \( 1.1 \times 10^{-9} \), \( 2.5 \times 10^{-9} \), and \( 8.3 \times 10^{-10} \) for Cs\(^+\), K\(^+\), and Na\(^+\), respectively [Szwarc, 1983]. This is the reverse of the order observed for polystyryl ion pairs in THF. Apparently, smaller counterions “fit better” or “more tightly” into the intramolecular solvation sphere.

### 5-3d-3 Degree of Polymerization

The number-average degree of polymerization for a living anionic polymerization is the ratio of the concentration of reacted monomer to the concentration of living ends (Eq. 5-58). For the usual situation where all the initiator I is converted into propagating chain ends, Eq. 5-58 becomes

\[
\bar{X}_n = \frac{2p[M]_0}{[I]_0}
\]

or

\[
\bar{X}_n = \frac{p[M]_0}{[I]_0}
\]

depending on the mode of initiation. Equation 5-98 applies to polymerizations initiated by electron transfer since each final polymer molecule originates from two initiator molecules (e.g., one dianionic propagating species is formed from two sodium naphthalenes). Initiation processes other than electron transfer (e.g., alkyllithium) involve one polymer molecule per initiator molecule, and Eq. 5-99 is applicable. For polymerization involving dormant species in equilibrium with ions and ion pairs (e.g., GTP), \([I]_0\) is the sum of the concentrations of ion, ion pair, and dormant species.

Narrow molecular weight distributions are obtained for systems with fast initiation and efficient mixing in the absence of depropagation, termination, and transfer reaction (Eq. 3-230). PDI values below 1.1–1.2 are found for many living polymerizations. The living polymer technique offers a unique method of synthesizing standard polymer samples of known and well-defined molecular weights. Commercially available molecular weight standards are now
available for a number of polymers—polystyrene, polyisoprene, poly(α-methylstyrene), poly(2-vinylpyridine), poly(methyl methacrylate), polyisobutylene, and poly(tetrahydrofuran). All except the last two polymers are synthesized by living anionic polymerization. The last two are obtained by living cationic polymerization with ring-opening polymerization (Chap. 7) used for poly(tetrahydrofuran). These polymer standards are useful as calibration standards in molecular weight measurements by size exclusion chromatography, membrane and vapor pressure osmometry, and viscometry.

The occurrence of any termination, transfer or side reactions result in broadening of the molecular weight distribution. The termination reactions in methacrylate polymerizations (at other than low temperatures in polar solvents) and depropagation in α-methylstyrene polymerizations broaden PDI [Chaplin and Yaddheige, 1980; Malhotra et al., 1977; Malhotra, 1978]. Although the bulk of propagation is carried by a small fraction of the propagating species (i.e., the free ions), this does not significantly broaden the molecular weight distribution since the free ions and ion pairs are in rapid equilibrium. Each polymer chain propagates as both free ions and ion pairs over its lifetime and the average fractions of its lifetime spent as free ions and ion pairs are not too different than for any other propagating chain.

5-3d-4 Energetics: Solvent-Separated and Contact Ion Pairs

The data available on the temperature dependence of the rates of living polymerization show the experimental activation energy $E_R$ is generally relatively low and positive. One should note that $E_R$ for living polymerization is the activation energy for propagation. The polymerization rates are relatively insensitive to temperature but increase with increasing temperature. Furthermore, the activation energy varies considerably depending on the solvent employed in the polymerization as was the case for cationic polymerization. Thus the activation energy for propagation in the system styrene–sodium naphthalene is 37.6 kJ mol$^{-1}$ in dioxane and only 4.2 kJ mol$^{-1}$ in tetrahydrofuran [Allen et al., 1960; Geacintov et al., 1962; Stretch and Allen, 1961]. The molecular weight of the polymer produced in a nonterminating polymerization is unaffected by temperature if transfer agents are absent. The situation can be different if transfer agents are initially present.

Most of the activation energy data reported in the literature are apparent activation energies corresponding to the values for the apparent propagation rate constant. The effect of temperature on propagation is complex—temperature simultaneously affects the relative concentrations of free ions and ion pairs and the individual rate constants for the free ions and ion pairs. Temperature affects the rate constants $k_p^-$ and $k_p^+$ in the manner all rate constants are affected, increasing temperature increases the values of $k_p^-$ and $k_p^+$. However, the effect of temperature on the concentration of free ions relative to ion pairs is in the opposite direction. The change with temperature of the equilibrium constant for dissociation of ion pairs into free ions is given by the relationship

$$\ln K = -\frac{\Delta H}{RT} + \frac{\Delta S}{R}$$

(5-100)

where $\Delta H$ is negative and $K$ increases with decreasing temperature [Schmitt and Schultz, 1975; Shimomura et al., 1976b]. For example, $\Delta H$ is about $-37$ kJ mol$^{-1}$ for polystyryl sodium in tetrahydrofuran, which corresponds to an increase in $K$ by a factor of about 300 as the temperature changes from 25 to $-70^\circ$C. The free-ion concentration is higher by a factor of about 20 at $-70^\circ$C compared to 25°C for a living end concentration of $10^{-3} \text{ M}$. The
change in $K$ with temperature is less for polystyryl cesium as $\Delta H$ is about $-8$ kJ mol$^{-1}$. The opposing effects of temperature on $K$ and on the propagation rate constants results in apparent activation energies that are often low. Apparent activation energies for propagation in poorer solvating media will be higher than those in better solvating media. Little ionization to free ions takes place in the former and temperature has little effect on $K$. Significant ionization occurs in better solvents, $K$ changes considerably with temperature, and the effect of $T$ on $K$ may come close to offsetting its effects on $k_p^-$ and $k_p^+$. This clearly is the reason why the apparent activation energy for polystyryl sodium is 37.6 kJ mol$^{-1}$ in dioxane but only $4.2$ kJ mol$^{-1}$ in tetrahydrofuran. Similarly, the effect of $T$ on $K$ in more polar solvents is greater for the smaller, better-solvated ions (Na$^+$) compared to the larger, more poorly solvated ions (Cs$^+$).

Evaluation of $k_p^-$ and $k_p^+$ and the corresponding activation parameters has been carried out for polystyryl sodium and cesium in several different ether solvents (THF, tetrahydropyran, 1,2-dimethoxyethane) [Muller, 1989; Schmitt and Schulz, 1975; Smid, 2000; Szwarz, 1968, 1974, 1983]. $k_p^-$ is independent of counterion, indicating that the observed value is for the free ion. Further, $k_p^-$ is independent of the solvent, although one expects a decrease in the rate constant with increasing solvating power for reaction between an ionic species and a neutral molecule (Sec. 5-2f-2). Apparently, the range of solvents studied (various ethers) did not contain a large enough difference in solvating power to observe the expected effect even though there was a significant variation in the dielectric constants of the ethers. The various ethers are assumed to be similar in their specific solvation of the free anionic propagating centers. (One should keep in mind that the range of solvents appropriate to anionic polymerization is quite limited—mostly hydrocarbons and ethers.) The activation energy $E_p^-$ and the frequency factor $A_p^-$ for the free ion are 16.7 kJ mol$^{-1}$ and $10^9$ L mol$^{-1}$ s$^{-1}$, respectively. It is useful to note that the propagation rate constant for the free polystyryl anion ($k_p^-\approx 10^5$) is larger than that for the free radical (165 L mol$^{-1}$ s$^{-1}$) by three orders of magnitude. Propagation by the anion is favored by both a lower activation energy and a higher frequency factor ($E_p^-=26$ and $A_p^-=4.5\times 10^6$ for radical propagation). The lower activation energy for anionic propagation is reasonable, since the interaction between anion and monomer should generate attractive forces (due to polarization) that reduce the potential-energy barrier to addition. The more favorable frequency factor results from a decrease in order of the surrounding reaction medium when the negative charge of the propagating anion is dispersed in the transition state. From Table 5-3 we can note that the propagation rate constant for the free polystyryl carbocation is larger than for the carbanion by factor of 10–100 as expected. Carbocation addition involves the use of vacant orbitals of the cabocation, while anionic propagation requires the use of antibonding orbitals, since all bonding orbitals on both monomer and carbanion are filled.

The calculation of $k_p^+$ and the corresponding activation parameter $E_p^+$ and $A_p^+$ proceeds in a reasonably straightforward manner for polymerizations in solvents of low polarity (no higher than dioxane). However, anomalous behavior is observed for polymerizations in solvents which are better solvating media than dioxane. $k_p^+$ is observed to increase with decreasing temperature in some systems, leading to negative activation energies. The activation energy for propagation by polystyryl sodium ion pairs in tetrahydrofuran is $-6.2$ kJ mol$^{-1}$ over the temperature range $-80$ to $25^\circ$C [Shimomura et al., 1967a,b]. $E_p^+$ for poly($\alpha$-methylstyryl) sodium in THF is $-8.8$ kJ mol$^{-1}$ over the range $-25$ to $5^\circ$C [Hui and Ong, 1976]. More significantly, experiments carried out over a sufficiently wide temperature range showed that $E_p^+$ changed sign with temperature. Figure 5-7 shows the Arrhenius plot of $k_p^+$ versus $1/T$ for polystyryl sodium in tetrahydrofuran and 3-methyltetrahydrofuran [Schmitt and Schulz, 1975]. The plots are S-shaped with two inflection points. These anomalous results.
indicate that two different types of ion pairs are present and undergoing propagation, the contact ion pairs and solvent-separated ion pairs.

The observed ion-pair propagation constant \( k_p^\pm \) is an apparent rate constant. \( k_p^\pm \) is a composite of the rate constants for the contact ion pair \( k_c \) and solvent-separated ion pair \( k_s \) according to

\[
k_p^\pm = xk_c + (1-x)k_s
\]

or

\[
k_p^\pm = \frac{(k_c + k_sK_{cs})}{(1 + K_{cs})}
\]

where \( x \) and \( 1-x \) are the fractions of solvent-separated and contact ion pairs, respectively, and \( K_{cs} \) is the equilibrium constant for interconversion between the two types of ion pairs:

\[
\begin{array}{c}
\text{\( \longrightarrow \)} P^- (C^+) \quad \overset{k_{cs}}{\longrightarrow} \quad \text{\( \longrightarrow \)} P^- || C^+
\end{array}
\]
The variation of $k_p^\pm$ with temperature depends on the interplay of the separate variations of $k_c$, $k_s$, and $K_{cs}$ on temperature according to

$$\ln k_c = \ln A_c - \frac{E_c}{RT}$$  \hspace{1cm} (5-104)

$$\ln k_s = \ln A_s - \frac{E_s}{RT}$$  \hspace{1cm} (5-105)

$$\ln K_{cs} = -\frac{\Delta H_{cs}}{RT} + \frac{\Delta S_{cs}}{R}$$  \hspace{1cm} (5-106)

A consideration of Eqs. 5-101, 5-102, and 5-104 to 5-106 indicates the reasons for the behavior observed in Fig. 5-7. There are no solvent-separated ion pairs at the highest temperature ($\sim$70°C in THF). Decreasing temperature decreases $k_p^\pm$ because $k_c$ is decreasing. As the temperature continues to decrease, a temperature is reached at which solvent-separated ion pairs are formed. Since $k_s > k_c$, $k_p^\pm$ goes through a minimum (at $\sim$30°C), and then increases (provided $E_s < -\Delta H_{cs}$). However, a further decrease in temperature causes the rate to go through another inflection. There is so much conversion of contact ion pairs to solvent-separated ion pairs that any additional increase in the fraction of the latter is insufficient to counter the conventional effect of $E_c$. $k_p$ decreases with decreasing $T$, $k_p^\pm$ reaches a maximum (at about $-75{^\circ}$C) and then decreases. The overall effect of $T$ on $k_p^\pm$ depends on the relative values of $E_c$, $E_s$, $\Delta H_{cs}$, and $\Delta S_{cs}$. In a poor solvent such as dioxane, there is a negligible fraction of solvent-separated ion pairs at all temperatures; $k_c$ and $k_p^\pm$ decrease with decreasing temperature over the complete temperature range. In a moderately good solvent (THF and 3-methyltetrahydrofuran), the behavior in Fig.5-7 is observed. For a sufficiently good solvent where the fraction of solvent-separated ion pairs is close to one, $k_s$ and $k_p^\pm$ would decrease continuously with decreasing temperature. Data indicate that hexamethylphosphoramide is such a solvent for polystyryl sodium [Schmitt and Schulz, 1975].

Experimental data of $k_p^\pm$ versus $1/T$ can be fitted to the preceding equations to yield values of the various activation and thermodynamic parameters pertinent to ion-pair propagation (Table 5-12). Corresponding values of the parameters for free-ion propagation are included in Table 5-12 for comparison. The solvent-separated ion pair is approximately half as reactive as the free ion, while the contact ion pair is more than 3 orders of magnitude

| $k_p^-$ (20°C) | $1.3 \times 10^5$ L mol$^{-1}$ s$^{-1}$ |
| $K$ (20°C) | $4.0 \times 10^{-8}$ mol L$^{-1}$ (20°C) |
| $79.1 \times 10^{-8}$ mol L$^{-1}$ (−48°C) |
| $E_p^-$ | $16.6$ kJ mol$^{-1}$ |
| $A_p^-$ | $1.0 \times 10^8$ L mol$^{-1}$ s$^{-1}$ |
| $A_c$ | $36.0$ kJ mol$^{-1}$ |
| $A_s$ | $6.3 \times 10^7$ L mol$^{-1}$ s$^{-1}$ |
| $k_s$ (20°C) | $24$ L mol$^{-1}$ s$^{-1}$ |
| $E_s$ | $19.7$ kJ mol$^{-1}$ |
| $A_s$ | $2.08 \times 10^8$ L mol$^{-1}$ s$^{-1}$ |
| $k_p^\pm$ (20°C) | $5.5 \times 10^4$ L mol$^{-1}$ s$^{-1}$ |
| $\Delta H_{cs}$ | $-19.7$ kJ mol$^{-1}$ |
| $\Delta S_{cs}$ | $-142$ J K$^{-1}$ mol$^{-1}$ |
| $K_{cs}$ | $2.57 \times 10^{-3}$ (20°C) |
| $2.57 \times 10^{-2}$ (−50°C) |

*aData for Schmitt and Schulz [1975].
less reactive. The fact that \( k_p^- \) is only slightly more than twice \( k_s \) clearly indicates that the solvent-separated ion pair is in an environment similar to that of the free ion. The frequency factors for the three types of propagating centers are very similar; reactivity differences are due to the differences in activation energies. The free ion and solvent-separated ion pair have comparable activation energies. The much higher value of \( E_c \) indicates the need to separate the anion and counterion in the transition state so that monomer can be inserted. The \( K_{cs} \) values show that a large fraction of the ion pairs in THF are solvent-separated ion pairs. Since \( k_s \gg k_c \), any significant concentration of solvent-separated ion pairs will contribute heavily to the overall propagation rate. The wide variation in the relative amounts of solvent-separated and contact ion pairs with solvent is evident from the values of \( K_{cs} \) (0.13, 0.002, 0.0001, and <10\(^{-5}\)) for 1,2-dimethoxyethane, tetrahydrofuran, tetrahydropyran, and dioxane, respectively, at 25°C [Szwarc, 1983].

The reactivity of the solvent-separated ion pair is hardly affected by the counterion. This can be observed from the \( k_p^- \) values in THF (Table 5-11). Most of the observed propagation in THF is due to solvent-separated ion pairs and \( k_p^- \) is a good indication of \( k_s \). The variation in \( k_p^- \) from Li\(^+\) to Cs\(^+\) is relatively small and is probably due more to differences in the fractions of solvent-separated ion pairs than to differences in \( k_s \). The reactivity of contact ion pairs is more sensitive to the counterion. The variation of \( k_p^- \) in dioxane is by a factor of 25 between the different counterions. Since the fraction of solvent-separated ion pairs is extremely small in dioxane, \( k_p^- \) is indicative of \( k_s \). The larger, more loosely held cesium counterion results in a higher reactivity for the contact ion pair. The variation of \( k_c \) and \( k_s \) with solvating power of the reaction medium is not established. Some data indicate that \( k_s \) is insensitive to solvent while \( k_c \) increases with increasing solvating power, but these results are limited to ether solvents.

### 5-3d-5 Association Phenomena in Alkylithium

A complication for polymerizations initiated by organolithium compounds in nonpolar solvents, such as cyclohexane, \( n \)-hexane, and benzene, is association (aggregation) of the various organolithium compounds because of the small size of lithium and its possessing more low-energy orbitals than electrons. Each lithium associates and participates in bonding with two or more organic moieties. The phenomenon is important since the associated species are generally unreactive and it is only the unassociated species that are active in initiation and propagation. There is an equilibrium between the dormant associated species and the reactive unassociated species. The effects of association have been extensively studied for styrene, isoprene, and 1,3-butadine polymerizations by \( n \)-, and \( t \)-butyllithium [Bywater, 1975, 1985; Hsieh and Quirk, 1996; Morton, 1983; Quirk, 1995, 1998, 2002; Van Beylen et al., 1988; Young et al., 1984].

The initiation and propagation reactions typically show fractional orders of dependence of rate on alkylithium. The situation is quite complex. The fractional orders for initiation and propagation are seldom the same and often vary depending on the monomer, solvent, and initiator and their absolute as well as relative concentrations. For styrene polymerization by \( n \)-butyllithium in aromatic solvents, the initiation and propagation rates are proportional to only the \( \frac{1}{5} \) and \( \frac{1}{4} \) powers of \( n \)-butyllithium concentration, respectively. These results have been interpreted in terms of the following association equilibria

\[
(C_4H_9Li)_6 \overset{k_1}{\longrightarrow} 6C_4H_9Li
\]  \hspace{1cm} (5-107)

\[
(C_4H_9-M^n/+_nLi)^2_2 \overset{k_2}{\longrightarrow} 2C_4H_9-M^n/+_nLi^+
\]  \hspace{1cm} (5-108)
with initiator and propagating ion pairs in equilibria with the corresponding hexamer and dimer, respectively. (Equation 5-107 is an oversimplification. Dissociation of hexamer to monomeric n-butyllithium probably takes place in stages.) One derives the concentrations of unassociated initiator and propagating ion pairs as

\[
[C_4H_9Li] = K_1^{1/6}([C_4H_9Li]_6)^{1/6} \quad (5-109)
\]

\[
[C_4H_9-M_n^+Li] = K_2^{1/2}([C_4H_9-M_n^+Li]_2)^{1/2} \quad (5-110)
\]

which explain the dependence of \( R_i \) and \( R_p \) on the \( \frac{1}{6} \) and \( \frac{1}{2} \) power, respectively, of the n-butyllithium concentration. Molecular weight measurements by viscometry and light scattering have been used to support the presence of the hexamer and dimer species, but the results from different workers are often contradictory [Van Beylen et al., 1988]. This interpretation of the fractional kinetic orders assumes that only monomeric initiator and propagating ion pairs are reactive. This assumption is not universally accepted for all reaction systems. It has been suggested that for some systems the fractional reaction orders are artifacts resulting from the complex manner in which concentration affects the reaction of monomer with associated initiator and propagating species [Young et al., 1984].

The results are slightly different with s- and t-butyllithium. \( R_p \) is still \( \frac{1}{2} \)-order in initiator but \( R_i \) is \( \frac{1}{4} \) instead of \( \frac{1}{6} \)-order in initiator. s- and t-butyllithium exist as tetramers, not hexamers like n-butyllithium, because of the more sterically hindered alkyl groups. The propagating species still associates as dimers, since the initiating alkyl groups becomes far removed from the propagating carbanion center. The rates of initiation by s- and t-butyllithium are greater than for n-butyllithium, a consequence of the greater nucleophilicity of tertiary and secondary carbanions over primary carbanions. The relative reactivities of s- and t-butyllithium are not always in the same order but depend on the monomer, indicating that steric effects are also important.

Polymerization in aliphatic hydrocarbons is considerably slower than in aromatic hydrocarbons because of decreased dissociation of initiator and propagating ion-pair aggregates. The course of reaction in aliphatic hydrocarbons is complex compared to that in aromatic solvents. Initiation is very slow at the start of reaction but proceeds with autoacceleration as cross- or mixed association of initiator and propagating ion pairs replaces self-association of initiator. Cross-association is weaker and results in an increased concentration of monomeric initiator. This effect may also explain the higher-order dependence of \( R_i \) on initiator (typically between \( \frac{1}{2} \) and 1-order) in aliphatic solvents, especially for s- and t-butyllithium. \( R_p \) is still \( \frac{1}{2} \)-order in initiator independent of solvent.

The situation is similar qualitatively but differs quantitatively for isoprene and 1,3-butadiene. The dependence of \( R_p \) on initiator varies from \( \frac{1}{6} \) to \( \frac{1}{2} \)-order depending on the specific reaction system. The reaction orders for all monomers are affected by the relative as well as absolute concentrations of initiator and monomer. Thus the dependence of \( R_p \) on initiator for the n-butyllithium polymerization of isoprene in benzene at 30°C is \( \frac{1}{2} \)-order at initiator concentrations above \( 10^{-4} \) M but \( \frac{1}{6} \)-order at initiator concentrations below \( 10^{-4} \) M [Van Beylen et al., 1988]. Higher initiator concentrations yield higher degrees of aggregation and lower kinetic orders. The excess of monomer over initiator is also important. Higher kinetic orders are often observed as the monomer : initiator ratio increases, apparently as a result of breakup of initiator and propagating ion-pair associations by monomer.

The association phenomena occurring with alkylithium initiators in nonpolar solvents results in very low polymerization rates. A typical styrene or isoprene polymerization by
butyllithium in benzene is orders of magnitude slower compared to the corresponding sodium naphthalene polymerization. When butyllithium polymerizations are carried out in polar solvents such as tetrahydrofuran, the association of initiator and propagating species vanishes completely and the polymerizations are much more rapid. The association phenomena can also be disrupted by adding a Lewis base, which can coordinate with the initiator (Alev et al., 1980; Cheminat et al., 1979; Dumas et al., 1978; Fontanille, 1989; Muller, 1989). Polyamines such as \( N, N, N', N'\)-tetramethylethylene diamine (TMEDA) and polyethers such as tetruglyme, \( \text{CH}_3\text{O}-(\text{CH}_2\text{CH}_2\text{O})_4\text{CH}_3 \), are more effective in breaking up the association than are simple ethers and amines such as diethyl ether or triethyl amine. The effectiveness of a Lewis base in promoting initiation and polymerization decreases if the base : initiator ratio is too high. One observes the polymerization rate to increase with increasing [base]/[RLi] and then level off at a maximum rate. With many Lewis bases, the polymerization rate decreases after reaching the maximum as [base]/[RLi] is increased further [Hay et al., 1976]. Complexation of base with initiator becomes so extensive as to decrease the reactivity of initiator.

The macrocyclic crown ethers such as 18-crown-6 (XXIXa) and cryptands such as 2.2.2-cryptand (XXIXb) are extremely powerful for breaking up association of organolithium compounds. These macrocyclic ligands complex lithium and also other counterions so strongly as to greatly increase the concentration of free-ion propagating species, resulting in very large rate increases (Cheng and Halasa, 1976; Deffieux and Boileau, 1976).

\[ \text{XXIXa} \]
\[ \text{XXIXb} \]

### 5-3d-6 Other Phenomena

The need for solvation in anionic polymerization manifests itself in some instances by other deviations from the normal reaction rate expressions. Thus the butyllithium polymerization of methyl methacrylate in toluene at \(-60^\circ\text{C}\) shows a second-order dependence of \( R_p \) on monomer concentration [L’Abbe and Smets, 1967]. In the nonpolar toluene, monomer is involved in solvating the propagating species [Busson and Van Beylen, 1978]. When polymerization is carried out in the mixed solvent dioxane–toluene (a more polar solvent than toluene), the normal first-order dependence of \( R_p \) on [M] is observed. The lithium diethylamide, \( \text{LiN(C}_2\text{H}_5)_2 \), polymerization of styrene at \( 25^\circ\text{C} \) in THF–benzene similarly shows an increased order of dependence of \( R_p \) on [M] as the amount of tetrahydrofuran is decreased [Hurley and Tait, 1976].

Propagation of two-ended (bifunctional) propagating species often proceeds at a rate lower than that of the corresponding monoanion species as a result of triple-ion formation [Bhattacharyya et al., 1964; Smid, 2002]. For example, ionic dissociation of the counterion from one end of the cesium salt of a two-ended propagating species XXX yields XXXI in which the newly dissociated anionic center remains near the ion pair at the other end of
XXXI. The result is XXXII, referred to as a triple ion. The triple ion propagates faster than a simple ion pair but slower than a free ion [Muller, 1989]. The major effect of triple ion formation is a lowering of the concentration of free ions and the overall result is a decrease in polymerization rate. Similar results are found for divalent counterions such as barium and strontium [de Groof et al., 1975, 1977; Mathis and François, 1978; Mathis et al., 1978]. Triple ion formation decreases with increasing molecular weight of the two-ended dicarbanion; thus, \( R_p \) increases with conversion. As the length of the intramolecular chain between the two anion centers increases, the probability of cyclization to the triple ion decreases.

The higher reactivity of 2-vinylpyridine relative to styrene has been attributed to a combination of intramolecular solvation and triple-ion formation [Sigwalt, 1975; Soum et al., 1977].

5-4 BLOCK AND OTHER POLYMER ARCHITECTURES

Anionic and cationic living polymerizations offer routes to block copolymers, star polymers, telechelic polymers, and other polymers [Charleux and Faust, 1999; Hadjichristidis et al., 2002].

5-4a Sequential Monomer Addition

Sequential addition of monomer works well in anionic polymerization for producing well-defined block copolymers [Morton, 1983; Morton and Fetters, 1977; Quirk, 1998; Rempp et al., 1988]. An AB diblock copolymer is produced by polymerization of monomer A to completion using an initiator such as butyllithium. Monomer B is then added to the living polyA carbanions. When B has reacted completely a terminating agent such as water or methanol is added and then the AB block copolymer isolated. Various types of block copolymers (di, tri, multiblocks) are obtained by using the proper sequencing of additions
of different monomers provided that each propagating carbanion can initiate polymerization of the next monomer. For example, polystyryl carbanion initiates polymerization of methyl methacrylate, but the reverse does not occur. Crossover from one carbanion to another occurs only when the new carbanion is comparable or higher in stability than the original carbanion. Poly(methyl methacrylate) carbanion is more stable than polystryrene carbanion. Carbanion stability can be estimated from the $pK_a$ of the conjugate acids of model carbanions. Toluene and ethyl acetate have $pK_a$ values of 43 and 30, in line with the higher stability of the PMMA carbanion.

Thus, the synthesis of a styrene-methyl methacrylate block polymer requires that styrene be the first monomer. Further, it is useful to decrease the nucleophilicity of polystyryl carbanions by adding a small amount of 1,1-diphenylethene to minimize attack at the ester function of MMA [Quirk et al., 2000]. Block copolymers of styrene with isoprene or 1,3-butadiene require no specific sequencing since crossover occurs either way. Block copolymers of MMA with isoprene or 1,3-butadiene require that the diene be the first monomer. The length of each segment in a block copolymer is controlled by the ratio of each monomer to initiator. The properties of the block copolymer vary with the block lengths of the different monomers.

Difunctional initiators such as sodium naphthalene are useful for producing ABA, BABAB, CABAC, and other symmetric block copolymers more efficiently by using fewer cycles of monomer additions. Difunctional initiators can also be prepared by reacting a diene such as $m$-diisopropenylbenzene or 1,3-bis(1-phenylethenyl)benzene with 2 equiv of butyllithium. Monomer B is polymerized by a difunctional initiator followed by monomer A. A polymerizes at both ends of the B block to form an ABA triblock. BABAB or CABAC block copolymers are synthetized by the addition of monomer B or C to the ABA living polymer. The use of a difunctional initiator is the only way to synthesize a MMA-styrene–MMA triblock polymer since MMA carbanion does not initiate styrene polymerization (except by using a coupling reaction—Sec. 5-4c).

Styrene–isoprene–styrene and styrene-1,2-butadiene–styrene ABA block copolymers, containing short styrene blocks on each side of a long diene block, are produced commercially. These are useful as the thermoplastic elastomers (trade names: Cariflex, Kraton, Solprene, Stereon), which behave as elastomers at ambient temperatures but are thermoplastic at elevated temperatures where they can be molded and remolded (Sec. 2-13c-2). The polystyrene blocks of the copolymer aggregate to form glassy (hard) domains at ambient temperatures. These effectively crosslink the rubbery (soft) polydiene segments and also act as reinforcing filler particles to increase strength. The physical crosslinking is reversible since heating above the glass transition temperature of polystyrene (100°C) softens the hard segments and the triblock copolymer flows under stress. Cooling reestablishes the hard polystyrene domains, and the material again act as a crosslinked elastomer. Thermoplastic elastomers have the advantage that they can be processed as thermoplastics instead of thermosets. Diblock copolymers do not show good elastomer behavior. One needs the triblock structure with the hard (physical crosslinking) blocks at both ends of the polymer chain to obtain rubbery behavior.

In addition to the triblock thermoplastic elastomers, other useful copolymers of styrene with a diene are produced commercially by living anionic polymerization. These include di- and multiblock copolymers, random copolymers, and tapered block copolymers. A tapered (gradient) copolymer has a variation in composition along the polymer chain. For example, S-S/D-D is a tapered block polymer that tapers from a polystyrene block to a styrene-diene random copolymer to polydiene block. (Tapered polymers need not have pure blocks at their ends. One can have a continuously tapered composition from styrene to diene by
polymerizing a continuously changing mixture of the two monomers—by starting out with one pure monomer and continuously adding the second monomer. Also, tapered polymers can be obtained from nonliving polymerizations—Chap. 6.)

Clear impact-resistant polystyrene is a commercial plastic with the desirable combination of toughness and exceptional clarity. It is a styrene-1,3-butadiene multiblock copolymer containing more than 60% styrene. Most of these products are mixtures of block copolymers formed by incremental additions of initiator and monomers followed by coupling (Sec. 5-4c). The products generally have a tapered and multiblock composition with branching (due to the coupling agent).

The annual worldwide production of triblock thermoplastic elastomers, clear impact-resistant polystyrene, and other styrene–diene products produced by anionic polymerization exceeds a couple of billion pounds. (Commercial utilization of anionic polymerization also includes the polymerization of 1,3-butadiene alone.)

The range of monomers that can be incorporated into block copolymers by the living anionic route includes not only the carbon–carbon double-bond monomers susceptible to anionic polymerization but also certain cyclic monomers, such as ethylene oxide, propylene sulfide, lactams, lactones, and cyclic siloxanes (Chap. 7). Thus one can synthesize block copolymers involving each of the two types of monomers. Some of these combinations require an appropriate adjustment of the propagating center prior to the addition of the cyclic monomer. For example, carbanions from monomers such as styrene or methyl methacrylate are not sufficiently nucleophilic to polymerize lactones. The block copolymer with a lactone can be synthesized if one adds a small amount of ethylene oxide to the living polystyryl system to convert propagating centers to alkoxide ions prior to adding the lactone monomer.

Group transfer polymerization allows the synthesis of block copolymers of different methacrylate or acrylate monomers, such as methyl methacrylate and allyl methacrylate [Hertler, 1996; Webster and Sogah, 1989]. The synthesis of mixed methacrylate–acrylate block copolymers requires that the less reactive monomer (methacrylate) be polymerized first. The silyl dialkylketene acetal propagating center from methacrylate polymerization is more reactive for initiation of acrylate polymerization than the silyl monoalkylketene acetal propagating center from acrylate polymerization is for initiation of methacrylate polymerization. Bifunctional initiators such as 1,4-bis(methoxytrimethylsiloxymethylene)cyclohexane (XXXIII) are useful for synthesizing ABA block copolymers where the middle block is methacrylate [Steinbrecht and Bandermann, 1989; Yu et al., 1988].

\[
\begin{align*}
\text{XXXIII} \\
(CH_3)_3SiO \quad & \quad C \quad & \quad \text{OSi(CH}_3)_3 \\
\text{CH}_3O \quad & \quad \text{CH}_3O \quad & \quad \text{OCH}_3
\end{align*}
\]

Various block copolymers have been synthesized by cationic living polymerization [Kennedy and Ivan, 1992; Kennedy, 1999; Kennedy and Marechal, 1982; Puskas et al., 2001; Sawamoto, 1991, 1996]. AB and ABA block copolymers, where A and B are different vinyl ethers, have been synthesized using HI with either I2 or ZnI2. Sequencing is not a problem unless one of the vinyl ethers has a substituent that makes its reactivity quite different. Styrene–methyl vinyl ether block copolymer synthesis requires a specific sequencing and manipulation of the reaction conditions because styrene is less reactive than methyl vinyl ether (MVE) [Ohmura et al., 1994]. Both monomers are polymerized by HCl/SnCl4 in the presence of (n-C4H9)4NCl in methylene chloride, but different temperatures are needed. The
Block copolymer is obtained by polymerization of MVE at $-78^\circ C$ followed by addition of styrene. Styrene adds to the polyMVE carbocations only when additional SnCl$_4$ is added and the temperature is raised to $-15^\circ C$. The reverse sequence, styrene first followed by MVE, is not generally successful. The first stage reaction conditions for styrene are too extreme for MVE polymerization and cannot be adjusted to achieve a controlled polymerization of MVE.

Block copolymers of isobutylene with styrene, isoprene, and vinyl ethers have been synthesized, often requiring an appropriate adjustment of reaction conditions for the second stage, as described above for styrene–MVE. Another approach is the use of a telechelic polymer (containing the first block) as the initiator for polymerization of the second monomer (Sec. 5-4b).

### 5-4b Telechelic (End-Functionalized) Polymers

Telechelic polymers, containing one or more end groups with the capacity to react with other molecules, are useful for synthesizing block and other copolymers [Fontanille, 1989; Hsieh and Quirk, 1996; Nuyken and Pask, 1989; Pantazis et al., 2003; Patil et al., 1998; Quirk et al., 1989, 1996; Rempp et al., 1988]. Living anionic polymers can be terminated with a variety of electrophilic reagents to yield telechelic polymers. For example, reaction with carbon dioxide, ethylene oxide, and allyl bromide yield polymers terminated with carboxyl, hydroxyl, and allyl groups, respectively. Functionalization with hydroxyl or carboxyl groups can also be achieved by reaction with a lactone or anhydride, respectively. Polymers with amine end groups are obtained by reaction with $N$-trimethylsilyl-protected imines followed by acid hydrolysis. When the telechelic polymer contains a bifunctional group, such as the allyl-terminated telechelic, it is called a macromonomer or macromer because it can undergo polymerization through that functional group. The efficiencies of these reactions depend on the specific reaction, steric factors, and reaction conditions. For example, efficiency is higher for polybutadienyl carbanion compared to polystyrene. Reaction of any of the polymer carbanions with carbon dioxide is quantitative in polar solvents, but not in hydrocarbons.

Telechelic polymers are also obtained by using initiators containing the desired functional group. This often requires that the functional group be protected or blocked during initiation and polymerization since many functional groups act as facile terminating agents. Thus an amine-terminated telechelic is obtained by prior synthesis of an initiator containing an amine end group.

$$\text{XXXIV}$$

$$\text{XXXIV}$$
function protected by trimethylsilylation [Dickstein and Lillya, 1989]. The protected initiator XXXIV is used to initiate polymerization and subsequently the trimethylsilyl group is removed by acid hydrolysis.

Monofunctional telechelic polymers containing groups such as hydroxyl, amine, or carboxyl can be used to obtain diblock copolymers by reaction with other telechelic polymers. The latter includes telechelics obtained by the anionic route or telechelics obtained by other routes (e.g., step and ring-opening polymerizations). Telechelic polymers containing functional groups at each chain end are obtained by carrying out the above reactions with two-ended living anionic polymers. These bifunctional telechelics can be used to synthesize triblock and multiblock copolymers as well as telechelic prepolymers to be used in step polymerization (Sec. 2-13b) [Register et al., 1988].

Telechelic polymers are obtained by group transfer polymerization by using initiators (XXXV) containing protected functional groups [Webster and Sogah, 1989]. Hydroxyl- and carboxyl-terminated telechelic polymers are obtained by using initiator XXXV with \( R = -C_2H_5CH_2OSi(CH_3)_3 \) and \(-Si(CH_3)_3\), respectively (\( R' = -CH_3 \)). The HO and COOH groups are obtained by hydrolysis of the silyl ketene acetal end groups of the polymer. Another approach is reaction of the living silyl ketene acetal end group with an electrophilic reagent, such as benzanaldehyde to yield a blocked hydroxyl function or \( p\)-bromomethylstyrene to yield a vinyl macromer.

Telechelic polymers via cationic living polymerizations are obtained in a similar manner [Higashimura and Sawamoto, 1989; Kennedy, 1985, 1999; Kennedy and Marechal, 1982; Kennedy and Smith, 1980; Sawamoto, 1991, 1996]. Termination of a polymerization with a nucleophile such as the sodiomalonate XXXVI yields a carboxyl-terminated telechelic after hydrolysis and decarboxylation for \( R = H \), and a vinyl-terminated telechelic is obtained for \( R = -C_2H_5CH_2OCH = CH_2 \). Functional groups can also be introduced by using appropriately substituted initiators; for example, initiation by XXXVII yields a telechelic with a vinyl end group. Telechelic polymers are useful for synthesizing block copolymers, such as a styrene–isobutylene–styrene triblock polymer. Isobutylene is polymerized by 1,4-bis (2-chloroisopropyl)benzene (often called dicumyl chloride) (XXXVIII) and \( BCl_3 \) to yield a bifunctional telechelic polyisobutylene with \( t\)-alkyl end groups (XXXIX). The telechelic polyisobutylene is used as the initiator together with diethylaluminum chloride to polymerize styrene and produce the triblock polymer.

\[
\begin{align*}
\text{XXXV} & : \quad R' = C\equiv C\overset{1}{\underset{\text{OR}}{\text{OSi(CH}}_{3}\text{)}_{3}} \\
\text{XXXVI} & : \quad (C_{2}H_{5}COO)_{2}C\overset{1}{\underset{\text{\text{Na}^{+}}}{\text{\text{CH}}_{2}\overset{1}{\underset{\text{\text{\text{OH}}} = \text{COOCH}}_{2}\text{CH}_{2}\text{OCH} \quad \text{I} \quad \text{I}}} \quad \text{CH}_{3} \\
\text{XXXVII} & : \quad (C_{2}H_{5}COO)_{2}C\overset{1}{\underset{\text{\text{Na}^{+}}}{\text{\text{CH}}_{2}C(=\text{CH})_{2}COOCH_{2}CH_{2}OCH = \text{CH}_{2}} \quad \text{I} \quad \text{I}} \\
\end{align*}
\]

Telechelic polymers via cationic living polymerizations are obtained in a similar manner [Higashimura and Sawamoto, 1989; Kennedy, 1985, 1999; Kennedy and Marechal, 1982; Kennedy and Smith, 1980; Sawamoto, 1991, 1996]. Termination of a polymerization with a nucleophile such as the sodiomalonate XXXVI yields a carboxyl-terminated telechelic after hydrolysis and decarboxylation for \( R = H \), and a vinyl-terminated telechelic is obtained for \( R = -C_{2}H_{5}CH_{2}OCH = CH_{2} \). Functional groups can also be introduced by using appropriately substituted initiators; for example, initiation by XXXVII yields a telechelic with a vinyl end group. Telechelic polymers are useful for synthesizing block copolymers, such as a styrene–isobutylene–styrene triblock polymer. Isobutylene is polymerized by 1,4-bis (2-chloroisopropyl)benzene (often called dicumyl chloride) (XXXVIII) and \( BCl_3 \) to yield a bifunctional telechelic polyisobutylene with \( t\)-alkyl end groups (XXXIX). The telechelic polyisobutylene is used as the initiator together with diethylaluminum chloride to polymerize styrene and produce the triblock polymer.

\[
\begin{align*}
\text{XXXVIII} & : \quad \text{Cl}[\overset{1}{\underset{\text{CH}_{3}}{\text{[C(CH}}_{3}\text{)}_{2}\text{CH}_{2}}}_{n} \overset{1}{\underset{\text{\text{Cl}}}{\overset{1}{\underset{\text{\text{C}}}{\text{\text{C}}}}}}_{\text{\text{C}}} \overset{1}{\underset{\text{\text{[C(H}}_{2}\text{C(CH}}_{3}\text{)}_{2}}}_{n} \text{Cl} \\
\text{XXXIX} & : \quad \overset{1}{\underset{\text{\text{[C(H}}_{2}\text{C(CH}}_{3}\text{)}_{2}]}_{n} \overset{1}{\underset{\text{\text{C}}}{\text{\text{C}}}} \overset{1}{\underset{\text{\text{[C(H}}_{2}\text{C(CH}}_{3}\text{)}_{2}]}_{n} \text{Cl} \\
\end{align*}
\]
Living anionic polymers and block copolymers can be linked by coupling reactions. A living AB block copolymer can be linked by 1,6-dibromohexane to yield an ABA triblock copolymer

\[
\sim A_n B_m \xrightarrow{Br(CH_2)Br} \sim A_n B_m (CH_2)_{6} B_m A_n \sim
\]  

(5-117)

Coupling reactions allow the synthesis of star (multiarmed) polymers (Sec. 3-15b-5) by using a multifunctional coupling agent such as SiCl\(_4\), C\(_3\)H\(_7\)SiCl\(_3\), (ClCH\(_2\))\(_4\), and 1,2,4,5-tetrachloromethylbenzene [Alward et al., 1986; Hadjichristidis et al., 2001; Lutz and Rempp, 1988; Quirk et al., 1999; Remp et al., 1988]; for example

\[
\sim A_n \xrightarrow{SiCl_4} \sim A_n \sim
\]  

(5-118)

An excess of living polymer is used to force the coupling reaction to completion. However, steric factors influence the extent and efficiency of coupling. Si—Cl bonds are more efficiently substituted compared to C—Cl bonds. Complete conversion is hindered when the coupling sites are closer together and for the more bulky living polymers. Polybutadienyl anions couple quantitatively with SiCl\(_4\) to give the tetrasubstituted star polymer, but polyisoprenyl and polystyryl anions form mostly the trisubstituted product. All carbanions react quantitatively with CH\(_3\)SiCl\(_3\). The coupling efficiency with SiCl\(_4\) becomes quantitative by adding a few units of 1,3-butadiene to the polystyryl and polyisoprenyl anions. Efficiency is also increased by using a coupling agent in which the Si—Cl bonds are more separated from each other.

Miktoarm star (or \(\mu\)-star) polymers are star polymers with branches of different polymers. These polymers are also called heteroarm or mixed-arm star polymers. Their synthesis is more difficult but success has been achieved by sequential coupling [Hadjichristidis, et al., 1999]. To obtain a 3-arm star with one polyisoprenyl (PI) and two polystyryl (PS) branches, polyisoprenyllithium is reacted with an excess of CH\(_3\)SiCl\(_3\) to form the one-arm polymer, the unreacted CH\(_3\)SiCl\(_3\) is removed, and then polystyryllithium is added:

\[
PILi \xrightarrow{excess} PISi(CH_3)Cl_2 \xrightarrow{PSLi} PISi(CH_3)(PS)_2
\]  

(5-119)

Much more extensively branched polymers, referred to as comb and brush polymers, are obtained by using coupling agents with much higher functionality [e.g., Si(CH\(_2\))\(_2\)SiCl\(_3\)]\(_4\), [CH\(_2\)Si(CH\(_2\))\(_2\)SiCl\(_3\)]\(_3\)\(_2\), and \(p\)-chloromethylated polystyrene] or a diene (e.g., \(p\)-divinylbenzene), sometimes together with a two-ended living polymer instead of a one-ended living polymer [Roovers et al., 1989; Taromi and Rempp, 1989; Schappacher and Deffieux, 2000]. The products obtained from polymeric coupling agents are also referred to as graft polymers. Hyperbranched and dendritic structures are also possible with appropriate coupling agents having very high functionality [Hadjichristidis et al., 2001; Knauss et al., 2000; Quirk et al., 1999]. The synthesis of other polymer topologies has also been studied. Cyclic and figure 8-shaped polystyrenes have been obtained by coupling a two-ended living anionic polymer with dichlorodimethylsilane and 1,2-bis(dichloromethylsilyl)ethane, respectively,
Compounds containing two or more carbon–carbon double bonds also act as coupling agents and also as multifunctional initiators [Hadjichristidis et al., 2001; Quirk et al., 2000]. Such compounds can also be used to synthesize multifunctional initiators that subsequently produce star polymers. Consider 1,3,5-tris(1-phenylethenyl)benzene (XL). Reaction with s-butyllithium produces a trifunctional initiator XLI, which initiates polymerization of a monomer such as styrene to form a 3-arm star polystyrene [Quirk and Tsai, 1998]. The 3-arm star polystyrene can also be synthesized by reaction XL with polystyryl carbanion to form XLII, which is then terminated with water or methanol. XLII can be used to produce a miktostar polymer containing three branches each of two different polymers: for instance, reaction with 1,3-butadiene forms a 6-arm star polymer containing three polystyrene branches and three polybutadiene branches.

Coupling of GTP living polymers with halide-terminating agents to form star polymers has been achieved [Hertler, 1996; Webster and Sogah, 1989]. Star polymers are also synthesized by using polyfunctional initiators or by copolymerization with dimethacrylate monomers.

Star and miktostar polymers have been synthesized by living cationic polymerization using dienes and trienes as coupling agents and/or multifunctional initiators [Faust and Shaffer, 1997; Hadjichristidis, et al., 1999; Hadjikyriacou and Faust, 2000; Kennedy and Jacob, 1998; Puskas et al., 2001; Sawamoto, 1991]. Multifunctional halides such as hexaiodo-methylmelamines have also been used to obtain star and comb polymers [Ryu and Hirao, 2001; Zhang and Goethals, 2001]. Hyperbranched and dendritic polymers have also been studied.
Another approach to block copolymer is the mutual termination of a living cationic polymer with a living anionic polymer, but the efficiency of coupling is generally low because of proton transfer from the carbocation to the carbanion, resulting in two homopolymers instead of the block copolymer [Richards et al., 1978].

**5-4d Transformation Reactions**

Another approach to block copolymers involves changing the type of propagating center part way through the synthesis via a *transformation reaction* [Burgess et al., 1977; Richards, 1980; Souel et al., 1977; Tung et al., 1985]. For example, after completion of the living anionic polymerization of monomer A, the carbanion centers are transformed into carbocations by reaction with excess phosgene followed by silver hexafluoroantimonate. The carbocations are then used to polymerize monomer B.

Anionic propagating centers are transformed into radical centers in the presence of a second monomer that undergoes radical propagation, by reaction with trimethyl lead chloride followed by heating:

\[
\begin{align*}
&\text{\(^{-}\text{AAA}^{-}\text{Li}^{+}\)} \underset{\text{CIPb(CH₃)}₃}{\xrightarrow{\text{ClPb(CH₃)}₃}} \text{\(^{-}\text{AAA}^{-}\text{Pb(CH₃)}₃\)}} \\
&\text{\(^{-}\text{AAA}^{-}\text{Pb(CH₃)}₃\)}} \underset{\text{heat}}{\xrightarrow{\text{heat}}} \text{\(^{-}\text{AAA}^{-}\text{Pb}^\circ\)}} \\
&\text{\(^{-}\text{AAA}^{-}\text{Pb}^\circ\)}} \underset{\text{B}}{\xrightarrow{\text{B}}} \text{\(^{-}\text{AAA}^{-}\text{BBB}^\circ\)}} \\
\end{align*}
\]

(5-124)

The potential of transformation reactions for synthesizing a wider range of block copolymers has not been realized because either the reactions are not quantitative or detrimental side reactions occur. Thus coupling of two propagating carbanions by one phosgene competes with the 1 : 1 transformation in Eq. 5-123. The anionic-to-radical transformation in Eq. 5-124 involves the formation of trimethyllead radical, which initiates homopolymerization of monomer B.

**5-5 DISTINGUISHING BETWEEN RADICAL, CATIONIC, AND ANIONIC POLYMERIZATIONS**

There is sometimes a question as to whether a particular initiator or initiator system initiates polymerization by radical, cationic, or anionic means. Such a question can easily arise, for example, in polymerizations initiated by ionizing radiation. The mode of initiation of a particular initiator can be distinguished by a consideration of its characteristics compared to those of known radical, cationic, and anionic initiators:

1. Ionic polymerizations usually proceed at lower temperatures than radical polymerizations. Although ionic reaction temperatures are usually below 0°C, there are numerous ionic polymerizations that proceed at temperatures somewhat above 0°C. Radical polymerizations, on the other hand, almost always proceed at temperatures appreciably above approximately 50°C. Furthermore, ionic polymerizations invariably have lower
activation energies than their radical counterparts and, in some cases, they may actually possess negative activation energies.

2. Ionic polymerizations are distinguished by their marked sensitivity to changes in the polarity and solvating ability of the reaction media and counterion effects. Radical polymerizations do not show such effects.

3. The addition of known radical scavengers such as the DPPH radical to a polymerizing system will halt polymerization if it is a radical reaction. Ionic polymerizations will be unaffected by such additions. One must be careful, however, not to use a radical scavengers that also affects ionic polymerization. Thus, benzoquinone would be a poor choice as a radical scavenger, since it can also act as an inhibitor in ionic polymerization.

4. The chain transfer constant for an additive or solvent in the polymerization can be determined. This value can then be compared with the transfer constants for the same substance in the polymerization of the same monomer by known radical, cationic, and anionic initiators.

5. Copolymerization behavior can also be used to distinguish between radical and ionic polymerizations (see Chap. 6).

5-6 CARBONYL POLYMERIZATION

The polymerization of the carbonyl group in aldehydes yields polymers, referred to as polyacetals, since they contain the acetal repeating structure

\[
\begin{align*}
\text{C} & \equiv \text{O} \\
\text{H} & \equiv \text{C} \quad \text{O} \quad \text{C} \quad \text{O} \quad \text{C} \quad \text{O} \\
\text{H} & \equiv \text{H} \quad \text{H} \quad \text{H} \quad \text{H}
\end{align*}
\]  

Besides the carbon–carbon double bond, this is the only other unsaturated linkage whose polymerization has been successfully carried out to an appreciable extent [Furukawa and Saegusa, 1963; Kubisa et al., 1980; Vogl, 1967, 1976, 2000]. The polymerization of formaldehyde has been studied much more intensely than that of other aldehydes. Although formaldehyde was successfully polymerized over a hundred years ago, it was not until much later that high-molecular-weight polymers of other aldehydes were obtained.

Progress in the polymerization of the carbonyl linkage did not result until there was an understanding of the effect of ceiling temperature \( (T_c) \) on polymerization (Sec. 3-9e). With the major exception of formaldehyde and one or two other aldehydes, carbonyl monomers have low ceiling temperatures (Table 5-13). Most carbonyl monomers have ceiling temperatures at or appreciably below room temperature. The low \( T_c \) values for carbonyl polymerizations are due primarily to the \( \Delta H \) factor. The entropy of polymerization of the carbonyl double bond in aldehydes is approximately the same as that for the alkene double bond. The enthalpy of polymerization for the carbonyl double bond, however, is appreciably lower. Thus \( \Delta H \) for acetaldehyde polymerization is only about 29 kJ mol\(^{-1}\) compared to the usual 80–90 kJ mol\(^{-1}\) for polymerization of the carbon–carbon double bond (Table 3-14) [Hashimoto et al., 1976, 1978].

Most of the early attempts to polymerize carbonyl compounds were carried out at temperatures that were, in retrospect, too high. The use of temperatures above \( T_c \) resulted in the absence of polymer formation, due to the unfavorable equilibrium between monomer and polymer. Carbonyl monomers were successfully polymerized to high polymer when the
polymerization reactions were carried out at temperatures below the ceiling temperatures of the monomers. Both anionic and cationic initiators, of the types used in alkene polymerizations, can be used to initiate the polymerization of the carbonyl double bond. These polymerizations are similar in their general characteristics to the ionic polymerizations of alkene monomers. The number of detailed mechanistic studies of carbonyl polymerizations is, however, very small.

A characteristic of aldehyde polymerization is the precipitation, often with crystallization, of the polymer during polymerization. Depending on the solvent used, polymerization rate, state of agitation, and other reaction conditions, the polymerization can slow down or even stop because of occlusion of the propagating centers in the precipitated polymer. The physical state and surface area of the precipitated polymer influence polymerization by their effect on the availability of propagating centers and the diffusion of monomer to those centers.

### 5-6a Anionic Polymerization

The carbonyl group is polymerized by a variety of anionic initiators. The strength of the base required to initiate polymerization depends on the substituent(s) attached to the carbonyl group.

#### 5-6a-1 Formaldehyde

The carbonyl group of formaldehyde is highly susceptible to nucleophilic attack and this monomer can be polymerized with almost any base. Metal alkyls, alkoxides, phenolates, and carboxylates, hydrated alumina, amines, phosphines, and pyridine are effective in polymerizing formaldehyde.

The polymerization proceeds as follows:

**Initiation**

\[
\text{A}^- (\text{G}^+) + \text{CH}_2=\text{O} \rightarrow \text{A}^- \text{CH}_2-\text{O}^- (\text{G}^+) \quad (5-126)
\]

**Propagation**

\[
\text{HO} \left\{ \text{CH}_2-\text{O}^- \right\}_n \text{CH}_2-\text{O}^- (\text{G}^+) + \text{CH}_2=\text{O} \rightarrow \text{HO} \left\{ \text{CH}_2-\text{O}^- \right\}_{(n+1)} \text{CH}_2-\text{O}^- (\text{G}^+) \quad (5-127)
\]
**Termination by chain transfer**

\[
\text{HO} \left\{ \text{CH}_2\text{O} \right\}_n\text{CH}_2\text{O}^{-}(\text{G}^+) + \text{ZH} \quad \longrightarrow \quad \text{HO} \left\{ \text{CH}_2\text{O} \right\}_n\text{CH}_2\text{OH} + \text{Z}^-(\text{G}^+)
\]

(5-128)

with initiation by anionic species \( A^- \) to form an alkoxide anion with nearby counterion \( \text{G}^+ \). Propagation proceeds in a like manner and termination occurs by transfer of a proton from \( \text{ZH} \). The chain-transfer agent \( \text{ZH} \) may be any of a variety of compounds that can transfer a proton to the propagating alkoxide anion, such as water or an alcohol. The chain-transfer agent can have an effect on the polymerization rate if \( Z^- \) is not as effective as \( A^- \) in reinitiating polymerization.

### 5-6a-2 Other Carbonyl Monomers

The polymerization of carbonyl monomers other than formaldehyde follows in a similar manner, although the basicity of the initiator required may be quite different. Strong bases are required to initiate the polymerization of aliphatic aldehydes such as acetaldehyde and higher aldehydes [Starr and Vogl, 1978, 1979]. The inductive effect of an alkyl substituent destabilizes the propagating anion \( \text{XLIII} \) by increasing the negative charge density on oxygen. The alkyl group also decreases reactivity for steric reasons. (Steric considerations are probably also responsible for the lower \( T_c \) values relative to formaldehyde.) Thus weak bases such as amines cannot be used to polymerize higher aldehydes than formaldehyde. Alkali metal alkyls and alkoxides are required. The presence of adventitious water is detrimental, since the initiator reacts to form hydroxide ion, which is too weak to initiate polymerization. Ketones are unreactive toward polymerization because of the steric and inductive effects of two alkyl groups. Exceptions to this generalization are some copolymerizations of ketones with formaldehyde and the polymerization of thiocarbonyl monomers [Colomb et al., 1978]

Aromatic aldehydes are also unreactive.

A side reaction occurring with acetaldehyde and higher aldehydes containing \( \alpha \)-hydrogens is aldol condensation [Hashimoto et al., 1976, 1978; Yamamoto et al., 1978]. Aldol reaction can be extensive at ambient temperatures and higher but is avoided by polymerization at low temperature.

The substitution of halogens on the alkyl group of an aliphatic aldehyde greatly enhances its polymerizability (both from the kinetic and thermodynamic view points [Kubisa and Vogl, 1980]. Trichloroacetaldehyde (chloral) is easily polymerized by such weak bases as pyridine, alkali thiocyanates, and even chloride ion. Further, the polymerization of chloral by butyllithium at \(-78^\circ\text{C}\) is complete in less than a second [Busfield and Whalley, 1965]. The electron-withdrawing inductive effect of the halogens acts to stabilize the propagating anion \( \text{XLIV} \) by decreasing the charge density on the negative oxygen.

The effect of halogens on reactivity is also seen for fluorothiocarbonyl monomers. Thio-carbonyl fluoride is polymerized at \(-78^\circ\text{C}\) by a trace of mild base such as dimethylformamide. The polymerization of hexafluorothioacetone is an extreme example of the effect of...
ceiling temperature on polymerization. \( T_c \) is very low but polymerization proceeds smoothly at \(-110^\circ C\).

\[
\begin{array}{c}
\text{S} \\
\text{F} \quad \text{C} \quad \text{F} \\
\text{Thiocarbonyl fluoride}
\end{array}
\quad
\begin{array}{c}
\text{S} \\
\text{CF}_3 \quad \text{C} \quad \text{CF}_3 \\
\text{Hexafluorothioacetone}
\end{array}
\]

Thioacetone polymerizes adventitiously even at very low temperature, in contrast to the inability of acetone to polymerize.

### 5-6b Cationic Polymerization

Carbonyl monomers can be polymerized by acidic initiators, although their reactivity is lower than in anionic polymerization. Protonic acids such as hydrochloric and acetic acids and Lewis acids of the metal halide type are effective in initiating the cationic polymerization of carbonyl monomers. The initiation and propagation steps in polymerizations initiated with protonic acids can be pictured as

\[
\begin{align*}
\text{R} & \quad \text{O} \quad \text{C} \\
\text{H} & \quad \text{HA} \quad \text{HO} \quad \text{C}^+ (A^-) \\
\end{align*}
\]

(5-129)

\[
\begin{align*}
\text{H} \quad \text{O} \quad \text{CHR} \quad \text{O} \quad \text{C} \quad (n+1) \\
\text{H} & \quad \text{H} \quad \text{R} \\
\end{align*}
\]

(5-130)

The termination reaction probably involves chain transfer with water or some other species present.

Competing side reactions in cationic polymerization of carbonyl monomers include cyclotrimerization and acetal interchange. Cyclotrimerization is minimized by low-polarity solvents, low temperatures, and initiators of low acidity. Acetal interchange reactions among different polymer chains do not occur except at higher temperatures. Acetaldehyde and higher aldehydes are reasonably reactive in cationic polymerization compared to formaldehyde. Haloaldehydes are lower in reactivity compared to their nonhalogen counterparts.

### 5-6c Radical Polymerization

The carbonyl double bond has not generally been susceptible to polymerization by radical initiators. There are two reasons for this behavior: (1) the carbonyl group is highly polarized and not prone to attack by a radical; and (2) most radicals are produced at temperatures above the ceiling temperatures of carbonyl monomers. There are, however, a few isolated cases of carbonyl polymerizations by radical initiators. Trifluoroacetaldehyde has been polymerized using benzoyl peroxide at 22°C. The polymerization is slow, with 18 h required to obtain 90% conversion [Busfield and Whalley, 1965]. However, fluorothiocarbonyl monomers such as thiocarbonyl fluoride have been polymerized at high rates by using a trialkylboron–oxygen redox system at \(-78^\circ C\) [Sharkey, 1975]. Thioacetone is also polymerized by this redox system.
Radical polymerizations are observed with these monomers because the electron-withdrawing substituents on the carbonyl and thiocarbonyl group decrease its polarity (and polarizability). The greater susceptibility of the thiocarbonyl double bond to radical polymerization is due to the lower electronegativity of sulfur compared to oxygen. The thiocarbonyl group is less polar than the carbonyl group and more prone to attack by a radical. The successful radical polymerization of thiocarbonyl monomers is also due in large part to the low temperature initiation process employed.

5-6d End Capping

Polyacetals are generally unstable at ambient or moderate temperatures because of facile depolymerization due to their low ceiling temperatures. This limits the commercial utility of most polyacetals. Polyformaldehyde (IUPAC: polyoxymethylene) is an exception to this generalization since its ceiling temperatures is higher than those of other polyacetals. Depolymerization occurs on heating when reactive carbanion or carbocation centers are formed by thermal bond scission at the hydroxyl end groups of polyoxymethylene (POM). The commercial utility of POM is increased when the temperature at which depolymerization occurs is increased, and this is accomplished by converting the less stable hydroxyl end groups into more stable ester groups by reaction with an anhydride:

\[
\text{HO} \quad \overset{\text{CH}_2\text{O}}{\smile} \overset{\text{CH}_2\text{OH}}{\smile} \rightarrow \quad \overset{\text{RCO}}{\text{RCOO}} \quad \overset{\text{CH}_2\text{O}}{\smile} \overset{\text{CH}_2\text{OCOR}}{\smile}
\]  

This reaction is referred to as end capping or end blocking. The result is that reactive carbanion or carbocation centers do not form and depolymerization does not occur at the ceiling temperature of the polymer. The polymer chains are end blocked from depolymerization. The effective ceiling temperature is increased considerably above the ceiling temperature. Acetic anhydride is the usual capping reagent.

The anionic polymerization formaldehyde to POM followed by end capping is carried out commercially. POM (trade name: Delrin) is highly crystalline (60–77%) because of the ease of packing of the simple, polar polymer chains \(T_m = 175^\circ\text{C}\). The commercial products have number-average molecular weights of 20,000–70,000 (PDI ~2). POM has a good combination of properties—high strength; toughness; resistance to creep, fatigue, and abrasion; low coefficient of friction; and low moisture absorption—and is used as an engineering plastic. It has excellent resistance to organic solvents, but the acetal structure is attacked by strong acids. The acetal structure is resistant to attack by base, but bases attack the ester end groups, and this results in depolymerization at higher temperatures. The annual worldwide production of POM is about one billion pounds. A large fraction of this is a copolymer (trade name: Celcon) produced by ring-opening copolymerization of trioxane (the cyclic trimer of formaldehyde) with a small amount of a cyclic ether or acetal compound (Sec. 7-2b-7). Copolymerization accomplishes the same objective as does endcapping. Depolymerization, when it occurs in a copolymer chain, proceeds only until the chain end is the other monomer unit. At that point further depolymerization does not take place. The melting temperature of the copolymer is about 10\(^\circ\text{C}\) lower than the homopolymer but is rated for continuous use at higher temperatures (104 vs. 86\(^\circ\text{C}\)) due to a decreased tendency toward depolymerization. The copolymer is also much more resistant to bases.

The applications of polyoxymethylene include plumbing and hardware (ballcock valves, shower heads, fittings and valves, pump and filter housings), machinery (gears, bearings, rollers, conveyor chains, airflow valves), transportation (fuel pump housing, cooling-fan parts, fuel
caps, window lift mechanisms and cranks, door handles, steering column–gear shift assemblies), appliances (can opener drivetrain, food mixer parts, pump and water sprinkler parts), and electronics (winders, reels, and guide rolls for audio/videocassettes, control disks, gears, transmission parts) [Dolce and Grates, 1985].

## 5-7 MISCELLANEOUS POLYMERIZATIONS

### 5-7a Monomers with Two Different Polymerizable Groups

Most monomers contain only one polymerizable group. There are some monomers with two polymerizable groups per molecule. Polymerization of such monomers can lead to more than one polymer structure. The polymerization of 1,3-dienes, of large industrial importance, is discussed in Sec. 8-6. 1-Substituted-1,2-dienes (*allenes*) undergo polymerization through both the substituted and unsubstituted double bonds

\[
\text{RCH} = \text{C} = \text{CH}_2 \rightarrow \begin{array}{c} \text{CHR} - \text{C} - \text{CHR}_n \\ \text{CH}_2 \\ \text{CHR} \end{array} \quad \text{and} \quad \begin{array}{c} \text{C} - \text{CH}_2 - \text{CHR}_n \\ \text{CH}_2 \end{array}
\]

Various types of initiators have been studied, including ionic, radical, and coordination (Chap. 8) [Ghalamkar-Moazzam and Jacobs, 1978; Leland et al., 1977]. Polymerization through the unsubstituted double bond is the predominant reaction. Some monomers such as acrolein and ketene contain two different types of polymerizable group (C=O and C=C). The polymerization of acrolein has been studied with radical, cationic, and anionic initiators [Calvaryrac et al., 1973; Gulino et al., 1981; Schulz, 1967; Yamashtia et al., 1979]. Radical polymerization proceeds exclusively through the vinyl group

\[
n\text{CH}_2 = \text{CH} \rightarrow \begin{array}{c} \text{CH}_2 - \text{CH} - \text{CHO}_n \\ \text{CHO} \end{array}
\]

Anionic polymerization yields a polymer containing two types of repeating units corresponding to reaction through both the alkene and carbonyl double bonds.

\[
\text{VL Ia} \quad \text{VL Ib}
\]

However, polymerization through the alkene group is the dominant reaction. 1,4-Polymerization also occurs:

\[
n\text{CH}_2 = \text{CH} = \text{O} \rightarrow \begin{array}{c} \text{CH}_2 - \text{CH} = \text{CH} = \text{O} - \text{CHR}_n \\ \text{CH}_2 \end{array}
\]

Cationic polymerization of acrolein has been reported to yield polymers containing both types of repeating units, although one would not expect the alkene group to be reactive toward cationic initiation.

Dimethylketene has been polymerized by anionic initiators. Three different repeat units are formed (XLVII, XLVIII, XLIX) corresponding to polymerization through the alkene group.
double bond, carbonyl double bond, and the two double bonds in an alternating manner, respectively [Pregaglia et al., 1963; Yamashita and Nunamoto, 1962]. Polymerization through the more polar carbonyl group to form the polyacetal is favored by solvents of high polarity. Polymerization of the less polar alkene group, either completely to form the polyketone or partially to form the polyester, is favored by nonpolar solvents. Polyketone formation is favored by Li, Mg, and Al counterions, and polyester by Na and K.

5-7b Hydrogen-Transfer Polymerization of Acrylamide

The polymerization of acrylamide (or methacrylamide) by strong bases such as sodium, organolithium compounds, and alkoxides yields a polymer structure

\[
\text{polyamide structure} \quad \frac{\text{nCH}_2\text{=CHCONH}_2}{\text{CH}_2\text{=CHCONH}_2} \quad \text{polyamide structure}
\]

which is quite unexpected [Bush and Breslow, 1968; Camino et al., 1970, 1977; Otsu et al., 1976]. The polyamide structure of the polymer has been confirmed by the hydrolysis of the polymer to 3-aminopropanoic acid.

The polymerization mechanism involves addition of the anionic initiator to the carbon–carbon double bond of the monomer

\[
\text{B}^- + \text{CH}_2\text{=CHCONH}_2 \rightarrow \text{BCH}_2\text{CHCONH}_2
\]

followed by proton abstraction from another monomer molecule to form the amide anion (L)

\[
\text{BCH}_2\text{CHCONH}_2 + \text{CH}_2\text{=CHCONH}_2 \rightarrow \text{BCH}_2\text{CHCONH}_2 + \text{CH}_2\text{=CHCO}\tilde{\text{N}}\text{H}
\]

The amide anion initiates polymerization via a similar reaction sequence by addition of L to monomer. Propagation follows in a like manner:

\[
\text{CH}_2\text{=CHCONH} + \text{CH}_2\text{CH}_2\text{CONH} + \text{CH}_2\text{CH}_2\text{CONH} + \ldots + \text{CH}_2\text{=CHCO}\tilde{\text{N}}\text{H}
\]

This polymerization follows a path that is quite different than any of the previously discussed polymerizations. The propagating center is not an ion or a radical but is the carbon–carbon double bond at one end of the propagating species L. In addition, it is not the monomer but
the monomer anion $L$ that adds to the propagating center. The evidence for this polymerization mechanism comes from analysis for the alkene end group. This mechanism is very similar to that for the anionic ring-opening polymerization of cyclic amides (Sec. 7-3c). By analogy to the latter, the monomer anion can be referred to as \textit{activated monomer}. The overall polymerization reaction is often referred to as a \textit{hydrogen-transfer polymerization}.

Polymerization of acrylamide does not proceed entirely through the hydrogen-transfer route under all reaction conditions. Polymers with mixed structures, resulting from concurrent hydrogen-transfer polymerization and normal polymerization through the carbon–carbon double bond, occur in some cases. The relative extents of the two modes of propagation are affected by the initiator, solvent, monomer concentration, and temperature [Imanishi, 1989]. The polymerization of $N,N$-dimethylacrylamide proceeds exclusively through the carbon–carbon double bond because there are no amide hydrogens for transfer [Kobayashi et al., 2000; Nakhmanovich et al., 2001].

5-7c\hspace{1em}Polymerization and Cyclotrimerization of Isocyanates

Isocyanates are polymerized through the carbon–nitrogen double bond to 1-nylons by anionic initiators such as metal alkyls, sodium naphthalene, and sodium cyanide [Bur and Fetters, 1976; Dabi and Zilka, 1980; Eromosele and Pepper, 1987; Kresta et al., 1979]. The polymerization has a low ceiling temperature and cyclotrimerization to the isocyanurate is the major reaction at ambient temperatures and above.

5-7d\hspace{1em}Monomers with Triple Bonds

Alkynes have been polymerized using ionic and radical initiators, but the polymer molecular weights are low. High molecular weights are obtained by using Ziegler–Natta coordination catalysts (Sec. 8-4d-2) [Chien et al., 1980]. The polymers are of considerable interest in terms of their potential as (semi)conducting materials.

\begin{equation}
R \mathrm{C}_n \mathrm{CH} \rightarrow \left[ \begin{array}{c} R \\ \mathrm{C} = \mathrm{CH} \end{array} \right]_n
\end{equation}

(5-140)

Nitriles have been polymerized by radical and ionic initiators. The polymer structures are often quite complex, although anionic polymerization yields the cleanest reaction [Wohrle, 1972, 1983; Wohrle and Knothe, 1988].

\begin{equation}
R \mathrm{C}_n \mathrm{N} \rightarrow \left[ \begin{array}{c} R \\ \mathrm{C} = \mathrm{N} \end{array} \right]_n
\end{equation}

(5-141)

Polymerization of isocyanides to polyiminomethylenes is best achieved with cationic initiators, although anionic and radical polymerizations also occur [Millich, 1988].

\begin{equation}
R \mathrm{NC} \rightarrow \left[ \begin{array}{c} \mathrm{NR} \\ \mathrm{C} \end{array} \right]_n
\end{equation}

(5-142)
REFERENCES


REFERENCES


Russell, K. E. and G. J. Wilson, “Cationic Polymerizations,” Chap. 10 in Polymerization Processes, C. E.


5-1 Consider the following monomers and initiating systems:

<table>
<thead>
<tr>
<th>Initiating Systems</th>
<th>Monomers</th>
</tr>
</thead>
<tbody>
<tr>
<td>((\phi\text{CO}_2)_2)</td>
<td>(\phi\text{CH}=\text{CH}_2)</td>
</tr>
<tr>
<td>(\text{CH}_3\text{CCOOH} + \text{Fe}^{2+})</td>
<td>(\text{CH}_2=\text{CHCN})</td>
</tr>
<tr>
<td>(\text{Na} + \text{naphthalene})</td>
<td>(\text{CH}_2=\text{C(\text{CH}_3)_2})</td>
</tr>
<tr>
<td>(\text{H}_2\text{SO}_4)</td>
<td>(\text{CH}_2=\text{CH-O-n-C}_4\text{H}_9)</td>
</tr>
<tr>
<td>(\text{BF}_3 + \text{H}_2\text{O})</td>
<td>(\text{CH}_2=\text{CH-Cl})</td>
</tr>
<tr>
<td>(n-\text{C}_4\text{H}_9\text{Li})</td>
<td>(\text{CH}_2=\text{C(\text{CH}_3)-CO}_2\text{CH}_3)</td>
</tr>
<tr>
<td>&amp; (\text{CH}_2=\text{O})</td>
<td></td>
</tr>
<tr>
<td>&amp; (\text{CF}_2=\text{S})</td>
<td></td>
</tr>
</tbody>
</table>

What is the actual initiating species that initiates polymerization for each of the initiating systems? Show equations. Which initiating system(s) can be used to polymerize each of the various monomers? Explain. What general reaction conditions (e.g., temperature, solvent) are required for each polymerization?

5-2 Isobutylene is polymerized under conditions where chain transfer to monomer is the predominant chain-breaking reaction. A 4.0-g sample of the polymer was found to decolorize 6.0 mL of an 0.01 M solution of bromine in carbon tetrachloride. Calculate the number-average molecular weight of the polyisobutylene.

5-3 The rates of most reactions increase with increasing temperature. For certain polymerizations, the rate decreases with temperature. Under what different conditions can this type of behavior occur? Explain. Consider step polymerizations as well as radical and ionic chain polymerization in answering this question.

5-4 Consider the cationic polymerization of isobutylene using \(\text{SnCl}_4\) as the coinitiator and water as the initiator. Under certain reaction conditions, the polymerization rate was found to be first-order in \(\text{SnCl}_4\), first-order in water, and second-order in isobutylene.
The number-average molecular weight of the initially formed polymer is 20,000. A 1.00-g sample of the polymer contains $3.0 \times 10^{-5}$ moles of OH groups; it does not contain chlorine. Show the reaction sequence of initiation, propagation, and termination steps for this polymerization and derive the appropriate expressions for the rate and degree of polymerization. Indicate clearly any assumptions made in the derivations.

5-5 Under what reaction conditions might a cationic polymerization with SnCl₄ plus water show a dependence of the polymerization rate that is

a. Zero-order in water or SnCl₄
b. Second-order in water or SnCl₄
c. First-order in monomer

5-6 A monomer Z is polymerized in the presence of an initiating system Y. The following experimental observations are made:

a. The degree of polymerization decreases as the reaction temperature increases.
b. The degree of polymerization is affected by the solvent used.
c. The degree of polymerization is first-order in monomer concentration.
d. The rate of polymerization increases as the reaction temperature increases.

Is this polymerization proceeding by a step, radical chain, cationic chain, or anionic chain mechanism? Discuss clearly how each experimental observation is consistent with your answer.

5-7 A 2.0 M solution of styrene in ethylene dichloride is polymerized at 25°C using $4.0 \times 10^{-4}$ M sulfuric acid. Calculate the initial degree of polymerization. What would be the degree of polymerization if the monomer solution contains isopropylbenzene at a concentration of $8.0 \times 10^{-5}$ M? Use the following data as needed: $k_p = 7.6$ L mol⁻¹ s⁻¹, $k_{tr,M} = 1.2 \times 10^{-1}$ L mol⁻¹ s⁻¹, $k_{ts} = 4.9 \times 10^{-2}$ s⁻¹, $k_i$ (combination) = $6.7 \times 10^{-3}$ s⁻¹, $C_s = 4.5 \times 10^{-2}$.

5-8 What experimental approaches are available for determining whether the polymerization of a particular monomer by ionizing radiation proceeds by a radical or ionic mechanism?

5-9 The sodium naphthalene polymerization of methyl methacrylate is carried out in benzene and tetrahydrofuran solutions. Which solution will yield the highest polymerization rate? Discuss the effect of solvent on the relative concentrations of the different types of propagating centers.

5-10 Assume that $1.0 \times 10^{-3}$ mol of sodium naphthalene is dissolved in tetrahydrofuran and then 2.0 mol of styrene is introduced into the system by a rapid injection technique. The final total volume of the solution is 1 liter. Assume that the injection of styrene results in instantaneous homogeneous mixing. It is found that half of the monomer is polymerized in 2000 s. Calculate the propagation rate constant. Calculate the degree of polymerization at 2000 and at 4000 s of reaction time.

5-11 A 1.5 M solution of styrene in tetrahydrofuran is polymerized at 25°C by sodium naphthalene at a concentration of $3.2 \times 10^{-3}$ M. Calculate the polymerization rate and degree of polymerization using appropriate data from Table 5-11. What fractions of the polymerization rate are due to free ions and ion pairs, respectively? Repeat the calculations for $3.2 \times 10^{-2}$ M sodium naphthalene.
5-12 Consider propagation by polystyryl sodium ion pairs in a 1 M styrene solution in tetrahydrofuran. For an ion pair concentration of $2.0 \times 10^{-3} \, M$, calculate the relative contributions of contact and solvent-separated ion pairs to the propagation process. Use appropriate data from Table 5-12.

5-13 Show by equations the synthesis of the following types of block copolymers

a. ABA

b. CABAC

where A, B, and C represent styrene, butadiene, and isoprene, respectively.
For most step polymerizations, for example, in the synthesis of poly(hexamethylene adipamide) or poly(ethylene terephthalate), two reactants or monomers are used in the process, and the polymer obtained contains two different kinds of structures in the chain. This is not the case for chain polymerizations, where only one monomer need be used to produce a polymer. However, chain polymerizations can be carried out with mixtures of two monomers to form polymeric products with two different structures in the polymer chain. This type of chain polymerization process in which two monomers are simultaneously polymerized is termed a **copolymerization**, and the product is a **copolymer**. It is important to stress that the copolymer is not an alloy of two homopolymers but contains units of both monomers incorporated into each copolymer molecule. The process can be depicted as

\[
\text{M}_1 + \text{M}_2 \rightarrow \text{M}_1\text{M}_2\text{M}_1\text{M}_2\text{M}_2\text{M}_1\text{M}_2\text{M}_1\text{M}_2\text{M}_2\text{M}_1\text{M}_1\text{M}_2\text{M}_1\text{M}_1\text{M}_2\text{M}_2\text{M}_1\text{M}_1\text{M}_2\text{M}_2\text{M}_1\text{M}_1\text{M}_2\text{M}_2\text{M}_1\text{M}_1
\]

(6-1)

The two monomers enter into the copolymer in overall amounts determined by their relative concentrations and reactivities. The simultaneous chain polymerization of different monomers can also be carried out with mixtures of three or more monomers. Such polymerizations are generally referred to as **multicomponent copolymerizations**; the term **terpolymerization** is specifically used for systems of three monomers.

Copolymerization is also important in step polymerization. Relatively few studies on step copolymerization have been carried out, although there are considerable commercial applications. Unlike the situation in chain copolymerization, the overall composition of the copolymer obtained in a step copolymerization is usually the same as the feed composition since step reactions must be carried out to close to 100% conversion for the synthesis of
high-molecular-weight polymers. Further, most step polymerizations are equilibrium reactions and the initially formed copolymer composition is rapidly changed by equilibration. This chapter is concerned entirely with chain copolymerization. The main features of step copolymerization have been covered in Sec. 2-13.

6-1 GENERAL CONSIDERATIONS

6-1a Importance of Chain Copolymerization

Chain copolymerization is important from several considerations. Much of our knowledge of the reactivities of monomers, free radicals, carbocations, and carbanions in chain polymerization comes from copolymerization studies. The behavior of monomers in copolymerization reactions is especially useful for studying the effect of chemical structure on reactivity. Copolymerization is also very important from the technological viewpoint. It greatly increases the ability of the polymer scientist to tailor-make a polymer product with specifically desired properties. Polymerization of a single monomer is relatively limited as to the number of different products that are possible. The term homopolymerization is often used to distinguish the polymerization of a single monomer from the copolymerization process.

Copolymerization allows the synthesis of an almost unlimited number of different products by variations in the nature and relative amounts of the two monomer units in the copolymer product. A prime example of the versatility of the copolymerization process is the case of polystyrene. More than 11 billion pounds per year of polystyrene products are produced annually in the United States. Only about one-third of the total is styrene homopolymer. Polystyrene is a brittle plastic with low impact strength and low solvent resistance (Sec. 3-14b). Copolymerization as well as blending greatly increase the usefulness of polystyrene. Styrene copolymers and blends of copolymers are useful not only as plastics but also as elastomers. Thus copolymerization of styrene with acrylonitrile leads to increased impact and solvent resistance, while copolymerization with 1,3-butadiene leads to elastomeric properties. Combinations of styrene, acrylonitrile, and 1,3-butadiene improve all three properties simultaneously. This and other technological applications of copolymerization are discussed further in Sec. 6-8.

6-1b Types of Copolymers

The copolymer described by Eq. 6-1, referred to as a statistical copolymer, has a distribution of the two monomer units along the copolymer chain that follows some statistical law, for example, Bernoullian (zero-order Markov) or first- or second-order Markov. Copolymers formed via Bernoullian processes have the two monomer units distributed randomly and are referred to as random copolymers. The reader is cautioned that the distinction between the terms statistical and random, recommended by IUPAC [IUPAC, 1991, in press], has often not been followed in the literature. Most references use the term random copolymer independent of the type of statistical process involved in synthesizing the copolymer. There are three other types of copolymer structures—alternating, block, and graft. The alternating copolymer contains the two monomer units in equimolar amounts in a regular alternating distribution:
Alternating, statistical, and random copolymers are named by following the prefix *poly* with the names of the two repeating units. The specific type of copolymer is noted by inserting *-alt-, -stat-, or -ran-* in between the names of the two repeating units with *-co-* used when the type of copolymer is not specified, for example, poly(styrene-*alt-*acrylonitrile), poly(styrene-*stat-*acrylonitrile), poly(styrene-*ran-*acrylonitrile), and poly(styrene-*co-*acrylonitrile) [Wilks, 2000].

Block and graft copolymers differ from the other copolymers in that there are long sequences of each monomer in the copolymer chain. A *block* copolymer is a linear copolymer with one or more long uninterrupted sequences of each polymeric species,

\[ \sim M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 \sim \]

II

while a *graft* copolymer is a branched copolymer with a backbone of one monomer to which are attached one or more side chains of another monomer,

\[ \sim M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 M_1 \sim \]

\[ M_2 M_2 M_2 M_2 M_2 M_2 M_2 M_2 M_2 M_2 M_2 M_2 M_2 M_2 M_2 M_2 M_2 M_2 M_2 M_2 M_2 \sim \]

III

This chapter is concerned primarily with the simultaneous polymerization of two monomers to produce statistical and alternating copolymers. The different monomers compete with each other to add to propagating centers, which can be radical or ionic. Graft and block copolymers are not synthesized by the simultaneous and competitive polymerization of two monomers. Each monomer undergoes polymerization alone. A sequence of separate, noncompetitive polymerizations is used to incorporate the different monomers into one polymer chain. The synthesis of block and graft copolymers and variations thereof (e.g., star, comb) are described in Secs. 3-15b-4, 3-15b-5, 5-4, and 9-9.

**6-2 COPOLYMER COMPOSITION**

**6-2a Terminal Model; Monomer Reactivity Ratios**

The *instantaneous copolymer composition*—the composition of the copolymer formed at very low conversions (about <5%)—is usually different from the composition of the comonomer feed from which the copolymer is produced, because different monomers have differing tendencies to undergo copolymerization. It was observed early that the relative copolymerization tendencies of monomers often bore little resemblance to their relative rates of homopolymerization [Staudinger and Schneiders, 1939]. Some monomers are more reactive in copolymerization than indicated by their rates of homopolymerization; other monomers are less reactive. Further, and most dramatically, a few monomers, such as maleic
anhydride and stilbene undergo facile copolymerization with radical initiation, although they have very little or no tendency to undergo homopolymerization.

The composition of a copolymer thus cannot be determined simply from a knowledge of the homopolymerization rates of the two monomers. The determinants of copolymerization composition have been elucidated by several workers by assuming the chemical reactivity of the propagating chain (which may be a free radical, carbocation, or carbanion) in a copolymerization is dependent only on the identity of the monomer unit at the growing end and independent of the chain composition preceding the last monomer unit [Alfrey and Goldfinger, 1944; Mayo and Lewis, 1944; Wall, 1944; Walling, 1957]. This is referred to as the first-order Markov or terminal model of copolymerization. Consider the case for the copolymerization of the two monomers M1 and M2. Although radical copolymerization has been more extensively studied and is more important than ionic copolymerization, we will consider the general case without specification as to whether the mode of initiation is by a radical, anionic, or cationic species. Copolymerization of the two monomers leads to two types of propagating species—one with M1 at the propagating end and the other with M2. These can be represented by M1* and M2* where the asterisk represents either a radical, a carbocation, or a carbanion as the propagating species depending on the particular case. If it is assumed that the reactivity of the propagating species is dependent only on the monomer unit at the end of the chain (referred to as the end or ultimate unit), four propagation reactions are then possible. Monomers M1 and M2 can each add either to a propagating chain ending in M1 or to one ending in M2, that is,

\[
\begin{align*}
M_1^* + M_1 & \rightarrow M_1^* \\ M_1^* + M_2 & \rightarrow M_2^* \\ M_2^* + M_1 & \rightarrow M_1^* \\ M_2^* + M_2 & \rightarrow M_2^*
\end{align*}
\]

where \(k_{11}\) is the rate constant for a propagating chain ending in M1 adding to monomer M1, \(k_{12}\) that for a propagating chain ending in M1 adding to monomer M2, and so on. The propagation of a reactive center by addition of the same monomer (i.e., Reactions 6-2 and 6-5) is often referred to as homopropagation or self-propagation; propagation of a reactive center by addition of the other monomer (Reactions 6-3 and 6-4) is referred to as cross-propagation or a crossover reaction. All propagation reactions are assumed to be irreversible.

Monomer M1 disappears by Reactions 6-2 and 6-4, while monomer M2 disappears by Reactions 6-3 and 6-5. The rates of disappearance of the two monomers, which are synonymous with their rates of entry into the copolymer, are given by

\[
\begin{align*}
-\frac{d[M_1]}{dt} &= k_{11} [M_1^*][M_1] + k_{21} [M_2^*][M_1] \\ -\frac{d[M_2]}{dt} &= k_{12} [M_1^*][M_2] + k_{22} [M_2^*][M_2]
\end{align*}
\]

Dividing Eq. 6-6 by Eq. 6-7 yields the ratio of the rates at which the two monomers enter the copolymer, that is, the copolymer composition, as

\[
\frac{d[M_1]}{d[M_2]} = \frac{k_{11} [M_1^*][M_1] + k_{21} [M_2^*][M_1]}{k_{12} [M_1^*][M_2] + k_{22} [M_2^*][M_2]}
\]
In order to remove the concentration terms in $M_1^*$ and $M_2^*$ from Eq. 6-8, a steady-state concentration is assumed for each of the reactive species $M_1^*$ and $M_2^*$ separately. For the concentrations of $M_1^*$ and $M_2^*$ to remain constant, their rates of interconversion must be equal. In other words, the rates of Reactions 6-3 and 6-4 must be equal:

\[
k_{21}[M_2^*]^{1/2}M_1^* = k_{12}[M_1^*]^{1/2}M_2^*
\]

Equation 6-9 can be rearranged and combined with Eq. 6-8 to yield

\[
\frac{d}{d[M_1]} = \frac{k_{11}k_{21}[M_2^*][M_1]}{k_{12}[M_2^*] + k_{21}[M_2^*][M_1]}
\]

Dividing the top and bottom of the right side of Eq. 6-10 by $k_{21}[M_2^*][M_1]$ and combining the result with the parameters $r_1$ and $r_2$, which are defined by

\[
r_1 = \frac{k_{11}}{k_{12}} \quad \text{and} \quad r_2 = \frac{k_{22}}{k_{21}}
\]

one finally obtains

\[
\frac{d}{d[M_2]} = \frac{[M_1](r_1[M_1] + [M_2])}{[M_2](r_1[M_1] + r_2[M_2])}
\]

Equation 6-12 is known as the copolymerization equation or the copolymer composition equation. The copolymer composition, $d[M_1]/d[M_2]$, is the molar ratio of the two monomer units in the copolymer. $d[M_1]/d[M_2]$ is expressed by Eq. 6-12 as being related to the concentrations of the two monomers in the feed, $[M_1]$ and $[M_2]$, and the parameters $r_1$ and $r_2$. The parameters $r_1$ and $r_2$ are termed the monomer reactivity ratios. Each $r$ as defined above in Eq. 6-11 is the ratio of the rate constant for a reactive propagating species adding its own type of monomer to the rate constant for its addition of the other monomer. The tendency of two monomers to copolymerize is noted by $r$ values between zero and unity. An $r_1$ value greater than unity means that $M_1^*$ preferentially adds $M_1$ instead of $M_2$, while an $r_1$ value less than unity means that $M_1^*$ preferentially adds $M_2$. An $r_1$ value of zero would mean that $M_1$ is incapable of undergoing homopolymerization.

The copolymerization equation can also be expressed in terms of mole fractions instead of concentrations. If $f_1$ and $f_2$ are the mole fractions of monomers $M_1$ and $M_2$ in the feed, and $F_1$ and $F_2$ are the mole fractions of $M_1$ and $M_2$ in the copolymer, then

\[
f_1 = 1 - f_2 = \frac{[M_1]}{[M_1] + [M_2]}
\]

and

\[
F_1 = 1 - F_2 = \frac{d[M_1]}{d[M_1] + d[M_2]}
\]

Combining Eqs. 6-13 and 6-14 with Eq. 6-12 yields

\[
F_1 = \frac{r_1 f_1^2 + f_1 f_2}{r_1 f_1^2 + 2f_1 f_2 + r_2 f_2^2}
\]
or

\[
\frac{F_1}{F_2} = \frac{f_1(r_1 f_1 + f_2)}{f_2(r_2 f_2 + f_1)} \tag{6-15b}
\]

Equation 6-15 gives the copolymer composition as the mole fraction of monomer M_1 in the copolymer and is often more convenient to use than the previous form (Eq. 6-12) of the copolymerization equation.

### 6-2b Statistical Derivation of Copolymerization Equation

Although the derivation above involves the steady-state assumption, the copolymerization equation can also be obtained by a statistical approach without invoking steady-state conditions [Farina, 1990; Goldfinger and Kane, 1948; Melville et al., 1947; Tirrell, 1986; Vollmert, 1973]. We proceed to determine the number-average sequence lengths, \( \bar{n}_1 \) and \( \bar{n}_2 \), of monomers 1 and 2, respectively. \( \bar{n}_1 \) is the average number of M_1 monomer units that follow each other consecutively in a sequence uninterrupted by M_2 units but bounded on each end of the sequence by M_2 units. \( \bar{n}_2 \) is the average number of M_2 monomer units in a sequence uninterrupted by M_1 units but bounded on each end by M_1 units.

The transition or conditional probability \( p_{11} \) of forming a M_1M_1 dyad in the copolymer chain is given by the ratio of the rate for M_1* adding M_1 to the sum of the rates for M_1* adding M_1 and M_2, that is

\[
p_{11} = \frac{R_{11}}{R_{11} + R_{12}} \tag{6-16}
\]

where \( R_{11} \) and \( R_{12} \) are the rates of Reactions 6-2 and 6-3, respectively. Substitution of the expressions for \( R_{11} \) and \( R_{12} \) into Eq. 6-16 yields

\[
p_{11} = \frac{r_1}{r_1 + ([M_2]/[M_1])} \tag{6-17}
\]

Similarly, the transition probabilities \( p_{12} \), \( p_{21} \), and \( p_{22} \) for forming the dyads, M_1M_2, M_2M_1, and M_2M_2, respectively, are given by

\[
p_{12} = \frac{R_{12}}{R_{11} + R_{12}} = \frac{[M_2]}{r_1[M_1] + [M_2]} \tag{6-18}
\]

\[
p_{21} = \frac{R_{21}}{R_{21} + R_{22}} = \frac{[M_1]}{r_2[M_2] + [M_1]} \tag{6-19}
\]

\[
p_{22} = \frac{R_{22}}{R_{21} + R_{22}} = \frac{r_2[M_2]}{r_2[M_2] + [M_1]} \tag{6-20}
\]

where \( R_{21} \) and \( R_{22} \) are the rates of Reactions 6-4 and 6-5, respectively.

The sum of the transition probabilities of addition to M_1\(^{\#}\) and M_2\(^{\#}\) are each, separately, equal to 1:

\[
p_{11} + p_{12} = 1 \tag{6-21a}
\]

\[
p_{21} + p_{22} = 1 \tag{6-21b}
\]
The number-average sequence length \( \bar{n}_1 \) of monomer \( M_1 \) is

\[
\bar{n}_1 = \sum_{x=1}^{\infty} x \langle N_x \rangle = \langle N_1 \rangle_1 + 2 \langle N_1 \rangle_2 + 3 \langle N_1 \rangle_3 + 4 \langle N_1 \rangle_4 + \cdots \quad (6-22)
\]

where \( \langle N_x \rangle \) is the mole fraction of a sequence of \( M_1 \) units of length \( x \) and the summation is over all-sized sequence lengths from 1 to infinity. \( \langle N_1 \rangle \) is the probability of forming such a sequence and is given by

\[
\langle N_1 \rangle = (p_{11})^{x-1} p_{12} \quad (6-23)
\]

The meaning of Eq. 6-23 can be seen by considering, for example, the probability of forming a sequence \( M_1M_1M_1 \). The probability of forming such a sequence is the probability \( p_{11} \) of \( M_1^* \) adding \( M_1 \) multiplied by the probability \( p_{11} \) of a second addition of \( M_1 \) multiplied by the probability \( p_{12} \) of addition of \( M_2 \) or \( p_{11}^3 p_{12} \).

\[
\bar{n}_1 = p_{12}(1 + 2p_{11} + 3p_{11}^2 + 4p_{11}^3 + \cdots) \quad (6-24)
\]

For \( p_{11} < 1 \), which holds in a copolymerization, the expansion series in Eq. 6-24 is \( 1/(1-p_{11})^2 \) and Eq. 6-24 becomes

\[
\bar{n}_1 = \frac{p_{12}}{(1-p_{11})^2} = \frac{1}{p_{12}} = \frac{r_1[M_1] + [M_2]}{[M_2]} \quad (6-25)
\]

In a similar manner one obtains

\[
\bar{n}_2 = \frac{p_{21}}{(1-p_{22})^2} = \frac{1}{p_{21}} = \frac{r_2[M_2] + [M_1]}{[M_1]} \quad (6-26)
\]

The mole ratio of monomers \( M_1 \) and \( M_2 \) contained in the copolymer is given by the ratio of the two number-average sequence lengths

\[
\frac{\bar{n}_1}{\bar{n}_2} = \frac{d[M_1]}{d[M_2]} = \frac{[M_1](r_1[M_1] + [M_2])}{[M_2](r_2[M_2] + [M_1])} \quad (6-27)
\]

which is exactly the same result as Eq. 6-12 (and Eq. 6-15). Thus the copolymerization equation holds for copolymerizations carried out under both steady-state and non-steady-state conditions provided that the reactivity of a propagating species is dependent only on the ultimate unit, depropagation does not occur, and high polymer is formed. Equation 6-27 (also 6-12 and 6-15) describes the \textit{first-order Markov or terminal model} of copolymerization.

\section*{6-2c Range of Applicability of Copolymerization Equation}

The copolymerization equation has been experimentally verified in innumerable comonomer systems. The copolymerization equation is equally applicable to radical, cationic, and anionic chain copolymerizations, although the \( r_1 \) and \( r_2 \) values for any particular comonomer pair can be drastically different depending on the mode of initiation.

Ionic copolymerizations are predictably much more selective than radical copolymerizations. Almost any pair of monomers undergoes radical copolymerization, in line with the
reactivity of almost all monomers in radical polymerization (Sec. 3-1b). However, only certain comonomer pairs undergo cationic or anionic copolymerization. For example, both styrene–acrylonitrile and styrene–ethyl vinyl ether undergo radical copolymerization, but there is great selectivity in ionic copolymerizations. Styrene–acrylonitrile undergoes anionic copolymerization, but not cationic copolymerization. Styrene–ethyl vinyl ether undergoes cationic copolymerization, but not anionic copolymerization.

For any specific type of initiation (i.e., radical, cationic, or anionic) the monomer reactivity ratios and therefore the copolymer composition equation are independent of many reaction parameters. Since termination and initiation rate constants are not involved, the copolymer composition is independent of differences in the rates of initiation and termination or of the absence or presence of inhibitors or chain-transfer agents. Under a wide range of conditions the copolymer composition is independent of the degree of polymerization. The only limitation on this generalization is that the copolymer be a high polymer. Further, the particular initiation system used in a radical copolymerization has no effect on copolymer composition. The same copolymer composition is obtained irrespective of whether initiation occurs by the thermal homolysis of initiators such as AIBN or peroxides, redox, photolysis, or radiolysis. Solvent effects on copolymer composition are found in some radical copolymerizations (Sec. 6-3a). Ionic copolymerizations usually show significant effects of solvent as well as counterion on copolymer composition (Sec. 6-4).

The monomer reactivity ratios and copolymer compositions in living copolymerizations are generally the same as those in the corresponding nonliving systems. However, Matyjaszewski [2002] has described reaction conditions that result in deviations in copolymer compositions for some living systems. The differences arise not from differences in monomer reactivity ratios, but from differences in the consumption of the two monomers. The effect is observed in living systems where there is a recycling equilibrium (activation and deactivation) between active and dormant species. This applies to radical systems such as ATRP, NMP, and RAFT, as well as many ionic systems, which involve an activation and deactivation equilibrium. For a copolymerization, there is a separate activation–deactivation equilibrium for each of two different propagating species (M1* and M2*). Deviations are possible only when two conditions exist. First, the two propagating species must have different activation and/or deactivation rate constants. Second, the homopropagation rate constant for each propagating species must be different from its cross-propagation rate constant; in other words, both r1 and r2 are not one. Under these conditions, one of the monomers is consumed faster than in the corresponding nonliving system. The comonomer feed and, therefore, the copolymer composition, change with conversion differently from the nonliving system. The deviations in copolymer composition are greater when homopropagation is faster than cross-propagation (r1, r2 > 1) than when cross-propagation is faster than homopropagation (r1, r2 < 1).

6-2d Types of Copolymerization Behavior

Different types of copolymerization behavior are observed depending on the values of the monomer reactivity ratios. Copolymerizations can be classified into three types based on whether the product of the two monomer reactivity ratios r1r2 is unity, less than unity, or greater than unity.

6-2d-1 Ideal Copolymerization: r1 r2 = 1

A copolymerization is termed ideal when the r1r2 product is unity. Ideal copolymerization occurs when the two types of propagating species M1* and M2* show the same preference for
adding one or the other of the two monomers. Under these conditions

\[
\frac{k_{22}}{k_{21}} = \frac{k_{12}}{k_{11}} \quad \text{or} \quad r_2 = \frac{1}{r_1}
\]

(6-28)

and the relative rates of incorporation of the two monomers into the copolymer are independent of the identity of the unit at the end of the propagating species. For an ideal copolymerization Eq. 6-28 is combined with Eq. 6-12 or 6-15 to yield the copolymerization equation as

\[
\frac{d[M_1]}{d[M_2]} = \frac{r_1[M_1]}{[M_2]} \quad \text{(6-29a)}
\]

or

\[
F_1 = \frac{r_1 f_1}{r_1 f_1 + f_2} \quad \text{(6-29b)}
\]

Most ionic copolymerizations (both anionic and cationic) are characterized by the ideal type of behavior.

When \( r_1 = r_2 = 1 \), the two monomers show equal reactivities toward both propagating species. The copolymer composition is the same as the comonomer feed with a random placement of the two monomers along the copolymer chain. Such behavior is referred to as \textit{random} or \textit{Bernoullian}. For the case where the two monomer reactivity ratios are different, that is, \( r_1 > 1 \) and \( r_2 < 1 \) or \( r_1 < 1 \) and \( r_2 > 1 \), one of the monomers is more reactive than the other toward both propagating species. The copolymer will contain a larger proportion of the more reactive monomer in random placement.

Figure 6-1 shows the variation in the copolymer composition as a function of the comonomer feed composition for different values of \( r_1 \) [Mayo and Walling, 1950]. The term \textit{ideal}
copolymersation is used to show the analogy between the curves in Fig. 6-1 and those for vapor–liquid equilibria in ideal liquid mixtures. The copolymer is richer in \( M_1 \) when \( r_1 > 1 \) and is poorer in \( M_1 \) when \( r_1 < 1 \).

One can distinguish between extreme and moderate ideal behavior depending on the difference between \( r_1 \) and \( r_2 \). Extreme ideal behavior occurs when \( r_1 \) and \( r_2 \) are very different (e.g., 10 and 1). Moderate ideal behavior occurs when \( r_1 \) and \( r_2 \) are not too different, (e.g., 0.5 and 2). The term ideal copolymerization does not in any sense connote a desirable process. An important consequence of ideal copolymerizations is that it becomes progressively more difficult to produce copolymers containing appreciable amounts of both monomers as the difference in \( r_1 \) and \( r_2 \) increases, that is, as one progresses from moderate to extreme ideal behavior. When, for example, \( r_1 = 10 \) and \( r_2 = 0.1 \), copolymers containing appreciable amounts of \( M_2 \) cannot be obtained. Thus a comonomer feed composition of 80 mol% \( M_2 \) \((f_2 = 0.8)\) would yield a copolymer containing only 18.5 mol% \( M_2 \) \((F_2 = 0.185)\). It is only when \( r_1 \) and \( r_2 \) do not differ markedly (e.g., \( r_1 = 0.5–2 \)) that there will exist a larger range of comonomer feed compositions, which yield copolymers containing appreciable amounts of both monomers.

6-2d-2 Alternating Copolymerization: \( r_1r_2 = 0 \)

Alternating copolymerization is characterized by \( r_1r_2 = 0 \), where neither \( r_1 \) nor \( r_2 \) is greater than one. As with ideal behavior, there are two types of alternating behavior—extreme and moderate alternating behavior. Both \( r_1 \) and \( r_2 \) are zero in extreme alternating behavior, and the two monomers enter into the copolymer in equimolar amounts in a nonrandom, alternating arrangement along the copolymer chain. Each of the two types of propagating species preferentially adds the other monomer, that is, \( M_1^* \) adds only \( M_2 \) and \( M_2^* \) adds only \( M_1 \). The copolymerization equation reduces to

\[
\frac{d[M_1]}{d[M_2]} = 1 \tag{6-30a}
\]

or

\[
F_1 = 0.5 \tag{6-30b}
\]

The copolymer has the alternating structure I irrespective of the comonomer feed composition. Moderate alternating behavior occurs when either (1) both \( r_1 \) and \( r_2 \) are small \((r_1r_2 = \text{very small, close to } 0)\) or (2) one \( r \) value is small and the other \( r \) is zero \((r_1r_2 = 0)\). The copolymer composition tends toward alternation but is not the perfectly alternating structure I.

The behavior of most comonomer systems lies between the two extremes of ideal and alternating copolymerization. As the \( r_1r_2 \) product decreases from one toward zero, there is an increasing tendency toward alternation. Perfect alternation occurs when \( r_1 \) and \( r_2 \) are both zero. The tendency toward alternation and the tendency away from ideal behavior increases as \( r_1 \) and \( r_2 \) become progressively less than unity. The range of behaviors can be seen by considering the situation where \( r_2 \) remains constant at 0.5 and \( r_1 \) varies between 2 and 0. Figure 6-2 shows the copolymer composition as a function of the feed composition in these cases. The curve for \( r_1 = 2 \) shows the ideal type of behavior described previously. As \( r_1 \) decreases below 2, there is an increasing tendency toward the alternating behavior with each type of propagating species preferring to add the other monomer. The increasing
alternation tendency is measured by the tendency of the product $r_1 r_2$ to approach zero. Of great practical significance is the fact that a larger range of feed compositions will yield copolymers containing sizable amounts of both monomers. However, when $r_1 r_2$ is very small or zero the alternation tendency is too great and the range of copolymer compositions that can be obtained is again limited. In the extreme case where both $r_1$ and $r_2$ are zero, only the 1 : 1 alternating copolymer can be produced. This would show in Fig. 6-2 as a horizontal line at $F_1 = 0.5$ (but the line would not touch either the left or right ordinates).

The plots in Fig. 6-2 illustrate an interesting characteristic of copolymerizations with a tendency toward alternation. For values of $r_1$ and $r_2$ both less than unity, the $F_1/f_1$ plots cross the line representing $F_1 = f_1$. At these intersections or crossover points the copolymer and feed compositions are the same and copolymerization occurs without a change in the feed composition. Such copolymerizations are termed azeotropic copolymerizations. The condition under which azeotropic copolymerization occurs, obtained by combination of Eq. 6-12 with $d[M_1]/d[M_2] = [M_1]/[M_2]$, is

$$\frac{[M_1]}{[M_2]} = \frac{(r_2 - 1)}{(r_1 - 1)} \quad (6-31a)$$

or

$$f_1 = \frac{(1 - r_2)}{(2 - r_1 - r_2)} \quad (6-31b)$$
A special situation arises when one of the monomer reactivity ratios is much larger than
the other. For the case of \( r_1 \gg r_2 \) (i.e., \( r_1 \gg 1 \) and \( r_2 \ll 1 \)), both types of propagating species
preferentially add monomer M₁. There is a tendency toward consecutive homopolymerization
of the two monomers. Monomer M₁ tends to homopolymerize until it is consumed; monomer
M₂ will subsequently homopolymerize. An extreme example of this type of behavior is
shown by the radical polymerization of styrene-vinyl acetate with monomer reactivity ratios
of 55 and 0.01. (See Sec. 6-3b-1 for a further discussion of this comonomer system.)

6-2d-3  Block Copolymerization: \( r_1 > 1, r_2 > 1 \)

If both \( r_1 \) and \( r_2 \) are greater than unity (and therefore, also \( r_1 r_2 > 1 \)) there is a tendency to
form a block copolymer (structure II) in which there are blocks of both monomers in the
chain. This type of behavior is rarely encountered.

6-2e  Variation of Copolymer Composition with Conversion

The various forms of the copolymerization equation (Eqs. 6-12 and 6-15) give the instantaneous copolymer composition—the composition of the copolymer formed from a particular feed composition at very low conversion (approximately <5%) such that the composition of the comonomer feed is relatively unchanged from its initial value. For all copolymerizations except azeotropic copolymerizations the comonomer feed and copolymer compositions are different. The comonomer feed changes in composition as one of the monomers preferentially enters the copolymer. Thus there is a drift in the comonomer composition toward the less reactive monomer as the degree of conversion increases. This results in a similar variation of copolymer composition with conversion. In order to determine the instantaneous copolymer composition as a function of conversion for any given comonomer feed, one must resort to an integrated form of the copolymerization equation. Direct integration of Eq. 6-12 for this purpose has resulted in solutions of varying utility [Kruse, 1967; Mayo and Lewis, 1944; Van der Meer et al., 1978; Wall, 1944].

A useful method for analyzing copolymer composition as a function of conversion is that developed by Skeist [1946]. Consider a system initially containing a total of M moles of the two monomers and in which the copolymer formed is richer in monomer M₁ that is the feed (i.e., \( F_1 > f_1 \)). When \( dM \) moles of monomers have been copolymerized, the polymer will contain \( F_1 dM \) moles of monomer 1 and the feed will contain \( (M - dM)(f_1 - d_f_1) \) moles of monomer 1. A material balance for monomer 1 requires that the moles of M₁ copolymerized equal the difference in the moles of M₁ in the feed before and after reaction, or

\[
M f_1 - (M - dM)(f_1 - d_f_1) = F_1 dM 
\] (6-32)

Equation 6-32 can be rearranged (neglecting the \( df_1 dM \) term, which is small) and converted to the integral form

\[
\int_{M_0}^{M} \frac{dM}{M} = \ln \frac{M}{M_0} = \int_{(f_1)_0}^{f_1} \frac{df_1}{f_1 - f_1} 
\] (6-33)

where \( M_0 \) and \( (f_1)_0 \) are the initial values of M and \( f_1 \).

Equation 6-15 allows the calculation of \( F_1 \) as a function of \( f_1 \) for a given set of \( r_1 \) and \( r_2 \) values. These can then be employed as \( (F_1 - f_1) \) to allow the graphical or numerical integration of Eq. 6-33 between the limits of \( (f_1)_0 \) and \( f_1 \). In this manner one can obtain the
variations in the feed and copolymer compositions with the degree of conversion (defined as $1 - M/M_0$).

Equation 6-33 has been integrated to the useful closed form

$$1 - \frac{M}{M_0} = 1 - \left[ \frac{f_1}{(f_1)_0} \right]^\alpha \left[ \frac{f_2}{(f_2)_0} \right]^\beta \left[ \frac{(f_1)_0 - \delta}{f_1 - \delta} \right]$$

which relates the degree of conversion to changes in the comonomer feed composition [Dionisio and O’Driscoll, 1979; Meyer and Chan, 1968; Meyer and Lowry, 1965]. The zero subscripts indicate initial quantities and the other symbols are given by

$$\alpha = \frac{r_2}{(1 - r_2)} \quad \beta = \frac{r_1}{(1 - r_1)}$$

$$\gamma = \frac{(1 - r_1 r_2)}{(1 - r_1)(1 - r_2)} \quad \delta = \frac{(1 - r_2)}{(2 - r_1 - r_2)}$$

Equation 6-34 or its equivalent has been used to correlate the drift in the feed and copolymer compositions with conversion for a number of different copolymerization systems [Capek et al., 1983; O’Driscoll et al., 1984; Stejskal et al., 1986; Teramachi et al., 1985]. The larger the difference in the $r_1$ and $r_2$ values of a comonomer pair, the greater is the variation in copolymer composition with conversion [Dadmun, 2001].

A few examples will illustrate the utility of Eqs. 6-33 and 6-34. Figure 6-3 shows the behavior observed in the radical copolymerization of styrene and methyl methacrylate. $F_1$ and $F_2$ are the instantaneous copolymer compositions for the instantaneous feed

![Figure 6-3 Variations in feed and copolymer compositions with conversion for styrene ($M_1$)-methyl methacrylate ($M_2$) with $(f_1)_0 = 0.80$, $(f_2)_0 = 0.20$ and $r_1 = 0.53$, $r_2 = 0.56$. After Dionisio and O’Driscoll [1979] (by permission of Wiley, New York).](image-url)
compositions $f_1$ and $f_2$, respectively. The average or cumulative composition of the copolymer as a function of conversion is also shown. The copolymer produced is slightly richer in methyl methacrylate than the feed because methyl methacrylate has a slightly larger monomer reactivity ratio than styrene. The feed becomes richer in styrene with conversion—leading to an increase in the styrene content of the copolymer with conversion. Figure 6-3 also shows the average composition of all the copolymer formed up to some degree of conversion as a function of conversion. The average copolymer composition becomes richer in styrene than methyl methacrylate but less so than the instantaneous copolymer composition.

One can show the drift of copolymer composition with conversion for various comonomer feed compositions by a three-dimensional plot such as that in Fig. 6-4 for the radical copolymerization of styrene ($M_1$)-2-vinylthiophene ($M_2$) with $r_1 = 0.35$ and $r_2 = 3.10$. This is an ideal copolymerization with $r_1 = 0.35$ and $r_2 = 3.10$. The greater reactivity of the 2-vinylthiophene results in its being incorporated preferentially into the first-formed copolymer. As the reaction proceeds, the feed and therefore the copolymer become progressively enriched in styrene. This is shown by Fig. 6-5, which describes the distribution of copolymer compositions at 100% conversion for several different initial feeds.

Corresponding data for the alternating radical copolymerization of styrene ($M_1$)-diethyl fumarate ($M_2$)($r_1 = 0.30$ and $r_2 = 0.07$) are shown in Figs. 6-6 and 6-7. This system undergoes azeotropic copolymerization at 57 mol% styrene. Feed compositions near the azeotrope yield narrow distributions of copolymer composition except at high conversion where there is a drift to pure styrene or pure fumarate depending on whether the initial feed contains more or less than 57 mol% styrene. The distribution of copolymer compositions becomes progressively wider as the initial feed composition differs more from the azeotropic composition.
Fig. 6-5  Distribution of copolymer composition at 100% conversion for styrene–2-vinylthiophene at the indicated values of mole fraction styrene in the initial comonomer feed. After Billmeyer [1984] (by permission of Wiley-Interscience, New York) from plot in Mayo and Walling [1950] (by permission of American Chemical Society, Washington, DC).

Fig. 6-6  Dependence of the instantaneous copolymer composition $F_1$ on the initial comonomer feed composition $f_1$ and the percent conversion of styrene ($M_1$)-diethyl fumarate ($M_2$) with $r_1 = 0.30$ and $r_2 = 0.07$. After Walling [1957] (by permission of Wiley, New York) from plot in Mayo and Walling [1950] (by permission of American Chemical Society, Washington, DC).
In the commercial use of copolymerization it is usually desirable to obtain a copolymer with as narrow a distribution of compositions as possible, since polymer properties (and therefore utilization) are often highly dependent on copolymer composition [Athey, 1978]. Two approaches are simultaneously used to minimize heterogeneity in the copolymer composition. One is the choice of comonomers. Choosing a pair of monomers whose copolymerization behavior is such that $F_1$ is not too different from $f_1$ is highly desirable as long as that copolymer has the desired properties. The other approach is to maintain the feed composition approximately constant by the batchwise or continuous addition of the more reactive monomer. The control necessary in maintaining $f_1$ constant depends on the extent to which the copolymer composition differs from the feed.

Although the monomer reactivity ratios in living radical polymerizations are generally the same as in nonliving polymerizations, there is a difference in the distribution of copolymer compositions for different polymer molecules [Hawker et al., 2001; Matyjaszewski and Xia, 2001]. All polymer chains do not have the same composition in nonliving systems because chains are initiated at different times in a polymerization and propagate under different feed compositions as conversion progresses. Almost all polymer chains have the same composition in living systems because all chains are initiated at time close to zero and propagate

![Fig. 6-7](image-url)
throughout the reaction. Even though there is a gradient in copolymer composition with time, all chains have the same composition gradient.

The synthesis of a gradient copolymer is sometimes desirable in a living polymerization to produce a copolymer with a variation in composition along the polymer chain. This is achieved either by carrying out the copolymerization without addition of monomer to maintain a constant feed composition or addition of monomer to deliberately change the feed composition from its original state.

6-2f Experimental Evaluation of Monomer Reactivity Ratios

Most procedures for evaluating $r_1$ and $r_2$ involve the experimental determination of the copolymer composition for several different comonomer feed compositions in conjunction with a differential form of the copolymerization equation (Eq. 6-12 or 6-15). Copolymerizations are carried out to as low degrees of conversion as possible (about $<5\%$) to minimize errors in the use of the differential equation. The copolymer composition is determined either directly by analysis of the copolymer or indirectly by analysis of comonomer feed. The techniques used for copolymer analysis include radioisotopic labeling and spectroscopy (IR, UV, NMR). Comonomer feed compositions are typically analyzed by high-pressure liquid chromatography (HPLC) or gas chromatography (GC). The techniques for analyzing comonomer compositions are inherently more sensitive than those for copolymer composition. However, this is offset by the fact that the determination of copolymer composition by comonomer feed analysis requires the measurement of small differences between large numbers.

Various methods have been used to obtain monomer reactivity ratios from the copolymer composition data. The most often used method involves a rearrangement of the copolymer composition equation into a form linear in the monomer reactivity ratios. Mayo and Lewis [1944] rearranged Eq. 6-12 to

$$r_2 = \frac{[M_1]}{[M_2]} \left( \frac{d[M_2]}{d[M_1]} \left( 1 + \frac{r_1 [M_1]}{[M_2]} \right) - 1 \right)$$

(6-36)

Data for the feed and copolymer compositions for each experiment with a given feed are substituted into Eq. 6-36 and $r_2$ is plotted as a function of various assumed values of $r_1$. Each experiment yields a straight line and the intersection of the lines for different feeds gives the best values of $r_1$ and $r_2$. Any variations observed in the points of intersection of various lines are a measure of the experimental errors in the composition data and the limitations of the mathematical treatment (see below). The composition data can also be treated by linear least-squares regression analysis instead of the graphical analysis.

Fineman and Ross [1950] rearranged Eq. 6-15 to

$$G = r_1 F - r_2$$

(6-37)

where $G = X(Y - 1)/Y, F = X^2/Y, X = [M_1]/[M_2]$, and $Y = d[M_1]/d[M_2]$. $G$ is plotted against $F$ to yield a straight line with slope $r_1$ and intercept $r_2$.

The experimental composition data are unequally weighted by the Mayo–Lewis and Fineman–Ross plots with the data for the high or low compositions (depending on the equation used) having the greatest effect on the calculated values of $r_1$ and $r_2$ [Tidwell and Mortimer, 1965, 1970]. This often manifests itself by different values of $r_1$ and $r_2$ depending on which monomer is indexed as $M_1$.

Kelen and Tudos [1975] refined the linearization method by introducing an arbitrary positive constant $\alpha$ into Eq. 6-37 to spread the data more evenly so as to give equal weight to all
data points. Their results are expressed in the form

\[ Z = r_1 + \frac{r_2}{x} \left( \frac{x}{C_0} \right)^{r_2} \]

where

\[ \eta = \frac{G}{\alpha + F} \] \hspace{1cm} (6-39a)

\[ \xi = \frac{F}{\alpha + F} \] \hspace{1cm} (6-39b)

Plotting \( \eta \) against \( \xi \) gives a straight line that yields \(-r_2/\alpha \) and \( r_1 \) as intercepts on extrapolation to \( \xi = 0 \) and \( \xi = 1 \), respectively. The value of \( \alpha \), chosen as \( \alpha = (F_m F_M)^{1/2} \) where \( F_m \) and \( F_M \) are the lowest and highest \( F \) values, respectively, distributes the experimental data symmetrically on the plot.

Even with the Kelen–Tudos refinement there are statistical limitations inherent in the linearization method. The independent variable in any form of the linear equation is not really independent, while the dependent variable does not have a constant variance [O’Driscoll and Reilly, 1987]. The most statistically sound method of analyzing composition data is the non-linear method, which involves plotting the instantaneous copolymer composition versus comonomer feed composition for various feeds and then determining which theoretical plot best fits the data by trial-and-error selection of \( r_1 \) and \( r_2 \) values. The pros and cons of the two methods have been discussed in detail, along with approaches for the best choice of feed compositions to maximize the accuracy of the \( r_1 \) and \( r_2 \) values [Bataille and Bourassa, 1989; Habibi et al., 2003; Hautus et al., 1984; Kelen and Tudos, 1990; Leicht and Fuhrmann, 1983; Monett et al., 2002; Tudos and Kelen, 1981].

The use of a differential form of the copolymerization equation assumes that the feed composition does not change during the experiment, but this is not true. One holds the conversion as low as possible, but there are limitations since one must be able to isolate a sample of the copolymer for direct analysis (or, if copolymer analysis is via the change in feed composition, there must be a significantly measurable change in the feed composition). The use of an integrated form of the copolymerization equation does not have this limitation [Hamielec et al., 1989; O’Driscoll and Reilly, 1987; Plaumann and Branston, 1989]. The change in copolymer composition or feed composition with conversion is measured and the results curve fitted to an integrated form of the copolymerization equation. For example, one method uses the previously described Eq. 6-34 [Meyer, 1966]. Experimental data on the variation of feed composition with conversion are plotted as \( f_1 \) or \( f_2 \) versus \( 1-M/M_0 \) to yield curves like those in Fig. 6-3. Using computational procedures, one then determines the best values of \( r_1 \) and \( r_2 \) that must be used with Eq. 6-34 to yield the same plot.

6-2g Microstructure of Copolymers

6-2g-1 Sequence Length Distribution

The copolymerization equation describes the copolymer composition on a macroscopic scale, that is, the overall composition of a copolymer sample produced from a comonomer feed. This leaves unanswered two details concerning composition copolymer. The first concerns the exact arrangement of the two monomers along the polymer chain. Although the
copolymers produced by copolymerization are often referred to as random copolymers, this term is inappropriate, since it indicates that the two monomer units are randomly placed along the copolymer chain. This only occurs for the case \( r_1 = r_2 = 1 \). There is a definite trend toward a regular microstructure for all other cases. For example, if \( r_1 > 1 \), once a propagating species of type \( M_1^* \) is formed, it will tend to a sequence of \( M_1 \) units. \( M_1^* \) will tend to add the other monomer unit if \( r_1 < 1 \). However, there is a random aspect to copolymerization due to the probabilistic nature of chemical reactions. Thus, an \( r_1 \) value of 2 does not imply that 100% of all \( M_1 \) units will be found as part of \( M_1M_1M_1M_2 \) sequences. A very large fraction of, but not all, \( M_1 \) units will be found in such a sequence; a small fraction of \( M_1 \) units will be randomly distributed.

The microstructure of a copolymer is defined by the distributions of the various lengths of the \( M_1 \) and \( M_2 \) sequences, that is, the sequence length distributions. The probabilities or mole fractions \( (N_1)_x \) and \( (N_2)_x \) of forming \( M_1 \) and \( M_2 \) sequences of length \( x \) are given (Sec. 6-2b) by

\[
(N_1)_x = (p_{11})^{(x-1)}p_{12} \tag{6-23}
\]

\[
(N_2)_x = (p_{22})^{(x-1)}p_{21} \tag{6-40}
\]

where the \( p \) values are defined by Eqs. 6-17 through 6-20. Equations 6-23 and 6-40 allow one to calculate the mole fractions of different lengths of \( M_1 \) and \( M_2 \) sequences. Distributions for a number of copolymerization systems have been described [Tirrell, 1986; Tosi, 1967–1968; Vollmert, 1973]. Figure 6-8 shows the sequence length distribution for an ideal copolymerization with \( r_1 = r_2 = 1 \) for an equimolar feed composition \( (f_1 = 0.5) \). For this system

![Fig. 6-8](https://example.com/fig68.png)
Although the most plentiful sequence is $M_1$ at 50%, there are considerable amounts of other sequences: 25%, 12.5%, 6.25%, 3.13%, 1.56%, and 0.78%, respectively, of dyad, triad, tetrad, pentad, hexad, and heptad sequences. The distribution of $M_2$ sequences is exactly the same as for $M_1$ sequences. For a feed composition other than equimolar, the distribution becomes narrower for the monomer present in lower amount and broader for the monomer in larger amount—a general phenomenon observed for all sequence length distributions. It is clear that the copolymer, with an overall composition of $F_1 = F_2 = 0.50$, has a microstructure that is very different from that of a perfectly alternating copolymer.

The sequence length distribution for an ideal copolymerization with $r_1 = 5$, $r_2 = 0.2$ and $f_1 = f_2$. $(N_1)_x$ is represented by ---; $(N_2)_x$, by - - - . The plots for $(N_2)_x$ are shown slightly to the left of the actual sequence length. After Vollmert (transl. Immergut) [1973] (by permission of Springer-Verlag New York, Inc., New York).

$\frac{p_{11}}{p_{12}} = \frac{p_{22}}{p_{21}} = 0.50$. Although the most plentiful sequence is $M_1$ at 50%, there are considerable amounts of other sequences: 25%, 12.5%, 6.25%, 3.13%, 1.56%, and 0.78%, respectively, of dyad, triad, tetrad, pentad, hexad, and heptad sequences. The distribution of $M_2$ sequences is exactly the same as for $M_1$ sequences. For a feed composition other than equimolar, the distribution becomes narrower for the monomer present in lower amount and broader for the monomer in larger amount—a general phenomenon observed for all sequence length distributions. It is clear that the copolymer, with an overall composition of $F_1 = F_2 = 0.50$, has a microstructure that is very different from that of a perfectly alternating copolymer.

The sequence length distribution for an ideal copolymerization with $r_1 = 5$, $r_2 = 0.2$ for an equimolar feed composition is shown in Fig. 6-9. This copolymerization has $p_{11} = p_{21} = 0.8333$ and $p_{12} = p_{22} = 0.1667$. Both $M_1^*$ and $M_2^*$ propagating centers have a 5 : 1 tendency to add $M_1$ over $M_2$, but $M_1$ pentad sequences are not the most plentiful, although they are among the most plentiful. The most plentiful sequence is $M_1$ at 16.7% with 14.0%, 11.6%, 9.7%, 8.1%, 6.7%, 5.6%, and 4.7%, respectively, of dyad, triad, tetrad, pentad, hexad, heptad, and octad $M_1$ sequences. There are smaller amounts of longer sequences: 3.2% of 10-unit, 1.3% of 15-unit, and 0.4% of 20-unit $M_1$ sequences. The sequence length distribution is much narrower for the less reactive $M_2$ monomer. Single $M_1$ units are by far the most plentiful (83.3%) with 13.9% dyads, 2.3% triads, and 0.39% tetrads.

An alternating copolymerization with $r_1 = r_2 = 0.1$ and $f_1 = f_2$ has the sequence length distribution shown in Fig. 6-10 ($p_{11} = p_{22} = 0.0910; p_{12} = p_{21} = 0.9090$). The sequence
length distributions for both monomer units are identical. The single M_1 and single M_2 sequences are overwhelmingly the most plentiful—the M_1M_2 makes up 90.9% of the copolymer structure. There are 8.3% and 0.75%, respectively, of dyad and triad sequences of both M_1 and M_2. Compare this distribution with that in Fig. 6-8 for the ideal copolymer having the identical overall composition. The large difference in the distributions for the two copolymers clearly indicates the difference between alternating and ideal behavior.

High-resolution nuclear magnetic resonance spectroscopy, especially ^13^C NMR, is a powerful tool for analysis of copolymer microstructure [Bailey and Henrichs, 1978; Bovey, 1972; Cheng, 1995, 1997a; Randall, 1977, 1989; Randall and Ruff, 1988]. The predicted sequence length distributions have been verified in a number of comonomer systems. Copolymer microstructure also gives an alternate method for evaluation of monomer reactivity ratios [Randall, 1977]. The method follows that described in Sec. 8-16 for stereochemical microstructure. For example, for the terminal model, the mathematical equations from Sec. 8-16a-2 apply except that \( P_{mm}, P_{mr}, P_{rm} \) and \( P_{rr} \) are replaced by \( p_{11}, p_{12}, p_{21}, \) and \( p_{22} \).

### 6-2g-2 Copolymer Compositions of Different Molecules

A second uncertainty concerning copolymer composition is the distribution of composition from one copolymer molecule to another in a sample produced at any given degree of conversion [Cheng, 1997b; Galvan and Tirrell, 1986; Tacx et al., 1988]. Stockmayer [1945] indicated that the distribution of copolymer composition due to statistical fluctuations generally follows a very sharp Gaussian curve. Although the distribution is wider for
low-molecular-weight copolymers and for ideal copolymerizations compared to alternating copolymerizations, it is relatively narrow in all practical cases. Thus it is calculated that for an ideal copolymer containing an average of 50 mol% of each component, only 12% of the copolymer molecules contain less than 43% of either monomer for $X_n = 100$, while only 12% contain less than 49% of either monomer at $X_n = 10,000$. These theoretical conclusions of Stockmayer have been experimentally verified in a limited manner [Phillips and Carrick, 1962a,b].

### 6-2h Multicomponent Copolymerization

Terpolymerization, the simultaneous polymerization of three monomers, has become increasingly important from the commercial viewpoint. The improvements that are obtained by copolymerizing styrene with acrylonitrile or butadiene have been mentioned previously. The radical terpolymerization of styrene with acrylonitrile and butadiene increases even further the degree of variation in properties that can be built into the final product. Many other commercial uses of terpolymerization exist. In most of these the terpolymer has two of the monomers present in major amounts to obtain the gross properties desired, with the third monomer in a minor amount for modification of a special property. Thus the ethylene–propylene elastomers are terpolymerized with minor amounts of a diene in order to allow the product to be subsequently crosslinked.

The quantitative treatment of terpolymerization is quite complex, since nine propagation reactions

\[
\begin{align*}
R_{11} &= k_{11}[M_1][M_1] \\
R_{12} &= k_{12}[M_1][M_2] \\
R_{13} &= k_{13}[M_1][M_3] \\
R_{21} &= k_{21}[M_2][M_1] \\
R_{22} &= k_{22}[M_2][M_2] \\
R_{23} &= k_{23}[M_2][M_3] \\
R_{31} &= k_{31}[M_3][M_1] \\
R_{32} &= k_{32}[M_3][M_2] \\
R_{33} &= k_{33}[M_3][M_3]
\end{align*}
\]

and six monomer reactivity ratios

\[
\begin{align*}
r_{12} &= \frac{k_{11}}{k_{12}} \\
r_{13} &= \frac{k_{11}}{k_{13}} \\
r_{21} &= \frac{k_{22}}{k_{21}} \\
r_{23} &= \frac{k_{22}}{k_{23}} \\
r_{31} &= \frac{k_{32}}{k_{31}} \\
r_{32} &= \frac{k_{33}}{k_{32}}
\end{align*}
\]

are involved (as well as six termination reactions). The expression for the rate $R$ of each of the propagation reactions is shown above. An expression for the terpolymer composition can be obtained by either the steady-state or statistical approach used for copolymerization (Sec. 6-2). The steady-state approach is described here [Alfrey and Goldfinger, 1944; Ham, 1964, 1966; Mirabella, 1977]. The rates of disappearance of the three monomers are given by

\[
\begin{align*}
-\frac{d[M_1]}{dt} &= R_{11} + R_{21} + R_{31} \\
-\frac{d[M_2]}{dt} &= R_{12} + R_{22} + R_{32} \\
-\frac{d[M_3]}{dt} &= R_{13} + R_{23} + R_{33}
\end{align*}
\]
The assumption of steady-state concentrations for \( M_1, M_2, \) and \( M_3 \) radicals can be expressed as:

\[
R_{12} + R_{13} = R_{21} + R_{31} \quad (6-44a)
\]

\[
R_{21} + R_{23} = R_{12} + R_{32} \quad (6-44b)
\]

\[
R_{31} + R_{32} = R_{13} + R_{23} \quad (6-44c)
\]

Combination of Eqs. 6-43 with 6-44, and the use of the appropriate rate expressions from Eq. 6-41 for each \( R \) term, yield the terpolymer composition as:

\[
d[M_1] : d[M_2] : d[M_3] = [M_1] \left\{ \frac{[M_1]}{r_{31}r_{21}} + \frac{[M_2]}{r_{21}r_{32}} + \frac{[M_3]}{r_{32}r_{23}} \right\} \left\{ \frac{[M_1]}{r_{12}} + \frac{[M_2]}{r_{13}} + \frac{[M_3]}{r_{13}} \right\} ;
\]

\[
[M_2] \left\{ \frac{[M_1]}{r_{31}r_{21}} + \frac{[M_2]}{r_{21}r_{32}} + \frac{[M_3]}{r_{32}r_{23}} \right\} \left\{ \frac{[M_1]}{r_{21}} + \frac{[M_1]}{r_{13}} + \frac{[M_3]}{r_{23}} \right\} ;
\]

\[
[M_3] \left\{ \frac{[M_1]}{r_{31}r_{21}} + \frac{[M_2]}{r_{21}r_{32}} + \frac{[M_3]}{r_{32}r_{23}} \right\} \left\{ \frac{[M_1]}{r_{31}} + \frac{[M_2]}{r_{32}} + \frac{[M_3]}{r_{32}} \right\} \quad (6-45)
\]

A simpler expression for the terpolymer composition has been obtained by expressing the steady state with the relationships:

\[
R_{12} = R_{21} \quad (6-46a)
\]

\[
R_{23} = R_{32} \quad (6-46b)
\]

\[
R_{31} = R_{13} \quad (6-46c)
\]

instead of those in Eq. 6-44 [Valvassori and Sartori, 1967]. The combination of Eqs. 6-46 and 6-43 yields the terpolymer composition as:

\[
d[M_1] : d[M_2] : d[M_3] = [M_1] \left\{ \frac{[M_1]}{r_{12}} + \frac{[M_2]}{r_{13}} + \frac{[M_3]}{r_{13}} \right\} ;
\]

\[
[M_2] \frac{r_{21}}{r_{12}} \left\{ \frac{[M_1]}{r_{21}} + \frac{[M_2]}{r_{23}} + \frac{[M_3]}{r_{23}} \right\} ;
\]

\[
[M_3] \frac{r_{31}}{r_{13}} \left\{ \frac{[M_1]}{r_{31}} + \frac{[M_2]}{r_{32}} + \frac{[M_3]}{r_{32}} \right\} \quad (6-47)
\]

Equations 6-45 and 6-47 and other variations have been useful for predicting the composition of a terpolymer from the reactivity ratios in the two component systems \( M_1/M_2, M_1/M_3, \) and \( M_2/M_3 \) [Alfrey and Goldfinger, 1944; Braun and Cei; 1987, Disselhoff, 1978; Ham, 1964; Hocking and Klimchuk, 1996; Janovic et al., 1983; Roland and Cheng, 1991; Tomescu and Simionescu, 1976; Valvassori and Sartori, 1967]. The two equations have been successfully extended to multicomponent copolymerizations of four or more monomers. Both equations yield essentially the same results, and there is good agreement with the experimental terpolymer compositions. Table 6-1 shows the calculated and experimental compositions in several systems.

The terpolymerization and multicomponent composition equations are generally valid only when all the monomer reactivity ratios have finite values. When one or more of the...
monomers is incapable of homopolymerization the equations generally become indeterminate. Various modified expressions based on both the conventional and simplified equations have been derived for these and other special cases [Braun and Elsasser, 2000; Chien and Finkenaur, 1985; Quella, 1989].

### 6-3 RADICAL COPOLYMERIZATION

The discussions thus far have been quite general without any specification as to whether copolymerization occurs by radical or ionic propagation. Consider now some of the specific characteristics of radical copolymerization.

#### 6-3a Effect of Reaction Conditions

##### 6-3a-1 Reaction Medium

Monomer reactivity ratios are generally but not always independent of the reaction medium in radical copolymerization. There is a real problem here in that the accuracy of \( r \) values is often insufficient to allow one to reasonably conclude whether \( r_1 \) or \( r_2 \) varies with changes in reaction media. The more recent determinations of \( r \) values by high-resolution NMR are much more reliable than previous data for this purpose. It has been observed that the
experimentally determined monomer reactivity ratios are affected by the reaction medium in certain systems. This occurs in some but not all polymerizations carried out under nonhomogeneous conditions. Emulsion and suspension polymerizations occasionally show copolymer compositions different from those in bulk or solution polymerization when there is monomer partitioning; thus, the local comonomer feed composition at the reaction site (monomer droplet, micelle) is different from that in the bulk of the reaction system [Doiuchi and Minoura, 1977; Plochocka, 1981]. This can occur in emulsion polymerization if the relative solubilities of the two monomers in the micelles are different from the feed composition in the dispersing medium or diffusion of one of the monomers into the micelles is too slow. Such behavior has been observed in several systems, such as styrene copolymerization with acrylonitrile or itaconic acid [Fordyce and Chapin, 1947; Fordyce and Ham, 1948]. The phenomenon also occurs in suspension polymerization if one of the monomers has appreciable solubility in the dispersing medium. Monomer partitioning is similarly observed for copolymerization in β-cyclodextrin-monomer complexes (Sec. 3-13c) [Ritter and Tabatabai, 2002]. The monomer reactivity ratios are unchanged in these systems. The apparent discrepancies are simply due to altered $f_1$ and $f_2$ values at the reaction sites. If the correct $f_1$ and $f_2$ values are determined and used in calculations of expected copolymer compositions, the discrepancies disappear [Smith, 1948].

Deviations are also observed in some copolymerizations where the copolymer formed is poorly soluble in the reaction medium [Pichot and Pham, 1979; Pichot et al., 1979; Suggate, 1978, 1979]. Under these conditions, altered copolymer compositions are observed if one of the monomers is preferentially adsorbed by the copolymer. Thus for methyl methacrylate ($M_1$)-N-vinylcarbazole ($M_2$) copolymerization, $r_1 = 1.80$, $r_2 = 0.06$ in benzene but $r_1 = 0.57$, $r_2 = 0.75$ in methanol [Ledwith et al., 1979]. The propagating copolymer chains are completely soluble in benzene but are microheterogeneous in methanol. N-vinylcarbazole (NVC) is preferentially adsorbed by the copolymer compared to methyl methacrylate. The comonomer composition in the domain of the propagating radical sites (trapped in the precipitating copolymer) is richer in NVC than the comonomer feed composition in the bulk solution. NVC enters the copolymer to a greater extent than expected on the basis of feed composition. Similar results occur in template copolymerization (Sec. 3-10d-2), where two monomers undergo copolymerization in the presence of a polymer. Thus, acrylic acid-2-hydroxyethylmethacrylate copolymerization in the presence of poly(N-vinylpyrrolidone) results in increased incorporation of acrylic acid [Rainaldi et al., 2000].

Some effect of viscosity on $r$ has been observed [Kelen and Tudos, 1974; Rao et al., 1976]. Copolymerization of styrene ($M_1$)-methyl methacrylate ($M_2$) in bulk leads to a copolymer containing less styrene than when reaction is carried out in benzene solution [Johnson et al., 1978]. The gel effect in bulk polymerization decreases the mobility of styrene resulting in a decrease in $r_1$ and an increase in $r_2$.

The monomer reactivity ratio for an acidic or basic monomer shows a dependence on pH since the identity of the monomer changes with pH. For example, acrylic acid ($M_1$)-acrylamide ($M_2$) copolymerization shows $r_1 = 0.90$, $r_2 = 0.25$ at pH = 2 but $r_1 = 0.30$, $r_2 = 0.95$ at pH = 9 [Ponratnam and Kapur, 1977; Truong et al., 1986]. Acrylic acid exists as the acrylate anion at high pH. Acrylate anion shows a decreased tendency to homopropagate as well as add to propagating centers with electron-rich substituents such as the amide group. This results in a decrease in $r_1$ and an increase in $r_2$. A related phenomenon is the increase in the monomer reactivity ratio for ethyl 3-oxo-4-pentenoate when it copolymerizes with styrene in a nonpolar solvent compared to a polar solvent [Masuda et al., 1987a,b]. Ethyl 3-oxo-4-pentenoate exists in a keto–enol equilibrium with the concentration of enol increasing with solvent polarity. The enol has a higher reactivity compared to the keto
form, and this results in a copolymer richer in ethyl 3-oxo-4-pentenoate for copolymerization in nonpolar solvents.

Copolymerizations involving the combination of polar (M₁) and nonpolar (M₂) monomers often show different behavior depending on the polarity of the reaction medium [Madrigu, 2002]. The copolymer composition is richer in the less polar monomer for reaction in a polar (either aprotic or protic) solvent compared to nonpolar solvent. Calculations of monomer reactivity ratios show a decrease in \( r_1 \) usually coupled with an increase in \( r_2 \) for copolymerization in the polar solvent relative to values in the nonpolar solvent. This behavior has been observed in systems such as styrene with acrylamide, acrylonitrile, 2-hydroxyethyl methacrylate, acrylic acid, or methacrylic acid with methy1 methacrylate [Boudevska and Todorova, 1985; Harwood, 1987; Lebduska et al., 1986; Plochocka, 1981]. For acidic monomers, ionization yields the carboxylate species, which has lower reactivity. (Similar effects are anticipated for basic monomers.) Several mechanisms have been proposed to describe the results for nonionizable monomers: radical–solvent complexation, monomer–solvent complexation, and the bootstrap effect. Complexation of the polar solvent with the more polar monomer or radical decreases the reactivity of the more polar monomer or radical. The bootstrap effect results from partitioning of the two monomers between the solution and the local feed composition in the domain of the growing polymer radical. Copolymers are richer in the less polar monomer for reaction in polar solvents because the local feed composition is richer in the less polar monomer. The magnitude of the bootstrap effect can be significant depending on the difference in polarity of the two monomers [Coote et al., 1998]. Thus, for 2-hydroxyethylmethacrylate (M₁)-t-butyl acrylate (M₂), \( r_1 = 4.35 \) and \( r_2 = 0.355 \) in bulk copolymerization compared to \( r_1 = 1.79 \) and \( r_2 = 0.510 \) in copolymerization in DMF [Fernandez-Monreal et al., 2001]. For a comonomer pair with a smaller difference in polarity such as styrene (M₁)-n-butyl acrylate (M₂), \( r_1 = 0.865 \) and \( r_2 = 0.189 \) in bulk compared to \( r_1 = 0.734 \) and \( r_2 = 0.330 \) [Fernandez-Garcia et al., 2000].

### 6-3a-2 Temperature

An examination of various compilations of monomer reactivity ratios [Greenley, 1989a, 1999; Young, 1975] shows that \( r_1 \) and \( r_2 \) are relatively insensitive to temperature provided that propagation is irreversible. Thus the \( r_1 \) and \( r_2 \) values for styrene-1,3-butadiene are 0.64 and 1.4 at 5°C, and 0.60 and 1.8 at 45°C. The \( r_1 \) and \( r_2 \) values for styrene–methyl methacrylate are 0.52 and 0.46 at 60°C, and 0.59 and 0.54 at 131°C. The monomer reactivity ratio is the ratio of two propagation rate constants, and its variation with temperature will depend on the difference in propagation activation energies according to

\[
 r_1 = \frac{k_{11}}{k_{12}} = \frac{A_{11}}{A_{12}} \exp \left[ \frac{(E_{12} - E_{11})}{RT} \right]
\]

(6-48)

where \( E_{11} \) and \( A_{11} \) are the propagation activation energy and frequency factor for M₁ radical adding M₁ monomer, respectively, and \( E_{12} \) and \( A_{12} \) are the corresponding values for M₁ radical adding M₂ monomer.

The effect of temperature on \( r \) is not large, since activation energies for radical propagation are relatively small and, more significantly, fall in a narrow range such that \( E_{12} - E_{11} \) is less than 10 kJ mol⁻¹ for most pairs of monomers. However, temperature does have an effect, since \( E_{12} - E_{11} \) is not zero. An increase in temperature results in a less selective copolymerization as the two monomer reactivity ratios of a comonomer pair each tend toward unity with decreasing preference of either radical for either monomer. Temperature has the greatest
effect on those systems for which the $r$ values deviate markedly from unity, behavior which is much more typical of ionic copolymerization than radical copolymerization.

### 6-3a-3 Pressure

The monomer reactivity ratio varies with pressure according to

$$\frac{d \ln r_1}{dP} = \frac{-(\Delta V_{11}^\ddagger - \Delta V_{12}^\ddagger)}{RT}$$  \hspace{1cm} (6-49)$$

where $\Delta V_{11}^\ddagger$ and $\Delta V_{12}^\ddagger$ are the propagation activation volumes for radical $M_1$ adding monomers $M_1$ and $M_2$, respectively [Buback and Dietzsch, 2001; Burkhart and Zutty, 1962; Jenner, 1979; Jenner and Aieche, 1978; Van Der Meer et al., 1977a,b]. Although propagation rates increase considerably with pressure, $r$ is less sensitive to pressure, since $(\Delta V_{11}^\ddagger - \Delta V_{12}^\ddagger)$ is smaller than either $\Delta V_{11}^\ddagger$ or $\Delta V_{12}^\ddagger$. The effect of pressure is in the same direction as that of temperature. Increasing pressure tends to decrease the selectivity of the copolymerization as the $r$ values change in the direction of ideal copolymerization behavior. Thus the $r_1r_2$ product for styrene-acrylonitrile changes from 0.026 at 1 atm to 0.077 at 1000 atm, while $r_1r_2$ for methyl methacrylate-acrylonitrile changes from 0.16 to 0.91. Copolymerizations which are ideal at lower pressure remain so at higher pressure.

### 6-3b Reactivity

The monomer reactivity ratios for many of the most common monomers in radical copolymerization are shown in Table 6-2. These data are useful for a study of the relation between structure and reactivity in radical addition reactions. The reactivity of a monomer toward a radical depends on the reactivities of both the monomer and the radical. The relative reactivities of monomers and their corresponding radicals can be obtained from an analysis of the monomer reactivity ratios [Walling, 1957]. The reactivity of a monomer can be seen by considering the inverse of the monomer reactivity ratio ($1/r$). The inverse of the monomer reactivity ratio gives the ratio of the rate of reaction of a radical with another monomer to its rate of reaction with its own monomer

$$\frac{1}{r_1} = \frac{k_{12}}{k_{11}}$$  \hspace{1cm} (6-50)$$

Table 6-3 shows $1/r$ values calculated from the data in Table 6-2. The data in each vertical column show the monomer reactivities of a series of different monomers toward the same reference polymer radical. Thus the first column shows the reactivities of the monomers toward the butadiene radical, the second column shows the monomer reactivities toward the styrene radical, and so on. It is important to note that the data in each horizontal row in Table 6-3 cannot be compared; the data can be compared only in each vertical column.

### 6-3b-1 Resonance Effects

The monomers have been arranged in Table 6-3 in their general order of reactivity. The order of monomer reactivities is approximately the same in each vertical column irrespective of the reference radical. The exceptions that occur are due to the strong alternating tendency
<table>
<thead>
<tr>
<th>M₂</th>
<th>r₁</th>
<th>M₂</th>
<th>r₂</th>
<th>T (°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Acrylic acid</td>
<td>0.24</td>
<td>n-Butyl methacrylate</td>
<td>3.5</td>
<td>50</td>
</tr>
<tr>
<td></td>
<td>0.25</td>
<td>Styrene</td>
<td>0.15</td>
<td>60</td>
</tr>
<tr>
<td></td>
<td>8.7</td>
<td>Vinyl acetate</td>
<td>0.21</td>
<td>70</td>
</tr>
<tr>
<td>Acrylonitrile</td>
<td>0.86</td>
<td>Acrylamide</td>
<td>0.81</td>
<td>40</td>
</tr>
<tr>
<td></td>
<td>0.046</td>
<td>1,3-Butadiene</td>
<td>0.36</td>
<td>40</td>
</tr>
<tr>
<td></td>
<td>0.69</td>
<td>Ethyl vinyl ether</td>
<td>0.060</td>
<td>80</td>
</tr>
<tr>
<td></td>
<td>0.98</td>
<td>Isobutylene</td>
<td>0.020</td>
<td>50</td>
</tr>
<tr>
<td></td>
<td>1.5</td>
<td>Methyl acrylate</td>
<td>0.84</td>
<td>50</td>
</tr>
<tr>
<td></td>
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### TABLE 6-2 (Continued)

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<th>M₂</th>
<th>r₂</th>
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<td>0.2</td>
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<td>70</td>
<td></td>
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<td>Vinylidene chloride</td>
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*Data from Young [1975]; all other data from Greenley [1989a, 1999].

### TABLE 6-3 Relative Reactivities (1/r) of Monomers with Various Polymer Radicals

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<th>Polymer Radical</th>
<th>Butadiene</th>
<th>Styrene</th>
<th>Vinyl Acetate</th>
<th>Vinyl Chloride</th>
<th>Methyl Methacrylate</th>
<th>Methyl Acrylate</th>
<th>Acrylonitrile</th>
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<td>1,3-Butadiene</td>
<td>—</td>
<td>1.7</td>
<td>—</td>
<td>29</td>
<td>4</td>
<td>20</td>
<td>50</td>
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<tr>
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<td>—</td>
<td>100</td>
<td>50</td>
<td>2.2</td>
<td>5.0</td>
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<td>1.9</td>
<td>67</td>
<td>10</td>
<td>—</td>
<td>2</td>
<td>6.7</td>
</tr>
<tr>
<td>Methyl vinyl ketone</td>
<td>—</td>
<td>3.4</td>
<td>20</td>
<td>10</td>
<td>—</td>
<td>—</td>
<td>1.7</td>
</tr>
<tr>
<td>Acrylonitrile</td>
<td>3.3</td>
<td>2.5</td>
<td>20</td>
<td>25</td>
<td>0.82</td>
<td>1.2</td>
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<td>1.3</td>
<td>10</td>
<td>17</td>
<td>0.52</td>
<td>—</td>
<td>0.67</td>
</tr>
<tr>
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<td>0.10</td>
<td>0.25</td>
<td>0.37</td>
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*1/r values calculated from data of Table 6-2.
<table>
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<th>Monomer (M₂)</th>
<th>1,3-Butadiene</th>
<th>Styrene</th>
<th>Methyl Methacrylate</th>
<th>Acrylonitrile</th>
<th>Methyl Acrylate</th>
<th>Vinyl Acetate</th>
<th>Vinyl Chloride</th>
<th>Q</th>
<th>ε</th>
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<td>225,000</td>
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<td>23,000</td>
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<td>52</td>
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<td>520</td>
<td>10,100</td>
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<td>0.026</td>
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*a k₁₂ values calculated from data in Tables 3-11 and 6-3.*
of certain comonomer pairs. Table 6-3 and other similar data show that substituents increase
the reactivity of a monomer toward radical attack in the general order

−φ, −CH=CH₂ > −CN, −COR > −COOH, −COOR >
−Cl > −OCOR, −R > −OR, −H

The order of monomer reactivities corresponds to the order of increased resonance sta-
bilization by the particular substituent of the radical formed from the monomer. Substituents
composed of unsaturated linkages are most effective in stabilizing the radicals because of the
loosely held π-electrons, which are available for resonance stabilization. Substituents such as
halogen, acetoxy, and ether are increasingly ineffective in stabilizing the radicals since only
the nonbonding electrons on halogen or oxygen are available for interaction with a radical.
The spread in the effectiveness of the various substituents in enhancing monomer reactivity is
about 50–200-fold depending on the reactivity of the radical. The less reactive the attacking
radical, the greater is the spread in reactivities of the different monomers. The effect of a
second substituent in the 1-position as in vinylidene chloride is approximately additive.

The order of radical reactivities can be obtained by multiplying the 1/r values by the
appropriate propagation rate constants for homopolymerization (k₁₁). This yields the values
of k₁₂ for the reactions of various radical–monomer combinations (Table 6-4). The k₁₂ values
in any vertical column in Table 6-4 give the order or monomer reactivities—as was the case
for the data in Table 6-3. The data in any horizontal row give the order of radical reactivities
toward a reference monomer. (The Q₁ and e₁ values in the last two vertical columns should
be ignored at this point; they will be considered in Sec. 6-3b-4.)

As with monomer reactivities it is seen that the order of radical reactivities is essentially
the same irrespective of the monomer used as reference. The order of substituents in enhan-
cing radical reactivity is the opposite of their order in enhancing monomer reactivity. A
substituent that increases monomer reactivity does so because it stabilizes and decreases
the reactivity of the corresponding radical. A consideration of Table 6-4 shows that the effect
of a substituent on radical reactivity is considerably larger than its effect on monomer reac-
tivity. Thus vinyl acetate radical is about 100–1000 times more reactive than styrene radical
toward a given monomer, while styrene monomer is only 50–100 times more reactive than
vinyl acetate monomer toward a given radical. A comparison of the self-propagation rate
constants (kₚ) for vinyl acetate and styrene shows that these two effects very nearly compen-
sate each other. The kₚ for vinyl acetate is only 16 times that of styrene (Table 3-11).

The interaction of radical reactivity and monomer reactivity in determining the rate of a
radical–monomer reaction can be more clearly seen by the use of the reaction coordinate
diagram in Fig. 6-11. Figure 6-11 shows the potential-energy changes accompanying the
radical–monomer reaction as a function of the separation between the atoms forming
the new bond. These energy changes are shown for the four possible reactions between
resonance-stabilized and nonstabilized monomers and radicals

\[
\begin{align*}
R \cdot + M & \rightarrow R \cdot \\
R \cdot + M_s & \rightarrow R_s \cdot \\
R_s \cdot + M & \rightarrow R \cdot \\
R_s \cdot + M_s & \rightarrow R_s \cdot
\end{align*}
\]  

(6-51a)  
(6-51b)  
(6-51c)  
(6-51d)

where the presence or absence of the subscript s indicates the presence or absence, respec-
tively, of a substituent that is capable of resonance stabilization. Vinyl acetate and styrene
monomers are examples of M and M_s, respectively; vinyl acetate and styrene radicals are examples of R/C_{15} and R_s/C_{15}, respectively.

There are two sets of potential energy plots in Fig. 6-11. One set of four repulsion plots represents the energetics of the approach of a radical to a monomer; the other set of two Morse plots represents the stability of the bond (or of the polymer radical) finally formed. The intersections of the plots represent the transition states for the monomer-radical reactions (Eqs. 6-51a to 6-51d) where the unbonded and bonded states have the same energies. The various activation energies and heats of reaction are represented by the solid-line and broken-line arrows, respectively. The separation between the two Morse plots is significantly larger than that between either the top or bottom two repulsion plots, since substituents are much more effective in decreasing radical reactivity than in increasing monomer reactivity.

Figure 6-11 shows that the order of reaction rate constants for the various monomer-radical reactions is

\[
\begin{align*}
R_s^* + M &< R_s^* + M_s < R^* + M < R^* + M_s \\
(6-51d) &< (6-51c) < (6-51a) < (6-51b)
\end{align*}
\]

since the order of activation energies is the exact opposite (This assumes that there are no appreciable differences in the entropies of activation—a reasonable assumption for sterically
unhindered monomers.) This order of reactivity concisely summarizes the data in Tables 6-3 and 6-4 as well as many homopolymerization data. It is clear that monomers without stabilizing substituents (e.g., vinyl chloride or vinyl acetate) will self-propagate faster than those with stabilizing substituents (e.g., styrene) (Reaction 6-51a versus 6-51c). Copolymerization, on the other hand, will occur primarily between two monomers with stabilizing substituents or between two monomers without stabilizing substituents. The combination of a monomer with a stabilizing substituent and one without (e.g., styrene–vinyl acetate) yields a system in which a combination of Reactions 6-51b and 6-51d is required to have facile copolymerization. This does not occur, since Reaction 6-51d is very slow. Thus in the styrene–vinyl acetate system copolymerization is not efficient, since styrene radical is too unreactive to add to the unreactive vinyl acetate monomer.

6-3b-2 Steric Effects

The rates of radical–monomer reactions are also dependent on considerations of steric hindrance. This is easily observed by considering the reactivities of di, tri-, and tetrasubstituted ethylenes in copolymerization. Table 6-5 shows the $k_{12}$ values for the reactions of various chloroethylenes with vinyl acetate, styrene, and acrylonitrile radicals. The effect of a second substituent on monomer reactivity is approximately additive when both substituents are in the 1- or $\alpha$-position. However, a second substituent when in the 2- or $\beta$-position of the monomer results in a decrease in reactivity due to steric hindrance between it and the radical to which it is adding. Thus 2–10-fold increases and 2–20-fold decreases in the reactivities of vinylidene chloride and 1,2-dichloroethylene, respectively, are observed compared to vinyl chloride.

Although the reactivity of 1,2-disubstituted ethylenes in copolymerization is low, it is still much greater than their reactivity in homopolymerization. It was observed in Sec. 3-9b-3 that the steric hindrance between a $\beta$-substituent on the attacking radical and a substituent on the monomer is responsible for the inability of 1,2-disubstituted ethylenes to homopolymerize. The reactivity of 1,2-disubstituted ethylenes toward copolymerization is due to the lack of $\beta$-substituents on the attacking radicals (e.g., the styrene, acrylonitrile, and vinyl acetate radicals).

A comparison of the cis- and trans-1,2-dichloroethylenes shows the trans isomer to be the more reactive by a factor of 6 [Dawson et al., 1969]. This is a general phenomenon observed in comparing the reactivities of cis- and trans-1,2-disubstituted ethylenes. The cis isomer, which is usually also the less stable isomer, is the less reactive one toward reaction with a radical. The difference in reactivity has been attributed to the inability of the cis isomer to

<table>
<thead>
<tr>
<th>Monomer</th>
<th>Polymer Radical</th>
<th>Vinyl Acetate</th>
<th>Styrene</th>
<th>Acrylonitrile</th>
</tr>
</thead>
<tbody>
<tr>
<td>Vinyl chloride</td>
<td></td>
<td>10,000</td>
<td>9.7</td>
<td>725</td>
</tr>
<tr>
<td>Vinylidene chloride</td>
<td></td>
<td>23,000</td>
<td>89</td>
<td>2,150</td>
</tr>
<tr>
<td>cis-1,2-Dichloroethylene</td>
<td></td>
<td>365</td>
<td>0.79</td>
<td>—</td>
</tr>
<tr>
<td>trans-1,2-Dichloroethylene</td>
<td></td>
<td>2,320</td>
<td>4.5</td>
<td>—</td>
</tr>
<tr>
<td>Trichloroethylene</td>
<td></td>
<td>3,480</td>
<td>10.3</td>
<td>29</td>
</tr>
<tr>
<td>Tetrachloroethylene</td>
<td></td>
<td>338</td>
<td>0.83</td>
<td>4.2</td>
</tr>
</tbody>
</table>

$k_{12}$ values calculated from data in Tables 3-11 and 6-2 and Eastman and Smith [1976].
achieve a completely coplanar conformation in the transition state—a requirement for resonance stabilization of the newly formed radical by the substituent.

The data on the reactivities of trichloroethylene and tetrachloroethylene further illustrate the competitive effects of substitutions on the 1- and 2-positions of ethylene. Trichloroethylene is more reactive than either of the 1,2-dichloroethylenes but less reactive than vinylidene chloride. Tetrachloroethylene is less reactive than trichloroethylene—analogous to the difference in reactivities between vinyl chloride and 1,2-dichloroethylene. The case of polyfluoroethylenes is an exception to the generally observed large decrease in reactivity with polysubstitution. Tetrafluoroethylene and chlorotrifluoroethylene show enhanced reactivity due apparently to the small size of the fluorine atoms.

6-3b-3 Alternation; Polar Effects and Complex Participation

It was noted earlier that the exact quantitative order of monomer reactivities is not the same when different reference radicals are considered (Tables 6-3 and 6-4). Analogously, the exact order of radical reactivities varies depending on the reference monomer. Monomer reactivity cannot be considered independent of radical reactivity and vice versa. One observes enhanced reactivities in certain pairs of monomers due apparently to subtle radical–monomer interactions. This effect is a very general one in radical copolymerization and corresponds to the alternating tendency of the comonomer pairs. The deviation of the $r_1 r_2$ product from unity and its approach to zero is a measure of the alternating tendency. One can list monomers in order of their $r_1 r_2$ values with other monomers is such a manner that the further apart two monomers are, the greater is their tendency toward alternation (Table 6-6). (Ignore the $e$ values until Sec. 6-3b-4). Thus acrylonitrile undergoes ideal copolymerization with methyl vinyl ketone $r_1 r_2 = 1.1$) and alternating copolymerization with 1,3-butadiene $r_1 r_2 = 0.006$).

The order of monomers in Table 6-6 is one based on the polarity of the double bond. Monomers with electron-pushing substituents are located at the top (left) of the table and those with electron-pulling substituents at the bottom (right). The $r_1 r_2$ value decreases progressively as one considers two monomers further apart in the table. The significant conclusion is that the tendency toward alternation increases as the difference in polarity between the two monomers increases. A dramatic and useful aspect of alternating copolymerization is the copolymerization of monomers that show little or no tendency to homopolymerize. Maleic anhydride, dialkyl fumarates, $N$-alkyl maleimides, and fumaronitrile are examples of such monomers (Sec. 3-9b-3). These monomers readily form alternating copolymers with electron-donor monomers such as styrene, $p$-methoxystyrene, vinyl ethers, and $N$-vinylcarbazole [Baldwin, 1965; Chiang et al., 1977; Hall and Padias, 2001; Rzaev, 2000; Yoshimura et al., 1978]. Copolymerization of stilbene and maleic anhydride takes place even though neither undergoes significant homopolymerization.

Two mechanisms have been proposed to explain the strong alternation tendency between electron-acceptor and electron-donor monomers. The polar effect mechanism (analogous to the polar effect in chain transfer—Sec. 3-6c-2) considers that interaction between an electron-acceptor radical and an electron-donor monomer or an electron-donor radical and
<table>
<thead>
<tr>
<th>Monomer</th>
<th>( r_1 )</th>
<th>( r_2 )</th>
<th>( r_1/r_2 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>n-Butyl vinyl ether (( /C_0 1.50 ))</td>
<td>0.78</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1,3-Butadiene (( -0.50 ))</td>
<td>0.31</td>
<td>0.34</td>
<td>0.39</td>
</tr>
<tr>
<td>Styrene (( -0.80 ))</td>
<td>0.55</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Vinyl acetate (( -0.88 ))</td>
<td>0.31</td>
<td>0.34</td>
<td>0.39</td>
</tr>
<tr>
<td>Vinyl chloride (0.16)</td>
<td>0.19</td>
<td>0.23</td>
<td>0.30</td>
</tr>
<tr>
<td>Methyl methacrylate (0.40)</td>
<td>&lt;0.1</td>
<td>0.16</td>
<td>0.6</td>
</tr>
<tr>
<td>Methyl vinyl ketone (1.06)</td>
<td>0.10</td>
<td>0.35</td>
<td>0.83</td>
</tr>
<tr>
<td>Vinyldene chloride (0.34)</td>
<td></td>
<td>0.11</td>
<td>0.96</td>
</tr>
<tr>
<td>Acrylonitrile (1.23)</td>
<td>0.0004</td>
<td>0.016</td>
<td>0.21</td>
</tr>
<tr>
<td>Diethyl fumarate (2.26)</td>
<td>0.006</td>
<td>0.0049</td>
<td>0.056</td>
</tr>
<tr>
<td>Maleic anhydride (3.69)</td>
<td>~0</td>
<td>0.021</td>
<td>0.11</td>
</tr>
<tr>
<td></td>
<td>~0.002</td>
<td>0.006</td>
<td>0.00017</td>
</tr>
</tbody>
</table>

\( r_1/r_2 \) values are calculated from data in Table 6-2 [Greenley 1989a, 1999].

Values are shown in parentheses after each monomer.
an electron-acceptor monomer leads to a decrease in the activation energy for cross-propagation [Price, 1948; Walling et al., 1948]. The transition state is stabilized by partial electron transfer between the electron-donor and electron-acceptor species, for example, between styrene monomer and maleic anhydride radical

\[
\begin{align*}
\sim \text{CH} & \sim \text{C} & \text{H} & \text{CH} = \text{CH} & \sim \text{CH} & \sim \text{C} & \text{O} & \text{O} \\
\text{CO} & & & & & & & & & & & & \text{C} & \text{O} & \text{O} & \sim \text{C} & \text{O}_- \\
\text{O} & & & & & & & & & & & & \text{C} & \text{O} & \text{O} & & & \\
\end{align*}
\]

and similarly between styrene radical and maleic anhydride monomer:

\[
\begin{align*}
\sim \text{CH} & \sim \text{C} & \text{H} & \text{C} & \text{CH} & \text{H} & \text{C} & \text{CH} & \text{CH} & \text{CH} & \text{CO} & \text{CO} \\
\text{CO} & & & & & & & & & & & & \text{O} & \text{O} & \text{O} & & & \\
\text{O} & & & & & & & & & & & & \text{C} & \text{O} & \text{O} & & & \\
\end{align*}
\]

The monomer complex participation (MCP) mechanism suggests that alternation results from homopolymerization of a 1 : 1 complex formed between donor and acceptor monomers [Cowie, 1989; Furukawa, 1986]:

\[
M_1 + M_2 \xrightleftharpoons[k]{\kappa} M_1M_2 \quad \text{complex} \quad (6-55)
\]

\[
\sim M_1M_2 \cdot + M_1M_2 \xrightarrow[k]{\kappa} \sim M_1M_2M_1M_2 \cdot \quad (6-56)
\]

The pros and cons of the two mechanisms have been reviewed [Coote et al., 1998; Hall and Padias, 2001]. Spectroscopic (UV, visible, and NMR) evidence supports the formation of charge transfer complexes between electron-donor and electron-acceptor monomers [Dodgson and Ebdon, 1977; Hirai, 1976; Kuntz et al., 1978]. For example, color develops when many comonomer pairs are mixed and the color disappears on polymerization. The stereochemistry of alkyl vinyl ether copolymerizations with fumaronitrile and maleonitrile supports the complex mechanism [Butler and Do, 1989; Olson and Butler, 1984]. The two copolymerizations yield different stereochemical results, indicating that the cis and trans arrangements of substituents in maleonitrile and fumaronitrile, respectively, are preserved in the copolymer. If maleonitrile and fumaronitrile entered the copolymer as individual monomer molecules, instead of as part of a complex with the alkyl vinyl ether, the two copolymers would possess the same stereochemistry. Contradictory evidence for the complex mechanism was found during radical-trapping experiments in the copolymerization of N-phenylmaleimide (NPM) and 2-chloroethyl vinyl ether (CEVE) [Jones and Tirrell, 1986, 1987; Prementine et al., 1989]. Only N-phenylmaleimide added to the radical trap, whereas both monomers should have added if reaction involved the 1 : 1 complex of NPM and CEVE. Perhaps the strongest argument against the MCP mechanism is that charge-transfer complexes have not been isolated and are not known to undergo chemical reactions.

Some pairs of very strongly electron-donor and electron-acceptor monomers, such as \(p\)-methoxystyrene and dimethyl cyanoformate, undergo spontaneous alternating copolymerizations without any added free-radical initiator, although heat may be required [Hall and Padias, 1997, 2001]. Initiation involves reaction of the comonomer pair to form a diradical,
which then propagates. The process, referred to as charge-transfer polymerization, is complicated. Some comonomer pairs do not form alternating copolymers, but instead form homopolymer and/or cyclobutane derivatives by $[2 + 2]$-cycloadDITION between the two monomers. For example, vinylidene cyanide and alkyl vinyl ether react spontaneously at $25^\circ C$ to form the separate homopolymers of the two monomers plus a small amount of the cyclobutane adduct.

The addition of a Lewis acid such as zinc chloride, dialkylaluminum chloride, and alkylaluminum sesquichloride ($\text{AlR}_1.5\text{Cl}_{1.5}$) to some comonomer pairs increases the tendency to form alternating copolymers. Comonomer pairs that are mildly alternating become strongly alternating [Ban et al., 2000; Cowie, 1989; Furukawa, 1986]. Even more surprising, strongly alternating behavior occurs between monomers that seldom copolymerize or whose alternation tendency is very low. Thus alternating copolymerization is achieved between electron-acceptor monomers such as acrylonitrile, methyl acrylate, methyl methacrylate, and methyl vinyl ketone and electron-donor monomers such as propene, isobutylene, vinyl chloride, vinylidene chloride, and vinyl acetate. A consideration of the $r$ values in Table 6-2 for these comonomer pairs clearly indicates that the alternating tendency is not high in the absence of the Lewis acid. In the presence of the Lewis acid these comonomer pairs become strongly alternating. Two mechanisms have been proposed to explain the effect of Lewis acids, both involving initial complexation of the Lewis acid with the electron-acceptor monomer to produce a binary complex with enhanced electron-acceptor properties. The binary complex participates in copolymerization either through a cross-propagation mechanism or via interaction with the electron-donor monomer to form a ternary complex that subsequently undergoes homopropagation. Both mechanisms explain why copolymerization is possible with monomers such as propene or isobutylene, which do not homopolymerize as a result of degradative chain transfer. Degradative chain transfer is less competitive with polymerization through the binary or ternary complex.

Both the cross-propagation and complex mechanisms may be operative in alternating copolymerizations with the relative importance of each depending on the particular reaction system. The tendency toward alternation, with or without added Lewis, acid, is temperature- and concentration-dependent. Alternation decreases with increasing temperature and decreasing total monomer concentration since the extent of complex formation decreases. When the alternation tendency is less than absolute because of high reaction temperature, low monomer concentration, absence of a Lewis acid, or an imbalance in the coordinating abilities of the two monomers, copolymerization proceeds simultaneously by the two mechanisms. The quantitative aspects of this situation are considered in Sec. 6-5.

6-3b-4 Q–e Scheme

Various attempts have been made to place the radical–monomer reaction on a quantitative basis in terms of correlating structure with reactivity. Success in this area would give a better understanding of copolymerization behavior and allow the prediction of the monomer reactivity ratios for comonomer pairs that have not yet been copolymerized. A useful correlation is the $Q$–$e$ scheme of Alfrey and Price [1947], who proposed that the rate constant for a radical–monomer reaction, for example, for the reaction of $M_1\cdot$ radical with $M_2$ monomer, be written as

$$k_{12} = P_1 Q_2 \exp(-e_1 e_2)$$

(6-57)

where $P_1$ represents the intrinsic reactivity of $M_1\cdot$ radical, $Q_2$ represents the intrinsic reactivity of $M_2$ monomer, $e_1$ represents the polarity of $M_1\cdot$ radical, and $e_2$ represents the polarity
of M₂ monomer. By assuming that the same e value applies to both a monomer and its corresponding radical (i.e., e₁ defines the polarities of M₁ and M₁*, while e₂ defines the polarities of M₂ and M₂*), one can write expressions for k₁₁, k₂₂, k₂₁ analogous to Eq. 6-57. These can be appropriately combined to yield the monomer reactivity ratios in the forms

\[ r₁ = \frac{Q₁}{Q₂} \exp[-e₁(e₁ - e₂)] \]  \hspace{1cm} (6-58)

\[ r₂ = \frac{Q₂}{Q₁} \exp[-e₂(e₂ - e₁)] \]  \hspace{1cm} (6-59)

which correlate monomer–radical reactivity with the parameters Q₁, Q₂, e₁, and e₂. The basis of the Q–e scheme (Eqs. 6-57 to 6-59) is the theoretically unsatisfactory suggestion that the alternating tendency is due to ground-state electrostatic interactions between permanent charges in the monomer and radical [Price, 1948]. Although there have been attempts to place it on a solid theoretical basis [Colthup, 1982; O’Driscoll and Yonezawa, 1966], the Q–e scheme is best considered as an empirical approach to placing monomer reactivity on a quantitative basis. Monomer reactivity is separated into the parameter Q, which describes the resonance factor (and to a slight extent the steric factor) present in the monomer, and the parameter e, which describes the polar factor.

Consider now the use of the Q–e scheme to predict monomer reactivity ratios. Values of Q and e have been assigned to monomers on the basis of their r values and the arbitrarily chosen reference values of Q = 1 and e = −0.80 for styrene [Greenley, 1989b, 1999]. Table 6-7 shows the average Q and e values for some common monomers. The practical success of the Q–e scheme in predicting the r₁ and r₂ values for comonomer pairs not previously copolymerized has been limited in its quantitative aspects. The reason for this is that the Q and e values for a monomer are not unique values for both experimental and theoretical reasons. The precision of the calculated Q and e values is often poor as a result of inaccuracies in the experimentally determined r values. Further, the Q and e values for a monomer vary considerably depending on the monomer with which it is copolymerized as a result of inherent deficiencies of the Q–e scheme. It does not explicitly take into account steric factors that may affect monomer reactivity ratios for certain radical–monomer combinations. The assumption of the same e value for a monomer and its corresponding radical is also inadequate. Attempts to refine the Q–e scheme by using separate e values for monomer and radical have not been successful.

In spite of these deficiencies the Q–e scheme is a reasonable qualitative and even semi-quantitative approach to the effect of structure on monomer reactivity. It can be used to give a general idea of the behavior to be expected from a comonomer pair that has not been studied. The Q–e values can be used to more quantitatively discuss reactivity data such as those in Table 6-4 and 6-6. The monomers are lined up in Table 6-6 in order of their e values. This order defines the polarities of the various monomers. The relative importance of resonance and polar factors in determining monomer reactivity can be discussed by considering the data in Table 6-4 in terms of the Q and e values of the monomers. The various reference radicals can be divided into two groups: one composed of the relatively unreactive radicals and the other composed of reactive radicals. For the reactive radicals, such as vinyl chloride and vinyl acetate, monomer reactivity depends on Q with k₁₂ increasing with increasing Q and polar effects are too subtle to discern. The unreactive radicals from styrene and 1,3-butadiene show the same trends except that one can discern the polar effects. There is enhanced reactivity of these radicals (processing negative e values) toward a monomer such as acrylonitrile...
with relatively high positive $e$ values. The resonance factor is, however, more important than the polar factor; the former determines the magnitude of monomer reactivity. Thus monomer reactivities toward the 1,3-butadiene and styrene radicals fall into two groups—one group of monomers with high $Q$ values and high reactivities and another group with low $Q$ values and low reactivities.

A number of useful generalizations are possible regarding which pairs of monomers will copolymerize and the behavior to be expected. Copolymerization proceeds poorly with monomers whose $Q$ values are very different, since copolymer formation would require the energetically unfavorable conversion of a resonance-stabilized radical to a less stabilized radical and vice versa (Fig. 6-11). Thus vinyl chloride and vinyl acetate do not copolymerize well with styrene or 1,3-butadiene. Copolymerization is more suitable between monomers of similar $Q$ values, preferably high $Q$ values, for example, styrene and 1,3-butadiene. Ideal copolymerization occurs between two monomers having similar $Q$ and $e$ values, for example, styrene–1,3-butadiene, vinyl chloride–vinyl acetate, and acrylonitrile–methyl acrylate. The tendency toward alternation is greatest for monomers having the same $Q$ values with high $e$ values of opposite sign.

### TABLE 6-7 $Q$ and $e$ Values for Monomers

<table>
<thead>
<tr>
<th>Monomer</th>
<th>$Q$</th>
<th>$e$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ethyl vinyl ether</td>
<td>0.018</td>
<td>-1.80</td>
</tr>
<tr>
<td>Propene</td>
<td>0.009</td>
<td>-1.69</td>
</tr>
<tr>
<td>$N$-Vinylpyrrolidone</td>
<td>0.088</td>
<td>-1.62</td>
</tr>
<tr>
<td>$n$-Butyl vinyl ether</td>
<td>0.038</td>
<td>-1.50</td>
</tr>
<tr>
<td>$p$-Methoxystyrene</td>
<td>1.53</td>
<td>-1.40</td>
</tr>
<tr>
<td>Isobutylene</td>
<td>0.023</td>
<td>-1.20</td>
</tr>
<tr>
<td>Vinyl acetate</td>
<td>0.026</td>
<td>-0.88</td>
</tr>
<tr>
<td>$\alpha$-Methylstyrne</td>
<td>0.97</td>
<td>-0.81</td>
</tr>
<tr>
<td>Styrene</td>
<td>1.00</td>
<td>-0.80</td>
</tr>
<tr>
<td>Isoprene</td>
<td>1.99</td>
<td>-0.55</td>
</tr>
<tr>
<td>1,3-Butadiene</td>
<td>1.70</td>
<td>-0.50</td>
</tr>
<tr>
<td>Ethylene</td>
<td>0.016</td>
<td>0.05</td>
</tr>
<tr>
<td>Vinyl chloride</td>
<td>0.056</td>
<td>0.16</td>
</tr>
<tr>
<td>Vinyldiene chloride</td>
<td>0.31</td>
<td>0.34</td>
</tr>
<tr>
<td>Methyl methacrylate</td>
<td>0.78</td>
<td>0.40</td>
</tr>
<tr>
<td>Acrylamide</td>
<td>0.23</td>
<td>0.54</td>
</tr>
<tr>
<td>Methacrylic acid</td>
<td>0.98</td>
<td>0.62</td>
</tr>
<tr>
<td>Methyl acrylate</td>
<td>0.45</td>
<td>0.64</td>
</tr>
<tr>
<td>Methacrylonitrile</td>
<td>0.86</td>
<td>0.68</td>
</tr>
<tr>
<td>Vinyl fluoride</td>
<td>0.008</td>
<td>0.72</td>
</tr>
<tr>
<td>4-Vinylpyridine</td>
<td>2.47</td>
<td>0.84</td>
</tr>
<tr>
<td>Acrylic acid</td>
<td>0.83</td>
<td>0.88</td>
</tr>
<tr>
<td>Methyl vinyl ketone</td>
<td>0.66</td>
<td>1.05</td>
</tr>
<tr>
<td>Diethyl maleate</td>
<td>0.053</td>
<td>1.08</td>
</tr>
<tr>
<td>Acrylonitrile</td>
<td>0.48</td>
<td>1.23</td>
</tr>
<tr>
<td>Tetrafluoroethylene</td>
<td>0.032</td>
<td>1.63</td>
</tr>
<tr>
<td>Diethyl fumarate</td>
<td>0.25</td>
<td>2.26</td>
</tr>
<tr>
<td>Fumaronitrile</td>
<td>0.29</td>
<td>2.73</td>
</tr>
<tr>
<td>Maleic anhydride</td>
<td>0.86</td>
<td>3.69</td>
</tr>
</tbody>
</table>

aData from Greenley [1989b, 1999].
6-3b-5 Patterns of Reactivity Scheme

The “patterns of reactivity” scheme is a more advanced treatment of copolymerization behavior. It follows the general form of the $Q-e$ scheme but does not assume that the same intrinsic reactivity or polarity factors apply both to a monomer and its corresponding radical [Bamford and Jenkins, 1965; Jenkins, 1999, 2000; Jenkins and Jenkins, 1999]. The monomer reactivity ratio for monomer 1 is expressed in terms of four parameters

$$\log r_{12} = \log \frac{r_1}{C_0} - \pi_1 u_2 - v_2$$  \hspace{1cm} (6-60a)

where $r_1$ represents the intrinsic reactivity of $M_1^*$ radical, $v_2$ represents the intrinsic reactivity of $M_2$ monomer, $\pi_1$ represents the polarity of $M_1^*$ radical, and $u_2$ represents the polarity of $M_2$ monomer. The intrinsic reactivity $r_1$ or $v_2$ contains all factors except the polarity factor, that is, they contain the resonance and steric factors, which affect reactivity.

The reactivity $r_1$ is the monomer reactivity ratio for copolymerization of monomer 1 with styrene. Since styrene has very little polar character, $r_1$ measures the intrinsic reactivity of $M_1^*$ radical. The polarity of $M_1^*$ radical $\pi_1$ is obtained from

$$\pi_1 = 0.385 \log \left[ \frac{r_{1A}}{0.377 r_1} \right]$$  \hspace{1cm} (6-61)

where $r_{1A}$ is the monomer reactivity ratio for copolymerization of monomer 1 with acrylonitrile; that is, the polarity of $M_1^*$ radical is related to the ratio of the radical’s reactivity toward the polar acrylonitrile compared to the nonpolar styrene.

The monomer reactivity ratio for monomer 2 follows from Eq. 6-60a as

$$\log r_{21} = \log \frac{r_2}{C_0} - \pi_2 u_1 - v_1$$  \hspace{1cm} (6-62a)

with

$$\pi_2 = 0.385 \log \left[ \frac{r_{2A}}{0.377 r_2} \right]$$  \hspace{1cm} (6-63)

Equations 6-60a and 6-62a parallel Eqs. 6-58 and 6-59 of the $Q-e$ scheme. Equations 3-60a and 3-62a are also given by

$$\log r_{12} = \log \frac{r_1}{C_0} - \pi_1 u_2 + \log r_{S2}$$  \hspace{1cm} (6-60b)
$$\log r_{21} = \log \frac{r_2}{C_0} - \pi_2 u_1 + \log r_{S1}$$  \hspace{1cm} (6-62b)

since $v_1 = -\log r_{S1}$ and $v_2 = -\log r_{S2}$.

The values of $v$ and $u$ for a monomer are obtained from monomer reactivity ratios for copolymerization of that monomer with a series of reference monomers. A plot of the data according to Eq. 6-60a as $[\log r_{12} - \log r_1]$ versus $\pi_1$ yields a straight line whose slope is $-u_2$ and intercept on the $y$-axis is $-v_2$.

Table 6-8 shows values of the various parameters needed to calculate monomer reactivity ratios from Eqs. 6-60 and 6-62 [Jenkins and Jenkins, 1999]. The monomers in Table 6-8 are lined up in order of their $u$ values. The Patterns of Reactivity scheme, like the $Q-e$ scheme, is an empirical scheme. Monomer reactivity ratios calculated by the patterns of reactivity scheme are generally closer to experimental values than those calculated by the $Q-e$ scheme, which supports the rationale of assigning different polarity values to a monomer and the radical derived from the monomer.
Appropriate manipulation of Eqs. 6-60 and 6-62 gives alternate expressions for the two monomer reactivity ratios

\[ \log r_{12} = \log \left( \frac{r_{1S} r_{S2}}{r_{1A} r_{SA}} \right) \]  
\[ \log r_{21} = \log \left( \frac{r_{2S} r_{S1}}{r_{2A} r_{SA}} \right) \]

which allow calculation of monomer reactivity ratios for the copolymerization of a pair of monomers from monomer reactivity ratios for each of those monomers copolymerizing separately with styrene and with acrylonitrile and from the monomer reactivity ratios for styrene–acrylonitrile copolymerization.

The patterns of reactivity parameters, like the \( Q-e \) parameters, can be used to analyze reactivity in both copolymerization and homopolymerization. Look at the data in Table 6-4 and compare with the parameters in Table 6-8. The highly reactive monomers are those with the more positive or less negative values of \( \nu \). However, \( \nu \) is not the only consideration, polarity is also important. For example, maleic anhydride is a monomer with one of the most positive \( \nu \) values, but it undergoes facile copolymerization only with monomers with which it has a polarity difference. This is the alternation tendency and is given by

\[ \log(r_{12}r_{21}) = (u_1 - u_2)(\pi_1 - \pi_2) \]

### TABLE 6-8 Patterns of Reactivity Parameters for Monomers

<table>
<thead>
<tr>
<th>Monomer</th>
<th>( r_{1S} )</th>
<th>( r_{1A} )</th>
<th>( r_{S1} )</th>
<th>( r_{S2} )</th>
<th>( \pi )</th>
<th>( \mu )</th>
<th>( \nu )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ethyl vinyl ether</td>
<td>0.05</td>
<td>0.06</td>
<td>0.69</td>
<td>100</td>
<td>0.192</td>
<td>1.11</td>
<td>-2.00</td>
</tr>
<tr>
<td>Styrene</td>
<td>1.00</td>
<td>0.38</td>
<td>0.04</td>
<td>1.00</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>( \alpha )-Methylstyrene</td>
<td>0.60</td>
<td>0.143</td>
<td>0.047</td>
<td>1.1</td>
<td>-0.077</td>
<td>-0.04</td>
<td>-0.03</td>
</tr>
<tr>
<td>1,3-Butadiene</td>
<td>1.20</td>
<td>0.07</td>
<td>0.036</td>
<td>0.64</td>
<td>-0.324</td>
<td>-0.21</td>
<td>0.19</td>
</tr>
<tr>
<td>Isoprene</td>
<td>1.84</td>
<td>0.45</td>
<td>0.03</td>
<td>0.458</td>
<td>-0.074</td>
<td>-0.32</td>
<td>0.34</td>
</tr>
<tr>
<td>Vinyl acetate</td>
<td>0.02</td>
<td>0.05</td>
<td>4.78</td>
<td>48</td>
<td>0.315</td>
<td>-0.44</td>
<td>-1.56</td>
</tr>
<tr>
<td>Vinyl chloride</td>
<td>0.055</td>
<td>0.045</td>
<td>3.29</td>
<td>18.7</td>
<td>0.128</td>
<td>-0.90</td>
<td>-1.16</td>
</tr>
<tr>
<td>4-Vinylpyridine</td>
<td>0.69</td>
<td>0.375</td>
<td>0.10</td>
<td>0.52</td>
<td>0.06</td>
<td>-0.94</td>
<td>0.30</td>
</tr>
<tr>
<td>Methacrylic acid</td>
<td>0.524</td>
<td>0.2</td>
<td>0.04</td>
<td>0.24</td>
<td>0.002</td>
<td>-0.95</td>
<td>0.39</td>
</tr>
<tr>
<td>2-Vinylpyridine</td>
<td>1.26</td>
<td>0.44</td>
<td>0.10</td>
<td>0.53</td>
<td>-0.014</td>
<td>-0.98</td>
<td>0.32</td>
</tr>
<tr>
<td>Methyl methacrylate</td>
<td>0.46</td>
<td>1.32</td>
<td>0.138</td>
<td>0.5</td>
<td>0.339</td>
<td>-1.18</td>
<td>0.29</td>
</tr>
<tr>
<td>Vinylidene chloride</td>
<td>0.108</td>
<td>0.32</td>
<td>0.64</td>
<td>1.79</td>
<td>0.346</td>
<td>-1.34</td>
<td>-0.24</td>
</tr>
<tr>
<td>Ethylene</td>
<td>0.05</td>
<td>0.05</td>
<td>7</td>
<td>14.9</td>
<td>0.162</td>
<td>-1.57</td>
<td>-1.23</td>
</tr>
<tr>
<td>Acrylamide</td>
<td>0.70</td>
<td>1.10</td>
<td>0.90</td>
<td>1.20</td>
<td>0.237</td>
<td>-1.82</td>
<td>-0.07</td>
</tr>
<tr>
<td>Methacrylonitrile</td>
<td>0.33</td>
<td>1.67</td>
<td>0.43</td>
<td>0.38</td>
<td>0.432</td>
<td>-2.08</td>
<td>0.44</td>
</tr>
<tr>
<td>Chloroprene</td>
<td>6.91</td>
<td>5.18</td>
<td>0.05</td>
<td>0.038</td>
<td>0.113</td>
<td>-2.18</td>
<td>1.44</td>
</tr>
<tr>
<td>Methyl acrylate</td>
<td>0.18</td>
<td>0.85</td>
<td>1.42</td>
<td>0.75</td>
<td>0.421</td>
<td>-2.34</td>
<td>0.16</td>
</tr>
<tr>
<td>Methyl vinyl ketone</td>
<td>0.32</td>
<td>1.57</td>
<td>0.61</td>
<td>0.29</td>
<td>0.427</td>
<td>-2.46</td>
<td>0.54</td>
</tr>
<tr>
<td>Diethyl maleate</td>
<td>0.04</td>
<td>0.05</td>
<td>16</td>
<td>7.03</td>
<td>0.199</td>
<td>-2.51</td>
<td>-0.83</td>
</tr>
<tr>
<td>Acrylonitrile</td>
<td>0.04</td>
<td>1.00</td>
<td>1.00</td>
<td>0.38</td>
<td>0.701</td>
<td>-2.60</td>
<td>0.42</td>
</tr>
<tr>
<td>Diethyl fumarate</td>
<td>0.06</td>
<td>0.05</td>
<td>9</td>
<td>0.33</td>
<td>0.131</td>
<td>-4.05</td>
<td>0.56</td>
</tr>
<tr>
<td>Maleic anhydride</td>
<td>0.011</td>
<td>0.05</td>
<td>6</td>
<td>0.36</td>
<td>0.416</td>
<td>-5.20</td>
<td>1.22</td>
</tr>
</tbody>
</table>

\( a \) Data from Jenkins and Jenkins [1999].
The alternation tendency is dependent only on the polarity parameters for the monomers and radicals.

The patterns of reactivity scheme has also been extended to chain transfer constants.

### 6-3b-6 Other Quantitative Approaches to Reactivity

Linear-free-energy relationships such as the Hammett and Taft equations [Lowry and Richardson, 1987] have been used to correlate copolymerization behavior with structure, but the approach is limited to considering a series of monomers that are similar in structure. Walling [1957] applied the Hammett equation to copolymerization among various meta- and para-substituted styrenes. The Taft equation in the form

\[
\log \left( \frac{1}{r} \right) = \sigma^* p^* + \delta E_S
\]  

has been used to correlate the reactivity of various vinyl esters (M2) toward the radical from ethylene (M1) [van der Meer et al., 1977b]. The variables \( p^* \) and \( \delta \) are proportionality constants indicative of the susceptibility of the radical–monomer reaction to the effect of polar and steric factors, respectively, present in the monomer. Variables \( \sigma^* \) and \( E_S \) are constants that indicate the polar and steric factors, respectively, due to the substituents on the double bond of the monomer. For the series of vinyl esters, CH2=CHCOR, \( \sigma^* \) and \( E_S \) are the substituent constants for the various R groups. Similar correlations have been successful for alkyl acrylates and methacrylates [Otsu, 1987].

### 6-3c Terminal Model for Rate of Radical Copolymerization

The rate of copolymerization, unlike the copolymer composition, depends on the initiation and termination steps as well as on the propagation steps. In the usual case both monomers combine efficiently with the initiator radicals and the initiation rate is independent of the feed composition. Two different models, based on whether termination is diffusion-controlled, have been used to derive expressions for the rate of copolymerization. The *chemical-controlled termination model* assumed that termination proceeds with chemical control, that is, termination is not diffusion-controlled [Walling, 1949]. But this model is of only historical interest since it is well established that termination in radical polymerization is generally diffusion-controlled [Atherton and North, 1962; Barb, 1953; Braun and Czerwinski, 1987; North, 1963; O’Driscoll et al., 1967; Prochazka and Kratochvil, 1983] (Sec. 3-10b).

The *diffusion-controlled termination model* considers the termination reaction as the reaction

\[
\begin{align*}
M_1^* + M_1^* & \rightarrow \bar{K}_t \rightarrow \text{dead copolymer} \\
M_1^* + M_2^* & \\
M_2^* + M_2^* &
\end{align*}
\]  

(6-68)

where the average termination rate constant \( \bar{K}_t \) is an average of the homopolymerization termination rate constants \( k_{11} \) and \( k_{22} \), each weighted on the basis of the copolymer composition in mole fractions according to

\[
\bar{K}_t = F_1 k_{11} + F_2 k_{22}
\]  

(6-69)
The rate of copolymerization is given by

$$R_p = \overline{k}_p[M] (R_i/2k_i)^{1/2}$$  \hspace{1cm} (6-70)$$

where $[M]$ is the total concentration of the two monomers and the average propagation rate constant $\overline{k}_p$ is dependent on the comonomer feed composition, monomer reactivity ratios, and homopropagation rate constants according to

$$\overline{k}_p = \frac{r_1f_1^2 + 2f_1f_2 + r_2f_2^2}{(r_1f_1/k_{11}) + (r_2f_2/k_{22})}$$  \hspace{1cm} (6-71)$$

Equation 6-71, derived by Fukuda and coworkers [Fukuda et al., 1985; Ma et al., 2001], follows from previous derivations of the rate of copolymerization [Melville et al., 1947; Walling, 1949, 1957].

Thus, the terminal model for copolymerization gives us expressions for copolymer composition (Eqs. 6-12 and 6-15), propagation rate constant (Eq. 6-71), and polymerization rate (Eq. 6-70). The terminal model is tested by noting how well the various equations describe the experimental variation of $F_1$, $\overline{k}_p$, and $R_p$ with comonomer feed composition.

There are also expressions that describe the terminal model in terms of monomer sequence distributions in the copolymer [Burke et al., 1994a,b, 1995; Cheng, 1995, 2000]. The $M_1$ centered triad fractions are given by

$$(111) = \frac{r_1f_1^2}{r_1^2f_1^2 + 2r_1f_1f_2 + f_2^2}$$ \hspace{1cm} (6-72a)$$

$$(112) = (211) = \frac{r_1f_1f_2}{r_1^2f_1^2 + 2r_1f_1f_2 + f_2^2}$$ \hspace{1cm} (6-72b)$$

$$(212) = \frac{f_2^2}{r_1^2f_1^2 + 2r_1f_1f_2 + f_2^2}$$ \hspace{1cm} (6-72c)$$

The $M_2$ centered triads $(222)$, $(221) = (122)$, and $(121)$ are derived from Eq. 6-72 by reversing the 1 and 2 subscripts.

Many comonomer pairs follow the terminal model, but more advanced models are needed to describe most comonomer pairs (Sec. 6-5).

### 6-4 IONIC COPOLYMERIZATION

Ionic copolymerizations are different from radical copolymerizations in several respects. Ionic copolymerizations are much more selective. The number of comonomer pairs that undergo either cationic or anionic copolymerization is relatively limited because of the wider range of monomer reactivities in ionic copolymerization [Bywater, 1976; Kennedy and Marechal, 1983; Morton, 1983]. Cationic copolymerization is limited to monomers with electron-donating substituents and anionic copolymerization to monomers with electron-withdrawing substituents. For comonomer pairs that undergo ionic copolymerization, the general tendency is toward the ideal type of behavior (Sec. 6-2c-1), with the $r_1r_2$ product approaching unity, where the relative reactivities of the two monomers toward the two different ionic propagating centers are approximately the same. There is a general lack of any tendency toward alternation. Furthermore, quite a few copolymerizations proceed with $r_1r_2$
values greater than unity. Thus there are relatively few monomer pairs that yield copolymers containing large proportions of both monomers.

Another characteristic feature of ionic copolymerizations is the sensitivity of the monomer reactivity ratios to changes in the initiator, reaction medium, or temperature. This is quite different from the general behavior observed in radical copolymerization. Monomer reactivity ratios in radical copolymerization are far less dependent on reaction conditions.

6-4a  Cationic Copolymerization

6-4a-1  Reactivity

The effect of a substituent on the reactivity of a monomer in cationic copolymerization depends on the extent to which it increases the electron density on the double bond and on its ability to resonance stabilize the carbocation that is formed. However, the order of monomer reactivities in cationic copolymerization (as in anionic copolymerization) is not nearly as well defined as in radical copolymerization. Reactivity is often influenced to a larger degree by the reaction conditions (solvent, counterion, temperature) than by the structure of the monomer. There are relatively few reports in the literature in which monomer reactivity has been studied for a wide range of different monomers under conditions of the same solvent, counterion, and reaction temperature.

Among the most extensive studies of monomer reactivity have been those involving the copolymerization of various meta- and para-substituted styrenes with other styrene monomers (styrene, \( \alpha \)-methylstyrene, and \( p \)-chlorostyrene) as the reference monomer [Kennedy and Marechal, 1983]. The relative reactivities of the various substituted styrenes have been correlated by the Hammett sigma–rho relationship:

\[
\log \left( \frac{1}{r_1} \right) = \rho \sigma \tag{6-73}
\]

For example, \( \log \left( \frac{1}{r_1} \right) \) values for a series of meta- and para-substituted styrenes copolymerized with styrene were plotted against the sigma substituent constants to yield a straight line with slope \( \rho \) of negative sign. The sigma value of a substituent is a quantitative measure of that substituent's total electron-donating or electron-withdrawing effect by both resonance and induction. Electron-withdrawing and electron-donating substituents have positive and negative sigma constants, respectively. A negative value of \( \rho \) means \( 1/r_1 \) is increased by electron-donating substituents as expected for cationic polymerization. (A positive value of \( \rho \) would mean \( 1/r_1 \) is increased by electron-withdrawing substituents.) Substituents increase the reactivity of styrene in the approximate order

\[
p-\text{OCH}_3 > p-\text{CH}_3 > p-\text{H} > p-\text{Cl} > m-\text{Cl} > m-\text{NO}_2
\]

\((-0.27) \quad (-0.17) \quad (0) \quad (+0.23) \quad (+0.37) \quad (+0.71)\)

which follows the order of their electron-donating effect as indicated by the sigma values shown in parentheses. \( \log \left( \frac{1}{r_1} \right) \) for meta- and para-substituted styrenes has also been correlated with the \( ^{13} \)C NMR chemical shifts of the \( \beta \)-carbon of the substituted styrenes [Hatada et al., 1977, 2002; Wood et al., 1989]. Similar correlations have been observed for the cationic copolymerizations of para-substituted benzylic vinyl ethers with benzylic vinyl ether. The correlation of \( \log \left( \frac{1}{r_1} \right) \) with chemical shift (\( \delta \)) is analogous to the correlation with \( \sigma \), since both \( \delta \) and \( \sigma \) measure the electron-donating ability of the substituent.
Although the Hammett-type approach is most useful for the quantitative correlation of monomer reactivity with structure, it is applicable only to substituted styrenes. One is, however, usually more interested in the relative reactivities of the commonly encountered monomers such as isoprene, acrylonitrile, and isobutylene. The appropriate quantitative data are relatively sparse for these monomers. The generally observed order of monomer reactivity is

Vinyl ethers > isobutylene > styrene, isoprene

which is the order expected on the basis of the electron-donating ability of the various substituents. Monomers with electron-withdrawing substituents such as acrylonitrile, methyl methacrylate, and vinyl chloride show negligible reactivity in cationic copolymerization. There has been some success in correlating \( \log \left( \frac{1}{r_1} \right) \) with the \( e \) values from the \( Q-e \) scheme [Ham, 1977].

Steric effects similar to those in radical copolymerization are also operative in cationic copolymerizations. Table 6-9 shows the effect of methyl substituents in the \( \alpha- \) and \( \beta- \) positions of styrene. Reactivity is increased by the \( \alpha- \)methyl substituent because of its electron-donating power. The decreased reactivity of \( \beta- \)methylstyrene relative to styrene indicates that the steric effect of the \( \beta- \)substituent outweighs its polar effect of increasing the electron density on the double bond. Furthermore, the trans-\( \beta- \)methylstyrene appears to be more reactive than the cis isomer, although the difference is much less than in radical copolymerization (Sec. 6-3b-2). It is worth noting that 1,2-disubstituted alkenes have finite \( r \) values in cationic copolymerization compared to the values of zero in radical copolymerization (Table 6-2). There is a tendency for 1,2-disubstituted alkenes to self-propagate in cationic copolymerization, although this tendency is low in the radical reaction.

### Table 6-9 Steric Effects in Cationic Copolymerization of \( \alpha- \) and \( \beta- \)Methylstyrenes (M₁) with \( p- \)Chlorostyrene (M₂) \(^{a,b}\)

<table>
<thead>
<tr>
<th></th>
<th>( r_1 )</th>
<th>( r_2 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Styrene</td>
<td>2.31</td>
<td>0.21</td>
</tr>
<tr>
<td>( \alpha- )Methylstyrene</td>
<td>9.44</td>
<td>0.11</td>
</tr>
<tr>
<td>trans-( \beta- )Methylstyrene</td>
<td>0.32</td>
<td>0.74</td>
</tr>
<tr>
<td>cis-( \beta- )Methylstyrene</td>
<td>0.32</td>
<td>1.0</td>
</tr>
</tbody>
</table>

\(^a\) Data from Overberger et al. [1951, 1954, 1958].

\(^b\) \( \text{SnCl}_4 \) in \( \text{CCl}_4 \) at 0°C.

---

**6-4a-2 Effect of Solvent and Counterion**

It has previously been shown that large changes can occur in the rate of a cationic polymerization by using a different solvent and/or different counterion (Sec. 5-2f). The monomer reactivity ratios are also affected by changes in the solvent or counterion. The effects are often complex and difficult to predict since changes in solvent or counterion often result in alterations in the relative amounts of the different types of propagating centers (free ion, ion pair, covalent), each of which may be differently affected by solvent. As many systems do not show an effect as do show an effect of solvent or counterion on \( r \) values [Kennedy and Marechal, 1983]. The dramatic effect that solvents can have on monomer reactivity ratios is illustrated by the data in Table 6–10 for isobutylene-\( p- \)chlorostyrene. The aluminum bromide-initiated copolymerization shows \( r_1 = 1.01, r_2 = 1.02 \) in \( n \)-hexane but
$r_1 = 14.7, r_2 = 0.15$ in nitrobenzene. The variation in $r$ values has been attributed to the preferential solvation of propagating centers in the nonpolar medium ($n$-hexane) by the more polar monomer ($p$-chlorostyrene). The increased local concentration of $p$-chlorostyrene at the reaction site results in its greater incorporation into the copolymer than expected, based on the composition of the comonomer feed in the bulk solution. Calculation of $r$ values using the bulk comonomer feed composition results in a lower value of $r_1$ coupled with a higher value of $r_2$. In the polar nitrobenzene the propagating centers are completely solvated by the solvent without participation by $p$-chlorostyrene, and the more reactive isobutylene exhibits its greater reactivity.

The effect of solvent on monomer reactivity ratios cannot be considered independent of the counterion employed. Again, the situation is difficult to predict with some comonomer systems showing altered $r$ values for different initiators and others showing no effects. Thus the isobutylene–$p$-chlorostyrene system (Table 6–10) shows different $r_1$ and $r_2$ for AlBr$_3$ and SnCl$_4$. The interdependence of the effects of solvent and counterion are shown in Table 6–11 for the copolymerization of styrene and $p$-methylstyrene. The initiators are listed in order of their strength as measured by their effectiveness in homopolymerization studies. Antimony pentachloride is the strongest initiator and iodine the weakest. The order is that based on the relative concentrations of different types of propagating centers.

The data in Table 6–11 show the copolymer composition to be insensitive to the initiator for solvents of high polarity (1,2-dichloroethane and nitrobenzene) and also insensitive to solvent polarity for any initiator except the strongest (SbCl$_5$). The styrene content of the copolymer decreases with increasing solvent polarity when SbCl$_5$ is the initiator. The styrene content also decreases with decreasing initiator strength for the low-polarity solvent

### Table 6-10 Effect of Solvent and Initiator on $r$ Values in Cationic Copolymerization

<table>
<thead>
<tr>
<th>$r_1$</th>
<th>$r_2$</th>
<th>Solvent</th>
<th>Initiator</th>
</tr>
</thead>
<tbody>
<tr>
<td>Isobutylene</td>
<td>$p$-Chlorostyrene</td>
<td>$n$-C$<em>6$H$</em>{14}$ (ε 1.8)</td>
<td>AlBr$_3$</td>
</tr>
<tr>
<td>1.01</td>
<td>1.02</td>
<td></td>
<td></td>
</tr>
<tr>
<td>14.7</td>
<td>0.15</td>
<td>$\phi$-NO$_2$ (ε 36)</td>
<td>AlBr$_3$</td>
</tr>
<tr>
<td>8.6</td>
<td>1.2</td>
<td>$\phi$-NO$_2$ (ε 36)</td>
<td>SnCl$_4$</td>
</tr>
</tbody>
</table>

$^a$ Data from Overberger and Kamath [1959].

$^b$ Temperature: 0°C.

### Table 6-11 Effects of Solvent and Counterion on Copolymer Composition in Styrene–$p$-Methylstyrene Cationic Copolymerization

<table>
<thead>
<tr>
<th>Initiator System</th>
<th>Toluene (ε 2.4)</th>
<th>1,2-Dichloroethene (ε 9.7)</th>
<th>Nitrobenzene (ε 36)</th>
</tr>
</thead>
<tbody>
<tr>
<td>SbCl$_5$</td>
<td>46</td>
<td>25</td>
<td>28</td>
</tr>
<tr>
<td>AlX$_3$</td>
<td>34</td>
<td>34</td>
<td>28</td>
</tr>
<tr>
<td>TiCl$_4$, SnCl$_4$, BF$_3$ · OEt$_2$, SbCl$_3$</td>
<td>28</td>
<td>27</td>
<td>27</td>
</tr>
<tr>
<td>Cl$_3$CCO$_2$H</td>
<td>27</td>
<td></td>
<td>30</td>
</tr>
<tr>
<td>I$_2$</td>
<td>17</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

$^a$ Data from O’Driscoll et al. [1996].

$^b$ Comonomer feed = 1 : 1 styrene–$p$-methylstyrene.
(toluene). These results can be interpreted in terms of the effect of solvent and counterion on the identity of the propagating centers and on the extent of preferential solvation of propagating centers by one of the monomers. In the styrene–p-methylstyrene system p-methylstyrene is both the more polar and the more reactive of the two monomers. In the poor solvent (toluene) the monomers compete, against the solvent, with each other to solvate the propagating centers. The more polar p-methylstyrene preferentially solvates the propagating centers and is preferentially incorporated into the copolymer. The selectivity increases in proceeding from SbCl₅ to AlCl₃ to the other initiators, which corresponds to increases in the amount of ion pairs relative to free ions. For the better solvents the counterion does not appreciably influence the reaction, since the monomers cannot compete with the solvent. In the SbCl₅ initiated copolymerization increasing the solvent power of the reaction medium also decreases the ability of the monomers to compete with the solvent to complex with propagating centers. The copolymer composition is then determined primarily by the chemical reactivities of the monomers.

6-4a-3  Effect of Temperature

Temperature has a greater influence on monomer reactivity ratios in cationic copolymerization than in radical copolymerization because of the greater spread of propagation activation energies for the ionic process. The ratio of any two rate constants is expected to tend toward unity with increasing temperature since the smaller rate constant (larger activation energy) will increase faster with increasing temperature than the larger rate constant (smaller activation energy). However, there is no general trend of $r$ values tending toward unity (i.e., less selective reaction) in cationic copolymerization with increasing temperature as there is in radical copolymerization. Some $r$ values increase with temperature and others decrease. Various combinations of effects have been observed for different comonomer pairs [Kennedy and Marechal, 1983]. There are comonomer systems where both $r_1$ and $r_2$ tend toward unity as expected, but there are also many systems where an $r$ value decreases below or increases above unity with increasing temperature. This unexpected behavior is probably the result of changes in the identities and relative amounts of different propagating species (free ion, ion pair, covalent) either directly as a result of a change in temperature, or indirectly by the effect of temperature on solvent polarity.

6-4b  Anionic Copolymerization

6-4b-1  Reactivity

Monomer reactivities in anionic copolymerization are the opposite of those in cationic copolymerization. Reactivity is enhanced by electron-withdrawing substituents that decrease the electron density on the double bond and resonance stabilize the carbanion formed. Although the available data are rather limited [Bywater, 1976; Morton, 1983; Szwarc, 1968], reactivity is generally increased by substituents in the order

\[ \text{CN} > \text{CO}_2\text{R} > \breve{\phi}, \ \text{CH} = \text{CH}_2 > \text{H} \]

The reactivity of monomers with electron-releasing substituents in anionic copolymerization is nil. Correlation of reactivity in copolymerization with structure has been achieved in some studies [Favier et al., 1977; Shima et al., 1962]. The reactivities of various substituted styrenes and methacrylates in anionic polymerization, as well as the reactivities of various vinyl
ethers in cationic polymerization, have been correlated with the $^1$H and $^{13}$C chemical shifts of monomer [Hatada et al., 2002].

The general characteristics of anionic copolymerization are very similar to those of cationic copolymerization. There is a tendency toward ideal behavior in most anionic copolymerizations. Steric effects give rise to an alternating tendency for certain comonomer pairs. Thus the styrene–$p$-methylstyrene pair shows ideal behavior with $r_1 = 5.3$, $r_2 = 0.18$, $r_1 r_2 = 0.95$, while the styrene–$\alpha$-methylstyrene pair shows a tendency toward alternation with $r_1 = 35$, $r_2 = 0.003$, $r_1 r_2 = 0.11$ [Bhattacharyya et al., 1963; Shima et al., 1962]. The steric effect of the additional substituent in the $\alpha$-position hinders the addition of $\alpha$-methylstyrene to $\alpha$-methylstyrene anion. The tendency toward alternation is essentially complete in the copolymerizations of the sterically hindered monomers 1,1-diphenylethylene and trans-1,2-diphenylethylene with 1,3-butadiene, isoprene, and 2,3-dimethyl-1,3-butadiene [Yuki et al., 1964].

### 6-4b-2 Effects of Solvent and Counterion

Monomer reactivity ratios and copolymer compositions in many anionic copolymerizations are altered by changes in the solvent or counterion. Table 6–12 shows data for styrene–isoprene copolymerization at 25°C by $n$-butyl lithium [Kelley and Tobolsky, 1959]. As in the case of cationic copolymerization, the effects of solvent and counterion cannot be considered independently of each other. For the tightly bound lithium counterion, there are large effects due to the solvent. In poor solvents the copolymer is rich in the less reactive (based on relative rates of homopolymerization) isoprene because isoprene is preferentially complexed by lithium ion. (The complexing of 1,3-dienes with lithium ion is discussed further in Sec. 8-6b). In good solvents preferential solvation by monomer is much less important and the inherent greater reactivity of styrene exerts itself. The quantitative effect of solvent on copolymer composition is less for the more loosely bound sodium counterion.

Copolymerizations of nonpolar monomers with polar monomers such as methyl methacrylate and acrylonitrile are especially complicated. The effects of solvent and counterion may be unimportant compared to the side reactions characteristic of anionic polymerization of polar monomers (Sec. 5-3b-4). In addition, copolymerization is often hindered by the very low tendency of one of the cross-propagation reactions. For example, poly(styryl) anions easily add methyl methacrylate but there is little tendency for poly(methyl methacrylate) anions to add styrene. Many reports of styrene–methyl methacrylate (and similar comonomer pairs) copolymerizations are not copolymerizations in the sense discussed in this chapter.

<table>
<thead>
<tr>
<th>Solvent</th>
<th>% Styrene in Copolymer for Counterion</th>
</tr>
</thead>
</table>
| None             | 66  
| Benzene          | 66  
| Triethylamine    | 77  
| Ethyl ether      | 75  
| Tetrahydrofuran  | 80  |
|                  | Na$^+$ | Li$^+$ |
|                  | 15     | 15     |
|                  | 59     | 59     |
|                  | 68     | 68     |
|                  | 80     | 80     |

$^a$ Data from Kelley and Tobolsky [1959].

$^b$ Comonomer feed = 1 : 1 styrene : isoprene.
The initial product is essentially poly(methyl methacrylate) homopolymer. Little styrene is incorporated into copolymer chains until most or all of the methyl methacrylate is exhausted. Reports of significant amounts of styrene in products from anionic copolymerization of styrene–methyl methacrylate are usually artifacts of the particular reaction system, a consequence of heterogeneity of the propagating centers and/or counterion.

The anionic copolymerization of methyl methacrylate and styrene with lithium emulsion and n-butyllithium initiators is interesting [Overberger and Yamamoto, 1966; Richards, 1978; Tobolsky et al., 1958]. Bulk copolymerization of an equimolar mixture of the two monomers with a lithium emulsion yields a copolymer with a high percentage of styrene, whereas n-butyllithium yields a copolymer with essentially no styrene. Further, the product from the lithium emulsion reaction is essentially a block copolymer. The results with lithium emulsion have been attributed to insolubility of lithium counterion. The lithium ion is part of an insoluble lithium particle and propagation takes place on that particle surface. Styrene is more strongly adsorbed than methyl methacrylate on these surfaces because of its dense π-electron system. Reaction occurs with a very high styrene concentration at the reaction site and initial reaction involves a polystyryl homopropagation. At some point the propagating chains detach from the metal surface and become solubilized in the bulk solution, where there is a much higher concentration of methyl methacrylate. Polystyryl anions add methyl methacrylate with very little tendency for reverse crossover back to styrene, and the result is a block copolymer. On the other hand, polymerization initiated by n-butyllithium proceeds in solution from the very beginning. The greater reactivity of methyl methacrylate coupled with the very small tendency for crossover from poly(methyl methacrylate) propagating centers to polystyryl results in the product being essentially poly(methyl methacrylate) homopolymer. Copolymer with significant amounts of styrene is obtained only at higher conversion where the feed composition is low in methyl methacrylate.

6-4b-3 Effect of Temperature

There are few studies of the effect of temperature on monomer reactivity ratios [Morton, 1983]. For styrene–1,3-butadiene copolymerization by s-butyllithium in n-hexane, there is negligible change in $r$ values with temperature with $r_1 = 0.03$, $r_2 = 13.3$ at 0°C and $r_1 = 0.04$, $r_2 = 11.8$ at 50°C. There is, however, a significant effect of temperature for copolymerization in tetrahydrofuran with $r_1 = 11.0$, $r_2 = 0.04$ at −78°C and $r_1 = 4.00$, $r_2 = 0.30$ at 25°C. The difference between copolymerization in polar and nonpolar solvents is attributed to preferential complexing of propagating centers and counterion by 1,3-butadiene as described previously. The change in $r$ values in polar solvent is attributed to the same phenomenon. The extent of solvation decreases with increasing temperature, and this results in 1,3-butadiene participating in the solvation process at the higher reaction temperature.

6-5 DEVIATIONS FROM TERMINAL COPOLYMERIZATION MODEL

The derivation of the terminal (or first-order Markov) copolymer composition equation (Eq. 6-12 or 6-15) rests on two important assumptions—one of a kinetic nature and the other of a thermodynamic nature. The first is that the reactivity of the propagating species is independent of the identity of the monomer unit, which precedes the terminal unit. The second is the irreversibility of the various propagation reactions. Deviations from the quantitative behavior predicted by the copolymer composition equation under certain reaction conditions have been ascribed to the failure of one or the other of these two assumptions or the presence of a comonomer complex which undergoes propagation.
6-5a Kinetic Penultimate Behavior

The behavior of some comonomer systems indicates that the reactivity of the propagating species is affected by the next-to-last (penultimate) monomer unit. This behavior, referred to as second-order Markov or penultimate behavior, manifests itself in a particular copolymerization by giving inconsistent values of the monomer reactivity ratios for different comonomer feed compositions. More specifically, plots of \( F_1, k_p \), and comonomer sequence versus feed composition do not fit Eqs. 6-15, 6-71, and 6-72, respectively, well over the entire range of feed compositions. The ability to discern the failure of the terminal model has not always been apparent. The failure of the terminal model is clear when the deviation is relatively large as it is in radical copolymerizations where the monomers contain highly bulky or polar substituents. For example, in the copolymerization of styrene and fumaronitrile, chains rich in fumaronitrile and having styrene as their last added unit show greatly decreased reactivity with fumaronitrile due to steric and polar repulsions between the penultimate fumaronitrile unit in the propagating chain and the incoming fumaronitrile monomer [Fordyce and Ham, 1951]. The deviation from the terminal model is most apparent for feeds rich in fumaronitrile. In systems where the deviation from the terminal model is smaller, the experimental limitations in \( F_1 \) and \( k_p \) measurements may mask the deviations. However, more recently, the improvements in \( F_1 \) and \( k_p \) measurements indicate that most comonomer systems deviate from the terminal model.

The original mathematical treatment of the penultimate effect was presented by Merz and coworkers [Barb, 1953; Ham, 1964; Merz et al., 1946]. Fukuda and coworkers developed a more extensive treatment, which distinguished between two penultimate models of copolymerization behavior—the explicit penultimate and implicit penultimate models [Coote and Davis, 1999, 2000; Davis, 2001; Fukuda et al., 1985, 1987, 1992, 2002; Ma et al., 2001]. The explicit penultimate model for copolymerization involves the use of eight propagation reactions

\[
\begin{align*}
&\sim M_1 M_1 \cdot + M_1 \xrightarrow{k_{111}} \sim M_1 M_1 M_1 \cdot \\
&\sim M_1 M_1 \cdot + M_2 \xrightarrow{k_{112}} \sim M_1 M_1 M_2 \cdot \\
&\sim M_2 M_2 \cdot + M_1 \xrightarrow{k_{221}} \sim M_2 M_2 M_1 \cdot \\
&\sim M_2 M_2 \cdot + M_2 \xrightarrow{k_{222}} \sim M_2 M_2 M_2 \cdot \\
&\sim M_2 M_1 \cdot + M_1 \xrightarrow{k_{331}} \sim M_2 M_1 M_1 \cdot \\
&\sim M_2 M_1 \cdot + M_2 \xrightarrow{k_{332}} \sim M_2 M_1 M_2 \cdot \\
&\sim M_1 M_2 \cdot + M_1 \xrightarrow{k_{121}} \sim M_1 M_2 M_1 \cdot \\
&\sim M_1 M_2 \cdot + M_2 \xrightarrow{k_{122}} \sim M_1 M_2 M_2 \cdot 
\end{align*}
\]

with four monomer reactivity ratios

\[
\begin{align*}
&r_1 = \frac{k_{111}}{k_{112}} & r'_1 = \frac{k_{211}}{k_{212}} \\
&r_2 = \frac{k_{222}}{k_{221}} & r'_2 = \frac{k_{122}}{k_{121}}
\end{align*}
\]
and two radical reactivity ratios:

\[ s_1 = \frac{k_{211}}{k_{111}} \]  
\[ s_2 = \frac{k_{122}}{k_{222}} \]  

(6-75b)

Each monomer is characterized by two monomer reactivity ratios. One monomer reactivity ratio represents the propagating species in which the penultimate and terminal monomer units are the same. The other represents the propagating species in which the penultimate and terminal units differ. The latter monomer reactivity ratios are signified by the prime notations. Each radical reactivity ratio is the ratio of the propagation rate constant for reaction of a radical in which the penultimate unit differs from the terminal unit compared to the rate constant where the penultimate and terminal units are the same.

The monomer and radical reactivity ratios are used to calculate the adjusted parameters \( r_1, r_2, k_{11}, \) and \( k_{22} \) according to

\[ r_1 = r_0 \frac{f_1 r_1 + f_2}{(f_1 r_1 + f_2/s_1)} \]  
\[ r_2 = r_0 \frac{f_2 r_2 + f_1}{(f_2 r_2 + f_1/s_2)} \]  

(6-76)

\[ k_{11} = k_{111} \frac{(f_1 r_1 + f_2)}{(f_1 r_1 + f_2/s_1)} \]  
\[ k_{22} = k_{222} \frac{(f_2 r_2 + f_1)}{(f_2 r_2 + f_1/s_2)} \]  

(6-77)

The parameters \( \overline{r_1}, \overline{r_2}, \overline{k_{11}}, \) and \( \overline{k_{22}} \) are used in place of \( r_1, r_2, k_{11}, \) and \( k_{22} \) in the terminal model equations for \( F_1 \) (Eq. 6-15) and \( k_p \) (Eq. 6-71).

The \( M_1 \) centered triad monomer sequence distributions are given by

\[ (111) = \frac{r_1 r_1^* f_1^2}{r_1 r_1^* f_1^2 + 2r_1^* f_1 f_2 + f_2} \]  
\[ (112) = (211) = \frac{r_1^* f_1 f_2}{r_1 r_1^* f_1^2 + 2r_1^* f_1 f_2 + f_2^2} \]  
\[ (212) = \frac{f_2^2}{r_1 r_1^* f_1^2 + 2r_1^* f_1 f_2 + f_2^2} \]  

(6-78a)

(6-78b)

(6-78c)

The \( M_2 \) centered triads \((222), (221) = (122), \) and \((121)\) are derived from Eq. 6-78 by reversing the 1 and 2 subscripts.

The implicit penultimate model was proposed for copolymerizations where the terminal model described the copolymer composition and monomer sequence distribution, but not the propagation rate and rate constant. There is no penultimate effect on the monomer reactivity ratios, which corresponds to

\[ \overline{r_1} = r_1^* = r_1 \]  
\[ \overline{r_2} = r_2^* = r_2 \]  

(6-79)
and the terminal model values of the monomer reactivity ratios are retained. There is a
penultimate effect on the radical reactivity ratios and the parameters $r_1$, $r_2$, $k_{11}$, and $k_{22}$
are used in place of $r_1$, $r_2$, $k_{11}$, and $k_{22}$ in the terminal model equation for $k_p$ (Eq. 6-71),
exactly as in the explicit penultimate model. The implicit penultimate model has a penulti-
mate effect on reactivity (which determines propagation rate and rate constant), but not on
selectivity (which determines copolymer composition and monomer sequence distribution).

Penultimate effects have been observed for many comonomer pairs. Among these are the
radical copolymerizations of styrene–fumaronitrile, styrene–diethyl fumarate, ethyl metha-
crylate–styrene, methyl methacrylate–4-vinylpyridine, methyl acrylate–1,3-butadiene,
methyl methacrylate–methyl acrylate, styrene–dimethyl itaconate, hexafluorobutylene–vinyl
acetate, 2,4-dicyano-1-butene–isoprene, and other comonomer pairs [Barb, 1953; Brown and Fujimori, 1987; Buback et al., 2001; Burke et al., 1994a,b, 1995; Cowie et al.,
1990; Davis et al., 1990; Fordyce and Ham, 1951; Fukuda et al., 2002; Guyot and Guillot,
1967; Hecht and Ojha, 1969; Hill et al., 1982, 1985; Ma et al., 2001; Motoc et al., 1978;
Natansohn et al., 1978; Prementeine and Tirrell, 1987; Rousefell and Pittman, 1979;
Van Der Meer et al., 1979; Wu et al., 1990; Yee et al., 2001; Zetterlund et al., 2002].

Although ionic copolymerizations have not been as extensively studied, penultimate effects
have been found in some cases. Thus in the anionic polymerization of styrene–4-vinylpyri-
dine, 4-vinylpyridine adds faster to chains ending in 4-vinylpyridine if the penultimate unit is
styrene [Lee et al., 1963].

The reader is cautioned that literature references prior to 1985–1990 did not distinguish
between the explicit and implicit penultimate models. The prior penultimate model did not
correspond to either the explicit or implicit penultimate models. The pre-1985–1990 penul-
timate model contained only the four monomer reactivity ratios (Eq. 6-74) with no radical
reactivity ratios.

The precision and accuracy of the experimental data must be sufficient to allow one to
discriminate between the terminal, explicit penultimate, and implicit penultimate models,
[Burke et al., 1994a,b, 1995; Landry et al., 2000]. This has not always been the case, espe-
cially in the older literature, and the result has sometimes been contradictory reports. Penul-
timate effects are most easily detected in experiments carried out by including data at very
low or very high $f_1$ values.

Figures 6-12 and 6-13 shows plots of copolymer composition and propagation rate
constant, respectively, versus comonomer feed composition for styrene–diethyl fumarate
copolymerization at 40°C with AIBN [Ma et al., 2001]. The system follows well the implicit
tenvelope model. The copolymer composition data follow the terminal model within
experimental error, which is less than 2% in this system. The propagation rate constant shows
a penultimate effect, and the results conform well to the implicit penultimate model with
$s_1 = 0.055$, $s_2 = 0.32$.

### 6-5b Depropagation during Copolymerization

In contrast to the kinetic approach, deviations from the terminal model have also been treated
from a thermodynamic viewpoint [Kruger et al., 1987; Lowry, 1960; Palmer et al., 2000,
2001]. Altered copolymer compositions in certain copolymerizations are accounted for in
this treatment in terms of the tendency of one of the monomers (M$_2$) to depropagate. An
essential difference between the kinetic and thermodynamic treatments is that the latter
implies that the copolymer composition can vary with the concentrations of the monomers.
If the concentration of monomer M$_2$ falls below its equilibrium value [M]$_e$ at the particular
reaction temperature, terminal M$_2$ units will be prone to depropagate. The result would be a
Fig. 6-12  Plot of $F_1$ versus $f_1$ for copolymerization of styrene ($M_1$) and diethyl fumarate ($M_2$). The solid line represents the terminal model with $r_1 = 0.22$, $r_2 = 0.021$. After Ma et al. [2001] (by permission of American Chemical Society, Washington, DC); an original plot, from which this figure was drawn, was kindly supplied by Dr. T. Fukuda.

Fig. 6-13  Plot of propagation rate constant versus $f_1$ for copolymerization of styrene ($M_1$) and diethyl fumarate ($M_2$). The dotted line represents the terminal model with $r_1 = 0.22$, $r_2 = 0.021$ (i.e., $s_1 = s_2 = 1$). The solid line represents the implicit penultimate model with $s_1 = 0.055$, $s_2 = 0.32$. After Ma et al. [2001] (by permission of American Chemical Society, Washington, DC); an original plot, from which this figure was drawn, was kindly supplied by Dr. T. Fukuda.
decrease in the amount of this monomer in the copolymer. The kinetic approach does not predict any dependence of the copolymer composition on the monomer concentration. Further, the thermodynamic approach differs from the kinetic approach in that the former emphasizes the temperature dependence of the copolymer composition since the polymerization–depolymerization equilibrium is temperature-dependent. (The penultimate model does not, however, predict the copolymer composition to be independent of temperature. The effect of temperature in the penultimate model comes from the variation of the four monomer reactivity ratios and two radical reactivity ratios with temperature.)

The present discussion will be almost completely limited to copolymerizations in which only one of the monomers has a tendency to depropagate. systems in which both monomers tend to depropagate are difficult to treat mathematically and also involve a large number of unknown parameters. Different types of copolymerization behavior can be considered depending on whether one assumes penultimate effects on the depropagation reaction. Thus Lowry [1960] considers two different cases in which monomer M1 has absolutely no tendency to depropagate irrespective of the preceding units in the chain, while monomer M2 has no tendency to depropagate if it is attached to an M1 unit. The two cases differ in the different tendencies of monomer M2 to depropagate. In case I, M2 tends to depropagate if it is attached to another M2 unit:

\[
\sim M_1M_2M_2^* \rightarrow \sim M_1M_2^* + M_2 \tag{6-80}
\]

In case II, M2 tends to depropagate only when it is attached to a sequence of two or more M2 units:

\[
\sim M_1M_2M_2M_2^* \rightarrow \sim M_1M_2M_2^* + M_2 \tag{6-81}
\]

Thus \(\sim M_1M_2^*\) does not depropagate in case I, while neither \(\sim M_1M_2^*\) nor \(\sim M_1M_2M_2^*\) depropagate in case II.

The copolymer composition for case I is given by [Kruger et al., 1987; Lowry, 1960; Szymanski, 1987]

\[
\frac{d|M_1|}{d|M_2|} = \frac{(r_1|M_1| + |M_2|)(1 - \alpha)}{|M_2|} \tag{6-82}
\]

with \(\alpha\) defined by

\[
\alpha = \frac{1}{2} \left( \left\{ 1 + K|M_2| + \left( \frac{K|M_1|}{r_2} \right) \right\} - \left[ \left\{ 1 + K|M_2| + \left( \frac{K|M_1|}{r_2} \right) \right\}^2 - 4K|M_2| \right]^{1/2} \right) \tag{6-83}
\]

where \(K\) is the equilibrium constant for the equilibrium in Eq. 6-80.

The copolymer composition for case II is given by

\[
\frac{d|M_1|}{d|M_2|} = \left\{ \left( \frac{r_1|M_1|}{|M_2|} \right) + 1 \right\} \left( \alpha + \frac{\alpha}{(1 - \alpha)} \right) \left( x\gamma - 1 + \left\{ \frac{1}{(1 - \alpha)} \right\}^2 \right) \tag{6-84}
\]
with \( \alpha \) defined by Eq. 6-83 and \( \gamma \) by

\[
\gamma = \frac{\left\{ K[M_2] + \frac{K[M_1]}{r_2} - \alpha \right\}}{k[M_2]} \tag{6-85}
\]

where \( K \) is now the equilibrium constant for the equilibrium in Eq. 6-81.

The *depropagation model* described above has been tested in several copolymerizations [Cais and Stuk, 1978; Florjanczyk and Krawiec, 1989; Hinton and Spencer, 1976; Ivin and Spensley, 1967; Motoc and Vancea, 1980; O’Driscoll and Gasparro, 1967; Palmer et al., 2000, 2001; Sawada, 1976]. The systems studied include the radical copolymerization of \( \alpha \)-methylstyrene-methyl methacrylate, \( N \)-phenylmaleimide–styrene, 1,1-diphenylethylene–methyl acrylate, styrene–\( \alpha \)-methylstyrene, styrene–methyl methacrylate, and acrylonitrile–\( \alpha \)-methylstyrene. (Vinylmesitylene is 2,4,6-trimethylstyrene.) Most of these copolymerizations were studied over a range of comonomer feed compositions, reaction temperatures, and monomer concentrations. There is a transition from behavior consistent with the terminal model to behavior described by the depropagation model as the reaction conditions are altered (increased temperature, decreased monomer concentration) to favor depropagation. Thus in the radical copolymerization of styrene–\( \alpha \)-methylstyrene, one observes a decrease in the \( \alpha \)-methylstyrene content of the copolymer as the reaction temperature is increased from 0 to 100°C [O’Driscoll and Gasparro, 1967]. With increased temperature, there is increased depropagation of \( \alpha \)-methylstyrene due to its low ceiling temperature (Sec. 3-9c). The effect is greatest for comonomer feed compositions rich in \( \alpha \)-methylstyrene. The data in this system followed the quantitative behavior expected for case II depropagation.

The anionic copolymerization of vinylmesitylene–\( \alpha \)-methylstyrene is an interesting system. The copolymerization was first studied at –78°C at high monomer concentrations to determine the monomer reactivity ratios under conditions where depropagation was negligible. At the higher reaction temperature of 0°C, depropagation was still not important as long as the concentration of vinylmesitylene \( [M_2] \) was sufficiently above the value of \( [M_2]_c \) at that temperature. \( [M_2]_c \) is 0.75 mol L\(^{-1}\) at 0°C. When the vinylmesitylene concentration decreased below \( [M_2] \), at constant \( [M_1]/[M_2] \), depropagation became significant and the vinylmesitylene content of the copolymer decreased (solid plot in Fig. 6-14). The theoretical plots for this copolymerization for the case I and case II mechanisms were calculated form Eqs. 6-82 and 6-84 using the values of \( [M_1] \), \( [M_2] \), \( r_1 \), \( r_2 \), and \( K \). The \( K \) value used in the calculations is, by necessity, that obtained from the polymerizaton–depolymerization equilibrium data for the homopolymerization of \( M_2 \). The results are shown as the dashed plots in Fig. 6-14. The case II mechanism fits the experimental data more closely than the case I mechanism. This is the general behavior that has been observed for most of the systems studied. It has been noted that the theoretical curve would fit the data even more closely if one assumed that monomer \( M_1 \) also tends to depropagate. Copolymerization with both \( M_1 \) and \( M_2 \) undergoing depropagation has been mathematically treated, but the result is difficult to apply [Lowry, 1960].

### 6-5c Copolymerization with Complex Participation

Another model used to describe deviations from the terminal model involves the participation of a comonomer complex (Sec. 6-3b-3) [Cais et al., 1979; Coote and Davis, 2002; Coote et al., 1998; Seiner and Litt, 1971]. The comonomer complex competes with each of the individual monomers in propagation. The *monomer complex participation model* involves eight
propagation steps, the four propagation steps of the individual monomers (Eqs. 6-2 through 6-5), the four propagation steps of the comonomer complex

\[
\begin{align*}
M_1^p + \frac{M_2M_1}{k_{122}} &\rightarrow M_1^p \\
M_1^p + \frac{M_1M_2}{k_{122}} &\rightarrow M_2^p \\
M_2^p + \frac{M_2M_1}{k_{221}} &\rightarrow M_1^p \\
M_2^p + \frac{M_1M_2}{k_{221}} &\rightarrow M_2^p
\end{align*}
\]

(6-86)

and the equilibrium between uncomplexed and complexed monomers

\[
M_1^p + M_2^o \xlongrightleftharpoons{K} M_1M_2
\]

(6-87)

with a total of six reactivity ratios

\[
\begin{align*}
r_1 &= \frac{k_{11}}{k_{12}} & r_2 &= \frac{k_{22}}{k_{21}} \\
r_{1C} &= \frac{k_{112}}{k_{121}} & r_{2C} &= \frac{k_{221}}{k_{212}} \\
s_{1C} &= \frac{k_{112}}{k_{11}} & s_{2C} &= \frac{k_{221}}{k_{22}}
\end{align*}
\]

(6-88)

where \(M_2M_1\) and \(M_1M_2\) represent the complex adding to a propagating center at the \(M_2\) and \(M_1\) ends, respectively.
The copolymer composition and propagation rate constant are given by

\[
\begin{align*}
F_1 &= f_1^0 (A_2B_1) r_1 f_1^0 + (A_1C_2) f_2^0 \\
F_2 &= f_2^0 (A_1B_2) r_2 f_2^0 + (A_2C_1) f_1^0 \\
K_p &= \frac{(A_2B_1) r_1 (f_1^0)^2 + (A_1B_2) r_2 (f_2^0)^2 + (A_1C_2 + A_2C_1) f_1^0 f_2^0}{(A_2r_1 f_1^0/k_{11}) + (A_1r_2 f_2^0/k_{22})}
\end{align*}
\]

where

\[
A_1 = 1 + r_1 s_1 C \frac{Q}{f_1} \\
B_1 = 1 + s_1 \left( 1 + \frac{1}{r_{1c}} \right) Q f_2 \\
C_1 = 1 + r_1 s_1 \left( 1 + \frac{1}{r_{1c}} \right) Q f_1 \\
A_2 = 1 + r_2 s_2 C \frac{Q}{f_2} \\
B_2 = 1 + s_2 \left( 1 + \frac{1}{r_{2c}} \right) Q f_1 \\
C_2 = 1 + r_2 s_2 \left( 1 + \frac{1}{r_{2c}} \right) Q f_2
\]

\[
2Q f_1^0 = \left[ Q(f_2 - f_1) + 1 \right]^2 + 4Q f_1 \right]^{1/2} - [Q(f_1 - f_2) + 1] \\
Q = K([M_1] + [M_2])
\]

\[
f_1 = \frac{[M_1]}{[M_1] + [M_2]} \quad f_2 = \frac{[M_2]}{[M_1] + [M_2]} \quad f_1^0 = \frac{[M_1]^2}{[M_1] + [M_2]} \quad f_2^0 = \frac{[M_2]^2}{[M_1] + [M_2]}
\]

Concentrations and mole fractions with superscript \(^0\) refer to uncomplexed monomer. Concentrations and mole fractions without superscript \(^0\) refer to the comonomer feed, specifically, the sum of complexed and uncomplexed monomer.

The complex participation model, like the depropagation model, predicts a variation of the copolymer composition with temperature and monomer concentration. The effect of temperature comes from the change in \(K\), resulting in a decrease in the concentration of the comonomer complex with increasing temperature. Increasing monomer concentration at a constant \(f_1\) increases the comonomer complex concentration.

The complex participation model has been tested in the radical copolymerizations of 1,1-diphenylethylene–methyl acrylate, styrene–β-cyanoacrolein, vinyl acetate–hexafluoroacetone, N-vinylcarbazole–diethyl fumarate, N-vinylcarbazole–fumaronitrile, maleic anhydride–vinyl acetate, styrene–maleic anhydride [Burke et al., 1994a,b; Cais et al., 1979; Coote and Davis, 2002; Coote et al., 1998; Dodgson and Ebdon, 1977; Fujimori and Craven, 1986; Georgiev and Zubov, 1978; Litt, 1971; Litt and Seiner, 1971; Yoshimura et al., 1978].

A variation of the complex participation model, referred to as the monomer complex dissociation model, involves disruption of the complex during reaction with a propagating chain end [Hill et al., 1983; Karad and Schneider, 1978]. Reaction of the propagating center with
the complex results in the addition of only one of the monomers with liberation of the unreacted monomer. The overall result is that the complex alters monomer reactivities.

6-5d Discrimination between Models

The ability to determine which copolymerization model best describes the behavior of a particular comonomer pair depends on the quality of the experimental data. There are many reports in the literature where different workers conclude that a different model describes the same comonomer pair. This occurs when the accuracy and precision of the composition data are insufficient to easily discriminate between the different models or composition data are not obtained over a wide range of experimental conditions (feed composition, monomer concentration, temperature). There are comonomer pairs where the behavior is not sufficiently extreme in terms of depropagation or complex participation or penultimate effect such that even with the best composition data it may not be possible to conclude that only one model fits the composition data [Hill et al., 1985; Moad et al., 1989].

The sequence distributions expected for the different models have been described [Hill et al., 1982, 1983; Howell et al., 1970; Tirrell, 1986] (Sec. 6-5a). Sequence distributions obtained by $^{13}$C NMR are sometimes more useful than composition data for discriminating between different copolymerization models. For example, while composition data for the radical copolymerization of styrene–acrylonitrile are consistent with either the penultimate or complex participation model, sequence distributions show the penultimate model to give the best fit.

The termination rate constants and molecular weights for the different copolymerization models have also been studied for purposes of discriminating between different copolymerization models [Buback and Kowollik, 1999; Landry et al., 1999].

6-6 COPOLYMERIZATIONS INVOLVING DIENES

6-6a Crosslinking

Diene monomers are often used in copolymerizations to obtain a crosslinked structure in the final product. The reaction is generally analogous to step polymerizations involving tri- and tetrafunctional reactants (Sec. 2-10). Crosslinking occurs early or late in the copolymerization depending on the relative reactivities of the two double bonds of the diene. The extent of crosslinking depends on the latter and on the amount of diene relative to the other monomer. There is an extensive literature on the mathematical treatment of the crosslinking process [Dotson et al., 1988; Enright and Zhu, 2000; Flory, 1947, 1953; Macosko and Miller, 1976; Matsumoto et al., 2000; Scranton and Peppas, 1990; Shultz, 1966; Szuromi et al., 2000; Tobita and Hamielec, 1989; Williams and Vallo, 1988]. Several different cases can be distinguished depending on the type of diene. In most instances it is assumed that the diene is present at low concentrations.

The first case is the copolymerization of monomer A with diene BB where all the double bonds (i.e., the A double bond and both B double bonds) have the same reactivity. Methyl methacrylate–ethylene glycol dimethacrylate (EGDM), vinyl acetate–divinyl adipate (DVA), and styrene–p- or m-divinylbenzene (DVB) are examples of this type of copolymerization system [Landin and Macosko, 1988; Li et al., 1989; Storey, 1965; Ulbrich et al., 1977]. Since $r_1 = r_2$, $F_1 = f_1$ and the extent of reaction $p$ of A double bonds equals that of B double bonds. There are $p[A]$ reacted A double bonds, $p[B]$ reacted B double bonds, and $p^2[BB]$ reacted BB monomer units. [A] and [B] are the concentrations of A and B double bonds,
[BB] is the concentration of BB, and \( [B] = 2[B] \). The number of crosslinks is simply the number of BB monomer molecules in which both B double bonds are reacted, that is, \( p^2[B] \). The number of polymer chains is the total number of A and B double bonds reacted divided by the degree of polymerization, \( ([A] + [B])p/X_w \) (the weight-average degree of polymerization is employed for reasons previously described in Sec. 2-10). The critical extent of reaction at the gel point \( p_c \) occurs when the number of crosslinks per chain is \( \frac{1}{2} \) and thus is given by

\[
p_c = \frac{[A] + [B]}{[B]X_w}
\]  

(6-92)

\( X_w \) in Eq. 6-92 is essentially the weight-average degree of polymerization that would be observed in the polymerization of monomer A in the absence of diene BB. Equation 6-92 predicts that extensive crosslinking occurs during this type of copolymerization. Thus gelation is observed at 12.5\% reaction in the methyl methacrylate–ethylene glycol dimethacrylate system containing 0.05 mol\% EGDM [Walling, 1945; Yoshimura et al., 1978]. The use of Eq. 6-92 for the styrene–\( p \)-divinylbenzene (DVB) system is shown in Table 6-13. The equation holds best for systems containing low concentrations of the diene monomer; its utility decreases as the concentration of diene increases. With increasing diene concentration, Eq. 6-92 predicts gel points at conversions that are increasingly lower than those found experimentally. This general behavior has been attributed to the wastage of the diene monomer due to intramolecular cyclization (Sec. 6-6b). Also, there is an indication that the reactivity of the second double bond in BB is decreased on reaction of the first double bond as a consequence of its presence in a polymer chain [Hild and Okasha, 1985].

An alternate expression for \( p_c \) is given by

\[
p_c = \frac{(1 - q)}{[af(f - 2)(q + \xi/2)]}
\]  

(6-93)

where \( q \) is the ratio of the propagation rate to the sum of the propagation rate and the rates of all termination and transfer reactions, \( \xi \) is given by the ratio of the rate of termination by coupling to the sum of all termination and transfer reaction, \( f \) is the functionality of the diene and is equal to 4 (i.e., each double bond is bifunctional), and \( a \) is the fraction of all functional groups in the reaction mixture belonging to the diene [Macosko and Miller, 1976; Williams and Vallo, 1988].

A second case is the copolymerization of A and BB in which the reactivities of the two groups are not equal but are, instead, \( r_1 \) and \( r_2 \), respectively. In this case the critical extent of

---

**TABLE 6-13 Crosslinking in the Copolymerization of Styrene–Divinylbenzene**

<table>
<thead>
<tr>
<th>Mole Fraction DVB</th>
<th>Calculated from Eq. 6-92</th>
<th>Observed*</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.004</td>
<td>0.21</td>
<td>0.16</td>
</tr>
<tr>
<td>0.008</td>
<td>0.10</td>
<td>0.14</td>
</tr>
<tr>
<td>0.02</td>
<td>0.042</td>
<td>0.076</td>
</tr>
<tr>
<td>0.032</td>
<td>0.026</td>
<td>0.074</td>
</tr>
<tr>
<td>0.082</td>
<td>0.010</td>
<td>0.052</td>
</tr>
<tr>
<td>0.30</td>
<td>0.0042</td>
<td>0.045</td>
</tr>
</tbody>
</table>

*Data from Storey [1965].
reaction at gelation is given by
\[ p_c = \frac{(r_1[A]^2 + 2[A][B] + r_2[B]^2)^2}{X_w[B][([A] + [B])(r_2[B] + [A])]} \] (6-94)

which reduces to
\[ p_c = \frac{[A]r_1^2}{B[X_w]} \] (6-95)

for \([A] \gg [B]\). When the double bonds of the diene are more reactive than that of the other monomer \((r_2 > r_1)\), crosslinking occurs in the early stages of the copolymerization. Crosslinking is delayed until the later stages if \(r_1 > r_2\). For the system where \(r_1 > r_2\) and \(r_1 > 1\) crosslinking is not as extensive at a given extent of reaction as that taking place in copolymerizations of the type governed by Eq. 6-92, where \(r_1 = r_2\).

The third case is the copolymerization of a monomer A with the diene BC where groups A and B have equal reactivity, but group C has a much lower reactivity. An example of such a case would be methyl methacrylate-allyl methacrylate, where A and B are the two methacrylate groups and C is the allyl group. If \(r\) is the reactivity ratio between the C and B groups, then the following hold for the radicals derived from the A and B groups:
\[ r = \frac{k_{AC}}{k_{AA}} = \frac{k_{AC}}{k_{AB}} = \frac{k_{BC}}{k_{BA}} = \frac{k_{BC}}{k_{BB}} \] (6-96)

For such a system the copolymer will consist of copolymerized A and B groups with pendant, unreacted C groups until the later stages of reaction. Crosslinking does not occur until relatively late in the reaction due to the low reactivity of the C group. The critical extent of reaction at gelation in this case is given by
\[ p_c = 1 - \exp\left(-\frac{1}{2qX_w r}\right) \] (6-97)

where \(q\) is the mole fraction of the diene in the initial comonomer feed.

In selecting the makeup of a crosslinking system one has a number of variables that can be used to control the process. Thus gelation can be delayed with the production of a high-conversion uncrosslinked product, which is amenable to subsequent crosslinking. Gelation can be delayed by reducing the amount of the diene, the degree of polymerization by using chain-transfer agents, or the reactivity of one of the double bonds of the diene by proper choice of the diene reactant. The extent of crosslinking in the final product is also controlled by these variables. Extensive crosslinking, with the formation of tight network structures, is obtained by avoiding chain transfer and using increased amounts of dienes whose double bonds have similar reactivities.

A special situation that is often encountered is that where the reaction of one of the double bonds of the diene results in a decrease in the reactivity of the remaining double bond. If the decrease in reactivity is large, the effect is to markedly delay the crosslinking reaction. This case then becomes very similar to the last one where the C group has a much lower reactivity than the A and B groups. The most notable case in which there is a large drop in reactivity of one group on reaction of the other is in the copolymerization of 1,3-dienes where 1,4-polymerization leads to residual 2,3-double bonds that have lowered reactivity. These are subsequently used to bring about crosslinking by reactions discussed in Sec. 9-2b.
The polymerization of unconjugated dienes [e.g., diallyl phthalate, diethylene glycol bis(allyl carbonate), diallyl maleate] and trienes (e.g., triallyl cyanurate) to form highly crosslinked thermoset products is a commercially important process. An example is the use of various dimethacrylate dental filling materials [Nicholson and Anstice, 1999]. This is also true of the use of such monomers to bring about crosslinking in copolymerization systems (Sec. 6-6a). The crosslinking reaction is almost always found to be somewhat inefficient in that the experimental gel points occur at higher extents of reaction than those predicted by theory. There is a wastage of the diene or triene monomer which has been ascribed to intramolecular cyclization of the diene or triene. This phenomenon is encountered not only in homo- and copolymerizations involving dienes and trienes but also in step polymerizations with trifunctional reactants (Sec. 2-10c).

The extent of cyclization varies considerably depending on the particular reaction system. There are some reactants for which cyclization is very extensive. The competition between the intermolecular and intramolecular reactions in the polymerization of a diene is depicted in Eqs. 6-98 through 6-100, where Z is a structural unit such as the benzene ring in divinylbenzene or the trimethylene group in 1,6-heptadiene. Intermolecular propagation proceeds according to the horizontal set of reactions (Eq. 6-98) to produce a linear polymer with pendant double bonds. The pendant double bonds of a propagating or terminated polymer chain give rise to a crosslinked final product by copolymerizing with either unreacted monomer or the pendant double bonds of other chains. Cyclization occurs when propagating species IV reacts intramolecularly with its own pendant double bond in preference to intermolecular propagation. Attachment of the radical center at the methylene and methine carbons of the pendant double bond yields different-sized ring structures as shown in VIII and IX, respectively. Similar reaction sequences would apply for the competition between inter- and intramolecular propagations in polymerizations involving trienes or copolymerizations in which one of the monomers is a diene or triene. Copolymerizations are more complicated since cyclization can occur before as well as after the addition of the second monomer to a propagating species such as IV.
The importance of intramolecular cyclization was emphasized when Butler and coworkers found that the radical polymerization of \( N, N, N, N \)-diallyldimethylammonium chloride (DADMAC) gave soluble, uncrosslinked polymers with little or no unsaturation (Eq. 6-101) [Butler and Angelo, 1957; Butler and Ingley, 1951; Wandrey et al., 1999]. There is a very low tendency for radical IV to propagate intermolecularly and undergo crosslinking. The predominant reaction is intramolecular cyclization, and the product is a linear product with cyclic structures in the backbone. The reaction is referred to as alternating intra/intermolecular polymerization or cyclopolymerization.

\[
\begin{align*}
\text{CH}_2=\text{CH} & \quad \text{CH} \equiv \text{CH}_2 \\
\text{CH}_2 & \quad \text{N} \quad \text{CH}_2 \\
\text{CH}_3 & \quad \text{CH}_3 \\
\text{Cl} &
\end{align*}
\]

The size of the ring structure that can be formed determines whether intermolecular polymerization or intramolecular cyclization is the predominant reaction for a particular monomer [Butler, 1986, 1989, 1992, 1996, 2000; Kodaira, 2000; Marvel and Vest, 1957, 1959]. The extent of cyclization generally increases in the following order: 5- and 6-membered rings appreciably greater than 7-membered rings and the latter greater than larger sized rings. 1,6-Dienes (\( Z \) in Eqs. 6-98 through 6-100 contains three ring atoms) such as acrylic and methacrylic anhydrides, diallyl quaternary ammonium salts, methyl allyl maleate and fumarate, and allyl methacrylate cyclopolymerize to 5- or 6-membered rings or mixtures of the two. Formation of the 5-membered ring involves kinetic control of the cyclization process proceeding through the less stable radical VII to form polymer IX instead of thermodynamic control, proceeding through radical VI to form the more stable 6-membered ring structure VIII. Interestingly, diallyl amines and ammonium salts and divinyl formal form 5-membered rings almost exclusively. Acrylic anhydride forms a mixture of 5- and 6-membered rings while methacrylic anhydride forms only 6-membered rings. Methyl allyl maleate forms mostly 5-membered rings, while methyl allyl fumarate forms mostly the 6-membered ring. Diallyldimethylsilane forms mostly 6-membered rings [Saigo et al., 1988]. Dimethacrylamide forms mostly the 6-membered ring, while \( N \)-substituted dimethacrylamides form mostly the 5-membered ring. Some systems show a considerable effect of reaction conditions on rings size. Decreasing reaction temperature and solvent polarity result in large decreases in the content of 5-membered rings in the polymerization of acrylic anhydride [Butler and Matsumoto, 1981]. The ring size for methacrylic anhydride is unaffected by reaction temperature and solvent polarity. The variety of behaviors for different diene structures and the sensitivity of some systems to reaction conditions indicate a complex competition between kinetic control and thermodynamic control.

Five-membered rings are usually formed from 1,5-dienes such as 1,5-hexadiene; there are no reports of the formation of the 4-membered ring structure (\( Z = \) two ring atoms). However, cyclopolymerization of \( o \)-divinylbenzene forms 7-membered rings via a ring closure reaction involving three double bonds per each pair of diene molecules [Costa et al., 1978] (Eq. 6-102). Cyclopolymerization is observed for ionic polymerizations as well as radical, although the former have been much less studied. Other types of cyclopolymerizations
The competition between the rates of intermolecular propagation $R_p$ and intramolecular cyclization $R_c$ can be expressed in terms of the fraction of cyclized units $f_c$ defined by

$$f_c = \frac{R_c}{R_c + R_p} \tag{6-103}$$

where

$$R_p = 2k_p[M^*][M] \tag{6-104}$$
$$R_c = k_c[M^*] \tag{6-105}$$

Equation 6-106 shows that the extent of cyclization is greater at low concentration. Intermolecular propagation is increasingly favored with increasing $[M]$. The cyclization ratio $k_c/k_p$ is obtained from the slope of a plot of $f_c$ versus $[M]$. Values of $k_c/k_p$ are in the range 2–20 mol L$^{-1}$ for most symmetric 1,6-dienes but some values are even higher; for instance, divinyl formal has a value of 200. 1,5-Dienes generally have lower $k_c/k_p$ values than their 1,6 counterparts. The high tendency toward cyclization is due to a favorable entropy factor. Cyclization has a higher activation energy than does intermolecular propagation. However, cyclization proceeds with a considerably smaller decrease in activation entropy than does intermolecular propagation. For example, for methacrylic anhydride, the activation energy factor favors intermolecular propagation by 10.9 kJ mol$^{-1}$, while cyclization is favored by the Arrhenius frequency factor by 256 mol L$^{-1}$. The overall result is a $k_c/k_p$ value of 2.4 mol L$^{-1}$. The tendency toward cyclization increases with increasing reaction temperature since cyclization has a higher activation energy than does intermolecular propagation. Cyclization is also increased by using more polar solvents but the mechanism for the solvent effect is not understood [Matsumoto et al., 1987].

The tendency toward cyclization decreases considerably (lower $k_c/k_p$ value) for unsymmetric 1,6-dienes, such as allyl methacrylate, where the two double bonds have significantly different reactivities. The polymer contains linear repeat units, rings, and pendant double bonds in relative amounts determined by $k_c/k_p$. The pendant double bonds eventually react to yield a crosslinked structure. Reactants with more than two double bonds per molecule,
whether symmetric such as triallylcyanurate and tetraallyl ammonium bromide or unsymmetric such as diallyl maleate, behave similarly with the formation of crosslinked network structures.

The extent of cyclization decreases quite sharply as one goes to ring sizes of 7 or more atoms. However, contrary to expectations, the extent of cyclization is still quite significant for many monomers. Thus the extent of cyclization (measured as the percent of monomer units that are cyclized) is 15–20% for diallyl esters giving ring structures containing up to 17 atoms [Holt and Simpson, 1956]. The polymerization of o-diallyl phthalate yields a polymer with more than 40% cyclization [Eaton et al., 1989; Matsumoto et al., 1980].

Cyclopolymerizations yielding more complex ring structures have also been reported [Butler, 19896, 1989]. For example, 1,4-dienes such as divinyl ether yield uncrosslinked products with little or no unsaturation and possessing different bicyclic structures. The formation of one of the bicyclic structures is shown in Eq. 6-107 [Tsukino and Kunitake, 1979].

\[
\begin{align*}
\text{Cyclo-copolymerization} & \text{ is cyclopolymerization of a pair of monomers [Butler, 2000]. An} \\
\text{example is the generation of pyran rings by copolymerization between maleic anhydride and} \\
\text{the two double bonds of divinyl ether:}
\end{align*}
\]

Recall the discussion in Sec. 2-3 concerning the competition between linear polymerization and cyclization in step polymerizations. Cyclization is not competitive with linear polymerization for ring sizes greater than 7 atoms. Further, even for most of the reactants, which would yield rings of 5, 6, or 7 atoms if they cyclized, linear polymerization can be made to predominate because of the interconvertibility of the cyclic and linear structures. The difference in behavior between chain and step polymerizations arises because the cyclic structures in chain polymerization do not depropagate under the reaction conditions; that is, the cyclic structure does not interconvert with the linear structure.

6-6c Interpenetrating Polymer Networks

An interpenetrating polymer network (IPN) (Sec. 2-13c-3) is obtained by carrying out a polymerization with crosslinking in the presence of another already crosslinked polymer [Klempner
and Berkowski, 1987]. For example, a crosslinked polyurethane is swollen with a mixture of methyl methacrylate, trimethylolpropane trimethacrylate, and benzoyl peroxide and heated. The methacrylate system polymerizes to a crosslinked network which interpenetrates the polyurethane network. An IPN has the potential for combining the properties of two different crosslinked polymers.

6-7 OTHER COPOLYMERIZATIONS

6-7a Miscellaneous Copolymerizations of Alkenes

A variety of reactants—including sulfur dioxide, carbon monoxide, and oxygen, which do not homopolymerize—undergo radical copolymerization with alkenes to form polymeric sulfones [Bae et al., 1988; Cais and O’Donnell, 1976; Dainton and Ivin, 1958; Florjanczyk et al., 1987; Soares, 1997], ketones [Sommazzi and Garbassi, 1997; Starkweather, 1987, and peroxides [Cais and Bovey, 1977; Mukundan and Kishore, 1987; Nukui et al., 1982]:

\[
\begin{align*}
\text{CH}_2\text{CHR} + \text{SO}_2 & \longrightarrow \left\{ \text{CH}_2\text{CHR-} \text{SO}_2 \right\}_n \quad (6-109) \\
\text{CH}_2\text{CHR} + \text{CO} & \longrightarrow \left\{ \text{CH}_2\text{CHR-} \text{CO} \right\}_n \quad (6-110) \\
\text{CH}_2\text{CHR} + \text{O}_2 & \longrightarrow \left\{ \text{CH}_2\text{CHR-} \text{O}_2 \right\}_n \quad (6-111)
\end{align*}
\]

The reaction with sulfur dioxide is the most studied of these copolymerizations. Only alkenes such as ethylene, \(\alpha\)-olefins, vinyl chloride, and vinyl acetate, without strong electron-withdrawing substituents and that yield highly reactive radicals, undergo facile copolymerization with sulfur dioxide. Many of these monomers yield 1 : 1 alternating copolymers as a result of the polar effect between the electropositive sulfur dioxide and alkene double bond. Copolymers with greater than 50% sulfur dioxide are not formed as a result of polar repulsions between adjacent SO\(_2\) units. Monomers without strong electron-withdrawing substituents but that yield relatively stable radicals, such as styrene and 1,3-butadiene, are less reactive toward sulfur dioxide or form copolymers containing less sulfur dioxide than the alternating structure. Monomers with strong electron-withdrawing substituents, such as acrylonitrile and methyl methacrylate, generally do not form copolymers due to polar repulsions with the electrophilic sulfur dioxide. Many copolymerizations with sulfur dioxide show a significant tendency toward depnovation. Depropagation is increasingly important as the substituent on the alkene monomer becomes bulkier or more electropositive.

There is a tendency toward alternation in the copolymerization of ethylene with carbon monoxide. Copolymerizations of carbon monoxide with tetrafluoroethylene, vinyl acetate, vinyl chloride, and acrylonitrile have been reported but with few details [Starkweather, 1987]. The reactions of alkenes with oxygen and quinones are not well defined in terms of the stoichiometry of the products. These reactions are better classified as retardation or inhibition reactions because of the very slow copolymerization rates (Sec. 3-7a). Other copolymerizations include the reaction of alkene monomers with sulfur and nitroso compounds [Green et al., 1967; Miyata and Sawada, 1988].

6-7b Copolymerization of Carbonyl Monomers

Although the homopolymerization of carbonyl monomers has been studied fairly extensively (Sec. 5-6), there are only a few reported studies on the copolymerization of these monomers

\[
\text{RCHO} + \text{R’CHO} \longrightarrow \left\{ \text{CHR-} \text{O-} \text{CHR’-} \text{O} \right\}_n \quad (6-112)
\]
Cationic copolymerizations of acetaldehyde with formaldehyde and other higher aldehydes have been carried out [Furukawa and Saegusa, 1963; Vogl, 1967, 2000]. Anionic copolymerizations have been reported with formaldehyde, acetaldehyde, and various chloro-substituted acetaldehydes [Furukawa and Saegusa, 1963]. Many of these studies are too fragmentary to give a clear picture of the reaction. In some cases it is unclear whether block or statistical copolymers were obtained. The identity of the initiator appeared to be important in other instances. Depending on the initiator, a comonomer pair might yield homopolymer, block copolymer, or statistical copolymer. The general tendency in the copolymerization of carbonyl monomers is ideal behavior. However, there is a trend toward alternation for comonomer pairs in which one of the monomers has a bulky substituent. Thus the anionic copolymerization of acetaldehyde (M₁)-chloral (M₂) at \(-78^\circ\text{C}\) shows an alternation tendency with \(r_1 = 0.18\) and \(r_2 = 0\) [Iwata et al., 1964].

The copolymerization of carbonyl monomers with alkenes has been even less studied than that between different carbonyl monomers. The radiation-initiated copolymerization of styrene with formaldehyde proceeds by a cationic mechanism with a trend toward ideal behavior, \(r_1 = 52\) and \(r_2 = 0\) at \(-78^\circ\text{C}\) [Castille and Stannett, 1966]. Hexafluoroacetone undergoes radiation-initiated copolymerization with ethylene, propene, and other \(\alpha\)-olefins [Watanabe et al., 1979]. Anionic copolymerizations of aldehydes with isocyanates have also been reported [Odian and Hiraoka, 1972].

### 6-8 APPLICATIONS OF COPOLYMERIZATION

#### 6-8a Styrene

Most polystyrene products are not homopolystyrene since the latter is relatively brittle with low impact and solvent resistance (Secs. 3-14b, 6-1a). Various combinations of copolymerization and blending are used to improve the properties of polystyrene [Moore, 1989]. Copolymerization of styrene with 1,3-butadiene imparts sufficient flexibility to yield elastomeric products [styrene–1,3-butadiene rubbers (SBR)]. Most SBR rubbers (trade names: Buna, GR-S, Philprene) are about 25% styrene–75% 1,3-butadiene copolymer produced by emulsion polymerization; some are produced by anionic polymerization. About 2 billion pounds per year are produced in the United States. SBR is similar to natural rubber in tensile strength, has somewhat better ozone resistance and weatherability but has poorer resilience and greater heat buildup. SBR can be blended with oil (referred to as oil-extended SBR) to lower raw material costs without excessive loss of physical properties. SBR is also blended with other polymers to combine properties. The major use for SBR is in tires. Other uses include belting, hose, molded and extruded goods, flooring, shoe soles, coated fabrics, and electrical insulation.

Styrene–1,3-butadiene copolymers with higher styrene contents (50–70%) are used in latex paints. Styrene and 1,3-butadiene terpolymerized with small amounts of an unsaturated carboxylic acid are used to produce latexes that can be crosslinked through the carboxyl groups. These carboxylated SBR products are used as backing material for carpets. Styrene copolymerized with divinyl benzene yields crosslinked products, which find use in size-exclusion chromatography and as ion-exchange resins (Sec. 9-6).

Radical copolymerization of styrene with 10–40% acrylonitrile yields styrene–acrylonitrile (SAN) polymers. Acrylonitrile, by increasing the intermolecular forces, imparts solvent resistance, improved tensile strength, and raises the upper use temperature of polystyrene although impact resistance is only slightly improved. SAN finds applications in houseware
Acrylonitrile–butadiene–styrene (ABS) polymers (trade names: Novodur, Terluran, Tybrene) combine the properties of SAN with greatly improved resistance to impact. ABS is produced by emulsion, suspension, or bulk copolymerization of styrene–acrylonitrile in the presence of a rubber. The rubber is either poly(1,3-butadiene) or SBR. NBR (also referred to as nitrile rubber), a copolymer of 1,3-butadiene and acrylonitrile, is also used. The product of the reaction is a physical mixture of styrene–acrylonitrile copolymer and the graft copolymer of styrene–acrylonitrile onto the rubber. Additionally, SAN is often blended into that mixture. The final product, ABS, consists of a glassy polymer (SAN) dispersed in a rubbery matrix (grafted rubber). About 2 billion pounds per year of ABS are produced in the United States. Applications for ABS include housewares (refrigerator doors, sewing machine and hair-dryer housings, luggage, furniture frames, margarine tubs), housing and construction (pipe, conduit, fittings, bathtubs and shower stalls), transportation (automotive instrument panels, light housings, grilles), business machine housings (telephone, calculator), and recreation (golf clubs, boat hulls, camper top or shell, snowmobile shroud). Mixtures of styrene–methyl methacrylate copolymer and the graft copolymer onto a rubber provide higher heat resistance and improved adhesion to fiber glass compared to ABS.

High-impact polystyrene (HIPS) is produced by polymerizing styrene in the presence of a rubber, usually poly(1,3-butadiene). HIPS has improved impact resistance compared to polystyrene and competes with ABS products at low-cost end applications such as fast-food cups, lids, takeout containers, toys, kitchen appliances, and personal-care product containers. HIPS as well as ABS and SMA are used in physical blends with other polymers, such as polycarbonates, polyesters, and polyamides, to improve impact resistance (Sec. 2-13c-3).

6-8b Ethylene

A significant fraction, more than 25%, of the low-density polyethylene (LDPE) (Sec. 3-14a) produced by radical polymerization consists of various copolymers of ethylene. LDPE has come under increasing economic pressure in recent years because of a combination of factors [Doak, 1986]. High-density polyethylene (HDPE) has displaced LDPE in applications such as blow-molded bottles and thin films where the increased strength of HDPE is preferred over the clarity of LDPE. Linear low-density polyethylene (LLDPE) (Sec. 8-11c) competes effectively with LDPE in terms of both cost and properties. New producers of ethylene have entered the LDPE market because of a lack of alternatives for their feedstocks. Many LDPE producers use copolymerization as a strategy to obtain products more resistant to displacement by HDPE and LLDPE.

Ethylene–vinyl acetate (EVA) copolymers (trade names: Elvax, Escorene, Ultrathene) represent the largest-volume segment of the ethylene copolymer market, with an annual production of more than 1 billion pounds in the United States. As the vinyl acetate content increases, there are decreases in crystallinity, glass and crystalline melting temperatures, and chemical resistance coupled with increases in optical clarity, impact and stress crack resistance, flexibility, and adhesion to a variety of substrates. Copolymers containing 2–18% vinyl acetate are used in meat, poultry, and frozen-food packaging, stretch and shrink films, drum liners, extrusion coating on aluminum foil and polyester film, and heat-sealable coextruded pouches. Copolymers containing up to 20% vinyl acetate are used for molding or extruding squeeze toys, hose, tubing, gaskets, and insulation for electrical wire and cable. Copolymers containing 20–30% vinyl acetate are used as blends with paraffin wax and elastomers.
Hydrolysis of EVA copolymers yields ethylene–vinyl alcohol copolymers (EVOH). EVOH has exceptional gas barrier properties as well as oil and organic solvent resistance. The poor moisture resistance of EVOH is overcome by coating, coextrusion, and lamination with other substrates. Applications include containers for food (ketchup, jelly, mayonnaise) as well as chemicals and solvents.

Ethylene copolymers with methyl methacrylate and ethyl, butyl, and methyl acrylates are similar to EVA products but have improved thermal stability during extrusion and increased low-temperature flexibility. The commercial products generally contain 15–30% of the acrylate or methacrylate comonomer. Applications include medical packaging, disposable gloves, hose, tubing, gaskets, cable insulation, and squeeze toys.

Terpolymers in which the acrylate monomer is the major component are useful as ethylene–acrylate elastomers (trade name: Vamac) [Hagman and Crary, 1985]. A small amount of an alkenoic acid is present to introduce sites (C=C) for subsequent crosslinking via reaction with primary diamines (Sec. 9-2d). These elastomers have excellent oil resistance and stability over a wide temperature range (−50 to 200°C). They are superior to nitrile and chloroprene rubbers. Although not superior to silicone and fluorocarbon elastomers, they are less costly; uses include automotive (hydraulic system seals, hoses) and wire and cable insulation.

Copolymers of ethylene with up to 15–20% acrylic or methacrylic acid offer improved adhesion, abrasion resistance, toughness, and low-temperature flexibility compared to EVA. Applications include extrusion coatings on aluminum foil for pouches, wire and cable, packaging film, laminations with metal and glass fibers (building and automotive products) and polyurethane (carpet backing).

Neutralization of ethylene copolymers containing up to 5–10% acrylic or methacrylic acid comonomer with a metal salt such as the acetate or oxide or zinc, sodium, magnesium, barium, or aluminum yields products referred to as ionomers (trade name: Surlyn). Ionomers act like reversibly crosslinked thermoplastics as a result of microphase separation between ionic metal carboxylate and nonpolar hydrocarbon segments. The behavior is similar to the physical crosslinking in thermoplastic elastomers (Secs. 2-13c-2, 5-4a). Processing by extrusion and molding can be accomplished at higher temperatures where aggregation of the ionic segments from different polymer chains is destroyed (or made mobile). Subsequent to processing, the product becomes crosslinked on cooling to ambient temperature since aggregation of ionic segments is reestablished. Ionomers possess outstanding low-temperature flexibility, abrasion and impact resistance, good optical clarity, and adhesion to metals. Applications include the heat-sealable layer in packaging composites for food, skin packaging for hardware and electronics products, golf-ball and bowling-ball covers, automotive bumper pads, insulating covers for hot-water tanks, and wrestling mats.

Copolymerization is also important for high-density polyethylene (Sec. 8-11b).

**6-8c Unsaturated Polyesters**

The crosslinking of unsaturated polyesters (Sec. 2-12a) is carried out by copolymerization [Selley, 1988]. Low-molecular-weight unsaturated polyester (prepolymer) and radical initiator are dissolved in a monomer, the mixture poured, sprayed, or otherwise shaped into the form of the desired final product, and then transformed into a thermoset by heating. Styrene is the most commonly used monomer. Vinyltoluene, methyl methacrylate, diallyl phthalate, α-methylstyrene, and triallyl cyanurate are also used, often together with styrene.
The crosslinking process involves copolymerization of the added monomer with the double bonds of the unsaturated polyester

\[
\begin{align*}
&\text{\textcolor{red}{\tiny \sim O2C\sim CH=CH\sim CO2\sim } + \text{CH}_2\text{=CHA}} \\
\{ &\text{\textcolor{red}{\tiny \sim O2C\sim CH=CH\sim CO2\sim } \cdots \cdots \sim O2C\sim CH=CH\sim CO2\sim } \\
\{ &\text{\textcolor{red}{\tiny (CH}_2\text{=CHA)}_n} \} \} \} \\
\{ &\text{\textcolor{red}{\tiny \sim O2C\sim CH=CH\sim CO2\sim } \cdots \cdots \sim O2C\sim CH=CH\sim CO2\sim } \\
\{ &\text{\textcolor{red}{\tiny (CH}_2\text{=CHA)}_n} \} \} \\
\end{align*}
\]

(6-113)

The mechanical properties of the crosslinked product depend on the average number of crosslinks between polyester chains (crosslink density) and the average length of the crosslinks. The crosslink density depends on the relative amounts of saturated and unsaturated acids used in synthesizing the prepolymer. The average length of the crosslinks depends not only on the relative amounts of prepolymer and monomer but also on the copolymerization behavior of the two double bonds. Thus for a polyester containing fumarate double bonds crosslinking by copolymerization with styrene yields a harder and tougher product than when methyl methacrylate is used. The fumarate–styrene system shows more of an alternating copolymerization behavior than does the fumarate–methyl methacrylate system. Methyl methacrylate tends to form a small number of long crosslinks (large value of \(n\) in Eq. 6-113), while styrene forms a larger number of short crosslinks (small value of \(n\)). Allyl monomers such as diallyl phthalate are useful for producing high densities of short crosslinks due to degradative chain transfer.

6-8d Allyl Resins

Diallyl and triallyl monomers are used in various formulations, together with unsaturated polyesters (Sec. 6-8c) or monomers containing one double bond per molecule (Sec. 6-6a), to produce a range of thermoset products. Several diallyl monomers are also used alone to form thermosets referred to as allyl resins [Schildknecht, 1986]. Diallyl phthalate and isophthalate (the \(o\)– and \(p\)-isomers, respectively) (DAP, DAIP) are used in moldings and coatings for connectors and insulators in communication, computer, and aerospace systems where high reliability is needed under adverse environmental conditions. Other applications include impregnated glass cloth for radomes, missile and aircraft parts, and impregnated textiles and papers for decorative stain- and heat-resistant top layers for wall panels and furniture. Diallyl diglycol carbonate (also referred to as diethylene glycol bis[allyl carbonate]) (DADC) is used in applications requiring optical transparency, such as plastic lenses for eyewear, safety shields, camera filters, instrument panel covers, and nuclear-track detectors.

Polymers of \(N, N, N, N\)-diallyldimethylammonium chloride (DADMAC) (and its copolymers with acrylamide) are allyl resins in terms of the monomers used but are very different in properties since they are not crosslinked. Cyclopolymerization is the mode of reaction (Sec. 6-6b) and the polymers are water-soluble. Applications include potable and wastewater treatment (flocculation aid) and paper and textile industries (antistatic coating, reinforcement, color removal).

6-8e Other Copolymers

Many other copolymers of commercial importance have been discussed previously; see Secs. 3-14c (vinyl acetate, vinylidene chloride), 3-14d (acrylic and methacrylic acids and esters,
acrylonitrile, acrylamide), and 3-14e (fluoropolymers). Other copolymers include fluorocarbon elastomers such as vinylidene fluoride with hexafluoropropene or 1-hydroperfluoroalkene (with and without tetrafluoroethylene as a third monomer) and perfluoro(methyl vinyl ether) with vinylidene fluoride or tetrafluoroethylene (trade names: Fluorel, Tecnoflon, Viton) [Lynn and Worm, 1987]. The fluorocarbon elastomers show superior performance in hostile environments (high and low temperature, chemicals, oils, fuels). Applications include engine oil and drivetrain seals, fuel system hoses and O-rings, and a variety of similar parts in the petroleum and chemical industry as well as in other high-performance machinery. Copolymerization of tetrafluoroethylene with $X$ yields perfluorosulfonate ionomers (trade name: Nafton) after hydrolysis to the sulfonic acid [Moore and Martin, 1988]. These materials have interesting properties as fuel cell, battery, and electrochemical membranes as well as acid catalysts.

Nitrile rubber (NBR), a copolymer of 1,3-butadiene with 20–40% acrylonitrile, is noted for its oil resistance. More than 150 million pounds are produced annually in the United States. Applications include fuel tanks, gasoline hoses, and creamery equipment. Nitrile resin is made by copolymerizing acrylonitrile with about 20–30% styrene or methyl methacrylate in the presence of NBR or SBR rubber to yield a blend of the graft terpolymer and homopolymer. Applications include extruded and blow-molded containers for household, automotive, and other products as well as some nonbeverage foods (spices, vitamins, candy).

Copolymers of methyl methacrylate and tributyltin methacrylate are used in formulating antifouling and self-polishing coatings for underwater structures [Manders et al., 1987]. Terpolymers of alkyl acrylate, acrylonitrile, and 1–5% of a monomer with groups capable of subsequent crosslinking (e.g., 2-chloroethyl vinyl ether) (Sec. 9-2d) are useful as elastomers for applications requiring good resistance to heat and oils, such as transmission and rear-axle seals. These acrylate elastomers as well as the ethylene–acrylate elastomers (Sec. 6-8b) are higher-performance elastomers than are the nitrile rubbers in terms of resistance to a combination of heat and oil.

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PROBLEMS

6-1 Discuss the differences in the structures of random, alternating, graft, and block copolymers.

6-2 What is the difference between the ideal and alternating behaviors in copolymerization?

6-3 Consider the following monomer reactivity ratios for the copolymerization of various pairs of monomers:

<table>
<thead>
<tr>
<th>Case</th>
<th>( r_1 )</th>
<th>( r_2 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.1</td>
<td>0.2</td>
</tr>
<tr>
<td>2</td>
<td>0.1</td>
<td>10</td>
</tr>
<tr>
<td>3</td>
<td>0.1</td>
<td>3</td>
</tr>
<tr>
<td>4</td>
<td>0</td>
<td>0.3</td>
</tr>
<tr>
<td>5</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>6</td>
<td>0.8</td>
<td>2</td>
</tr>
<tr>
<td>7</td>
<td>1</td>
<td>15</td>
</tr>
</tbody>
</table>

What is the composition of the copolymer that would be formed at low conversion from equimolar mixtures of the two monomers in each case?

6-4 Using the \( r_1 \) and \( r_2 \) values from Table 6-2, construct plots showing the initial copolymer composition as a function of the comonomer feed composition for the radical copolymerizations of methyl acrylate–methyl methacrylate and styrene–maleic anhydride. Are these examples of ideal or alternating copolymerization?

6-5 Calculate the composition of the initial terpolymer that would be produced from the radical polymerization of a solution containing acrylonitrile, styrene, and 1,3-butadiene in mole fractions of 0.47, 0.47, and 0.06, respectively.

6-6 Ferrocenylmethyl acrylate (FMA) and 2-ferrocenylethyl acrylate (FEA) have been synthesized and copolymerized with styrene, methyl acrylate, and vinyl acetate [C. U. Pittman, Jr., Macromolecules, 4, 298 (1971)]. The following monomer reactivity ratios were found:
a. Predict whether FEA or FMA will have the higher $k_p$ in homopolymerization. Explain the basis of your prediction. How can the difference in $k_p$ values be explained in relation to the structures of FEA and FMA?

b. Which of the comonomer pairs above could lead to azeotropic copolymerization?

c. Is styrene monomer a more or less reactive monomer than FMA monomer toward the FMA propagating center? By what factor?

d. List styrene, methyl acrylate, and vinyl acetate in order of increasing reactivity toward the FMA propagating center. Is the trend in reactivity toward the FMA propagating center the same?

e. List the styrene, methyl acrylate, and vinyl acetate propagating centers in order of increasing reactivity toward FEA monomer.

f. Are the copolymerization data above indicative of radical, cationic, or anionic copolymerization? Explain.

6-7 Consider the radical copolymerization of a benzene solution that is 1.5 $M$ in styrene and 3.0 $M$ in methyl acrylate.

a. What is the initial copolymer composition if the polymerization is carried out at 60°C using benzoyl peroxide at a concentration of $5.0 \times 10^4 M$? How is the copolymer composition affected if $3.0 \times 10^3 M$ benzoyl peroxide is used?

b. How will the presence of $5.0 \times 10^5 M$ $n$-butyl mercaptan affect the initial copolymer composition?

c. What would you expect (qualitatively) for the copolymer composition if the reaction were initiated by $n$-butyllithium? by BF$_3$ plus water?

6-8 List the following monomers in order of their increasing tendency toward alternation with 1,3-butadiene in radical copolymerization:

a. $n$-Butyl vinyl ether

b. Methyl methacrylate

c. Methyl acrylate

d. Styrene

e. Maleic anhydride

f. Vinyl acetate

g. Acrylonitrile

Explain the relative alternating tendencies in these copolymerizations.
6-9 If the copolymerizations in Problem 6-8 were carried out using cationic initiation, what would be expected qualitatively for the copolymer compositions? List the copolymers in order of their increasing 1,3-butadiene content. Would copolymers be formed from each of the comonomer pairs? Explain. What would be observed if one used anionic initiation?

6-10 Using the \( Q \) and \( e \) values in Table 6-7, calculate the monomer reactivity ratios for the comonomer pairs styrene–1,3-butadiene and styrene–methyl methacrylate. Compare the results with the \( r_1 \) and \( r_2 \) values in Table 6.2.

6-11 Discuss the general effects of temperature, solvent, and catalyst on the monomer reactivity ratios in ionic copolymerizations. How do these compare with the corresponding effects in radical copolymerizations?

6-12 What are the differences between the two treatments (kinetic penultimate effect and depropagation) used to account for the deviations observed in the copolymer composition equation?

6-13 Discuss qualitatively the course of the radical copolymerization of each of the following comonomer pairs in terms of the degree of reaction at which gelation would be expected to occur:
   a. Styrene–divinylbenzene
   b. Methyl methacrylate–allyl methacrylate
   c. Vinyl acetate–ethylene glycol dimethacrylate
   d. Methyl methacrylate–divinyl adipate
   e. Styrene–1,3-butadiene

6-14 The product obtained in the polymerization of 4-methyl-1,6-heptadiene contains no residual unsaturation. What is its chemical structure?

6-15 Calculate the monomer reactivity ratios for chloroprene–2-vinylpyridine using the data from Table 6–8 for the “patterns of reactivity” scheme.
RING-OPENING POLYMERIZATION

In addition to step and chain polymerizations, another mode of polymerization is of importance. This is the ring-opening polymerization (ROP) of cyclic monomers such as cyclic ethers, acetals, amides (lactams), esters (lactones), and siloxanes. Ring-opening polymerization is of commercial interest in a number of systems, including the polymerizations of ethylene oxide

\[ \triangle O \rightarrow \{ \text{OCH}_2\text{CH}_2 \}_n \]  \hspace{1cm} (7-1)

trioxane

\[ \text{O} \begin{array}{c} \text{O} \\ \text{O} \end{array} \rightarrow \{ \text{OCH}_2 \}_n \]  \hspace{1cm} (7-2)

e-caprolactam

\[ \text{O} \text{N} \begin{array}{c} \text{H} \\ \text{C} \\ \text{O} \end{array} \rightarrow \{ \text{NHCOCH}_2\text{CH}_2\text{CH}_2\text{CH}_2 \}_n \]  \hspace{1cm} (7-3)
and octamethylcyclotetrasiloxane:

\[
\begin{align*}
\text{CH}_3 & \text{Si} \quad \text{CH}_3 \\
\text{CH}_3 & \text{Si} \quad \text{O} \quad \text{Si} \quad \text{CH}_3 \\
\text{CH}_3 & \text{Si} \quad \text{O} \quad \text{Si} \quad \text{CH}_3 \\
\text{CH}_3 & \text{Si} \quad \text{O} \quad \text{Si} \quad \text{CH}_3
\end{align*}
\]

\[\text{O-Si} \quad \text{CH}_3\]

(7-4)

### 7-1 GENERAL CHARACTERISTICS

#### 7-1a Scope; Polymerizability

A wide variety of cyclic monomers have been successfully polymerized by the ring-opening process [Frisch and Reegan, 1969; Ivin and Saegusa, 1984; Saegusa and Goethals, 1977]. This includes cyclic amines, sulfides, olefins, cyclotriphosphazenes, and \(N\)-carboxy-\(\alpha\)-amino acid anhydrides, in addition to those classes of monomers mentioned above. The ease of polymerization of a cyclic monomer depends on both thermodynamic and kinetic factors as previously discussed in Sec. 2-5.

The single most important factor that determines whether a cyclic monomer can be converted to linear polymer is the thermodynamic factor, that is, the relative stabilities of the cyclic monomer and linear polymer structure [Allcock, 1970; Sawada, 1976]. Table 7-1 shows the semiempirical enthalpy, entropy, and free-energy changes for the conversion of cycloalkanes to the corresponding linear polymer (polymethylene in all cases) [Dainton and Ivin, 1958; Finke et al. 1956]. The \(lc\) (denoting liquid-crystalline) subscripts of \(\Delta H\), \(\Delta S\), and \(\Delta G\) indicate that the values are those for the polymerization of liquid monomer to crystalline polymer.

Polymerization is favored thermodynamically for all except the 6-membered ring. Ring-opening polymerization of 6-membered rings is generally not observed. The order of thermodynamic feasibility is \(3,4 > 8 > 5,7\) which follows from the previous discussion (Sec. 2-5c) on bond angle strain in 3- and 4-membered rings, eclipsed conformational strain in the 5-membered ring, and transannular strain in 7- and 8-membered rings. One notes that

<table>
<thead>
<tr>
<th>(\text{(CH}_2\text{)}_n)</th>
<th>(\Delta H_{lc}) (kJ mol(^{-1}))</th>
<th>(\Delta S_{lc}) (J mol(^{-1}) K(^{-1}))</th>
<th>(\Delta G_{lc}) (kJ mol(^{-1}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>(-113.0)</td>
<td>(-69.1)</td>
<td>(-92.5)</td>
</tr>
<tr>
<td>4</td>
<td>(-105.1)</td>
<td>(-55.3)</td>
<td>(-90.0)</td>
</tr>
<tr>
<td>5</td>
<td>(-21.2)</td>
<td>(-42.7)</td>
<td>(-9.2)</td>
</tr>
<tr>
<td>6</td>
<td>(+2.9)</td>
<td>(-10.5)</td>
<td>(+5.9)</td>
</tr>
<tr>
<td>7</td>
<td>(-21.8)</td>
<td>(-15.9^a)</td>
<td>(-16.3)</td>
</tr>
<tr>
<td>8</td>
<td>(-34.8)</td>
<td>(-3.3^a)</td>
<td>(-34.3)</td>
</tr>
</tbody>
</table>

\(^a\)Data from Cubbon [1964]; all other data are from Dainton and Ivin [1958] and Finke et al. [1956].
$\Delta H_{lc}$ is the major factor in determining $\Delta G_{lc}$ for the 3- and 4-membered rings, while $\Delta S_{lc}$ is very important for the 5- and 6-membered rings. The enthalpy and entropy factors $\Delta H_{lc}$ and $\Delta S_{lc}$ contribute about equally for larger-sized rings. Since both $\Delta H_{lc}$ and $\Delta S_{lc}$ are negative, $\Delta G_{lc}$ becomes less negative with increasing temperature. Above some temperature (the ceiling temperature) $\Delta G_{lc}$ becomes positive, and polymerization is no longer favorable. For all-sized rings the presence of substituents decreases thermodynamic feasibility for polymerization. Interactions between substituents are more severe in the linear polymer than in the cyclic monomer [Cubbon, 1964; Sawada, 1976]; $\Delta H_{lc}$ is less negative, while $\Delta S_{lc}$ is more negative. Exceptions to this generalization occur when the substituents are linked to each other to form a second ring in such a manner that there is increased strain in the ring containing the polymerizable functional group. Structures I and II, cis- and trans-8-oxabicyclo[4.3.0]-nonane, illustrate this point. The 5-membered ring in the cis isomer (I), is almost completely free of strain and does not polymerize. However, the trans isomer undergoes polymerization since the tetrahydrofuran ring is twisted and highly strained [Kops and Spangaard, 1975].

![Structures I and II](image)

Although ring-opening polymerization is thermodynamically favored for all except the 6-membered cycloalkane, polymerization of cycloalkanes has been achieved in very few cases, almost exclusively with cyclopropane derivatives, and only oligomers are obtained [Pinazzi et al., 1971; Sogo et al., 1978]. This points out that thermodynamic feasibility does not guarantee the actual polymerization of a cyclic monomer. Polymerization requires that there be a kinetic pathway for the ring to open and undergo reaction. The cycloalkanes do not have a bond in the ring structure that is easily prone to attack by an initiator species. The lactams, lactones, cyclic ethers and acetals, and other cyclic monomers stand in marked contrast to the cycloalkanes. The presence of a heteroatom in the ring provides a site for nucleophilic or electrophilic attack by an initiator species, resulting in initiation and subsequent propagation by ring opening. Such monomers polymerize, since both thermodynamic and kinetic factors are favorable. Overall, one observes that polymerizability (a combination of thermodynamic and kinetic feasibility) is higher for rings of 3,4, and 7–11 members, lower for rings of 5 members, and much lower for rings of 6 members. Some variations from this generalization are observed for certain families of cyclic monomers. For example, some 6-membered rings with two or more heteroatoms in the ring undergo polymerization (Sec. 7-2b-4). The 6-membered lactam undergoes polymerization (Sec. 7-3d). From a practical viewpoint ROP is usually limited to monomers of less than 9 members because of the general unavailability of larger-sized cyclic monomers. Also, 3-membered rings are not available for a number of classes of compounds (lactams, lactones, cycloalkenes, cyclosiloxanes, and acetals).

7-1b Polymerization Mechanism and Kinetics

Ring-opening polymerizations are generally initiated by the same types of ionic initiators previously described for the cationic and anionic polymerizations of monomers with carbon–carbon and carbon–oxygen double bonds (Chap. 5). Most cationic ring-opening polymerizations involve the formation and propagation of oxonium ion centers. Reaction
involves the nucleophilic attack of monomer on the oxonium ion:

\[
\begin{array}{c}
\text{Z} + \text{Z+} \\
\rightarrow \text{Z–} \\
\end{array}
\]  

(7-5a)

The typical anionic ring-opening polymerization involves the formation and propagation of anionic centers. Reaction proceeds by nucleophilic attack of the propagating anion on monomer:

\[
\begin{array}{c}
\text{Z}+ \\
\rightarrow \text{Z–} \\
\end{array}
\]  

(7-6)

In Eq. 7-5a Z represents a functional group, such as O, NH, Si–O, CO–O, and CO–NH in ethers, amines, siloxanes, esters, and amides, respectively. In Eq. 7-6 Z– represents an anionic propagating center, such as alkoxide or carboxylate, derived from the cyclic monomer.

Ionic ROP shows most of the characteristics described in Chap. 5. There is minimal discussion in this chapter of those characteristics that are similar to those for carbon–carbon and carbon–oxygen double-bond polymerizations. Ionic ROP shows analogous effects of solvent and counterion, propagation by different species (covalent, ion pair, free ion), and association phenomena.

Some ring-opening polymerizations proceed by a different route called activated monomer (AM) polymerization, which typically involves a cationic or anionic species derived from the monomer. For example, cationic AM polymerization proceeds not with monomer, but with protonated monomer that reacts with the neutral functional end group of the propagating polymer

\[
\begin{array}{c}
\text{ZH} + \text{HZ} \\
\rightarrow \text{ZH} \\
\end{array}
\]  

(7-5b)

Ring-opening polymerization (ROP) is a chain polymerization, consisting of a sequence of initiation, propagation, and termination. Only monomer adds to the growing chains in propagation. Unlike step polymerization, monomer does not react with monomer and larger-sized species do not generally react with each other in ROP. Many ring-opening polymerizations proceed as living polymerizations—polymer molecular weight increases linearly with conversion and the ratio of monomer to initiator, and block copolymers can be synthesized.

Ring-opening polymerizations usually differ from chain polymerizations of carbon–carbon double-bond monomers in an important aspect. The propagation rate constants for ring-opening polymerizations are generally similar to the rate constants in most step polymerizations, which makes them several orders of magnitude lower than those in typical polymerizations of carbon–carbon double-bond monomers. Thus, the buildup of polymer molecular weight is slower for ROP compared to chain polymerizations of carbon–carbon double-bond monomers. Unlike ROP, high molecular weights are achieved at all conversions, including very low conversions, in chain polymerizations of carbon–carbon double-bond monomers.

Polymerization–depolymerization equilibria are more often encountered in ROP than in the chain polymerizations, both radical and ionic, of carbon–carbon double-bond monomers.

ROP offers an alternate to step polymerization for the synthesis of many polymers. Thus, polyesters are produced by ROP of lactones as well as step polymerization of diacids with...
diols. Since the two routes differ considerably in their reaction characteristics, one can visualize situations where ROP is the preferred route, such as when it is desirable to take advantage of the different dependence of polymer molecular weight (MW) on reaction parameters. MW is dependent on stoichiometric balance and conversion in step polymerization. In ROP, MW generally depends on conversion and the monomer : initiator ratio. However, the cyclic monomers required for ROP are not nearly as available as the bifunctional reactants for step polymerization.

7-2 CYCLIC ETHERS

Cyclic ethers can be named simply as oxacycloalkanes, such as oxacyclop propane, oxacyclobutane, oxacyclopentane, and oxacyclohexane, where the prefix ox means the replacement of CH₂ by O in corresponding cycloalkanes. Most cyclic ethers, however, are known by other names. The 3-, 4-, 5-, and 6-membered rings are oxirane, oxetane, oxolane, and oxane, respectively, or ethylene oxide (or epoxide), trimethylene oxide, tetrahydrofuran, and tetrahydropyran.

The carbon–oxygen bond in ethers is a strong bond, and the ether oxygen is basic in the Lewis sense. The result is that ring-opening polymerization of cyclic ethers is generally initiated only by cationic species except for epoxides. Epoxides are polymerized by both anionic and cationic initiators because of the high degree of strain in the 3-membered ring.

The polymerization of simple cyclic ethers (i.e., those with a single ether linkage) has been generally limited to those of 3, 4 and 5 members, although some work has been done with the 7-membered (oxepane) ring. The study of larger-sized rings has been carried out mostly with cyclic acetals (Sec. 7-2b-4). The reactivity of different-sized cyclic ethers follows the generally expected order. Cyclic ethers of less than 5 members or more than 6 members are relatively easily polymerized. The 5-membered cyclic ethers polymerize with more difficulty. Substituted 5-membered cyclic ethers are usually unreactive, although some cyclic acetals undergo polymerization. The 6-membered cyclic ethers such as tetrahydrofuran (III) and 1,4-dioxane (IV) are unreactive under a wide range of reaction conditions, but the 6-membered cyclic acetal, trioxane (V), undergoes polymerization.

7-2a Anionic Polymerization of Epoxides

7-2a-1 Reaction Characteristics

The anionic polymerization of epoxides such as ethylene and propylene oxides can be initiated by metal hydroxides, alkoxides, oxides, and amides as well as metal alkys and aryls, including radical–anion species such as sodium naphthalene [Boileau, 1989; Dreyfuss and Dreyfuss, 1976; Inoue and Aida, 1984; Ishii and Sakai, 1969]. Thus the polymerization of ethylene oxide by MrA− involves initiation

\[ \text{H}_2\text{C} \rightarrow \text{CH}_2 + \text{MrA}^+ \rightarrow \text{A} \rightarrow \text{CH}_2\text{CH}_2\text{O}^-\text{Mr}^+ \] (7-7)
followed by propagation

$$A\text{CH}_2\text{CH}_2\text{O}^-\text{M}^+ + \text{H}_2\text{C}^-\text{CH}_2 \rightarrow A\text{CH}_2\text{CH}_2\text{OCH}_2\text{CH}_2\text{O}^-\text{M}^+ \quad (7-8a)$$

which may be generalized as

$$A\left(\text{CH}_2\text{CH}_2\text{O}\right)^{\pi}\text{CH}_2\text{CH}_2\text{O}^-\text{M}^+ + \text{H}_2\text{C}^-\text{CH}_2 \rightarrow A\left(\text{CH}_2\text{CH}_2\text{O}\right)^{(\pi + 1)}\text{CH}_2\text{CH}_2\text{O}^-\text{M}^+ \quad (7-8b)$$

Some initiators polymerize epoxides through an anionic coordination mechanism. These initiators include a ferric chloride–propylene oxide adduct ClFe[OCH(CH_3)CH_2Cl]_2 (referred to as the Pruitt-Baggett initiator), adducts such as Zn(OCH_3)_2 and ([Zn(OCH_3)_2]_2\cdot [C_2H_4ZnOCH_3])_6 derived by reaction of dialkylzinc with alcohol, bimetallic μ-oxoalkoxides such as [(RO)_2AlO]_2Zn, and metalloporphyrin derivatives of aluminum and zinc (e.g., VI with Z = Cl, OR, R, OOCR, SR) [Aida and Inoue, 1996; Hagiwara et al., 1981; Hasebe and Tsurata, 1988; Inoue, 1988, 2000; Kasperczyk and Jedlinski, 1986; Kuroki et al., 1988a, b; Nuytens et al., 2000; Slomkowski and Duda, 1993; Sugimoto and Inoue, 1999].

![VI](image)

Propagation with the anionic coordination initiators, especially the aluminum and zinc initiators such as aluminum isopropoxide or the metalloprophyrins such as VI, involves covalent propagation in which the epoxide monomer is inserted into a metal–oxygen bond [Penczek and Duda, 1993; Penczek et al., 1995; Szwarc and Van Beylen, 1993] (Eq. 7-9). The propagation is categorized as an anionic coordination process since one can visualize the formation of an incipient alkoxide anion on cleavage of the metal–oxygen bond at the propagating center. (Polymerization with some initiators such as AlR_3/H_2O and AlR_3/ROH probably proceed as cationic, not anionic, processes [Antelmann et al., 2001; Bansleban et al., 1984].)

Although generally presented as a covalent propagation, it is difficult to preclude the possibility that propagation occurs mostly or even exclusively through a small concentration of
ionic species (ions and/or ion pairs) in equilibrium with the covalent species. The strongest
evidence in support of covalent propagation is the decrease in polymerization rate with
increasing solvent polarity [Szwarc and Van Beylen, 1993]. If ionic propagation occurred,
increased solvent polarity should enhance the polymerization rate by facilitating the ioniza-
tion of covalent species to ions and ion pair. This is what occurs with ionic initiators such as
the alkali metal initiators (e.g., RLi, NaOH), but not with the aluminum and zinc covalent
initiators.

The metalloporphyrin-initiated polymerizations are accelerated by the presence of steri-
cally hindered Lewis acids [Inoue, 2000; Sugimoto and Inoue, 1999]. The Lewis acid coor-
dinates with the oxygen of monomer to weaken the C−O bond and facilitate nucleophilic
attack. The Lewis acid must be sterically hindered to prevent its reaction with the propagat-
ing center attached to the porphyrin structure. Thus, aluminium ortho-substituted phenolates
such as methylaluminum bis(2,6-di-tert-butyl-4-methylphenolate) accelerate the polymeriza-
tion by factors of 10^2–10^3 or higher. Less sterically hindered Lewis acids, including the aluminium
phenolates without ortho substituents, are much less effective.

The polymerization of an unsymmetric epoxide such as propylene oxide involves the pos-
sibility of two different sites (at carbons 1 and 2 or \(\alpha\) and \(\beta\)) on the epoxide ring for the
nucleophilic ring-opening reaction. Two different propagating species are then possible:

\[
\begin{align*}
\text{CH}_3\text{CH}−\text{CH}_2\text{O} & \quad \text{CH}_3\text{CH}−\text{CH}_2\text{O}^+ \quad (7-10) \\
& \quad \sim \text{CH}−\text{CH}_2−\text{O}^+\text{K}^+ \\
\text{CH}_3\text{CH}−\text{CH}_2\text{O} & \quad \text{CH}_3\text{CH}−\text{CH}_2\text{O}^+ \quad (7-11)
\end{align*}
\]

The polymer has a predominantly head-to-tail structure with propagation occurring almost
exclusively by attack at the \(\beta\)-carbon—the less sterically hindered site (Eq. 7-11), that is, an
\(S_N2\) attack [Kasperczyk and Jedlinski, 1986; Oguni et al., 1973; Price and Osgan, 1956;
Quirk, 2002]. Propylene oxide and other substituted epoxides polymerize more slowly
than does ethylene oxide because of steric hindrance.

Most anionic polymerizations of epoxides proceed as living polymerizations with the
ability to polymerize successive monomer charges and form block copolymers. The expres-
sions for the rate and degree of polymerization are essentially those used to describe living
chain polymerizations of alkene monomers. For example, in the sodium methoxide initiated
polymerization of ethylene oxide [Gee et al., 1959], the polymerization rate is given by
Eq. 5-49, where \([M^*]\) is the total concentration of free ion and ion pairs. (If covalent species
are present and undergoing propagation, \([M^*]\) must be replaced by the appropriate concen-
tration term, including all types of propagating species—ionic and covalent.)

\[
R_p = k_{\text{app}}^* [M^*][\text{M}] 
\]

The effects of reaction media on \(R_p\) are similar to those described in Chap. 5. Changes in
solvent and counterion affect reaction rates and the observed rate expressions by altering the
relative amounts of free ion and ion-pair propagating species, and the extent of association of
initiator and propagating species. Using the approach described in Sec. 5-3d-2-a, one can
obtain the individual rate constants for propagation of free ions and ion pairs, although exten-
sive studies have not been carried out [Sigwalt and Boileau, 1978]. Reported values of \(k_p^-\) are
in the range of 10^−2–10 L mol\(^{-1}\) s\(^{-1}\), where \(k_p^±\) values are usually lower by 1–2 orders of
magnitude [Boileau, 1989].
The degree of polymerization follows the expression

\[ \bar{X}_n = \frac{p[M]_0}{[I]_0} \]  

(7-12)

which is the same as the expressions for living radical and ionic polymerizations of C=C monomers (Eqs. 3-227, 5-58, 5-99). The \([I]_0\) term in Eq. 7-12 must take into account the number of propagating chains per initiator molecule. For an aluminum porphyrin initiator, \([I]_0\) is the concentration of the aluminum porphyrin since there is one propagating chain per aluminum atom. However, for aluminum isopropoxide, \([I]_0\) is 3 times the concentration of aluminum isopropoxide since each aluminum atom carries three propagating chains, that is, each isopropoxide group is an initiator.

7-2a-2 Exchange Reactions

Epoxide polymerizations taking place in the presence of protonic substances such as water or alcohol involve the presence of exchange reactions. Examples of such polymerizations are those initiated by metal alkoxides and hydroxides that require the presence of water or alcohol to produce a homogeneous system by solubilizing the initiator. Such substances increase the polymerization rate not only by solubilizing the initiator but probably also by increasing the concentration of free ions and loose ion pairs. In the presence of alcohol the exchange

\[ \text{R OCH}_2\text{CH}_2\text{OH} + \text{ROH} \rightleftharpoons \text{R OCH}_2\text{CH}_2\text{O}^-\text{Na}^+ + \text{RO}^-\text{Na}^+ \]  

(7-13)

reaction (Eq. 7-13) between a propagating chain and the alcohol is possible. Similar exchange reactions are possible between the newly formed polymeric alcohol in Eq. 7-13 and other propagating chains:

\[ \text{R OCH}_2\text{CH}_2\text{OH} \rightleftharpoons \text{R OCH}_2\text{CH}_2\text{O}^-\text{Na}^+ \]

\[ \text{R OCH}_2\text{CH}_2\text{O}^-\text{Na}^+ \rightleftharpoons \text{R OCH}_2\text{CH}_2\text{OH} \]  

(7-14)

These exchange reactions lower the polymer molecular weight. The number-average degree of polymerization is given by

\[ \bar{X}_n = \frac{p[M]_0}{[I]_0 + [\text{ROH}]_0} \]  

(7-15)

since each alcohol molecule contributes equally with an initiator species to determining the number of propagating chains. The exchange reactions appear equivalent to chain-transfer reactions, but they are not. Any polymeric alcohol formed via exchange is not dead but simply dormant. All alcohol and alkoxide molecules in the reaction system are in dynamic equilibrium. Each polymer chain alternates between the active propagating alkoxide and dormant alcohol forms.

The exchange reaction places an upper limit on the polymer molecular weight that is possible for polymerizations performed in the presence of alcohols or other protonic substances. There are very few reports of polymers with molecular weights above 10,000 for ethylene...
oxide polymerizations initiated by alkoxides or hydroxides in alcohol, although molecular weights as high as 50,000 appear (very rarely) in the literature [Boileau, 1989; Clinton and Matlock, 1986]. (Another reason for the upper limit on molecular weight is dehydration from the hydroxy end groups of the dormant polymeric alcohol [Clinton, and Matlock, 1986]. This would adversely affect the living nature of the polymerization by converting dormant alcohol species to dead polymer.) Polymerizations initiated by alkoxides and hydroxides in aprotic polar solvents do not have this limitation. This limitation also does not apply to polymerizations initiated by the other initiators, including metal alkyls and aryls and the various coordination initiators (e.g., aluminum alkoxides and metalloporphyrins), since those initiators are soluble in solvents such as benzene or tetrahydrofuran. Homogeneous reactions can be obtained without the need for a solvent such as alcohol. Molecular weights as high as $10^5$–$10^6$ have been achieved in a number of systems. However, the addition of alcohol or other protonic substance is useful for control of polymer molecular weight. Equation 7-15 allows one to calculate the amount of added alcohol or other substance required to achieve some desired value of the number-average molecular weight.

A number of different situations are possible depending on the relative rates of initiation, propagation, and exchange. When exchange is absent and initiation is much faster than propagation, initiation is essentially complete before propagation begins. All polymer chains start growing at the same time and grow for the same period with the result that the molecular weight distribution is very narrow as in living chain polymerizations; that is, the distribution is Poisson as defined by Eq. 3-228. When initiation is slow, some chains are growing while others have not yet been initiated. The polymerization proceeds with an initial period in which the reaction rate shows an acceleration as initiator is converted to propagating species; thereafter, the rate is constant. The molecular weight distribution broadens since chains grow for different periods of time. This effect is observed in most anionic coordination polymerizations because the initiators are generally aggregated and possess different initiator sites with different reactivities. An exception to this generalization are the metalloporphyrin initiators, which yield living polymers with narrow molecular weights.

The effects of exchange depends on the relative acidities of the alcohol (or other protonic substance) and the polymeric alcohol. The exchange reaction occurs throughout the course of the polymerization if the acidities of the two alcohols are approximately the same. The polymerization rate is unaffected while the molecular weight decreases (Eq. 7-15), but the molecular weight distribution (MWD) is Poisson.

If the added alcohol ROH is much more acidic than the polymeric alcohol, most of it will undergo reaction with the first-formed propagating species before polymerization begins.

\[
\text{ROCH}_2\text{CH}_2\text{O}^-\text{Na}^+ + \text{ROH} \rightarrow \text{ROCH}_2\text{CH}_2\text{OH} + \text{RO}^-\text{Na}^+ \tag{7-16}
\]

Reinitiation by RO$^-$Na$^+$ would usually be slower, since ROH is relatively acidic. This results in a decreased polymerization rate and a broadening of the polymer molecular weight. The rate of polymerization will be relatively unaffected during most of the polymerization for the case in which ROH is less acidic than the polymeric alcohol. Exchange will occur in the later stages of reaction with a broadening of the MWD.

The use of protonic compounds such as HCl or RCOOH in place of ROH or H$_2$O yields a different result in most systems. When such substances take part in the exchange reaction, the result is not exchange as described above but inhibition or retardation since an anion, such as Cl$^-$ or RCOO$, possesses little or no nucleophilicity. Reinitiation does not occur or is very slow. The polymeric alcohols are no longer dormant but are dead. Both the polymerization rate and polymer molecular weight decrease along with a broadening of the polymer.
molecular weight. Hydrogen chloride and RCOOH act as the equivalent of inhibitors or retarders and the polymerization rate can be treated by the expressions developed in Sec. 3-7a. the number-average degree of polymerization is analyzed by the expression used to handle chain transfer (Eq. 3-119). Polymerizations initiated by the metalloporphyrins do not follow this pattern. Reinitiation occurs even when HCl or RCOOH is present, that is, VI with Z = Cl or RCOO is an effective initiator. Polymerizations initiated by metalloprophyrins are difficult to terminate and have been termed immortal polymerizations [Aida et al., 1988; Inoue, 2000].

Although anionic polymerization of cyclic ethers is generally limited to oxiranes, there are reports of successful oxetane and tetrahydrofuran polymerizations in the presence of a Lewis acid. Aluminum porphyrin alone does not polymerize oxetane, but polymerization proceeds in the presence of a Lewis acid [Sugimoto and Inoue, 1999]. Similarly, THF is polymerized by sodium triphenylmethyl in the presence of a Lewis acid such as aluminum alkoxide [Kubisa and Penczek, 1999]. The Lewis acid complexes at the ether oxygen, which weakens (polarizes) the carbon–oxygen bond and enhances nucleophilic attack.

7-2a-3 Chain Transfer to Monomer

Excluding polymerizations with anionic coordination initiators, the polymer molecular weights are low for anionic polymerizations of propylene oxide (<6000) [Clinton and Matlock, 1986; Boileau, 1989; Gagnon, 1986; Ishii and Sakai, 1969; Sepulchre et al., 1979]. Polymerization is severely limited by chain transfer to monomer. This involves proton abstraction from the methyl group attached to the epoxide ring followed by rapid ring cleavage to form the allyl alkoxide anion VII, which isomerizes partially to the enolate anion VIII. Species VII and VIII reinitiate polymerization of propylene oxide as evidenced by the presence of infrared absorptions for allyl ether and 1-propenyl ether groups in the polymer. The monomer chain-transfer constant has values of 0.013 and 0.027 at 70 and 93°C, respectively, in the sodium methoxide polymerization of propylene oxide [Gee et al., 1961]. These values are larger by factors of $10^2$–$10^3$ than the usual monomer transfer
constants (Tables 3-5 and 5-4). The extent of this transfer reaction increases with increasing number of methyl groups on the epoxide ring.

Chain transfer to monomer is much less prevalent for polymerizations with most of the anionic coordination initiators and higher polymer molecular weights have been obtained [Bots et al., 1987].

7-2b Cationic Polymerization

7-2b-1 Propagation

Propagation in the cationic polymerization of cyclic ethers is generally considered as proceeding via a tertiary oxonium ion, for example, for the polymerization of 3,3-bis(chloromethyl)oxetane (R = CH₂Cl)

\[
\text{OCH}_2\text{CR}_2\text{CH}_2 + \overset{+}{\text{R}} \rightarrow \text{OCH}_2\text{CR}_2\text{CH}_2 + \overset{+}{\text{R}}
\]

(7-20)

where A⁻ is the counterion [Frisch and Reegan, 1969; Inoue and Aida, 1984; Kubisa, 1996; Penczek, 2000; Penczek and Kubisa, 1989a,b].

The α-carbon of the oxonium ion is electron-deficient because of the adjacent positively charged oxygen. Propagation is a nucleophilic attack of the oxygen of a monomer molecule on the α-carbon of the oxonium. The nucleophilic reaction is an S_N2 reaction for most cyclic ethers [Saegusa et al., 1976]. However, S_N1 ring opening has been suggested for a monomer with two alkyl substituents at the α-position (e.g., 2,2-dimethyloxetane [Dreyfuss and Dreyfuss, 1987; Kops and Spangaard, 1982].

Most cationic ring-opening polymerizations are highly regioselective with the formation of head-to-tail structures, although varying amounts of head-to-head and tail-to-tail structures are found in some systems [Dreyfuss and Dreyfuss, 1987].

The species present in cationic ring-opening polymerizations are covalent ester (IX), ion pair (X), and free ion (XI) in equilibrium. The relative amounts of the different species depend on the monomer, solvent, temperature, and other reaction conditions, similar to the situation described for ionic polymerization of C=C monomers (Chap. 5).

\[
\text{OCH}_2\text{CH}_2\text{CH}_2\text{CH}_2\text{A} \rightleftharpoons \overset{+}{\text{A}} \rightleftharpoons \overset{+}{\text{A}}
\]

(7-21)

There is usually little or no difference in reactivity between free ions and ion pairs, similar to the situation in the polymerization of carbon–carbon double bond monomers [Penczek, 2000]. Covalent species are present in many systems as detected by NMR and other methods, but whether they are reactive or dormant is not always clear. When propagation by covalent species occurs, it is not covalent-to-covalent propagation in which monomer is inserted into a covalent bond to produce a new covalent propagating species containing an additional monomer unit [Penczek et al., 1995]. Covalent propagation is a two-step process. Monomer adds to the covalent species to form an ionic species (Eq. 7-22a), which collapses to (is in
equilibrium with) the covalent species (Eq. 7-22b). Covalent propagation has been confirmed in the polymerization of THF by triflic esters. Whereas methyl triflate is covalent, a mixture

\[
\begin{align*}
\text{O} & \quad \text{OCH}_2\text{CH}_2\text{CH}_2\text{CH}_2\text{A} \\
\leftrightarrow & \quad \text{O(CH}_2\text{)}_4\text{OCH}_2\text{CH}_2\text{CH}_2\text{CH}_2^+\text{A}^- \\
\text{O(CH}_2\text{)}_4\text{OCH}_2\text{CH}_2\text{CH}_2\text{CH}_2\text{A} & \quad (7-22a)
\end{align*}
\]

of oxonium ion and macroester is obtained when methyl triflate is mixed with THF. Covalent propagation is slower than ionic propagation, typically by a factor of \(10^2\)–\(10^3\) or more. The covalent species predominate over ionic species in most systems. In the THF/methyl triflate system, covalent species account for about 95% of species in CCl₄ solution. Ionic species predominate, about 95%, in the very polar solvent CH₃NO₂, but this solvent is not one that would generally be employed in industrial applications. When covalent species are the major species present, they act effectively as dormant species because of their lower reactivity compared to ionic species. This slows down propagation and allows sufficient time for initiation to be complete. The result is living polymerization by reversible deactivation of ionic propagating species, similar to the situation in living radical and ionic polymerizations of C=C monomers.

7-2b-2 Initiation

A variety of initiator systems, of the types used in the cationic polymerization of alkenes (Sec. 5-2a); can be used to generate the tertiary oxonium ion–propagating species [Dreyfuss and Dreyfuss, 1969, 1976; Inoue and Aida, 1984; Penczek and Kubisa, 1989a,b].

Strong protonic acids such as trifluoroacetic, fluorosulfonic, and trifluoromethanesulfonic (triflic) acids initiate polymerization via the initial formation of a secondary oxonium ion

\[
\begin{align*}
\text{H}^+\text{A}^- & \quad + \quad \text{O \quad R \quad R} \\
\text{HO} & \quad \text{A \quad R \quad R} \\
\text{HOCH}_2\text{CR}_2\text{CH}_2\text{A} & \quad (7-23)
\end{align*}
\]

which reacts with a second monomer molecule to form the tertiary oxonium ion

\[
\begin{align*}
\text{HO} & \quad \text{A \quad R \quad R} \\
\text{O \quad R \quad R} & \quad + \quad \text{HOCH}_2\text{CR}_2\text{CH}_2\text{A} \\
\text{HOCH}_2\text{CR}_2\text{CH}_2\text{A} & \quad (7-24)
\end{align*}
\]

This type of initiation is limited by the nucleophilicity of the anion \(\text{A}^-\) derived from the acid. For acids other than the very strong acids such as fluorosulfonic and triflic acids, the anion is sufficiently nucleophilic to compete with monomer for either the proton or secondary and tertiary oxonium ions. Only very-low-molecular-weight products are possible. The presence of water can also directly disrupt the polymerization since its nucleophilicity allows it to compete with monomer for the oxonium ions.
Lewis acids such as BF$_3$ and SbCl$_5$, almost always in conjuction with water or some other protogen, initiate polymerization of cyclic ethers. The initiator and cointitiator form an initiator–cointitiator complex [e.g., BF$_3$·H$_2$O, H$^+$·(SbCl$_6$)$_-$], which acts as a proton donor (Sec. 5-2a-2). Cationic photopolymerizations are achieved when similar proton donors are formed by the photolysis of diaryliodonium and triarylsulfonium salts (Sec. 5-2a-4).

The use of a cationogen such as an alkyl or acyl halide with a Lewis acid generates carbocations and acylium ions, either in situ or as isolable salts, which can initiate polymerization, for example

\[
\phi_3\text{Cl} + \text{AgSbF}_6 \rightarrow \text{AgCl} + \phi_3\text{C}^+\text{(SbF}_6^-) \\
\phi_3\text{Cl} + \text{SbCl}_5 \rightarrow \phi\text{C}^+\text{(SbCl}_6^-) 
\]

(7-25)

(7-26)

The initiation with some carbocations, especially trityl, does not involve direct addition to monomer. The carbocation abstracts a hydride ion from the $\alpha$-carbon of monomer and the newly formed carbocation initiates polymerization [Afsar-Taromi et al., 1978; Kuntz, 1967]. This hydride ion abstraction is so facile with 1,3-dioxolane that it is used to preform stable 1,3-dioxolan-2-ylum salts (XII) that can be used subsequently as initiators [Jedlinski et al., 1985].

\[
\phi_3\text{C}^+\text{A}^- + \phi_3\text{CH} + \text{O} 
\]

\[
\rightarrow \phi_3\text{CH} + \text{O} + \text{A}^- 
\]

(7-27)

(7-28)

Since the tertiary oxonium ion is the propagating species, preformed oxonium ions such as triethyloxonium tetrafluoroborate can be used for initiation (Eq. 7-28) [Meerwein et al., 1960]:

\[
\text{(C}_2\text{H}_5)_3\text{O}^+ \cdot \text{(BF}_4^-) + \text{O} \rightarrow \text{C}_2\text{H}_5\text{O}^- + \text{(C}_2\text{H}_5)_2\text{O} 
\]

(7-28)

Combinations of a Lewis acid, protogen or cationogen, and a reactive cyclic ether (e.g., oxirane or oxetane) have been used to initiate the polymerization of less reactive cyclic ethers such as tetrahydrofuran [Saegusa and Matsumoto, 1968]. Initiation occurs by formation of the secondary and tertiary oxonium ions of the more reactive cyclic ether, which then act as initiators for polymerization of the less reactive cyclic ether. The reactive cyclic ether, referred to as a promoter, is used in small amounts relative to the cyclic ether being polymerized and increases the ability of the latter to form the tertiary oxonium ion.

### 7-2b-3 Termination and Transfer Processes

Under certain conditions, irreversible chain-breaking reactions are absent and cationic ROPs of cyclic ethers proceed as living polymerizations. These conditions are found for polymerizations initiated with acylium and 1,3-dioxolan-2-ylum salts containing very stable counterions such as AsF$_6^-$, PF$_6^-$, and SbCl$_6^-$ or with very strong acids (fluorosulfonic and
trifluoromethanesulfonic) or their esters whose anions may form covalent ester bonds but in a reversible manner [Jedlinski et al., 1985; Penczek and Kubisa, 1989a,b; Penczek and Matyjaszewski, 1976]. The rate and degree of polymerization are given by expressions described previously (Sec. 7-2a-1, Eqs. 5-49, 7-12).

7-2b-3-a Transfer Reactions. Transfer reactions occur in many instances by a variety of reactions, some of which are analogous to those in the cationic polymerization of alkenes. Chain transfer to polymer is a common mode by which a propagating chain is terminated, although the kinetic chain is unaffected. The reaction involves nucleophilic attack by the ether oxygen in a polymer chain on the oxonium ion–propagating center, the same type of reaction involved in propagation, to form the tertiary oxonium ion XII. Subsequent nucleophilic attack on XIII by monomer yields XIV and regenerates the propagating species. The overall effect is an exchange of polymer chain segments with a broadening of the MWD from the narrow distribution for a living polymerization [Goethals, 1977]. The MWD in some reaction systems is close to the distribution expected for a step polymerization ($\bar{X}_w/\bar{X}_n \sim 2$). Chain transfer to polymer also occurs as an intramolecular reaction as well intermolecular reaction. The intramolecular reaction, also referred to as backbiting, results in the formation of cyclic oligomers instead of linear polymer; in other words, the chain ends in XIV are connected to each other. The competition between propagation and chain transfer to polymer depends on several factors. Propagation is favored on steric grounds since attack by monomer is less hindered than attack by the ether oxygen in a polymer chain. The relative nucleophilic activities of the two different ether oxygens is important and varies considerably depending on monomer ring size. Finally, intramolecular chain transfer to polymer (but not intermolecular transfer) becomes progressively more important at lower monomer concentrations.

The distribution of different-sized cyclic oligomers formed in cyclic ether polymerizations generally follows what is expected from the relative stabilities of different-sized rings (Secs. 2-5, 7-1a). The presence of a polymer–cyclic oligomer equilibrium (often in addition to a polymer–monomer equilibrium) is well documented in many different cyclic ether polymerizations [Bucquoye and Goethals, 1978; Dreyfuss and Dreyfuss, 1969, 1987; Dreyfuss et al., 1989; Kubisa, 1996; McKenna et al., 1977; Penczek and Slomkowski, 1989a,b]. Polymerization of an oxirane yields more cyclic oligomer than obtained from any other-sized cyclic ether. The relative nucleophilicity of a cyclic ether compared to a polymer chain ether is lowest for the 3-membered ring. Propagation for an oxirane involves an increase in bond angle strain on conversion of the $sp^3$-hybridized oxygen in monomer to the $sp^2$-hybridized oxygen in the oxonium ion. The cyclic dimer 1,4-dioxane is the major cyclic oligomer
formed in the polymerization of ethylene oxide (Eq. 7-30). In fact, 1,4-dioxane is the major product in the typical polymerization of ethylene oxide (>80–90%) with only minor amounts of low molecular weight (<10^3) linear polymer [Kubisa, 1996; Libiszowski et al., 1989].

\[
\overset{+}{\text{O}}\quad \overset{\text{O}}{\text{A}}\quad \overset{+}{\text{O}}\quad \overset{\text{O}}{\text{A}} \quad \overset{+}{\text{O}}\quad \overset{\text{O}}{\text{A}}
\]

Cationic ROP of ethylene oxide is not useful for the synthesis of linear polymer, but is used to produce crown ethers. Propylene oxide gives less cyclic dimer than does ethylene oxide for steric reasons; cyclic tetramer predominates.

The nucleophilicity of a cyclic ether relative to the ether oxygen in a polymer chain increases with ring size so that cyclic oligomer formation is somewhat less for oxetane and much less for tetrahydrofuran compared to oxirane. The cyclic tetramer is the most abundant cyclic oligomer, up to ~50%, with lesser amounts of trimer and sizes from pentamer to nonamer for oxetane. No cyclic dimer is found. The cyclic oligomer fraction decreases with increasing size of substituents on the oxetane ring. For example, 3,3-bis(chloromethyl)oxirane yields linear polymer with high molecular weights (10^4–10^5) and no more than a few percent cyclic oligomer. The total cyclic oligomer fraction in tetrahydrofuran polymerization is less than a few percent. The cyclic tetramer is the most abundant species followed by pentamer and hexamer; only very small amounts of other-sized cyclics are formed.

7-2b-3-b Activated Monomer Polymerization. Cyclic oligomer formation can be greatly suppressed and even eliminated by carrying out cationic polymerization as an activated monomer (AM) polymerization by using an acid initiator such as BF_3 or triflic acid in the presence of an alcohol [Biedron et al., 1990; Kubisa and Penczek, 1999; Kubisa et al., 2000; Penczek et al., 1986; Wojtania et al., 1986].

Activated monomer polymerization competes with conventional cationic ROP. Initiation in conventional ROP involves the reaction of protonated monomer with unprotonated monomer (Eq. 7-31a), whereas initiation in AM ROP involves the reaction of protonated monomer with alcohol (Eq. 7-31b).

\[
\overset{\text{O}}{\text{OH}}\quad \text{ROH} \quad \overset{+}{\text{O}}\quad \overset{\text{O}}{\text{A}}\quad \overset{+}{\text{O}}\quad \overset{\text{O}}{\text{A}} \quad \overset{+}{\text{O}}\quad \overset{\text{O}}{\text{A}}
\]

There is competition between conventional and AM ROPs. Initiation in conventional ROP is first-order each in protonated monomer and unprotonated monomer. AM ROP is first-order each in protonated monomer and alcohol. The ratio of the rates of AM-to-conventional ROP depends on [ROH]/[M] and the ratio of the rate constants for the two reactions. Assuming that the two rate constants are comparable, AM ROP becomes the dominant process at high [ROH] and low [M]. Thus, AM ROP is carried out under monomer-starved conditions. The instantaneous monomer concentration is very low, but monomer is continuously added to the reactor at a rate equal to its rate of consumption.
AM propagation continues in a similar manner with nucleophilic attack by hydroxyl end groups of polymer on protonated monomer (Eq. 7-32). Cyclic oligomer is minimized by minimizing the extent of convention ROP. For example, conventional ROP of propylene oxide with BF$_3$ in CH$_2$Cl$_2$ at 25°C gives mostly cyclic oligomers, the yield of cyclic tetramer alone is 50%. The cyclic tetramer drops below 1% when the reaction is changed to an AM polymerization by including an alcohol and slowly adding monomer.

The degree of polymerization in AM ROP is given by the ratio of the total amount of monomer supplied to the reactor to the amount of alcohol. AM polymerization has been successfully demonstrated for the synthesis of telechelic polymers of propylene oxide and epichlorohydrin with number-average molecular weights of 1000–4000. Higher molecular weights are difficult to achieve because a large amount of alcohol is needed to suppress conventional ROP.

7-2b-3-c Termination Reactions. Termination occurs to varying degrees by combination of the propagating oxonium ion with either the counterion or an anion derived from the counterion. It has been mentioned that the use of protonic acids as initiators is limited by the nucleophilicity of the anion of the acid. Transfer of an anion from the counterion, for example, occurs to varying degrees depending on the stability of the counterion. Thus, counterions such as (PF$_6$)$^-$ and (SbCl$_6$)$^-$ have little tendency to bring about termination by transfer of a halide ion, while counterions of aluminum and tin have appreciable transfer tendencies; others such as (BF$_4$)$^-$ and (FeCl$_4$)$^-$ are intermediate in behavior.

Termination may also occur by chain transfer with the initiator (e.g., water or alcohol) or a deliberately added chain-transfer agent. Deliberate termination of growth is carried out to produce polymers with specific molecular weights or, more often, telechelic polymers with specific end groups. Hydroxyl and amine end groups are obtained by using water and ammonia as chain-transfer agents. Carboxyl-ended telechelics can be obtained by termination with ketene silyl acetal followed by hydrolysis with base [Kobayashi et al., 1989].

The polymerization of 3,3-bis(chloromethyl)oxetane is complicated by the insolubility of the polymer in the reaction mixture. Termination may involve burial of the propagating oxonium ion centers in the solid polymer, resulting in their inaccessibility to further propagation.

7-2b-4 Cyclic Acetals

Cyclic acetals contain at least one 1,1-dialkoxy grouping [i.e., (RO)$_2$CH$_2$ or (RO)$_2$CHR] as part of a cyclic structure. A variety of cyclic acetals undergo facile cationic polymerization [Kubisa, 1996; Penczek and Kubisa, 1977, 1989b; Schulz et al., 1984]. This includes various
1,3-dioxacycloalkanes such as 1,3-dioxolane \((m=2)\), 1,3-dioxepane \((m=4)\), and 1,3-dioxocane \((m=5)\) [Kawakami and Yamashita, 1977a,b; Matyjaszewski et al., 1980; Okada et al., 1978; Plesch, 1976]. The polymers can be considered as copolymers of the \(\text{O}(\text{CH}_2)_m\) and \(\text{OCH}_2\) units. 1,3-Dioxane \((m=3)\) does not polymerize as a result of the stability of the 6-membered ring.

Other cyclic acetals that have been studied are 1,3,5-trioxane, 1,3,5-trioxepane, 1,3,6,9-tetraoxacycloundecane, and 1,3,5,7-tetroxocane (also referred to as 1,3,5,7-tetroxane) [Kawakami and Yamashita, 1979; Muñoz-Escalona, 1978; Schulz et al., 1984; Szwarc and Perrin, 1979]. Polymerization of bicyclic acetals has been of interest for synthesizing polysaccharides [Good and Schuerch, 1985; Hirasawa et al., 1988; Okada, 1991; Okada et al., 1989; Sumitomo and Okada, 1984].

There has been considerable debate on the details of cyclic acetal polymerizations [Penczek, 2000; Plesch, 1976; Szymanski et al., 1983]. First, it was thought that polymerization proceeded exclusively to yield cyclics, but this was not the case. As with all ROPs, reaction conditions can be manipulated to maximize the formation of either polymer or cyclics. (Study of the relative extents of cyclic and polymer has been complicated by the experimental difficulties involved in identifying the presence of cyclics. One needs to bring a variety of experimental tools and skills to bear on the problem, including a combination of size exclusion chromatography and high-pressure liquid chromatography to separate the different components of a reaction mixture followed by high-resolution NMR and mass spectroscopy for chemical identification.) Second, there has been controversy over whether the propagating species in cyclic acetal polymerization are oxonium ions (XVIII) as in cyclic ether polymerization or oxycarbocations (also referred to as alkoxycarbocations) (XIX). One assumes the oxycarbocation XIX is more stable than its carbocation counterpart in cyclic ether polymerization since XIX is stabilized via charge dispersal by the adjacent oxygen. However, this stabilization is apparently insufficient to have the oxycarbocation as the propagating species in preference to the oxonium ion. Both experimental and computational data indicate that more than 99.9% of the propagating species are oxonium ions for unsubstituted 1,3-dioxacycloalkanes [Lahti et al., 1990; Penczek, 2000; Szymanski et al., 1983; Xu et al., 1987]. Since oxonium ions are apparently only 100-fold lower in reactivity toward propagation than oxycarbocations, propagation is predominately carried by oxonium ions [Penczek and Kubisa, 1989a,b]. However, propagation by oxycarbocations is significant for 2-alkyl-1,3-dioxacycloalkanes because of additional stabilization of the positive charge center by the 2-alkyl substituent coupled with steric hindrance toward propagation through oxonium ions.
1,3,5-Trioxane, the cyclic trimer of formaldehyde, yields the same polymer, polyoxy-methylene (Eq. 7-2), as obtained by the ionic polymerization of formaldehyde (Sec. 5-6). This polymerization is carried out on an industrial scale using boron trifluoride etherate [Cui et al., 2003; Dolce and Grates, 1985]. The presence of water is required for polymerization as noted by the lack of polymer formation in the complete absence of water [Collins et al., 1979]. That 1,3,5-trioxane polymerizes in spite of containing the stable 6-membered ring is a consequence of the polymerization occurring with simultaneous precipitation of the polymer in crystalline form. The heat of crystallization makes the total process of converting monomer to polymer a significantly exothermic process.

In addition to the usual polymer–monomer propagation–depropagation equilibrium that may be present, trioxane polymerization proceeds with the occurrence of a polymer–formaldehyde equilibrium:

\[
\sim \text{OCH}_2\text{OCH}_2\text{OCH}_2 \leftrightarrow \sim \text{OCH}_2\text{OCH}_2^+ + \text{CH}_2\text{O}
\]  

(7-37)

The formation of formaldehyde probably occurs through the small concentration of oxycarbocations present, as shown above, and not through the more abundant oxonium ions.

1,3,5-Trioxane polymerizations proceed with induction periods, which correspond to the buildup of the equilibrium concentration of formaldehyde [Lu et al., 1990]. This also corresponds to a buildup in 1,3,5,7-tetroxocane, apparently by insertion of formaldehyde into 1,3,5-trioxane. Polymer is not formed until after both formaldehyde and 1,3,5,7-tetroxocane appear. Formaldehyde and, to a lesser extent, 1,3,5,7-tetroxocane decrease the induction period by increasing the rate of formation of propagating species of sufficient size to precipitate from solution. Subsequent polymerization by addition of 1,3,5-trioxane is accelerated as the reaction proceeds with conversion of monomer to crystalline polymer. The relative importance of participation by formaldehyde and 1,3,5,7-tetroxocane in propagation relative to 1,3,5-trioxane after the induction period is unclear.

Polymerization of 1,3,5-trioxepane involves more complicated propagation–depropagation equilibria. The initially formed oxycarbocation \text{XX} loses formaldehyde to yield oxycarbocation \text{XXI}, which in turn loses 1,3-dioxolane to regenerate \text{XX}:

\[
\sim \text{OCH}_2\text{CH}_2\text{OCH}_2\text{OCH}_2 \leftrightarrow \sim \text{OCH}_2\text{OCH}_2^+ + \text{CH}_2\text{O}
\]  

(7-38)

\[
\text{XX} \leftrightarrow \sim \text{OCH}_2\text{CH}_2\text{OCH}_2\text{OCH}_2^+
\]

(7-39)

Both \text{XX} and \text{XXI} undergo propagation (presumably through the corresponding oxonium ions). The two equilibria (Eqs. 7-38 and 7-39) do not proceed to the same extent, with the result that the copolymer structure deviates from that of the monomer [Szwarc and Perrin, 1979].

Transfer and termination occur by the modes described previously for cyclic ether polymerizations. Chain transfer to polymer (both inter- and intramolecular) is facilitated in cyclic acetal polymerizations compared to cyclic ethers because acetal oxygens in the polymer chain are more basic than the corresponding ether oxygens [Penczek and Kubisa, 1989a,b]. Working at high monomer concentrations, especially bulk polymerizations, is used to depress cyclic oligomer formation.
An additional termination in the trioxane polymerization is chain transfer to monomer by hydride ion transfer, which results in terminating the propagating chain with a methoxyl group while carbocation XXII reinitiates polymerization [Kern et al., 1966; Weissermel et al., 1967].

\[
\sim \text{OCH}_2\text{OCH}_2\text{OCH}_2^+ + \text{CH}_2\text{O} - \text{CH}_2 \rightarrow \sim \text{OCH}_2\text{OCH}_2\text{OCH}_3 + \text{CH}_2\text{O} - \text{CH}_2 \quad \text{XXII}
\]

(7-40)

### 7-2b-5 Kinetics of Reversible ROP

#### 7-2b-5-a Rate of Polymerization

The rate laws that describe conventional cationic ring-opening polymerizations take several forms. Some polymerizations can be described by expressions similar to those in alkene polymerizations (Sec. 5-2d). In polymerizations with little or no termination one can use kinetic expressions similar to those of living polymerizations (Secs. 5-2g, 7-2b-3).

Some cationic ring-opening polymerizations take place without termination and are reversible. Oxirane and oxetane polymerizations are seldom reversible, but polymerizations of larger-sized rings such as tetrahydrofuran are often reversible. The description of reversible ROP is presented below [Afshar-Taromi et al., 1978; Beste and Hall, 1964; Kobayashi et al., 1974; Szwarc, 1979]. It is also applicable to other reversible polymerizations such as those of alkene and carbonyl monomers. The propagation–depropagation equilibrium can be expressed by

\[
M_n^* + M \rightleftharpoons k_p \frac{k_p}{k_d} M_{n+1}^* \quad (7-41)
\]

which is analogous to Eq. 3-174. The polymerization rate is given by the difference between the rates of the propagation and depropagation reactions:

\[
R_p = \frac{-d[M]}{dt} = k_p[M^*][M] - k_d[M^*] \quad (7-42)
\]

At equilibrium, the polymerization rate is zero and Eq. 7-42 becomes

\[
k_p[M]_c = k_d
\]

(7-43)

where \([M]_c\) is the equilibrium monomer concentration (as in Eq. 3-178). (The derivations in Sec. 3-9c for \([M]_c\) and \(T_c\) as a function of \(\Delta S^\circ\) and \(\Delta H^\circ\) are applicable to the present system.) Combination of Eqs. 7-42 and 7-43 gives the polymerization rate as

\[
\frac{-d[M]}{dt} = k_p[M^*][[M] - [M]_c) \quad (7-44)
\]

which can be integrated to yield

\[
\ln \left( \frac{[M]_0 - [M]_c}{[M] - [M]_c} \right) = k_p[M^*]t \quad (7-45)
\]
where \( \frac{1}{2}M/C_{138} \) is the initial monomer concentration. (A corresponding consideration of the degree of polymerization in an equilibrium polymerization is given in Sec. 7-2b-5-c.)

The equilibrium monomer concentration is obtained by direct analysis or as the intercept of a plot of polymerization rate versus initial monomer concentration. Figure 7-1 shows such a plot for the polymerization of THF in dichloroethane solution at 0°C using triethyloxonium tetrafluoroborate as the initiator [Vofsi and Tobolsky, 1965]. The polymerization data are then plotted in accordance with Eq. 7-45 as the left side of that equation versus time to yield a straight line (Fig. 7-2) whose slope is \( kp \frac{1}{2}M^*/C_{138} \). Since \( \frac{1}{2}M^*/C_{138} \) for a living polymer can be obtained from measurements of the number-average molecular weight, one can evaluate the propagation rate constant. The concentration of the propagating species and the polymerization rate in a polymerization will be determined by the concentrations of initiator and coinitiator.

For the case where the concentration of propagating centers changes with time, integration of Eq. 7-44 yields

\[
\ln \left( \frac{[M]_1 - [M]_c}{[M]_2 - [M]_c} \right) = k_p \int_{t_1}^{t_2} [M^*] \, dt
\]

(7-46)

where \( [M]_1 \) and \( [M]_2 \) are the monomer concentrations at times \( t_1 \) and \( t_2 \), respectively.
Values of Kinetic Parameters. The availability of reliable kinetic and thermodynamic data is far less for ring-opening polymerizations than for step and chain polymerizations. However, there is a significant trend—ROP, although a chain polymerization, has propagation rate constants much more similar to step polymerization rate constants than to the propagation rate constants in the chain polymerizations of carbon–carbon double-bond monomers. For various oxirane, oxetane, THF, 1,3-dioxepane, and 1,3,6-trioxocane polymerizations, $k_p$ is in the range $10^{-1}$–$10^{-3}$ L mol$^{-1}$ s$^{-1}$ [Chien et al., 1988; Dreyfuss et al., 1989; Matyjaszewski et al., 1984; Mijangos and Leon, 1983; Penczek and Kubisa, 1989a,b; Saegusa, 1972; Xu et al., 1987]. Oxepane has a $k_p$ of $1.3 \times 10^{-4}$ L mol$^{-1}$ s$^{-1}$ [Matyjaszewski et al., 1984]. These values can be compared to the corresponding values for step and chain polymerizations (Tables 2-8, 3-10, 5-3, and 5-11). The $k_p$ values for cyclic ether and acetal polymerizations are close to the rate constants for polyesterification and similar reactions and much smaller than those for various chain polymerizations. (The concentration of propagating centers in the typical ring-opening polymerization is $10^{-2}$–$10^{-3}$ $M$, which is comparable to cationic chain polymerizations of alkenes.) There is a glaring exception to this generalization—the $k_p$ value for 1,3-dioxolane is reported as $10^2$–$10^4$ L mol$^{-1}$ s$^{-1}$ [Penczek and Kubisa, 1989a,b; Szymanski et al., 1983].

A number of interesting observations have been made for tetrahydrofuran polymerizations. The observed rate constants $k_p^+$ and $k_p^\pm$ for propagation by free ions and ion pairs are the same [Baran et al., 1983; Matyjaszewski et al., 1979; Penczek and Kubisa, 1989a,b]. [The equal reactivity of free ions and ion pairs has been observed in various solvents (CCl$_4$, CH$_2$Cl$_2$, CH$_3$NO$_2$) where the relative concentration of free ions varied from a few percent to over 95%.] This is only slightly different from the situation in cationic polymerizations of alkenes where the ion pair is about an order of magnitude less reactive than the free ion (Sec. 5-2e-3). The ion pair in THF polymerization is apparently even looser than in alkene polymerizations. The equal reactivity of free ions and ion pairs is generally assumed in all cyclic ether (as well as most ring-opening) polymerizations, but there are data for few systems other than tetrahydrofuran [Gandini and Cheradame, 1985].

The value of $k_p^+$ ($=k_p^\pm$) decreases with increasing solvent polarity for mixtures of THF with CCl$_4$ and CH$_3$NO$_2$ [Dreyfuss et al., 1989]. For free ions or their equivalent, loose and
highly solvated ion pairs, the transition state XXIII involves greater charge delocalization than does the initial state. Polar solvents stabilize the initial state more than the transition state. This is the typical behavior for reaction between a charged substrate and neutral nucleophile or between a neutral substrate and charged nucleophile in S_N2 reactions.

It was indicated earlier that the covalent species detected in many systems by NMR and other methods may be dormant, not active (propagating), species. However, propagation rate constants can be calculated on the assumption that covalent species are active. This has been done in a number of systems, such as in polymerizations of THF by very strong acids and their esters (CF_3SO_2H, C_2H_5OSO_2CF_3) in low-polarity solvents such as CCl_4 and CH_2Cl_2. The rate constant for covalent propagation is about 10^2–10^3 lower than the rate constant for the corresponding ionic species [Kobayashi et al., 1975; Matyjaszewski, 1986; Penczek and Kubisa, 1989a,b]. Even if one assumes covalent propagation, the reactivity of covalent species is so much lower than the reactivity of ionic species that more than 95% of the total polymerization rate is carried by the ionic propagating species.

7-2b-5-c Degree of Polymerization. The quantitative dependence of the degree of polymerization on various reaction parameters has been described [Hirota and Fukuda, 1987; Tobolsky, 1957, 1958; Tobolsky and Eisenberg, 1959, 1960] for an equilibrium polymerization involving initiation

\[
I + M \overset{\kappa_i}{\underset{K_p}{\rightleftharpoons}} M^* 
\]

followed by propagation (Eq. 7-41). The degree of polymerization is given by

\[
X_n = \frac{[M]_0 - [M]_c}{[I]_0 - [I]_c} 
\]

where [M]_c and [I]_c are the unreacted monomer and initiator concentrations at equilibrium. The polymer molecular weight increases with decreasing [I]_0 and increasing [M]_0. Larger values of \(K_p\), the equilibrium constant for Eq. 7-41, and smaller values of \(K_i\) yield higher polymer molecular weights by decreasing [M]_c and increasing [M]_c, respectively.

7-2b-6 Energetic Characteristics

7-2b-6-a Effect of Temperature on Rate and Degree of Polymerization. The effects of temperature on the rate and degree of polymerization of cyclic ethers and acetals vary considerably depending on the specific reaction system. Variations due to different monomers, solvents, initiators, and coinitiators are generally analogous to those observed in ionic polymerizations of alkenes (Secs. 5-2f, 5-3d-2). Increased temperature almost always results in an increase in the rate of polymerization; that is, \(E_{R_p}\) is positive. Few \(E_{R_p}\) or individual activation energies for initiation, propagation, and termination–transfer are available. Typical values of \(E_{R_p}\) or \(E_p\) are in the range 20–80 kJ mol\(^{-1}\) with most values in the upper part of that
range. The $E_p$ value is 25, 47, 61, 49, 75, and 86 kJ mol$^{-1}$ for epichlorohydrin, oxetane, THF, 1,3-dioxolane, oxepane, and 1,3-dioxepane, respectively [Chien et al., 1988; Dreyfuss and Dreyfuss, 1976; Sims, 1966]. The $E_{R_p}$ value is 72 kJ mol$^{-1}$ for 3,3-bis(chloromethyl)oxetane [Chapiro and Penczek, 1962; Penczek and Penczek, 1963]. As with ionic polymerizations of alkenes, the activation energies can vary considerably with reaction conditions. Thus $E_{R_p}$ for 3,3-bis(chloromethyl)oxetane is only 12–16 kJ mol$^{-1}$ for radiation-initiated polymerization in the crystalline state. The lower activation energy may be a consequence of a favorable orientation of the monomer for propagation in the crystalline state.

The effect of temperature on the degree of polymerization is more complex. For most polymerizations, increasing the temperature decreases the polymer molecular weight as a result of increases in the rates of transfer and termination relative to propagation. Table 7-2 shows this effect for the polymerization of oxetane by boron trifluoride [Rose, 1956]. (The intrinsic viscosity is a measure of polymer molecular weight.) The decrease in polymer molecular weight in this polymerization is due primarily to an increase in intramolecular chain transfer to polymer as indicated by the corresponding increase in the yield of cyclic tetramer with increasing temperature. In other polymerizations the termination and transfer reactions may not be appreciably affected by increasing temperature, while the propagation reaction rate increases. The result is an increase in polymer molecular weight with increasing temperature. Figure 7-3 shows a THF polymerization in which the polymer molecular weight increases initially with increasing temperature up to about $-5^\circ C$ and then

![Table 7-2 Effect of Temperature on Polymerization of Oxetane](image)

<table>
<thead>
<tr>
<th>Temperature ($^\circ C$)</th>
<th>Intrinsic Viscosity of Polymer (dl g$^{-1}$)</th>
<th>Ultimate Conversion of Monomer (%)</th>
<th>Proportion of Tetramer (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>-80</td>
<td>2.9</td>
<td>95</td>
<td>4</td>
</tr>
<tr>
<td>0</td>
<td>2.1</td>
<td>94</td>
<td>10</td>
</tr>
<tr>
<td>50</td>
<td>1.3</td>
<td>64</td>
<td>66</td>
</tr>
<tr>
<td>100</td>
<td>1.1</td>
<td>62</td>
<td>62</td>
</tr>
</tbody>
</table>

aData from Rose [1956].

![Fig. 7-3 Effect of temperature on polymer molecular weight in the BF$_3$ polymerization of tetrahydrofuran. After Burrows and Crowe [1962] (by permission of Wiley-Interscience, New York).](image)
subsequently decreases at higher temperatures. Termination is relatively unaffected at the lower temperatures but increases with temperature at the higher temperatures [Burrows and Crowe, 1962].

Table 7-2 shows a decrease in the ultimate conversion of monomer to polymer for the oxetane polymerization as the reaction temperature is increased. In this polymerization the effect appears to be due to thermal destruction of the initiator [Rose, 1956]. The same trend is observed for most cyclic ether and acetal polymerizations but for a different reason. Increased temperature usually decreases the conversion of monomer to polymer by a ceiling temperature effect. The propagation–depropagation equilibrium (Eq. 7-41) is shifted to the left with increasing temperature. The equilibrium monomer concentration increases with increasing temperature in accord with Eq. 3-178 (keep in mind that $\Delta H^\circ$ is negative). Figure 7-4 shows this effect for THF polymerization in bulk using benzene diazonium hexafluorophosphate as the initiator.

7-2b-6-b Thermodynamics of Polymerization. The enthalpies and entropies of polymerization for various cyclic ethers and acetals are shown in Table 7-3. Data for formaldehyde and chloral are also included. A comparison of the $\Delta H$ and $\Delta S$ values for alkenes, carbonyl monomers, and the cyclic monomers can be made from Tables 7-3 and 3-14. The $\Delta H$ for the 3- and 4-membered cyclics are comparable to those for alkenes, and both are appreciably larger than the values for the two carbonyl monomers. The conversion of a carbonyl $\pi$-bond to a $\sigma$-bond is not as exothermic as the corresponding conversion of an alkene $\pi$-bond. The $\Delta H$ values for the larger-sized cyclic monomers are much lower than those for alkenes. The $\Delta S$ value is considerably smaller for most cyclic monomers compared to the alkenes and carbonyls. The cyclic monomers, having less degrees of freedom to begin with, have $\Delta S$ values indicating that the loss in disorder on polymerization is less than for noncyclic monomers. Ethylene oxide is an exception because of the highly strained nature of the 3-membered ring. The $\Delta S$ values for a few of the cyclic monomers, THF and 3,3-bis (chloromethyl)oxetane, are similar to the lowest values observed for alkene monomers.
The $\Delta H$ values for the various cyclic ethers and acetals follow closely the order expected based on considerations of relative stability as a function of ring size (Secs. 7-1a, 2-5). The 3- and 4-membered cyclic monomers undergo the most exothermic polymerizations. There is a fast decrease in the exothermicity of polymerization for the larger-sized rings. Trioxane, the only 6-membered ring monomer to undergo polymerization, has a $\Delta H$ very close to zero. Substituents on a ring structure decrease the tendency to polymerize, as noted by the less exothermic polymerizations for the substituted 1,3-dioxolane, 1,3-dioxepane, and 1,3,6-trioxocane monomers relative to the corresponding unsubstituted monomers. Substituted oxetanes are an exception to this generalization.

### Commercial Applications

There are a number of commercial applications of ring-opening polymerization of cyclic ethers. Polymerizations and copolymerizations of ethylene and propylene oxides as well as polymerization of tetrahydrofuran are used to produce polyether macrodiols, specifically, telechelic polyethers having hydroxyl end groups [Clinton and Matlock, 1986; Dreyfuss et al., 1989; Gagnon, 1986]. The commercial materials are typically in the molecular weight range 500–6000 and are used to produce polyurethane and polyester block copolymers, including the thermoplastic polyurethane and polyester elastomers (Secs. 2-12e, 2-13b-3, 2-13c-2). The polyether macrodiols are also referred to as polyether glycols or polyols (trade names: Carbowax, Jeffox, Polyglycol, Polymeg, Terathane). Ethylene oxide and propylene oxide polymers and copolymers are also available in molecular weights of up to $10^5$, and are used as hydraulic fluids and lubricants, additives in cosmetics, and binders in ceramic and powder metallurgy. Ethylene oxide polymers with molecular weights of $10^5$–$10^6$.

<table>
<thead>
<tr>
<th>Monomer</th>
<th>Ring Size</th>
<th>$-\Delta H$ (kJ mol$^{-1}$)</th>
<th>$-\Delta S$ (J mol$^{-1}$ K$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ethylene oxide</td>
<td>3</td>
<td>94.5</td>
<td>174</td>
</tr>
<tr>
<td>Oxtane</td>
<td>4</td>
<td>81</td>
<td></td>
</tr>
<tr>
<td>3,3-Bis(chloromethyl)oxetane</td>
<td>4</td>
<td>84.5</td>
<td>83</td>
</tr>
<tr>
<td>Tetrahydrofuran</td>
<td>5</td>
<td>23.4</td>
<td>82.4</td>
</tr>
<tr>
<td>1,3-Dioxolane</td>
<td>5</td>
<td>17.6</td>
<td>47.7</td>
</tr>
<tr>
<td>4-Methyl-1,3-dioxolane</td>
<td>5</td>
<td>13.4</td>
<td>53.1</td>
</tr>
<tr>
<td>Trioxane</td>
<td>6</td>
<td>4.5</td>
<td>18</td>
</tr>
<tr>
<td>1,3-Dioxepane</td>
<td>7</td>
<td>15.1</td>
<td>48.1</td>
</tr>
<tr>
<td>2-Methyl-1,3-dioxepane</td>
<td>7</td>
<td>8.8</td>
<td>37.2</td>
</tr>
<tr>
<td>4-Methyl-1,3-dioxepane</td>
<td>7</td>
<td>9.2</td>
<td>38.9</td>
</tr>
<tr>
<td>1,3-Dioxocane</td>
<td>8</td>
<td>18.3</td>
<td></td>
</tr>
<tr>
<td>1,3,6-Trioxocene</td>
<td>8</td>
<td>13.0</td>
<td>21.3</td>
</tr>
<tr>
<td>2-n-Butyl-1,3,6-trioxocane</td>
<td>10</td>
<td>7.9</td>
<td>16.3</td>
</tr>
<tr>
<td>1,3,6,9-Tetraoxacycloundecane</td>
<td>11</td>
<td>8.0</td>
<td>6.2</td>
</tr>
<tr>
<td>Formaldehyde</td>
<td></td>
<td>31.1</td>
<td>79.2</td>
</tr>
<tr>
<td>Chloral</td>
<td></td>
<td>20</td>
<td>95</td>
</tr>
</tbody>
</table>

$^{a}$ Data from Busfield [1989] unless otherwise noted.
$^{b}$ Dreyfuss and Dreyfuss [1989].
$^{c}$ Okada et al. [1976].
$^{d}$ Okada et al. [1978].
$^{e}$ Xu et al. [1987].
$^{f}$ Rentsch and Schulz [1978].
referred to as poly(ethylene oxide), find applications that take advantage of the high viscosity of their aqueous solutions. This includes flocculation, denture adhesives, packaging films (pesticides, herbicides, seed tapes), thickening of acid cleaners and water-based paints, and friction reduction. There is considerable effort aimed at using ethylene oxide polymers and copolymers complexed with ionic salts as the electrolyte in all-solid rechargeable batteries.

Polyepichlorohydrin and copolymers and terpolymers of epichlorohydrin with ethylene oxide and allyl glycidyl ether are useful elastomers [Body and Kylfinstad, 1986].

\[
\text{CH}_2=\text{CHCH}_2\text{OCH}_2\text{CH}=-\text{CH}_2
\]

Allyl glycidyl ether

These materials (trade names: Epichlomer, Herclor, Hydrin) have good resistance to fuel, oil, ozone, and heat combined with low-temperature flexibility and resistance to vapor permeation by air, hydrocarbons, and fluorocarbons.

Polyoxymethylene, also referred to as acetal resin or POM, is obtained either by anionic polymerization of formaldehyde or cationic ring-opening copolymerization of trioxane with a small amount of a cyclic ether or acetal (e.g., ethylene oxide or 1,3-dioxolane) [Cherdron et al., 1988; Dolce and Grates, 1985; Yamasaki et al., 2001]. The properties and uses of POM have been discussed in Sec. 5-6d.

Both anionic and cationic initiation are used to cure (polymerize and crosslink) epoxy resins (Sec. 2-12d) by ROP of the oxirane end groups. Photochemical cationic initiation (Sec. 5-2a-4) is important in various coating applications (3-4c) [Decker et al., 2001].

### 7-3 LACTAMS

The polymerization of lactams (cyclic amides) can be initiated by bases, acids, and water [Reimschuessel, 1977; Sebenda, 1976, 1978; Sekiguchi, 1984]. Initiation by water, referred to as hydrolytic polymerization, is the most often used method for industrial polymerization of lactams. Anionic initiation is also practiced, especially polymerization in molds to directly produce objects from monomer. Cationic initiation is not useful because the conversions and polymer molecular weights are considerably lower.

Nylon 6 is produced commercially, accounting for almost one-third of all polyamides (Sec. 2-8f). Nylons 11 and 12 are specialty polyamides, which find use in applications requiring higher moisture resistance and hydrolytic stability.

Lactams are named in several ways. They are named as alkanolactams by the IUPAC substitutive system, such as 3-propanolactam, 4-butanolactam, 5-pentanolactam, and 6-hexanolactam, respectively, for the 4-, 5-, 6-, and 7-membered rings, respectively. An alternate IUPAC method, the specialist heterocyclic nomenclature system, names these lactams as 2-azetidinone, 2-pyrrolidinone, 2-piperidinone, and hexahydro-2H-azepin-2-one, respectively. These lactams are also known by the trivial names \(\beta\)-propiolactam, \(\alpha\)-pyrrolidone (\(\gamma\)-valerylactam), \(\alpha\)-piperidone (\(\delta\)-valerolactam), and \(\epsilon\)-caprolactam, respectively.
7-3a Cationic Polymerization

A variety of protonic and Lewis acids initiate the cationic polymerization of lactams [Bertalan et al., 1988a,b; Kubisa, 1996; Kubisa and Penczek, 1999; Puffr and Sebenda, 1986; Sebenda, 1988]. The reaction follows the mechanism of acid-catalyzed nucleophilic substitution reactions of amides. More specifically, polymerization follows an activated monomer mechanism. Initiation occurs by nucleophilic attack of monomer on protonated (activated) monomer (XXIV) to form an ammonium salt (XXV) that subsequently undergoes proton exchange with monomer to yield XXVI and protonated monomer. The conversion of XXIV to XXV involves several steps—attachment of nitrogen to C\(^+\), proton transfer from one N to the other N, ring opening of the HO-containing ring, and transfer from HO–C\(^+\) to N with formation of XXV. Some literature references present variations of the preceding equation whereby protonation of lactam is shown as occurring at nitrogen. This does not correspond to the generally accepted mechanism for acid-catalyzed substitution reactions of amides, such as hydrolysis of acetamide. The available data on such reactions are consistent with protonation occurring almost exclusively at the carbonyl oxygen [Lowry and Richardson, 1987].

Propagation follows in a similar manner as a nucleophilic attack by the primary amine end group of a growing polymer chain (XXVII) on protonated monomer to yield XXVIII,

\[
\text{XXVII} \rightarrow \text{XXVIII}
\]

which then undergoes proton exchange with monomer

\[
\text{XXVIII} \rightarrow \text{XXVII}
\]
Simultaneously with propagation by Eqs. 7-52 and 7-53, there is propagation by self-reaction of XXVII. XXVII is an AB type of monomer, and step polymerization occurs by reaction between amine and lactam end groups. Actually, the lactam end groups are protonated prior to reaction. The reaction is generally the same as Eq. 7-52—nucleophilic attack of amine on protonated lactam. Although this reaction is only a minor contribution to the overall conversion of lactam to polymer, it determines the final degree of polymerization. There are also exchange reactions that involve intermolecular nucleophilic attack of amine on amide linkages within a polymer chain. Intramolecular versions of the various reactions result in cyclic oligomer formation. Overall, one generally observes the molecular weight distribution (MWD) of the polymer (excluding cyclic oligomer and monomer) to be close to the Flory most probable distribution.

For cationic polymerization with an acid whose anion $Z^-$ is nucleophilic, initiation involves the sequence described by Eq. 7-51 plus the formation of XXIX. XXIX propagates by a sequence similar to that described by Eqs. 7-52 and 7-53 except that a growing polymer chain possesses a $Z^-$ end group instead of a lactam end group.

$$\text{Z}^- + \text{HN}R \rightarrow \text{ZCORNH}_2$$

(7-54)

XXIX

Various side reactions greatly limit the conversions and polymer molecular weights that can be achieved in cationic polymerization of lactams. The highest molecular weights obtained in these polymerizations are 10,000–20,000. The most significant side reaction is amidine (XXXI) formation [Bertalan et al., 1984]. Propagation of the polymer chain and amidine formation proceed through the common intermediate XXX formed by attachment of an amine group to the protonated carbonyl of any amide group (that in lactam monomer or the lactam end group in polymer or the amide groups in the repeat units of the polymer). Propagation involves cleavage of the C–N bond (overall result is substitution at carbonyl), while amidine formation involves loss of water from XXX (overall result is addition to carbonyl followed by dehydration). Amidine formation decreases the concentration of amine groups in the reaction system, and this leads to a slower rate of reaction. The water released during amidine formation can initiate polymerization (Sec. 7-3b), but at a slower rate. Furthermore, amidine groups react rapidly with acidic initiators to give relatively unreactive salts, and this limits the rate and degree of polymerization.

Cationic polymerization is the only route to the polymerization of N-alkylated lactams. Both the hydrolytic and anionic routes require that a lactam have a hydrogen on the nitrogen. However, there are no commercial applications for N-alkylated polyamides, probably because their lack of hydrogen bonding results in lower melting points than for polyamides without an N-alkyl group.
Hydrolytic polymerization of ε-caprolactam to form nylon 6 (Sec. 2-8f) is carried out commercially in both batch and continuous processes by heating the monomer in the presence of 5–10% water to temperatures of 250–270°C for periods of 12 h to more than 24 h [Anton and Baird, 2002; Zimmerman, 1988]. Several equilibria are involved in the polymerization [Bertalan et al., 1984; Sekiguchi, 1984]. These are hydrolysis of the lactam to ε-aminocaproic acid (Eq. 7-56), step polymerization of the amino acid with itself (Eq. 7-57), and initiation of ring-opening polymerization of lactam by the amino acid. The amino acid is the equivalent of XXIX in Eq. 7-54 (Z = OH). The COOH group of the amino acid protonates the lactam to form XXVI followed by nucleophilic attack of amine on the protonated lactam. The propagation process follows in the same manner with nucleophilic attack of XXXII on protonated lactam to form XXXIII [R = (CH₂)₃]. Species XXXIII subsequently protonates lactam and propagation continues. The sequence is the same as in Eqs. 7-52 and 7-53 except for the propagating chain possessing a carboxyl end group instead of lactam end group. Hydrolytic polymerization is simply a special case of cationic polymerization. [The commercial processes often add ε-aminocaproic acid or the 1 : 1 ammonium carboxylate salt from a diamine and diacid (Eq. 2-128) along with water. This is a faster route to initiation as it supplies amine and carboxyl groups at the very beginning instead of waiting for hydrolysis of the lactam to supply those groups.]

The overall rate of conversion of ε-caprolactam to polymer is higher than the polymerization rate of ε-aminocaproic acid by more than an order of magnitude [Hermans et al., 1958, 1960]. Step polymerization of ε-aminocaproic acid with itself (Eq. 7-57) accounts for only a few percent of the total polymerization of ε-caprolactam. Ring-opening polymerization (Eq. 7-58) is the overwhelming route for polymer formation. Polymerization is acid-catalyzed as indicated by the observations that amines and sodium ε-aminocaproate are poor initiators in the absence of water and the polymerization rate in the presence of water is first-order in lactam and second-order in COOH end groups [Majury, 1958].

Although step polymerization of ε-aminocaproic acid with itself is only a minor contribution to the overall conversion of lactam to polymer, it does determine the final degree of polymerization at equilibrium since the polymer undergoes self-condensation. The final
degree of polymerization is dependent in large part on the equilibrium water concentration (Sec. 2-4). Most of the water used to initiate polymerization is removed after about 80–90% conversion in order to drive the system to high molecular weight. Molecular weight control at a desired level also requires control of the initial water and monomer concentrations (7-2b-5-c) and the addition of small but specific amounts of a monofunctional acid (Sec. 2-6). The MWD is essentially the Flory most probable distribution except for the presence of monomer and cyclic oligomers.

The final product in the industrial polymerization of \( \varepsilon \)-caprolactam contains about 8% monomer and 2% cyclic oligomer [DiSilvestro et al., 1987; Reimschuessel, 1977; Zimmerman, 1988]. About one-half of the cyclic fraction is the cyclic dimer with the remaining one-half consisting mostly of the trimer and tetramer, although small amounts of cyclics up to the nonamer have been identified [Rothe, 1958; Zahn, 1957]. Cyclic oligomers are formed when any of the propagations discussed above occur intramolecularly (both for cationic and hydrolytic polymerizations). The monomer and cyclic oligomer are removed in the industrial production of poly(\( \varepsilon \)-caprolactam) by extraction with hot water (or vacuum). The water content of the final product is lowered to less than about 0.1% by vacuum drying at 100–200°C and about 1 torr pressure.

Amidines are formed in hydrolytic polymerizations of lactams but do not limit the polymer molecular weight. Molecular weight buildup is not impeded since the carboxyl end groups of growing polymer are quite reactive toward amidine groups [Bertalan et al., 1984].

### 7-3c Anionic Polymerization

#### 7-3c-1 Use of Strong Base Alone

Strong bases such as alkali metals, metal hydrides, metal amides, metal alkoxides, and organometallic compounds initiate the polymerization of a lactam by forming the lactam anion XXXIV [Hashimoto, 2000; Sebenda, 1989; Sekiguchi, 1984], for example, for \( \varepsilon \)-caprolactam with a metal

\[
\begin{align*}
\text{O} & \quad \text{(CH}_2\text{)}_5 \text{NH} + \text{M} \quad \text{XXXIV} \\
\text{O} & \quad \text{(CH}_2\text{)}_5 \text{N}^- \text{M}^+ + \frac{1}{2} \text{H}_2
\end{align*}
\tag{7-59a}
\]

or with a metal derivative

\[
\begin{align*}
\text{O} & \quad \text{(CH}_2\text{)}_5 \text{NH} + \text{B}^- \text{M}^+ \quad \text{XXXIV} \\
\text{O} & \quad \text{(CH}_2\text{)}_5 \text{N}^- \text{M}^+ + \text{BH}
\end{align*}
\tag{7-59b}
\]

There are advantages and disadvantages with almost any choice of base. The use of weaker bases produces a lower concentration of lactam anion unless the equilibrium is pushed to the right. The use of an alkali metal or metal hydride gives a high concentration of lactam anion, but side reactions contaminate the product with amines and water that destroy reactive initiating and propagating species. The use of most bases contaminates the system with the conjugate acid (BH) of the base, and this also destroys reactive species. The preferred method of initiation consists of preforming and purifying the lactam anion followed by addition to the reaction system.
The lactam anion reacts with monomer in the second step of the initiation process by a ring-opening transamidation to form the primary amine anion XXXV. Species XXXV, unlike the lactam anion, is not stabilized by conjugation with a carbonyl group. The primary amine anion is highly reactive and rapidly abstracts a proton from monomer to form the imide dimer XXXVI, \( N-(\epsilon\text{-aminocaproyl})\text{caprolactam} \), and regenerate the lactam anion.

\[
\begin{align*}
\text{(CH}_2\text{)}_5\text{N}^-\text{M}^+ & + \text{HN-}\text{(CH}_2\text{)}_5 \\
\rightarrow \\
\text{(CH}_2\text{)}_5\text{N}^+\text{CO(CH}_2\text{)}_5\text{N}^-\text{M}^+ \\
\end{align*}
\]

XXXV

The imide dimer has been isolated and is the actual initiating species necessary for the onset of polymerization [Hall, 1958; Rothe et al., 1962]. Lactam polymerization is characterized by an initial induction period of low reaction rate as the concentration of imide dimer builds up slowly. The imide dimer is necessary for polymerization because the amide linkage in the lactam is not sufficiently reactive (i.e., not sufficiently electron deficient) toward transamidation by lactam anion. The presence of the \( \text{exo-carbonyl} \) group attached to the nitrogen in the \( N\)-acyllactam increases the electron deficiency of the amide linkage. This increases the reactivity of the amide ring structure toward nucleophilic attack by the lactam anion. Propagation follows in the same manner as the reaction of a propagating \( N\)-acyllactam species (XXXVII) and the lactam anion (Eq. 7-62), followed by fast proton exchange with monomer to regenerate the lactam anion and the propagating \( N\)-acyllactam XXXVIII (Eq. 7-63).

\[
\begin{align*}
\text{(CH}_2\text{)}_5\text{N}^-\text{CO(CH}_2\text{)}_5\text{NH} & \leftrightarrow + \text{(CH}_2\text{)}_5\text{N}^-\text{M}^+ \\
\rightarrow \\
\text{(CH}_2\text{)}_5\text{N}^+\text{CO(CH}_2\text{)}_5\text{N}^-\text{M}^+ \\
\end{align*}
\]

XXXVII

\[
\begin{align*}
\text{(CH}_2\text{)}_5\text{N}^-\text{CO(CH}_2\text{)}_5\text{N}^-\text{CO(CH}_2\text{)}_5\text{NH} & \leftrightarrow + \text{(CH}_2\text{)}_5\text{N}^-\text{M}^+ \\
\rightarrow \\
\text{(CH}_2\text{)}_5\text{N}^+\text{CO(CH}_2\text{)}_5\text{N}^-\text{CO(CH}_2\text{)}_5\text{NH} + \text{(CH}_2\text{)}_5\text{N}^-\text{NH} \\
\end{align*}
\]

XXXVIII
The anionic polymerization of lactams proceeds by a mechanism analogous to the activated monomer mechanism for anionic polymerization of acrylamide (Sec. 5-7b) and some cationic polymerizations of epoxides (Sec. 7-2b-3-b). The propagating center is the cyclic amide linkage of the N-acyllactam. Monomer does not add to the propagating chain; it is the monomer anion (lactam anion), often referred to as activated monomer, which adds to the propagating chain [Szwarc, 1965, 1966]. The propagation rate depends on the concentrations of lactam anion and N-acyllactam, both of which are determined by the concentrations of lactam and base.

7-3c-2 Addition of N-Acylactam

The use of a strong base alone for lactam polymerization is limiting. There are the induction periods previously noted and, more importantly, only the more reactive lactams, such as ε-caprolactam and 7-heptanolactam (ζ-enantholactam), readily undergo polymerization. The less reactive lactams, 2-pyrrolidinone and 2-piperidinone, are much more sluggish toward polymerization by strong base alone. Formation of the imide dimer is difficult from these relatively unreactive lactams. Both limitations are overcome by forming an imide by reaction of lactam with an acylating agent such as acid chloride or anhydride, isocyanate, monocarbodiimide, and others [Luisier et al., 2002]. Thus, ε-caprolactam can be readily converted to an N-acylcaprolactam XXXIX by reaction with an acid chloride. The N-acyllactam can be synthesized in situ or preformed and then added to the reaction system.

\[
\begin{align*}
\text{XXXIX} & : \quad \text{(CH}_2\text{)}_5 \text{NH} \xrightarrow{\text{RCOCI}} \text{(CH}_2\text{)}_5 \text{N}−\text{CO−R} \\
\end{align*}
\]

Initiation consists of the reaction of the N-acyllactam with activated monomer followed by fast proton exchange with monomer

\[
\begin{align*}
\text{XL} & : \quad \text{(CH}_2\text{)}_5 \text{N}−\text{CO−R} + \text{(CH}_2\text{)}_5 \text{N}−\text{M}^+ \\
\text{XLI} & : \quad \text{(CH}_2\text{)}_5 \text{N}−\text{CO(CH}_2\text{)}_5 \text{N}−\text{CO−R} + \text{(CH}_2\text{)}_5 \text{NH}−\text{CO−R} + \text{(CH}_2\text{)}_5 \text{N}−\text{M}^+ \\
\end{align*}
\]

Species XL and XLI correspond to species XXXV and XXXVI for polymerization in the absence of an acylating agent. The acylating agent achieves facile polymerization of many
lactams by substituting the fast initiation sequence in Eqs. 7-65 and 7-66 for the slower sequence in Eqs. 7-60 and 7-61. The use of an acylating agent is advantageous even for the more reactive lactams as induction periods are absent, polymerization rates are higher, and lower reaction temperatures can be used.

Polymerizations in the absence and presence of an acylating agent are often referred to as nonassisted and assisted polymerizations, respectively. The terms nonactivated and activated polymerization are also used, but this is confusing since both reactions involve the lactam anion, which is usually referred to as activated monomer. The literature is also confusing with regard to terms used to describe the acylating agent. Activator, promoter, catalyst, and initiator are terms that have been used. Terminology for the strong base is also a problem since its role is not the same for activated and nonactivated polymerizations. The base is needed in both polymerizations for forming the lactam anion (activated monomer). For non-assisted polymerization, the lactam anion is not only the “real” monomer but is also the species required to form the initiating species (imide dimer). This text will avoid the use of any of these terms for the strong base and acylating agent.

Propagation follows in the same manner as for propagation of species XXXVII except that the propagating chain has an acylated end group instead of the amine end group:

\[
\text{Initiation in activated lactam polymerization may involve contributions from both the imide dimer (XXXVI) and N-acyllactam (XXXIX). However, in the usual case the latter is by far the most important and the former may be ignored. Few detailed kinetic studies of these lactam polymerizations have been achieved, but some of the main reaction characteristics are indicated [Kuskova et al., 1978; Sebenda, 1989; Tani and Konomi, 1966]. The polymerization rate is dependent on the concentrations of base and N-acyllactam, which determine the concentrations of activated monomer and propagating chains, respectively. The degree of polymerization increases with conversion and with increasing concentration of monomer and decreasing N-acyllactam concentration. These characteristics are qualitatively similar to those of living polymerizations, but lactam polymerizations seldom are living. There is a fairly rapid decay of both the activated monomer and propagating chain concentrations due to a complex set of side reactions [Roda et al., 1976; Sebenda and Kouril, 1971, 1972; Sekiguchi, 1984]. These side reactions include hydrogen abstraction from C–H bonds α- to amide carbonyls (which result in the formation of various β-ketoimides and β-ketoamides via nucleophilic substitution by the carbanions on lactam end groups of propagating}
chains) and subsequent Claisen-type condensation reactions of the β-ketoimides and β-keto-
amides. The latter reaction yields water as a by-product, and water reacts with and decreases
the concentrations of both activated monomer and N-acyllactam.

Lactam polymerizations (nonassisted as well as assisted) are usually complicated by
heterogeneity, usually when polymerization is carried out below the melting point of the
polymer [Fries et al., 1987; Karger-Kocsis and Kiss, 1979; Malkin et al., 1982; Roda et al.,
1979]. (This is probably the main reason why there are so few reliable kinetic studies of lac-
tam polymerizations.) An initially homogeneous reaction system quickly becomes heteroge-
neous at low conversion, for example, 10–20% conversion (attained at a reaction time of no
more than 1 min) for 2-pyrrolidinone polymerization initiated by potassium \( t \)-butoxide and
N-benzoyl-2-pyrrolidinone. The (partially) crystalline polymer starts precipitating from solu-
tion (which may be molten monomer), and subsequent polymerization occurs at a lower rate
as a result of decreased mobility of N-acyllactam propagating species.

The MWD is usually broader than the most probable distribution as a result of branching,
which occurs in the later stages of reaction. As the monomer and lactam anion concentrations
decrease, there is an increasing tendency for the polymeric amide anion \( \text{XLII} \) to attack the

\[
\begin{align*}
\sim \text{N}–\text{CO} & \quad + \quad \text{(CH}_2\text{)}_5–\text{N}–\text{CO} \\
\text{XLII} & \quad \rightarrow \quad \sim \text{N}–\text{CO(CH}_2\text{)}_3\tilde{\text{N}}–\text{CO} \quad \text{(7-69)}
\end{align*}
\]

lactam end group of another polymer chain. Further, branching, and to some extent cross-
linking, result from the Claisen-type condensations mentioned above. The MWD is consid-
erably broader when an N-acyllactam is not used, since initiation is slow and polymer chains
initiated early grow for longer times than those initiated later [Costa et al., 1979].

7-3d Reactivity

Lactam reactivity toward polymerization depends on ring size and the type of initiation. The
slower cationic and hydrolytic polymerizations result in a wider spread of reactivities than
does anionic polymerization. The 6-membered lactam undergoes polymerization in anionic
polymerization, whereas most 6-membered cyclic monomers are unreactive toward ring-
opening polymerization. Substituted lactams show the expected lower reactivity relative to
unsubstituted lactams, a consequence of steric hindrance at the reaction site [Cubbon, 1964].
However, the effects of substitution can be complex. In the polymerization of \( \alpha,\alpha \)-dialkyl-β-
propiolactams (\( \text{XLIII} \)), the propagation rate constant increased about twofold as \( R \) increased
from methyl to \( n \)-butyl. The enhanced reactivity may result from the larger hydrophobic \( R \)
group preventing strong interaction of the counterion and propagating center, resulting in a
looser ion pair.
7-4 N-CARBOXY-α-AMINO ACID ANHYDRIDES

N-Carboxy-α-amino acid anhydrides, also referred to as 4-substituted oxazolidine-2,5-diones, Leuchs’s anhydrides, or N-carboxyamides (NCA), are polymerized by bases and transition metal complexes. Polymerization proceeds with simultaneous decarboxylation to produce a polyamide

\[
\text{RNH}_2 + \text{O} \xrightarrow{-\text{CO}_2} \text{RNHCOCHRNH}_2 \tag{7-71a}
\]

\[
\text{RNH} \sim \text{COCHRNH}_2 + \text{O} \xrightarrow{-\text{CO}_2} \text{RNH} \sim \text{COCHRNHCOCHRNH}_2 \tag{7-71b}
\]

The polyamide is a substituted nylon 2, that is, it is derived from an α-amino acid—the same type used in living organisms to produce polypeptides. NCA polymerizations have been used to synthesize polypeptides, both homopolymers and copolymers, that may be useful in biotechnology applications such as artificial tissues, drug delivery, and biosensors.

7-4a Polymerization by Bases

Polymerization is accomplished with amines and metal alkoxides, hydroxides, and hydrides [Bamford and Block, 1976; Giannakidis and Harwood, 1978; Goodman et al., 1977; Imanishi, 1984; Imanishi et al., 1977; Kricheldorf, 1986, 1989; Shalitin, 1969]. Two different mechanisms are operative depending on the relative nucleophilicity and basicity of the initiator—the amine and activated monomer mechanisms. Primary aliphatic amines, which have a high nucleophilicity relative to basicity, polymerize N-carboxyamides by the amine mechanism involving nucleophilic attack by nitrogen at the C-5 carbonyl of NCA with evolution of carbon dioxide (Eqs. 7-71a,b). Studies with \(^{14}\text{C}\)-labeled NCA show that the carbon dioxide is derived from the C-2 carbonyl. The polymerization rate is directly dependent on the concentrations of monomer and amine. Most NCA polymerizations have similar but not exactly the same characteristics as living polymerizations. The degree of polymerization is proportional but not always equal to the monomer/amine ratio, and the MWD is usually broadened or bimodal. The overall lack of control is attributed to termination, transfer, and other side reactions [Deming, 2000; Kricheldorf, 1989; Sekiguchi, 1981].

Polymerization by aromatic primary amines (which are weaker nucleophiles) proceeds with considerable molecular weight broadening due to the slower rate of initiation relative to propagation. Water has also been used as an initiator, but the molecular weights are considerably lower, no higher than 10,000–20,000, as a result of slow initiation.
Polymerizations initiated by strong bases (R⁻, HO⁻, RO⁻) and tertiary amines (which are poor nucleophiles) proceed at much faster rates than do polymerizations initiated by primary amines. Also, unlike the latter, where each polymer chain contains one initiator fragment (i.e., RNH—), these polymerizations do not result in incorporation of the initiator into the polymer chain. Polymerization proceeds by an activated monomer mechanism similar to that in the anionic polymerization of lactams. The reacting monomer is the NCA anion XLIV

\[
\text{XLIV}
\]

formed by proton transfer from monomer to base (Eq. 7-72). Initiation involves nucleophilic attack by NCA anion on NCA followed by proton transfer with another monomer molecule to regenerate an anion. Propagation proceeds in a similar manner (Eq. 7-73):

\[
\text{H(NHCHRCO)}_n^- + \text{NCA} \rightarrow \text{H(NHCHRCO)}_n^- \text{NCA} \rightarrow \text{H(NHCHRCO)}_{(n+1)}^-
\]

Polymerization by trialkylamines is useful for synthesizing polypeptides of molecular weights of up to ~0.5 million, and the polymerization has many characteristics similar to those of living polymerizations. Polymerizations by the most powerful bases, especially organometallic compounds, are not as useful for polymerizations to such high molecular weights because of side reactions [Imanishi, 1984; Kricheldorf, 1989].

NCA polymerization by secondary amines may involve the amine or activated monomer mechanisms or both mechanisms simultaneously. Unhindered secondary amines such as dimethylamine and piperidine react like primary amines, and polymerization occurs by the amine mechanism. Polymerization by slightly hindered amines such as diethylamine, N-methylbenzylamine, and di-\(n\)-propylamine involves a combination of the amine and activated monomer mechanisms. More hindered secondary amines, such as di-\(n\)-isopropylamine and dicyclohexylamine, react almost exclusively via the activated monomer mechanism.

NCA polymerizations in aprotic solvents such as 1,4-dioxane and THF proceed with acceleration in rate at about 20–30% conversion where the propagating species have grown
to the hexamer to dodecamer size [Kim et al., 1979]. Since this is approximately the size at which \( \alpha \)-helical conformations become established for many poly(\( \alpha \)-amino acids), the auto-acceleration is generally attributed to a conformational enhancement of reactivity; the reacting species are bound to the \( \alpha \)-helix in a steric arrangement that enhances reactivity. Molecular weight broadening occurs under these conditions.

### 7-4b  Polymerization by Transition Metal Complexes

Various transition metal compounds have been studied to achieve better control of NCA polymerization [Deming, 2000; Deming and Curtin, 2000]. Covalent early transition metal alkoxides, amides, alkyls and other derivatives, such as \( \text{CpTiCl}_2\text{OR} \) (\( \text{Cp} = \text{cyclopentadienyl} \)), do not initiate NCA polymerization, contrary to the high reactivity of the corresponding ionic derivatives such as lithium alkoxide (Sec. 7-4a). However, late transition metal complexes, including various nickel and cobalt derivatives, initiate NCA polymerization with the level of control of molecular weight dependent on the structure of the initiator, especially its ligands. Zero-valence Ni and Co initiators such as \( \text{bpyNi(COD)} \) and \( [\text{P(CH}_3\text{)}_3\text{C}_13\text{Co (bpy = 2, 2'-bipyridyl, COD = 1, 5-cyclooctadiene)} \) are effective initiators for NCA polymerization. The reactions proceed as living polymerizations with good control over molecular weight. Molecular weights as high as 500,000 have been achieved with PDI <1.2.

A transition metal complex such as \( \text{bpyNi(COD)} \), generalized as \( \text{L}_2\text{Ni} \), reacts with NCA in a complex reaction sequence that generates a propagating species \( \text{XLV} \) whose active center is a 5-membered amido–amidate metallacyclic complex. Propagation involves a nucleophilic attack by the amido nitrogen of the amido–amide at the C-5 carbonyl of NCA. The

\[
\text{XLV} \quad \xrightarrow{\text{L}_2\text{Co}} \quad \text{XLVI}
\]

reaction forms the 10-membered intermediate \( \text{XLVI} \). The metallic center of the amido–amidate bonds (coordinates) with the carboxylate chain end, and this is largely responsible for molecular weight control and a lack of side reactions. The 10-membered intermediate contracts to the 5-membered amido–amidate by proton migration and loss of carbon dioxide. Molecular weight control is also attributed to the stability of the amido–amidate.
When polymerization is carried out in DMF the degree of polymerization is given by the monomer : initiator ratio as expected. However, polymerization in solvents less polar than DMF, such as THF, dioxane, toluene, and ethyl acetate, yields polymers with higher molecular weights than indicated by the monomer : initiator ratio [Deming and Curtin, 2000]. Higher molecular weights are also observed by altering the ligands bound to Ni or Co. The higher molecular weights are achieved while maintaining a narrow PDI. Solvent and ligand changes do not alter the propagation process, but do hinder the initiation process. This effectively increases the monomer : initiator ratio by decreasing the concentration of initiator species and results in the increased molecular weights.

7-5 LACTONES

Lactones (cyclic esters) undergo anionic and cationic polymerization to form polyesters (Eq. 7-75) [Duda and Penczek, 2001; Johns et al., 1984; Kubisa, 1996; Lundberg and Cox, 1969; Young et al., 1977]. The reactivity of different lactones generally follows the pattern for other cyclic monomers, except that the 5-membered lactone (γ-butyrolactone) does not generally polymerize (although low-molecular-weight oligomers and some copolymers with ε-caprolactone have been obtained) and the 6-membered δ-valerolactone polymerizes. The 3-membered lactone is not known or is too reactive to isolate. Polymerization of ε-caprolactone (also referred to as 2-oxepanone) is practiced commercially. Telechelic poly(ε-caprolactone), with hydroxyl end groups, is used in synthesizing polyurethane block copolymers. Poly(ε-caprolactone) is also blended with other polymers to improve stress crack resistance, dyeability, and adhesion.

7-5a Anionic Polymerization

A variety of anionic initiators, both ionic and covalent, have been used to polymerize lactones [Duda and Penczek, 2001; Jedlinski, 2002; Jerome and Teyssie, 1989; Penczek and Duda, 1993]. Much of the more recent activity involves the use of anionic covalent (coordination) initiators such as alkylmetal alkoxides and metal alkoxides such as R₂AlOR' and Al(OR)₃, metal carboxylates such as tin(II) 2-ethylhexanoate, metalloporpyrins (VI), and aluminoxanes such as oligomeric [Al(CH₃)O]ₙ [Biela et al., 2002; Duda et al., 1990; Endo et al., 1987a,b; Gross et al., 1988; Kricheldorf et al., 1990; Penczek et al., 2000a,b; Sugimotoa and Inoue, 1999].

Anionic polymerization proceeds by acyl–oxygen cleavage for almost all lactones, consistent with the mechanism for alkaline saponification of esters [Duda and Penczek, 2001; Hofman et al., 1985; Kricheldorf et al., 1988]. For example, initiation by methoxide ion proceeds as

\[
\text{CH}_3\text{O}^- + \text{O} \quad \text{R} \quad \rightarrow \quad \text{CH}_3\text{O}^-\text{CO} \quad \text{R} \quad \text{O}^- 
\]
with propagation as

\[
\text{CH}_3\text{O} \left( \text{CO} - \text{R} - \text{O} \right)_n\text{CO} - \text{R} - \text{O}^- + \text{O} - \text{R} \rightarrow \text{CH}_3\text{O} \left( \text{CO} - \text{R} - \text{O} \right)_{(n+1)}\text{CO} - \text{R} - \text{O}^- \quad (7-77)
\]

For coordination initiators, the metal coordinates with the carbonyl oxygen followed by insertion of an alkoxy (or other anionic fragment depending on the initiator) into the acyl–oxygen bond.

The experimental evidence for the acyl–oxygen cleavage mechanism comes from end-group analysis of the polymer. For example, the polymer produced by the sequence in Eqs. 7-76 and 7-77 possesses methyl ester and hydroxyl end groups after termination with water or other acidic terminating agent. If polymerization proceeded by alkyl–oxygen cleavage, the end groups would be different—methoxyl and COOH. NMR analysis of the polymer indicates that acyl–oxygen cleavage occurs. Additional support for acyl–oxygen cleavage comes from trapping experiments in which specific terminating agents are used to identify the propagating centers [Hofman et al., 1987a,b]. Polymerization of optically active lactones where the tetrahedral stereocenter (previously referred to as a chiral carbon) is attached to the alkyl oxygen are especially useful for detecting the mode of ring opening. Thus the polymerization of \(\beta\)-butyrolactone (XLVII) proceeds with retention of configuration, indicating acyl–oxygen cleavage (bond \(b\)) instead of alkyl–oxygen cleavage (bond \(a\)) [Le Borgne and Spassky, 1989]. Cleavage at the alkyl–oxygen bond would result in racemization instead of retention.

Control of the polymerization, specifically, achieving living polymerization conditions, is achieved by using the covalent initiators, especially the less active initiators. The polymerization rate is first-order in both monomer and initiator, \(X_n\) is given by the ratio of monomer to initiator, and narrow MWDs are obtained. The limiting factor in achieving high molecular weights is chain transfer to monomer, that is, \(\beta\)-proton abstraction from monomer. This is extensive for \(\beta\)-butyrolactone, limiting number-average molecular weights to about 20,000. This is not nearly as important for other monomers; for example, molecular weights higher than \(10^5\) have been achieved for \(\beta\)-propiolactone.

Chain transfer to polymer by transesterification is present and responsible for molecular weight broadening. Intramolecular transfer results in cyclic oligomers; intermolecular transfer results in scrambling of chain segments between different polymer chains. The extent of chain transfer to polymer as well as to monomer is greater for the more active (more ionic) initiators, for example, alkoxides of Na, Mg, and Zn instead of Al [Hofman et al., 1987a,b; Kricheldorf et al., 1988]. Rare-earth alkoxides (La, Y, Sm) strike a good balance with polymerization rates similar to ionic initiators, but with lowered side reactions similar to covalent initiators [Save and Soum, 2002; Save et al., 2002].
Tin(II) 2-ethylhexanoate is an important industrial initiator for cyclic ester polymerization [Duda and Penczek, 2001; Kricheldorf et al., 2001; Storey and Sherman, 2002]. Metal carboxylates are useful initiators only in the presence of alcohols. The polymerization rate is very slow in the absence of alcohol, less than 1% of the rate in the presence of alcohol. The actual initiator is the metal alkoxide formed by the reaction between metal carboxylate and alcohol.

Each alkoxide group in an alkylmetal alkoxides or metal alkoxide initiates growth of a polymer chain. Thus, one, two, and three propagating chains are generated per metal atom with $\text{R}_2\text{AlOR}$, $\text{Sn(OR)}_2$, and $\text{Al(OR)}_3$, respectively. However, fewer propagating chains per metal atom are observed under some conditions, for example, with aluminum isopropoxide, which aggregates to form trimers and tetramers. The trimers are very active in polymerization, ranging from $10^2$- to $10^5$-fold more active than the tetramers. Each aluminum atom (and its associated alkoxide groups) in the reaction system will not be active in polymerization unless the equilibrium exchange between trimer and tetramer is fast. The equilibrium is rapid at higher temperatures, at lower initiator concentrations, and in more polar solvents, and one observes the theoretical maximum stoichiometry between propagating chains and metal atoms. Under other conditions, less than the maximum stoichiometry is observed.

Aggregation phenomenon are also observed for the propagating chains, with an equilibrium between aggregated and unaggregated chains. This is the equivalent of a reversible deactivation between dormant and active propagating chains that preserves the livingness of the polymerization. In other living systems the reversible deactivation involves a different phenomenon. Cationic living polymerization of C=C monomers involves an equilibrium between covalent (dormant) and ionic (active) species. ATRP involves reversible formation of radicals from the reaction of an alkyl halide with a metal.

The presence of aggregated species results in fractional-order dependencies of initiation and propagation rates on initiator and propagating species (Sec. 5-3d-5).

Polymerization of $\beta$-propiolactone (also called 2-oxetanone) shows some interesting features due to the high strain in the 4-membered ring [Duda, 1992; Jerome and Teyssie, 1989]. Polymerization with the less nucleophilic initiators such as tertiary amines, metal carboxylates, and phosphines proceeds with ring opening at the alkyl–oxygen bond instead of the acyl–oxygen bond. Initiation by stronger nucleophiles occurs by acyl–oxygen as well as alkyl–oxygen cleavage to give a mixture of carboxyl and alkoxide propagating centers. However, the carboxylate centers are unable to propagate by cleavage of acyl–oxygen bonds while alkoxide propagating centers cleave both alkyl–oxygen and acyl–oxygen bonds. Alkoxide propagating centers convert to carboxylates with time, and carboxylate centers constitute more than 95% of all propagating centers after only several propagations.

Polymerization of $\beta$-propiolactone in a highly polar solvent (DMF) in the presence of a crown ether shows the unexpected feature that ion-pair reactivity decreases more slowly with decreasing temperature compared to free-ion reactivity [Penczek et al., 2000a,b; Slomkowski, 1986]. Solvation of free ions becomes so extensive at 20°C that they are less reactive than ion pairs.

7-5b Cationic Polymerization

Cationic polymerization of lactones is achieved with the range of initiators used for cyclic ethers (Sec. 7-2b) [Hofman et al., 1987a,b; Kricheldorf and Sumbel, 1988a,b; Kricheldorf et al., 1986, 1987a,b; Kubisa, 1996; Penczek and Slomkowski, 1989a,b]. Initiation was formerly thought to involve attack of a positive species on the endocyclic oxygen to form an
oxonium ion followed by propagation through acyl–oxygen cleavage. However, polymer end-group analysis combined with trapping of propagating centers by reaction with triphenylphosphine indicates that this is not the mechanism. Initiation involves attack of a positive center on the exocyclic oxygen (the more basic oxygen) to form a dioxocarbocation (XLVIII). For example, for initiation by methyl carbocation derived from \( \text{CH}_3\text{OSO}_2\text{CF}_3 \) or \( (\text{CH}_3)_2\text{I}^+\text{SbF}_6^- \)

\[
\begin{align*}
\text{CH}_3^+ + \text{O}=\text{C} & \text{C} = \text{O} \quad \rightarrow \quad \text{CH}_3\text{O} = \text{C} = \text{O} \\
\text{XLVIII}
\end{align*}
\]

Propagation follows in a similar manner with alkyl–oxygen cleavage

\[
\begin{align*}
\text{CH}_3\left\{\text{O}=\text{C} = \text{O} \right\}_n & \text{C} = \text{O} \quad + \quad \text{O}=\text{C} = \text{O} \quad \rightarrow \\
\text{CH}_3\left\{\text{O}=\text{C} = \text{O} \right\}_{(n+1)} & \text{C} = \text{O} \\
\end{align*}
\]

Cationic polymerization is not nearly as useful as anionic polymerization for synthesizing high-molecular-weight polyesters. The cationic route appears to be limited by intramolecular transesterification (cyclization) as well as other chain transfer to polymer reactions (including hydride and proton transfers) although there are few details in the literature. However, molecular weights in the 100,000 range have been observed for the highly reactive monomer \( \beta \)-propiolactone. The highly strained \( \beta \)-propiolactone undergoes a mixture of alkyl–oxygen and acyl–oxygen cleavages under some reaction conditions.

Cationic ROP of lactones in the presence of an alcohol proceeds by an activated monomer mechanism similar to that for cyclic ethers (Sec. 7-2b-3-b) [Endo et al., 2002; Lou et al., 2002]. Propagation proceeds by nucleophilic attack of the hydroxyl end group of a propagating chain on protonated (activated) monomer:

\[
\begin{align*}
\text{OH} + \quad \text{O} \quad \rightarrow & \quad \text{OCCH}_2\text{CH}_2\text{OH} \\
\end{align*}
\]

AM polymerization offers the potential for suppressing side reactions and achieving living polymerization with the ability to control MW and achieve high molecular weights.

**7-5c Enzymatic Polymerization**

Lipases catalyze the polymerization of lactones [Duda et al., 2002; Gross et al., 2001; Kobayashi, 1999; Kobayashi et al., 2001]. The reaction mechanism is similar to that for the enzymatic polymerization of hydroxyacids (Sec. 2-17a-2). Lipase reacts with lactone to produce enzyme-activated hydroxyacid and some of the latter reacts with water to produce hydroxyacid (Eqs. 7-81). Hydroxyacid and enzyme-activated hydroxyacid react to initiate polymerization (Eq. 7-82). Propagation proceeds by nucleophilic attack of
the hydroxyl end group of the propagating chain on the enzyme-activated hydroxyacid (Eq. 7-83a).

\[
\begin{align*}
\text{R-C-O} & \quad + \quad \text{lipase-OH} \quad \rightarrow \quad \text{HO-R-C-O-lipase} \quad \rightarrow \quad \text{HO-R-C-OH} \\
\text{HO-R-C-O-lipase} & \quad + \quad \text{HO-R-C-OH} \quad \rightarrow \quad \text{HO-R-C-O-R-C-OH}
\end{align*}
\]

(7-81)

(7-82)

(7-83a)

(7-83b)

7-5d Other Cyclic Esters

Polymerization and copolymerization of the two 1,4-dioxane-2,5-diones (dilactones), glycolide and lactide (XLIX with R = H and CH₃, respectively) proceeds using anionic initiators; cationic initiators are not as useful [Bero et al., 1990; Chamberlain et al., 2001; Chisholm et al., 2001; Kowalski et al., 1998; Kricheldorf and Kreiser-Saunders, 1990; Kricheldorf et al., 1987a,b, 2000; Leenslag and Pennings, 1987; Shibasaki et al., 2000; Stridsberg et al., 2000]. The polymerization rates are generally lower than those for lactones. Polylactide is of interest because it is both biocompatible and biodegradable. It has been used for absorbable sutures and has the potential for other biomedical applications such as drug delivery.

Polymerization of a cyclic carbonate ester yields a linear polycarbonate [Kuhling et al., 1989; Rokicki, 2000]. For example, the cyclic oligomer (m = 2–20 in Eq. 7-85) of the

\[
\begin{align*}
\text{R-CO} & \quad \rightarrow \quad \left\{ \text{O-CHR-CO} \right\}_m \\
\text{XLIX}
\end{align*}
\]

(7-84)
carbonate derived from bisphenol A, 2,2'-bis(4-hydroxyphenyl)propane, offers an alternate route to polycarbonates other than step polymerization of bisphenol A with phosgene or ester interchange with diphenyl carbonate (Sec. 2-8e) [Brunelle et al., 1989; Stewart, 1989].

The ROP route to polycarbonates offers potential advantages relative to the step polymerization process. One advantage is that higher MW can be more easily achieved. ROP, especially with anionic initiators, proceeds as a living system and MW is determined by conversion and the ratio of monomer to initiator. MW control in step polymerization is dependent on stoichiometric ratio and conversion. Molecular weights as high as 100,000–300,000 are reported for the ROP, while the highest MWs achieved by step polymerization are 40,000–60,000. It is more difficult to achieve the very high conversions needed in step polymerization to reach the $10^5$-MW range than to control the monomer–initiator ratio in ROP. Another advantage of the ROP process is the absence of by-products, which allows the use of reactive processing techniques in which cyclic monomer is directly polymerized into final objects by extrusion or molding. ROP as an alternate to step polymerization is also being studied for other high-performance polymers such as polyesters, polyamides, and polyetherimides. The ROP route is viable when the cyclic oligomer can be synthesized and polymerized in high yield.

### 7-6 NITROGEN HETEROCYCLICS

#### 7-6a Cyclic Amines

Cyclic amines (referred to as *imines*) are polymerized by acids and other cationic initiators [Goethals, 1984, 1989a,b; Hauser, 1969; Kubisa, 1996; Tomalia and Killat, 1985]. The 3-membered imines (IUPAC: aziridines) are the most studied of the cyclic amines. Polyethyleneimine (IUPAC name: poly(iminoethylene)) had been commercially available and used in the treatment of paper and textiles. It is no longer available in the United States because of the high toxicity of the monomer.

The high degree of ring strain results in an extremely rapid polymerization for ethyleneimine. Initiation involves protonation or cationation of ethyleneimine followed by nucleophilic attack by monomer on the iminium $\text{C}^+/\text{C}_0^-$ bond. Propagation follows in the same manner. The propagating species is an iminium ion, and the reaction is analogous to the cationic polymerization of cyclic ethers. Extensive branching occurs during polymerization as evidenced by the presence of primary, secondary, and tertiary amine groups in the approximate ratio $1:2:1$. Tertiary amine groups result from intermolecular nucleophilic attack of secondary amine nitrogens in polymer repeat units on iminium propagating centers. This reaction simultaneously increases the primary amine group content of a polymer chain. The detailed mechanism is quite complicated since there are many equilibria present involving proton transfers among the different types of amine groups present.
Polyethyleneimine is also extensively cyclized as a result of intramolecular nucleophilic attack of primary and secondary amines on the iminium group. This results in cyclic oligomer as well as polymer molecules containing large-sized rings as part of their structure.

Substitution on the aziridine ring hinders polymerization [Baklouti et al., 1989; Van de Velde, 1986]. The 1,2- and 2,3-disubstituted aziridines do not polymerize; 1-and 2-substituted aziridines undergo polymerization, but the yield of polymer relative to low-molecular-weight linear and cyclic oligomers and the molecular weight of the polymer depend on the substituent (both electronic and steric effects are important).

Cationic polymerization of 4-membered imines (IUPAC: azetidines) generally follows the same patterns as the aziridines [Matyjaszewski, 1984a,b; Muhlbach and Schulz, 1988]. Imines are generally unreactive toward anionic polymerization presumably because of the instability of an amine anion (which would constitute the propagating species). The exception occurs with \( N \)-acylaziridines as a result of the electron deficiency of the nitrogen coupled with the highly strained 3-membered ring.

7-6b Other Nitrogen Heterocyclics

Various endo-imino cyclic ethers (\( L \)) undergo cationic polymerization to yield poly(\( N \)-acrylalkyleneimine)s (\( LI \)). The most widely studied monomers are the 2-substituted 2-oxazolines (\( m = 2 \)) (also referred to as 2-substituted-1,3-oxazolin-2-enes) [Culbertson, 2002; Goethals, 1989a,b; Kobayashi and Saegusa, 1984, 1986; Kobayashi and Uyama, 2002; Kobayashi et al., 1990a,b; Kubisa, 1996; Tomalia and Killat, 1985]. Propagation proceeds via nucleophilic attack of monomer on the \( C-O \) bond of an oxazolinium ion:

\[
\begin{align*}
\text{LI} & \text{ hydrolysis} \\
\text{LII}
\end{align*}
\]

\( LI \) can be hydrolyzed to the corresponding polyamine \( LII \). This is the only route to linear polyethyleneimine (\( m = 2 \)) [Tanaka et al., 1983]. The polymerization of ethyleneimine yields a highly branched and cyclized product.

\( \text{exo} \)-Imino cyclic compounds (\( LIII \)) such as iminocarbonates (\( Y = O \)), 2-imino-1,3-oxazolidines (\( Y = NR \)), and 2-iminotetrahydrofurans (\( Y = CH_2 \)) have also been polymerized:

\[
\begin{align*}
\text{LIII} & \text{ } \\
\text{LIV} & \text{ heating} \\
\text{LVII}
\end{align*}
\]

An alternate approach to forming polymers by ring opening of 2-oxazolines involves the 2-mercaptoalkyl-2-oxazoline \( LIV \), which polymerizes to \( LVII \) on heating [Gunatillake
et al., 1987] (Eq. 7-91). The reaction occurs through the zwitterion intermediate LV formed by proton transfer from sulfur to nitrogen. This reaction is a step polymerization of the zwitterion (an AB reactant). The zwitterion reacts with itself through nucleophilic attack of $S^-$ on the oxazolinium ring to break the C–O bond and form a propagating zwitterion (LVI). Propagation continues in the same way to form the polymer LVII. 2-Carboxyalkyl-2-oxazolines polymerize in a similar manner with nucleophilic attack of carboxylate anion on the oxazolinium ring [Gunatillake et al., 1988].

7-7 SULFUR HETEROCYCLICS

The 3- and 4-membered cyclic sulfides, referred to as thiiranes (also episulfides) and thietanes, respectively, are easily polymerized by both cationic and anionic initiators, such as

$$\begin{align*}
\text{S} & \rightarrow \{\text{SCH}_2\text{CH}_2\}_n
\end{align*}$$

(7-92)

the polymerization of ethylene sulfide to poly(ethylene sulfide) [IUPAC: poly(sulfanediylethylene)] [Aida et al., 1990; Boileau, 1989; Boucard et al., 2001; Goethals, 1989a,b; Kubisa, 1996; Sigwalt and Spassky, 1984]. Polymerization is more facile than with the corresponding cyclic ethers because of the more polarizable carbon–sulfur bond. This also explains the polymerization of the thietanes by anionic initiators. However, cyclic sulfides are less strained than their oxygen analogs because of the larger size of the sulfur atom, and the 5-membered ring tholane (tetrahydrothiophene), unlike tetrahydrofuran, does not undergo polymerization. There are no reported polymerizations of larger-sized cyclic sulfides. By analogy to the cyclic ethers, the propagating species in cyclic sulfide polymerization are considered to be the cyclic sulfonium (LVIII) and sulfide anion (LIX) for cationic and anionic polymerization, respectively.

$$\begin{align*}
\sim\text{SCH}_2\text{CH}_2\vdash & \rightarrow \sim\text{CH}_2\text{CH}_2\text{SCH}_2\text{CH}_2\text{S}^-
\end{align*}$$

LVIII LIX
Although there are no reported polymerizations of simple cyclic sulfides of ring size 5 and higher, polymerizations of 1,3,5-trithane (the cyclic trimer of thioformaldehyde) (LX), disulfides such as 1-oxa-4,5-dithiacycloheptane (LXI), and trisulfides such as norbonene trisulfide (LXII) have been achieved [Andrzejewski et al., 1988; Baran et al., 1984; Moore et al., 1977; Zuk and Jeczalik, 1979].

The polymerization of LXIII, a stable isolable zwitterion, on heating or photolysis involves nucleophilic attack by phenoxide anion on the cyclic sulfonium ring [Hoyle et al., 2001; Odian et al., 1990]. The reaction proceeds as a step polymerization.

\[
\text{LXIII} \rightarrow \left\{ \text{CH}_2\text{S}_{4} \right\}_n \quad (7-93)
\]

### 7-8 CYCLOALKENES

Cycloalkenes undergo ring-opening polymerization in the presence of coordination initiators based on transition metals to yield polymers containing a double bond, for instance, cyclopentene yields polypentenamer [IUPAC: poly(pent-1-ene-1,5-diyi)] [Amass, 1989; Cazalis et al., 2000, 2002a,b; Claverie and Soula, 2003; Doherty et al., 1986; Ivin, 1984, 1987; Ivin and Mol, 1997; Ofstead, 1988; Schrock, 1990, 1994; Trnka and Grubbs, 2001]. The polymerization is referred to as ring-opening metathesis polymerization (ROMP) by analogy to the olefin metathesis reaction, which results in a transalkylidenation between two alkenes:

\[
\text{RCH=CHR} + \text{R'C=CHR'} \rightarrow 2\text{RCH'C=CHR'} \quad (7-95)
\]

Both olefin metathesis and ROMP require similar initiators and proceed by the same reaction mechanism. The initiating and propagating species are metal–alkylidene (carbene) complexes. The original initiators used for ROMP were two-component systems, composed of a halide or oxide of an early transition metal such as W, Mo Rh, or Ru with an alkylating agent (Lewis acid) such as R₄Sn or RAlCl₂, which generate metal–carbenes in situ. These initiator
systems have limitations—the strong Lewis acids make MW control more difficult, there is incompatibility with a variety of functional groups, the actual metal–carbene initiators are formed in low concentrations, and temperatures of 100°C are needed. Since these initiators are relatively inexpensive, they still find use in commercial applications.

Better control of the reaction is achieved by using stable, isolable metal–carbene complexes, such as the Schrock initiators based on molybdenum and tungsten (LXIV, Mt = W, Mo) and the Grubbs initiators based on ruthenium (LXV). The Schrock initiators are limited compared to the Grubbs initiators, because of their sensitivity to air and moisture and their intolerance of monomers with oxygen-containing functional groups such as carboxyl, carboxyl, and hydroxyl. The Grubbs initiators are relatively tolerant to a variety of functional groups and reaction conditions. There has been and still is considerable effort in fine-tuning the initiator by variations in the ligands attached to the metal to allow one to achieve good polymerization rates with control of side reactions. For example, the activity of the Grubbs initiators increases with larger and more electron-donating phosphines, but decreases with larger and more electron-donating halides, and these trends have been rationalized in terms of the ROMP mechanism [Trnka and Grubbs, 2001]. ROMP proceeds as a living polymerization for most of the metal–carbene initiators. Narrow MWD and block copolymers can be obtained. Only modest temperatures of 25–50°C are required with the Schrock and Grubbs initiators.

Initiation involves coordination of the double bond of monomer with the transition metal (imino and OR’ ligands not shown), cleavage of the π-bond with formation of a 4-membered metallocyclobutane intermediate, followed by rearrangement to form a metal–carbene propagating center:

\[
\begin{align*}
\text{RCH=Cl} & \quad \text{RCH=Cl} \\
\text{OR}’ & \quad \text{PR}_3
\end{align*}
\]

(7-96)

Propagation follows in a similar manner (Eq. 7-97), and the overall result is the insertion of the halves of the double bond of monomer into the metal–carbene bond. Evidence for cleavage of the double bond instead of an adjacent single bond comes from analysis of the ozonolysis products from a copolymer of cyclooctene and 1-14C-cyclopentene. The metal–carbene propagating centers can be terminated by conversion to double bonds by a Wittig-type reaction with an aldehyde. The final polymer has terminal double bonds at both chain ends as well as a double bond in the repeat unit.

Aside from cyclohexene, which yields only very-low-MW oligomers, a wide range of cycloalkene and bicycloalkenes have been polymerized to high-MW products. There are

\[
\begin{align*}
\text{RCH=Cl} & \quad \text{RCH=Cl} \\
\text{OR}’ & \quad \text{PR}_3
\end{align*}
\]

(7-97)
several commercial applications of ROMP [Feast, 1989; Janiak and Lassahn, 2001; Ofstead, 1988; Streck, 1989]. Polymerization of cis-cyclooctene yields a polymer [IUPAC: poly (oct-1-ene-1,8-diyl)] (trade name: Vestenamer) used as the minor component in elastomer blends with SBR and natural rubbers for gaskets, brake hoses, and printing rollers. Polynorbornene (LXVI) [IUPAC: poly(cyclopentane-1,3-diyethene-1,2-diyl] (trade name: Norsorex), synthesized from norbornene (bicyclo[2.2.1]hept-2-ene) is a specialty rubber that can absorb up to several times its own weight of plasticizer oil and still retain useful properties. It has high tear strength and high dynamic damping properties and finds applications in noise control (e.g., under the hoods of diesel-powered automobiles) and vibration damping (automobile-body mounts and instrument isolation pads). It has also been used for cleaning up oil spills. Polymerization of endo-dicyclopentadiene yields a commercial plastic (trade name: Metton). Polymerization initially yields LXVII, but subsequent ROP through the pendant cyclopentene ring results in crosslinking. Polymerization and crosslinking occur in the same process,

\[
\text{LXVI} \quad (7-98a)
\]

\[
\text{LXVII} \quad (7-98b)
\]

and this is useful for producing large-sized articles such as satellite antenna dishes, snowmobile bodies, and automobile-body parts by reaction injection molding.

ROMP is generally an irreversible process, and relief of ring strain is the driving force for the forward reaction. Reversibility (with the formation of macrocyclic oligomers) is possible for less strained cycloalkenes like cyclooctene when the lifetimes for propagating chains are high.

Polymerization of cycloalkenes through the double bond without ring opening occurs when initiators other than the ROMP initiators are used, including initiators based on various early transition (Ti, Zr, Hf, V), late transition (Pd, Ni), central transition (Cr, Co), and rare-earth (Ln) metals [Janiak and Lassahn, 2001]. This mode of polymerization is discussed in Secs. 8-1f and 8-6a.

Other ROMPs include the polymerizations of 1,3,5,7-cyclooctatetraene and cyclooctyne:

\[
\text{1,3,5,7-cyclooctatetraene} \quad (7-99a)
\]

\[
\text{cyclooctyne} \quad (7-99b)
\]
Polymerization of cis-cyclooctene with the cyclic ruthenium initiator LXVIII produces cyclopolyoctenamer LXIX as the monomer undergoes ring opening and insertion into the ruthenium–carbene bond of the initiator [Bielawski et al., 2002]. Unlike most ROMPs with initiators that produce linear polymers, polymerization with the cyclic initiator LXVIII is a reversible reaction. The result is intramolecular backbiting transfer, which yields the cyclopolymer with regeneration of the initiator. Although the propagating chain is nonliving, the initiator remains intact, and each initiator molecule produces many cyclopolymer molecules. MW is ultimately limited by the transfer reaction, but also depends on the concentrations of initiator and monomer. Higher monomer concentrations and monomer : initiator ratios yield higher molecular weights. Polymer number-average molecular weights as high as one million have been achieved. The polydispersity index is close to 2.0, as it is in chain polymerizations dominated by chain transfer (Sec. 3-11a). The cyclic polymer was hydrogenated to cyclic polyethylene and its properties compared to linear polyethylene—some differences were observed.

Acyclic diene metathesis polymerization (ADMET) is a related polymerization in which an unconjugated diene polymerizes with loss of ethene [Lehman and Wagener, 2002, 2003; Schwendeman et al., 2002]. ADMET is carried out using the Schrock and Grubbs initiators at about 40–80°C. The process is a step polymerization, not a ROP chain reaction. The reaction is reversible, and high polymer MW is achieved by removal of ethene (usually by reduced pressure) to drive the system to high conversion. Number-average molecular weights close to 100,000 have been achieved in some systems.

 Spiroorthocarbonates and spiroorthoesters have four and three oxygens, respectively, connected to the spiro carbon (the carbon common to two rings). Polymerizations of spiroorthocarbonates and spiroorthoesters proceed with either no volume shrinkage or an expansion in volume due to the opening of two or more rings. All other ROPs as well as other chain and step polymerizations proceed with volume shrinkage. Polymerizations without volume shrinkage, and especially those with volume expansion, are of interest for applications such as high-strength adhesives, dental fillings, and prestressed castings [Moszner and Salz, 2001].

 Spiroorthocarbonates and spiroorthoesters are stable toward bases and nucleophiles but easily undergo cationic ROP. Cationic ROP of a spiroorthocarbonate (LXX) proceeds by initial formation of carbocation LXXI in which the carbocation center is stabilized by...
interaction with three adjacent oxygens. Depending on ring size and the identity of substitu-
ents on the ring, LXXI propagates by cleavage at bonds a, b, and c to yield polymers LXXII, 
LXXIII, and LXXIV, respectively [Bailey and Endo, 1978; Kubisa, 1996; Rokicki, 2000; 

\[
\text{LXX} \quad \xrightarrow{\text{a}} \quad \text{LXXI} \\
\text{LXXII} \quad \xrightarrow{\text{b}} \quad \text{LXXIII} \\
\text{LXXIV} \quad \xrightarrow{\text{c}} \quad \text{LXXV}
\]

(7-101)

Takata and Endo, 1988]. A cyclic carbonate and cyclic ether are eliminated as by-products 
in reaction pathways a and b, respectively. Polymer LXXIV contains both ether and carbo-
nate functional groups in the polymer chain.

Various spiroorthoesters also undergo cationic polymerization, for example, 1,4,6-triox-
aspiro[4.4]nonane (LXXV) yields a polymer containing both ether and ester groups in the 
polymer chain [Bailey, 1975; Matyjaszewski, 1984 a,b].

\[
\text{LXXV} \quad \xrightarrow{\text{R}} \quad \left\{\text{OCH}_2\text{CH}_2-\text{O}-\text{CO}-\text{CH}_2\text{CH}_2\text{CH}_2\right\}_n
\]

(7-102)

The polymerization of spiroorthoesters or spiroorthocarbonates that contain a pendant 
carbon–carbon double bond have been studied. The behavior of such monomers is essentially 
the sum of the behaviors of the ring and C=C. For example, a compound similar to LXX that 
also contains a pendant double bond undergoes radical polymerization through the double 
bond and cationic ROP [Endo et al., 1987a,b; Herweh, 1989]. Further, crosslinked polymers 
are obtained by sequential radical and cationic ROP. An unexpected result is the radical poly-
merization of 4-phenyl-2-methylene-1,3-dioxepane (LXXVI), a cyclic ketene acetal [Bailey, 
1985; Bailey et al., 1988; Endo et al., 1985; Sanda and Endo, 2001]. Radical polymerization 
results in a concerted reaction involving both the C=C and ring opening. The initially formed 
radical LXXVII undergoes ring opening to form the benzyl radical, which subsequently 
propagates in the same manner to form a polyester. This is one of the very few ring-opening
polymerizations proceeding via a radical process. The extent of ring opening is dependent on the presence of a ring substituent such as phenyl to stabilize the radical formed on ring opening and on the extent of strain in the ring structure. Varying degrees of ring-opening polymerization with radical initiators have been observed with methylene spiro orthocarbonates and orthoesters [Endo and Bailey, 1975, 1980; Pan et al., 1988; Sanda and Endo, 2001; Tagoshi and Endo, 1989].

7-10 OTHER RING-OPENING POLYMERIZATIONS

There is considerable literature on efforts to polymerize cycloalkanes [Hall and Snow, 1984]. With very few exceptions, ring-opening polymerization by cleavage of σ-σ bonds does not occur or produces very-low-molecular-weight products. The few exceptions to this generalization involve monomers that possess some structural feature conducive to ring-opening reaction. Many vinylcyclopropane derivatives (LXXVIII) undergo a radical 1,5-polymerization. Radical addition occurs initially at the double bond to form radical LXXIX followed by ring opening to radical LXXX. High-MW polymers are obtained only when R1 and/or R2 are substituents such as COOR or CN, which stabilize radicals [Cho, 2000; Endo and Suga, 1989; Endo et al., 1989; Sanda and Endo, 2001]. Vinylicyclopropanes undergo polymerization exclusively through the double bond with cationic and Ziegler–Natta (Chap. 8) initiators. Anionic polymerization of cyclopropanes with electron-withdrawing substituents proceeds exclusively through ring opening [Penelle and Xie, 2000].

The polymerization of a variety of other monomers, such as vinyloxiranes, vinyllactones, dihydrofurans, and bicyclobutanes, have been studied [Cho, 2000].

Kricheldorf and coworkers have found that some heterocyclic compounds containing two reactive bonds behave as bifunctional reactants in a ROP that proceeds by a step polymerization mechanism [Kricheldorf, 2000]. An example is the polymerization of 2,2-dibutyl-2-stanna-1,3-dioxepeane with an aliphatic diacid chloride:

\[ \text{Bu}_2\text{Sn} \left(\text{CH}_2\right)_4 \text{O} + \text{CICO} \text{R} \text{COCl} \rightarrow \text{Bu}_2\text{SnCl}_2 \left[ \text{O} \left(\text{CH}_2\right)_4 \text{OCO} \text{R} \text{CO} \right]_n \] (7-105)
The surprising aspect of this polymerization is that the polymer product is cyclic with number-average molecular weight above 10,000.

### 7-11 INORGANIC AND PARTIALLY INORGANIC POLYMERS

As noted in Sec. 2-15, there has been considerable interest in the synthesis of inorganic and partially inorganic polymers. Some of the polymers have been synthesized by ROP.

#### 7-11a Cyclosiloxanes

The commercial importance of polysiloxanes (silicone polymers) was discussed in Sec. 2-12f. The higher-MW polysiloxanes are synthesized by anionic or cationic polymerizations of cyclic siloxanes [Bostick, 1969; Kendrick et al., 1989; Noll, 1968; Saam, 1989; Wright, 1984]. The most commonly encountered polymerizations are those of the cyclic trimers and tetramers, for example, for octamethylcyclotetrasiloxane

\[
\text{Si} = \text{O} = \text{Si} = \text{Si} = \text{O} = \text{Si} = \text{Si} = \text{O} = \text{Si} = \text{O} \\
\text{CH}_{3} \quad \text{CH}_{3} \quad \text{CH}_{3} \quad \text{CH}_{3} \quad \text{CH}_{3} \quad \text{CH}_{3} \quad \text{CH}_{3} \quad \text{CH}_{3}
\]

The polymer is commonly referred to as poly(dimethylsiloxane), but the IUPAC name is either poly(oxydimethylsilanediyl) or catena-poly[[(diphenylsilicon)-\(\mu\)-oxo] depending on whether one uses the nomenclature rules for organic or inorganic polymers. The prefix catena refers to a linear polymer, not branched or crosslinked.

The anionic polymerization of cyclic siloxanes can be initiated by alkali metal hydroxides, alkyls, and alkoxides, silanolates such as potassium trimethylsilanoate, \((\text{CH}_{3})_{3}\text{SiOK}\), and other bases. Both initiation

\[
\text{A}^{-} + \text{SiR}_{2} = \text{OSiR}_{2} \quad \rightarrow \quad \text{A}^{+} \text{SiR}_{2} \text{O}_{2} \text{SiR}_{2} \text{O}^{-}
\]

and propagation

\[
\text{\(\text{SiR}_{2} \text{O}^{-}\)} + \text{SiR}_{2} = \text{OSiR}_{2} \quad \rightarrow \quad \text{\(\text{SiR}_{2} \text{O}_{2}\)}_{3} \text{SiR}_{2} \text{O}^{-}
\]

involve a nucleophilic attack on monomer analogous to the anionic polymerization of epoxides [Mazurek and Chojnowski, 1977; Mazurek et al., 1980].

An interesting aspect of this polymerization is that \(\Delta H\) is nearly zero and, amazingly, \(\Delta S\) is positive by 6.7 \(\text{J mol}^{-1} \text{K}^{-1}\) [Lee and Johannson, 1966, 1976]. The driving force in this polymerization is the increase in entropy (disorder) on polymerization. A positive value of
ΔS is very rare for a polymerization process. The only other reported instances of positive ΔS values are those for the polymerizations of the cyclic octamers of sulfur and selenium and cyclic carbonate oligomers (Sec. 7-5c) [Brunelle et al., 1989]. All other polymerizations involve a decrease in entropy because of the decreased disorder for a polymer relative to its monomer. The positive ΔS values for the cyclic siloxane, S, and Se probably result from the high degree of flexibility of the linear polymer chains due to the large-sized atoms that they contain. This flexibility leads to greater degrees of freedom in the linear polymer compared to the cyclic monomer.

Cationic polymerization has been initiated by a variety of protonic and Lewis acids [Kubisa, 1996; Toskas et al., 2001]. The cationic process is more complicated and less understood than the anionic process. Polymerization under most reaction conditions involves the presence of a step polymerization simultaneously with ROP. This appears to be the only way to reconcile the observed (complicated) kinetics for the overall process [Chojnowski and Wilczek, 1979; Chojnowski et al., 2002; Cypryk et al., 1993; Rubinsztain et al., 1993; Sigwalt, 1987; Wilczek et al., 1986].

Initiation consists of protonation of monomer followed by subsequent reaction with monomer to form the tertiary oxonium ion LXXXI (Eq. 7-109). Propagation for the ring-opening chain polymerization follows in the same manner with nucleophilic attack of monomer on the tertiary oxonium ion (Eq. 7-110). (This is analogous to the cationic polymerization of cyclic ethers; see Eq. 7-20.)

\[
\text{Initiation: } \text{HOSiR}_2 \text{OSiR}_2 \text{OSiR}_2 \text{OSiR}_2 \rightarrow \text{SiR}_2 \text{OSiR}_2 \text{OSiR}_2 \text{OSiR}_2 \rightarrow \text{SiR}_2 \text{OSiR}_2 \text{OSiR}_2 \text{OSiR}_2 \quad \text{monomer}
\]

\[
\text{Propagation: } \text{OSiR}_2 \text{OSiR}_2 \text{OSiR}_2 \text{OSiR}_2 \rightarrow \text{SiR}_2 \text{OSiR}_2 \text{OSiR}_2 \text{OSiR}_2 \rightarrow \text{SiR}_2 \text{OSiR}_2 \text{OSiR}_2 \text{OSiR}_2 \quad \text{monomer}
\]

LXXXI

The silicenium ion (LXXXII) has been proposed as an alternative to the oxonium ion as the propagating center [Sigwalt and Stannett, 1990].
The products of most anionic and cationic polymerizations contain as much as 10–20% cyclic oligomers, mostly tetramer to hexamer.

7-11b Cyclotriphosphazenes

Thermal polymerization of hexachlorocyclotriphosphazene (LXXXIII) (also referred to as phosphonitrilic chloride) yields poly(dichlorophosphazene) (LXXXIV) (IUPAC: poly[nitrilo (dichloro-κ5-phosphanetriyl)] or catena-poly[(dichlorophosphorus)-μ-nitrido]) [Allcock, 1976, 1986, 2002; Allcock and Connolly, 1985; Archer, 2001; De Jaeger and Gleria, 1998; Liu and Stannett, 1990; Majumdar et al., 1989, 1990; Manners, 1996; Potts et al., 1989; Scopelianos and Allcock, 1987; Sennett et al., 1986].

\[
\text{Cl}_2\text{P} = \text{N}_2 \quad \text{Cl}_2\text{P} = \text{N} = \text{P} = \text{Cl}_2 \quad \text{Cl}_2\text{P} = \text{N} = \text{P} = \text{Cl}_2
\]

Although poly(dichlorophosphazene) is a hydrolytically unstable elastomer, it can be converted to stable alkoxy and amino derivatives by nucleophilic substitution reactions with RONa (R can be aliphatic or aromatic) and amines (1° or 2°) (Eqs. 7-111, 7-112). The polyphosphazene backbone has a high inherent flexibility (the glass transition temperature \(T_g\) is \(-60\) to \(-100^\circ\text{C}\)) combined with photolytic, oxidative, and solvent resistance. A wide range of properties can be imparted to the polymer by varying the organic moiety. Most poly(organophosphazene)s are elastomers, and, indeed, the first commercial specialty application involves the use of fluorinated alkoxy derivatives as high-performance elastomers in O-rings, pipelines, and seals used in oil and fuel delivery and storage systems in the aerospace industry. Some of the derivatives are microcrystalline (due to the R groups) and form flexible films and fibers. The incorporation of CH\(_3\)NH or glucose units as side groups imparts water solubility. Many of the derivatives are biocompatible, some are biodegradable, and others are bioactive and are being studied for medical applications (e.g., drug delivery). Some poly(organophosphazene)s have potential as solid electrolytes for lightweight rechargeable batteries.

Polymerization of hexachlorocyclotriphosphazene is typically carried out as a melt polymerization at 220–250°C. Conversions must be limited to about 70% to prevent branching and crosslinking since the crosslinked product is insoluble and cannot be derivatized. High yields of soluble polymer require purified monomer, but exceptionally pure and dry monomer shows very low reactivity except in polymerizations initiated by ionizing radiation. Various Lewis acids (BCl\(_3\) is the most studied) show a significant catalytic effect and allow higher conversions, without crosslinking, to be achieved at lower reaction temperatures (150–210°C). Polymerization in inert solvents such as chlorinated aromatics and carbon disulfide is also useful for this purpose.

A main feature of the melt polymerization is the sharp increase in electrical conductivity at temperatures (\(>220^\circ\text{C}\)) where polymerization occurs. This observation together with those described above support a cationic polymerization mechanism based on ionization of a P–Cl bond (Eq. 7-113) followed by electrophilic attack of \(\text{P}^+\) on monomer (Eq. 7-114). Boron
trichloride and trace amounts of water accelerate the polymerization by facilitating ionization of the P–Cl bond. Other reaction characteristics further support the mechanism. The inability of cyclotriphosphazenes without any halogens (e.g., hexamethylenecyclotriphosphazene or hexamethylaminocyclotriphosphazene) to polymerize is ascribed to the absence of an easily ionizable bond to phosphorus. However, polymerization is possible for partially substituted chlorocyclotriphosphazenes, although the reaction is less efficient than that for the fully halogenated monomer.

Many mechanistic features of (NPCl\textsubscript{2})\textsubscript{3} polymerization are unclear. Termination may involve reaction of propagating centers with PCl\textsubscript{5} (which is used in monomer preparation and may be present as a trace impurity) or other Lewis acid (including water) present as a catalyst. The branching and crosslinking that can occur during polymerization are increased by the presence of water concentrations above \(\sim 0.1\%\), although the water also acts as a retarder. Below the 0.1\% level water accelerates the polymerization rate. This is reminiscent of the effect of water in many cationic polymerizations of alkenes (Sec. 5-2a-2).

Alkyl and aryl derivatives of poly(dichlorophosphazene) are not efficiently synthesized by nucleophilic reaction of LXXXIV with metal alkyls or aryls. The halogen substitution reaction occurs but is accompanied by polymer chain cleavage. Use of poly(difluorophosphazene) or introduction of aryl and alkyl groups at the monomer stage offer some improvement, but neither method is fully satisfactory. The best route to alkyl and aryl derivatives is polymerization of \(N\)-(trimethylsilyl)-\(P,P,P\)-trichlorophosphoranimine at moderate temperatures (25–60°C) in the presence of a Lewis acid [Allcock et al., 1996, 2000, 2001a,b; Neilson and Wisian-Neilson, 1988]. The reaction proceeds as a cationic chain polymerization:

\[
\begin{align*}
\text{Cl} & \quad \text{NPCl}_{2}^{+} \quad \text{NPCl}_{2}^{-} \\
\text{R} & \quad \text{NPCl}_{2}^{+} \quad \text{PCl}_{6}^{-} \\
\end{align*}
\]

The phosphoranimine route also allows an alternate route to poly(dichlorophosphazene) by using \(N\)-(trimethylsilyl)-\(P,P,P\)-trichlorophosphoranimine as the monomer. The phosphoranimine route not only efficiently produces alkyl and aryl poly(phosphazene)s but also offers
other potential benefits compared to the ROP route from hexachlorocyclotriphosphazene [Allcock et al., 2001a,b]. The ROP route produces high-molecular-weight polymers (up to $10^5$–$10^6$), but the molecular weights are not easily controlled and the molecular weight distributions are broad (usually bimodal). The phosphoranimine reaction has some characteristics of a living polymerization. Polymers with narrower MWD with molecular weights as high as $10^5$ have been obtained.

The polymerizations of other cyclic phosphazenes have also been studied, including carbophosphazene, thiophosphazene, and thionylphosphazene [De Jaeger and Gleria, 1998; McWilliams et al., 2000]

\[
\begin{align*}
\text{Carbophosphazene} & \quad \text{Thiophosphazene} & \quad \text{Thionylphosphazene}
\end{align*}
\]

**7-11c Metallocenophanes**

The silicon-bridged [1]ferrocenophane **LXXXV** undergoes polymerization at 120–150°C to yield polymers of number-average molecular weights up to $10^5$ with PDI $\sim$1.5–2.5

\[
\text{LXXXV}
\]

[Manners, 2002]. Anionic polymerization proceeds under milder conditions (25°C) with good MW control (PDI <1.2) [Kulbaba and Manners, 2001; Ni et al., 1996]. A variety of other metallocenophanes have also been studied, including ferrocenophanes with GeR$_2$, S, CH$_2$CH$_2$, and CH$_2$S bridges and the chromium and ruthenium analogs.

**7-11d Phosphorus-Containing Cyclic Esters**

Anionic polymerization of cyclic phosphates (**LXXXVI**) and phosphonates (**LXXXVII**) yields high-MW polymers,

\[
\begin{align*}
\text{LXXXVI} & \quad \text{LXXXVII}
\end{align*}
\]
Cationic polymerization yields only very-low MW products because of extensive chain-transfer reactions [Kubisa, 1996; Lapienis and Penczek, 1984; Penczek and Libiszowski, 1988; Penczek and Slomkowski, 1989a,b; Wodzki and Kaluzynski, 1989].

Other monomers that have been studied include cyclic phosphonites and phosphites as well as some sulfur analogs and nitrogen derivatives [Baran et al., 1989; Kobayashi et al., 1986].

### 7-11e Sulfur and Sulfur Nitride Polymers

The stable form of sulfur under normal conditions is crystalline cyclooctasulfur, referred to as rhombic sulfur. Heating rhombic sulfur causes it to change into monoclinic sulfur (which is still cyclooctasulfur but with a different crystalline structure) at about 95°C. Further heating causes melting at about 119°C and ring-opening polymerization to catena-polysulfur at 150–180°C via a biradical propagating species [Laitinen et al., 1987; Meyer, 1976; Ray, 1978]. Catena polysulfur is elastomeric but is unstable—it slowly reverts to rhombic sulfur on standing. Attempts to prevent this reversal by various means such as addition of small amounts of P, As, or alkenes (presumably to end-cap the polymer) have been unsuccessful. The polymerizations of selenium and tellurium proceed in a similar way as sulfur.

![Polysulfur structure](image)

Solid-state (topochemical) polymerization of cyclic disulfur dinitride to poly(sulfur nitride) (or polythiazyl), \((\text{SN})_n\), occurs on standing at ambient temperature or higher [Banister and Gorrell, 1998; Labes et al., 1979; Ray, 1978]. Disulfur dinitride is obtained by sublimation of tetrasulfur tetranitride. Polythiazyl is a potentially useful material, since it behaves like a metal. It has an electrical conductivity at room temperature about the same order of magnitude as a metal like mercury and is a superconductor at 24°C. Polythiazyl also has high light reflectivity and good thermal conductivity. However, it is insoluble and infusible, which prevents its practical utilization.

### 7-12 COPOLYMERIZATION

Considerable work has been published on the copolymerizations of various cyclic monomers reacting through the same type of functional group (e.g., two cyclic ethers or two cyclic siloxanes) or through different types of functional groups (e.g., copolymerization of a cyclic ether with a lactone), and also the copolymerizations of cyclic monomers with alkenes and other compounds. Some copolymerizations of cyclic monomers are of commercial importance. These include the various cyclic ether and acetal copolymerizations described previously (Sec. 7-2b-7). Copolymerization is used extensively for silicone polymers. Varying amounts of substituents such as phenyl or vinyl are introduced into the basic poly(dimethylsiloxane) structure to modify properties of the final product. Phenyl groups improve the low-temperature flexibility of silicone polymers by decreasing their low-temperature crystallinity. High-temperature performance and miscibility with organic solvents is also improved. Vinyl groups allow more efficient crosslinking by either hydrosilation or peroxides.

Although the literature contains much on copolymerizations of cyclic monomers, including data on monomer reactivity ratios, the reader is cautioned that most of the data are less reliable than corresponding data for radical copolymerizations of alkenes (Chap. 6). The
situation is much more like that which occurs in ionic copolymerizations. Ring-opening copolymerizations are complicated in several ways:

1. For copolymerizations proceeding by the activated monomer mechanism (e.g., cyclic ethers, lactams, N-carboxy-α-amino acid anhydrides), the actual monomers are the activated monomers. The concentrations of the two activated monomers (e.g., the lactam anions in anionic lactam copolymerization) may be different from the comonomer feed. Calculations of monomer reactivity ratios using the feed composition will then be incorrect.

2. Most ring-opening copolymerizations involve propagation–depropagation equilibria, which require that experimental data be handled in the appropriate manner (Sec. 6-5b), but this is usually not done. The situation is more complicated in many systems because of additional equilibria—between polymer and cyclic oligomer and by intermolecular chain transfer to polymer—which result in reshuffling of monomer units. It may be possible to avoid or minimize the reshuffling equilibria by using mild initiators, low conversions, and highly reactive (more strained) monomers. However, the situation in industrial practice usually involves conditions that result in near-complete reshuffling of monomer units. The effect of reshuffling is evident in the anionic copolymerization of octamethylcyclotetrasiloxane (M₁) and 1,3,5,7-tetramethyl-1,3,5,7-tetrayncyclotetrasiloxane (M₂) (feed ratio 9 : 1) by potassium silanolate at 130°C [Ziemelis and Saam, 1989]. The initial copolymer is very rich in M₂, and this monomer is exhausted early. Further reaction results not only in conversion of M₁ but also redistribution of the M₂ units. Silicon 29 NMR shows the M₂ units to be in blocks at short reaction times but statistically distributed at long reaction times. Similar results have been observed in the cationic copolymerization of methyl glyoxylate and 1,3-dioxolane [Basko et al., 2000].

3. Counterion effects similar to those in ionic chain copolymerizations of alkenes (Secs. 6-4a-2, 6-4b-2) are present. Thus, copolymerizations of cyclopentene and norbornene with rhenium- and ruthenium-based initiators yield copolymers very rich in norbornene, while a more reactive (less discriminating) tungsten-based initiator yields a copolymer with comparable amounts of the two comonomers [Ivin, 1987]. Monomer reactivity ratios are also sensitive to solvent and temperature. Polymer conformational effects on reactivity have been observed in NCA copolymerizations where the particular polymer chain conformation, which is usually solvent-dependent, results in different interactions with each monomer [Imanishi, 1984].

4. Some ROPs proceed with the simultaneous operation of two different mechanisms, for example, NCA copolymerizations initiated by some secondary amines proceed with both the amine and activated monomer mechanisms. The monomer reactivity ratios for any comonomer pair are unlikely to be the same for the two different propagations. Any experimentally determined $r$ values are each composites of two different $r$ values.

5. The initiator used is important for copolymerizations between monomers containing different polymerizing functional groups. Basic differences in the propagating centers (oxonium ion, amide anion, carbocation, etc.) for different types of monomer preclude some copolymerizations. Even when two different monomer types undergo polymerization with similar propagating centers, there may not be complete compatibility in the two crossover reactions. For example, oxonium ions initiate cyclic amine polymerization, but ammonium ions do not initiate cyclic ether polymerization [Kubisa, 1996].

7-12a Monomers with Same Functional Group

Copolymerizations between pairs of cyclic esters, acetals, sulfides, siloxanes, alkenes, lactams, lactones, N-carboxy-α-amino acid anhydrides, imines, and other cyclic monomers
have been studied [Frisch and Reegan, 1969; Ivin, 1987; Ivin and Saegusa, 1984; Kendrick et al., 1989; Sebenda, 1989; Tomalia and Killat, 1985]. Copolymerizations have also been achieved between closely related types of monomers such as cyclic ethers with cyclic acetics or lactones with lactides and cyclic carbonates [Basko et al., 2000; Keul et al., 1988; Kricheldorf et al., 1985].

The interpretation of experimental monomer reactivity ratios is subject to the cautions described above. When copolymerization proceeds with minimal complications, the $r$ values can often be analyzed by considering the effects of ring size on the general tendency toward ring opening (see considerations in Sec. 2-5b) and the reactivity toward attack by the particular propagating species. For those polymerizations involving a cyclic propagating center (e.g., oxonium ions in cyclic ether polymerization), there is also the need to consider the effect of ring size on formation of the propagating center.

Some monomers with no tendency toward homopolymerization are found to have some (not high) activity in copolymerization. This behavior is found in cationic copolymerizations of tetrahydrofuran, 1,3-dioxane, and 1,4-dioxane with 3,3-bis(chloromethyl)oxetane [Dreyfuss and Dreyfuss, 1969]. These monomers are formally similar in their unusual copolymerization behavior to the radical copolymerization behavior of sterically hindered monomers such as maleic anhydride, stilbene, and diethyl fumarate (Sec. 6-3b-3), but not for the same reason. The copolymerizability of these otherwise unreactive monomers is probably a consequence of the unstable nature of their propagating centers. Consider the copolymerization in which $M_2$ is the cyclic monomer with no tendency to homopolymerize. In homopolymerization, the propagation–depropagation equilibrium for $M_2$ is completely toward monomer. However, with the second monomer $M_1$ present, the species LXXXVIII adds $M_1$ before depropagation can occur and copolymerization of $M_1$ and $M_2$ results. Similar behavior has been observed for the comonomer pairs $\beta$-propiolactone–$\gamma$-butyrolactone and cyclopentene–cyclohexene [Ivin et al., 1979; Tada et al., 1964]. The second monomer in each pair does not homopolymerize, but copolymerization occurs.

The anionic copolymerization (using an acetylated initiator) of $\epsilon$-caprolactam ($M_1$) and $\alpha$-pyrrolidinone ($M_2$) illustrates the problem of interpreting $r_1$ and $r_2$ values obtained by employing the standard copolymerization equation (Eq. 6-12). The monomer reactivity ratios have been calculated as $r_1 = 0.75$ and $r_2 = 5.0$ with the conclusion that $\alpha$-caprolactam is about 8 times more reactive than $\epsilon$-pyrrolidinone [Kobayashi and Matsuya, 1963]. However, a detailed study of the system indicates that the copolymer composition is not determined by the rate constants $k_{11}$, $k_{12}$, $k_{22}$, and $k_{21}$ for the various homo- and cross-propagation reactions [Bar-Zakay et al., 1967]. Transacylation involving an exchange of the monomer segments in the initiating and propagating imides, occurs at a much faster rate than any of the various

\[
\begin{align*}
\text{LXXXVIII} & \\
O & \xrightarrow{\text{K_1}} O
\end{align*}
\]
propagation reactions. The copolymer composition is thus dependent on the transacylation equilibrium according to

$$\frac{d[M_1]}{d[M_2]} = \frac{K_t[M_1^\nu]}{[M_2^\nu]} \quad (7-122)$$

where $[M_1^\nu]$ and $[M_2^\nu]$ represent the concentrations of the lactam anions. The ratio $[M_1^\nu]/[M_2^\nu]$ is determined by the relative acidities of the two monomers by the equilibrium

$$M_2^- + M_1 \xrightleftharpoons[K_a]{K_i} M_2 + M_1^\nu \quad (7-123)$$

Combining the equilibrium expression for Eq. 7-123 with Eq. 7-122 yields

$$\frac{d[M_1]}{d[M_2]} = \frac{K_aK_t[M_1]}{[M_2]} \quad (7-124)$$

where $K_a$ and $K_i$ have been independently determined as 0.4 and 0.3, respectively. The greater reactivity of $\alpha$-pyrrolidone in the copolymerization with $\epsilon$-caprolactam can then be attributed to the greater acidity of $\alpha$-pyrrolidone (by a factor of $\sim 2.5$) and the greater nucleophilicity of the $\alpha$-pyrrolidone anion in the transacylation equilibrium (by a factor of $\sim 3.3$).

### 7-12b Monomers with Different Functional Groups

Copolymerization between monomers containing different functional groups is selective. One of the cross-propagation steps in a contemplated copolymerization may be highly unfavorable because of the wide variations in the types of propagating centers involved and, often, in the energies of the bonds being broken during propagation. Copolymerization between certain types of monomers does not occur and that between others is difficult to achieve, while some copolymerizations occur with relative ease. Thus, the combination of a lactam with any other type of monomer, such as a lactone, epoxide, or alkene, is incompatible because of differences in their propagation mechanisms. For example, anionic copolymerization of a lactam with an epoxide does not occur since the anion derived from the epoxide terminates by proton abstraction from lactam monomer.

Epoxides readily undergo anionic copolymerization with lactones and cyclic anhydrides because the propagating centers are similar—alkoxide and carboxylate [Aida et al., 1985; Cherdron and Ohse, 1966; Inoue and Aida, 1989; Luston and Vass, 1984]. Most of the polymerizations show alternating behavior, with the formation of polyester, but the mechanism for alternation is unclear. There are few reports of cationic copolymerizations of lactones and cyclic ethers other than the copolymerizations of $\beta$-propiolactone with tetrahydrofuran and 3,3-bis(chloromethyl)oxetane, probably indicative of the difference in propagating centers (dioxocarboxocation and oxonium ion, respectively) [Yamashita et al., 1966]. The copolymerizations tend toward ideal behavior with the product containing large amounts of the cyclic ether.

Anionic copolymerization of an episulfide and epoxide shows extreme ideal behavior with only small amounts of epoxide incorporated into the copolymer, since episulfides are much more reactive than epoxides. Cationic copolymerization does not occur to any extent because sulfonium ion centers do not add epoxide, although oxonium ion centers do add episulfide.
There are very few reported copolymerizations between cyclic monomers and carbon–
carbon double-bond monomers. Such copolymerizations would require a careful selection
of the monomers and reaction conditions to closely match the reactivities of the different
monomers and propagating centers. The almost complete absence of successes indicates
that the required balancing of reactivities is nearly impossible to achieve. There are a
few reports of copolymerizations between carbon–carbon double-bond monomers and
cyclic ethers or acetals [Higashimura et al., 1967; Inoue and Aida, 1984; Yamashita et al.,
1966].

Some copolymerizations have been studied where one of the reactants is a compound not
usually considered as a monomer. These include copolymerizations of epoxides and higher
cyclic ethers with carbon dioxide, episulfides with carbon dioxide and carbon disulfide, and
epoxides with sulfur dioxide [Aida et al., 1986; Baran et al., 1984; Chisholm et al., 2002;
Inoue and Aida, 1989; Soga et al., 1977]. The copolymers are reported to be either 1 : 1 alternating
copolymers or contain 1 : 1 alternating sequences together with blocks of the cyclic
monomer.

7-12c Block Copolymers

A wide range of different block copolymers have been synthesized by using the sequential
addition method applicable to living polymer systems. These include various copolymers in
which the different blocks are derived from two different cyclic monomers containing
the same functional group, such as two cycloalkenes, cyclic ethers, lactams, lactones, N-
carboxy-α-amino acid anhydrides, and episulfides [Cannizzo and Grubbs, 1988; Dreyfuss
and Dreyfuss, 1989; Greene et al., 1988; Hashimoto, 2000; Imanishi, 1984; Inoue and
Aida, 1989; Jedlinski et al., 1987; Sigwalt and Spassky, 1984; Yasuda et al., 1984]. There
are very few reports of block copolymers of lactams or cyclic siloxanes produced by sequential
addition, probably indicative of the exchange reactions that occur in polymerizations of
these monomers.

The sequential addition method also allows the synthesis of many different block copo-
lymers in which the two monomers have different functional groups, such as epoxide with
lactone, lactide or cyclic anhydride, cyclic ether with 2-methyl-2-oxazoline, imine or episul-
fide, lactone with lactide or cyclic carbonate, cycloalkene with acetylene, and ferrocenophane
with cyclodisiloxane [Aida et al., 1985; Barakat et al., 2001; Dreyfuss and Dreyfuss, 1989;
Farren et al., 1989; Inoue and Aida, 1989; Keul et al., 1988; Kobayashi et al., 1990a,b,c;
Massey et al., 1998; Yasuda et al., 1984].

Further, there have been a number of successes in synthesizing block copolymers by
sequential polymerization of a cyclic monomer and an alkene monomer. Examples include
the combination of methyl methacrylate with epoxide, episulfide or lactone, polystyrene with
hexamethyleneclotrisiloxane, lactone or cyclic carbonate, and 2-isopropenynaphtalene with
hexamethyleneclotrisiloxane [Keul and Hocker, 1986; Krause et al., 1982; Kuroki et al.,
1988a,b; Rhein and Schulz, 1985; Sigwalt and Spassky, 1984]. It turns out to be much easier
to obtain block copolymers from these combinations than to obtain the corresponding statisti-
cal copolymers. Synthesis of a statistical copolymer requires that there not be a large imbalance
between the various homo- and cross-propagation rates. Synthesis of a block copolymer
by sequential addition requires that the system be living with one or the other cross-propa-
gation proceeding at a reasonable rate. Thus, anionic copolymerization of styrene with ethylene
oxide does not occur because the addition of alkoxide ion to the carbon–carbon double bond
and homopropagation of polystyryl anion are much less favored relative to addition of poly-
styryl anion to ethylene oxide and homopropagation of alkoxide anion. However, block
copolymerization is easily achieved by adding ethylene oxide to living polystyrene. Triblock polymers can be obtained in some systems by using appropriate difunctional initiators.

Another route to block copolymers is the use of a macroinitiator, a telechelic homopolymer with appropriate end group, to initiate the polymerization of the second monomer. For example, polybutadiene containing a terminal hydroxyl group is reacted with triethylaluminum to form an aluminum alkoxide initiator that polymerizes lactide [Wang and Hillmyer, 2000]. Polystyrene and polysiloxane with $p$-toluenesulfonyl ester end groups initiate the polymerizations of 2-methyl-2-oxazoline and N-$t$-butylaziridine [Ishizu et al., 1985; Kazama et al., 1988]. The macroinitiator route has been used for many different combinations, including styrene–NCA, ethylene oxide–lactam, ethylene oxide–phosphazene, ADMET-NCA [Allcock et al., 2001a,b; Brzezinska and Deming, 2001; Hashimoto, 2000; Janssen et al., 1988]. Coupling reactions have also been studied for producing block copolymers.

Although not extensively studied, various architectures such as star and comb polymers have also been synthesized [Bielawski et al., 2000; Goethals et al., 2000].

### 7-12d Zwitterion Polymerization

Certain combinations of nucleophiles and electrophiles undergo polymerization without the need for initiator [Culbertson, 2002; Kobayashi and Saegusa, 1985; Kobayashi and Uyama, 2002; Saegusa, 1977, 1979, 1981]. The polymerization, referred to as zwitterion polymerization, proceeds via zwitterion intermediates. For example, polymerization between 2-oxazoline and $\beta$-propiolactone involves nucleophilic attack of 2-oxazoline on $\beta$-propiolactone to form the dimer zwitterion LXXXIX, which reacts with itself to form the tetramer zwitterion LXXXX. The latter reacts with itself and with LXXXIX to form octamer and hexamer zwitterions respectively. Propagation continues in this manner as various-sized zwitterions react with each other to form larger zwitterions.

Among the nucleophilic monomers studied are 5,6-dihydro-$4H$-1,3-oxazines, cyclic phosphites and phosphonites, iminodioxolanes, and imines; electrophilic monomers include...
cyclic anhydrides, lactones and sultones as well as acyclic compounds such as acrylic acid and acrylamide. With only a very few exceptions, these polymerizations do not yield polymer molecular weights higher than 1000–3000. Low molecular weights are a consequence of the low concentration of the reacting species, the zwitterions, coupled with facile termination of the zwitterion + and − centers by reaction with the nucleophilic and electrophilic monomers [Odian and Gunatillake, 1984; Odian et al., 1990]. High molecular weights are obtained in zwitterion polymerizations only when the zwitterion concentrations are high relative to other materials present that can act as terminating agents. This has been successfully achieved in several systems. One of the systems (Eq. 7-91) has a low concentration of zwitterion intermediate, but there are no materials present (such as the electrophilic and nucleophilic monomers) to act as terminating agents. The other system (Eq. 7-93) contains only zwitterion since the zwitterion is isolated and is stable. Polymerization occurs when the zwitterion is heated.

REFERENCES

REFERENCES


REFERENCES


7-1 Consider the following initiators and monomers:

<table>
<thead>
<tr>
<th>Initiator</th>
<th>Monomer</th>
</tr>
</thead>
<tbody>
<tr>
<td>Grubbs initiator</td>
<td>Propylene oxide</td>
</tr>
<tr>
<td>n-Butyl lithium</td>
<td>ε-Caprolactam</td>
</tr>
<tr>
<td>bpyNi(COD)</td>
<td>Cyclooctene</td>
</tr>
<tr>
<td>BF$_3$ + H$_2$O</td>
<td>Oxacyclobutane</td>
</tr>
<tr>
<td>H$_2$SO$_4$</td>
<td>δ-Valerolactone</td>
</tr>
<tr>
<td>NaOC$_2$H$_5$</td>
<td>NCA</td>
</tr>
<tr>
<td>H$_2$O</td>
<td>1,5-Hexadiene</td>
</tr>
<tr>
<td></td>
<td>Octamethylcyclotetrasiloxane</td>
</tr>
<tr>
<td></td>
<td>Propylene sulfide</td>
</tr>
<tr>
<td></td>
<td>Trioxane</td>
</tr>
</tbody>
</table>

Which initiator(s) can be used to polymerize each of the monomers? For each monomer, give the structure of the polymer product.

7-2 Give the cyclic monomer(s), initiator, and reaction conditions necessary to synthesize each of the following polymers:

a. \( \left[ \text{NHCO(CH}_2\text{)}_4 \right]_n \)

b. \( \left[ \text{NH} - \text{CH} - \text{CO} \right]_n \)

c. \( \left[ \text{NHCH}_2\text{CH}_2\text{CH}_2 \right]_n \)

d. \( \left[ \text{O(CH}_2\text{)}_2\text{OCH}_2 \right]_n \)

e. \( \left[ \text{CH}=\text{CH(CH}_2\text{)}_2 \right]_n \)

f. \( \left[ \text{Si(CH}_3\text{)}_2\text{O} \right]_n \)

7-3 Discuss the effect of ring size on the tendency of a cyclic monomer toward ring-opening polymerization.

7-4 Anionic polymerization of propylene oxide is usually limited to producing a relatively low-molecular-weight polymer. Discuss the reasons for this occurrence.

7-5 T. Saegusa, H. Fujii, S. Kobayashi, H. Ando, and R. Kawase, *Macromolecules*, 6, 26 (1973), have found that the polymerization rate for the BF$_3$ polymerization of oxetane follows the equation:

\[
-\frac{d[M]}{dt} = k_p [P^*][M]
\]

a. Describe by an equation the mechanism for the propagation step in this polymerization.
b. The values of \( k_p \) at \(-20^\circ\text{C}\) are 0.18 and 0.019 L mol\(^{-1}\) s\(^{-1}\), respectively, for polymerizations carried out in methylcyclohexane and methylene chloride. Explain why propagation is faster in the less polar solvent.

c. The following rate constants and activation parameters for propagation were observed for oxetane and 3-methyloxetane:

<table>
<thead>
<tr>
<th></th>
<th>Oxetane</th>
<th>3-Methyloxetane</th>
</tr>
</thead>
<tbody>
<tr>
<td>( k_p ) at (-20^\circ\text{C}) (L mol(^{-1}) s(^{-1}))</td>
<td>0.019</td>
<td>0.11</td>
</tr>
<tr>
<td>( \Delta G_p^\ddagger ) (kJ mol(^{-1}))</td>
<td>71.2</td>
<td>65.7</td>
</tr>
<tr>
<td>( \Delta H_p^\ddagger ) (kJ mol(^{-1}))</td>
<td>57.4</td>
<td>65.3</td>
</tr>
<tr>
<td>( \Delta S_p^\ddagger ) (J mol(^{-1}) K(^{-1}))</td>
<td>-50.7</td>
<td>-5.4</td>
</tr>
</tbody>
</table>

Discuss why 3-methyloxetane is more reactive than oxetane. Is a negative entropy of activation consistent with the proposed propagation mechanism?

7-6 The polymerization of an epoxide by hydroxide or alkoxide ion is often carried out in the presence of an alcohol. Why? How is the degree of polymerization affected by alcohol? Discuss how the presence of alcohol affects both the polymerization rate and molecular weight distribution.

7-7 Explain the following observations:

a. A small amount of epichlorohydrin greatly increases the rate of the polymerization of tetrahydrofuran by BF\(_3\) even though epichlorohydrin is much less basic than tetrahydrofuran.

b. The addition of small amounts of water to the polymerization of oxetane by BF\(_3\) increases the polymerization rate but decreases the degree of polymerization.

7-8 An equilibrium polymerization is carried out with an initial concentration of 12.1 M tetrahydrofuran, \([M^*] = 2.0 \times 10^{-3} M\), and \(k_p = 1.3 \times 10^{-2}\) L mol\(^{-1}\) s\(^{-1}\). Calculate the initial polymerization rate if \([M]_c = 1.5 M\). What is the polymerization rate at 20% conversion?

7-9 What are the roles of an acylating agent and activated monomer in the anionic polymerization of lactams?

7-10 Consider the equilibrium polymerization of \(\varepsilon\)-caprolactam initiated by water at 220\(^\circ\text{C}\). For the case where \([I]_0 = 0.352, [M]_0 = 8.79\) and \([M]_c = 0.484\), the degree of polymerization at equilibrium is 152, calculate the values of \(K_i\) and \(K_p\) at equilibrium.

7-11 Discuss by means of equations the occurrence of backbiting, ring-expansion reactions in the polymerizations of cyclic ethers, acetics, and amines.

7-12 \(\varepsilon\)-Caprolactone is polymerized using aluminum isopropoxide as the initiator in THF at 25\(^\circ\text{C}\) [A. Duda and S. Penczek, Macromolecules, 28, 5981 (1995)]. The initial monomer concentration is 1.47 mol L\(^{-1}\); the initial aluminum isopropoxide concentration is 1.63 \times 10^{-4} mol L\(^{-1}\). The reaction mixture is subjected to hydrolysis at the point where 100% conversion has been reached. The number-average degree of polymerization of the hydrolyzed polymer is 2.99 \times 10^3. Compare this value with the theoretical degree of polymerization.
Constitutional (formerly: structural) isomerism is encountered when polymers have the same overall chemical composition (i.e., same molecular formula) but differ in connectivity—the order in which the atoms are connected to each other. Polyacetaldehyde, poly(ethylene oxide), and poly(vinyl alcohol) are constitutional isomers. The first two polymers are obtained from isomeric monomers, acetaldehyde and ethylene oxide. The third is obtained by hydrolysis of poly(vinyl acetate) since vinyl alcohol does not exist (it is the enol form of acetaldehyde). Poly(methyl methacrylate) and poly(ethyl acrylate) are isomeric polymers formed from isomeric monomers. Poly(ϵ-caprolactam) and poly(hexamethylene adipamide) are isomeric even though the monomers are not isomeric. Similarly, the 1:1 copolymer of
ethylene and 1-butene is isomeric with polypropene.

\[
\text{Poly(\varepsilon\text{-caprolactam})} \quad \text{Poly(hexamethylene adipamide)}
\]

Isomeric polymers can also be obtained from a single monomer if there is more than one polymerization route. The head-to-head placement that can occur in the polymerization of a vinyl monomer is isomeric with the normal head-to-tail placement (see structures III and IV in Sec. 3-2a). Isomerization during carbocation polymerization is another instance whereby isomeric structures can be formed (Sec. 5-2b). Monomers with two polymerizable groups can yield isomeric polymers if one or the other of the two alternate polymerization routes is favored. Examples of this type of isomerism are the 1,2- and 1,4-polymers from 1,3-dienes (Secs. 3-14f and 8-10), the separate polymerizations of the alkene and carbonyl double bonds in ketene and acrolein (Sec. 5-7a), and the synthesis of linear or cyclized polymers from non-conjugated dienes (Sec. 6-6b). The different examples of constitutional isomerism are important to note from the practical viewpoint, since the isomeric polymers usually differ considerably in their properties.

This chapter is concerned primarily with a different type of isomerism in polymers—that arising as a result of stereoisomerism in the structure of polymers as a consequence of the polymerization reaction. This is an important topic because of the significant effect that stereoisomerism has on many polymer properties. Considerations of stereoisomerism in chain polymerizations of vinyl monomers were recognized early [Staudinger et al., 1929]. However, the possibility that each of the propagation steps in the growth of a polymer chain could give rise to stereoisomerism was not fully appreciated until more than two decades later. Further, the synthesis of polymers with ordered configurations in which the stereoisomerism of repeating units in the chain would show a regular or ordered arrangement instead of a random one was essentially not considered. One of the major developments in the polymer field has been the elucidation of the occurrence of stereoisomerism in polymers. More importantly, the pioneering works of Ziegler and Natta and their coworkers led to the convenient synthesis of polymers with highly stereoregular structures [Boor, 1979; Ketley, 1967a,b; Natta, 1955a,b, 1965; Natta et al., 1955; Ziegler et al., 1955]. We are now doing what nature has been doing for eons. Stereoregular polymers of different kinds are commonly found in nature; these include natural rubber, cellulose, starch, polypeptides, and nucleic acids.

Enormous commercial applications flowed from the revolution initiated by Ziegler and Natta. These include high-density and linear low-density polyethylenes (HDPE, LLDE), polypropene, ethene-propene co- and terpolymers, and polymers from 1,3-dienes (Sec. 8-10). The annual United States production of these polymers exceeded 40 billion pounds in 2000; the global production was about 3–3.5 times the U.S. production. Ziegler–Natta chemistry accounts for the production of one-third of all polymers.

**8-1 TYPES OF STEREOISOMERISM IN POLYMERS**

Stereoisomers have the same connectivity, but differ in their configurations. Configuration is the relative orientation in space of the atoms of a stereoisomer, independent of spatial
changes that occur by rotations about single bonds [Blei and Odian, 2000; Farina, 1987; Farina and Bressan, 1968; Goodman, 1967]. Cis–trans (geometric) isomers arise from different configurations of substituents on a double bond or on a cyclic structure. Enantiomers arise from different configurations of substituents on a sp³ (tetrahedral) carbon or other atom. The term configuration should not be confused with conformation. Conformation refers to the different orientations of atoms and substituents in a molecule that result from rotations around single bonds. Examples of different polymer conformations are the fully extended planar zigzag, random coil, helical, and folded-chain arrangements. Conformational isomers can be interconverted one into the other by bond rotations. Configurational isomers differ in the spatial arrangements of their atoms and substituents in a manner such that they can be interconverted only by breaking and reforming primary chemical bonds.

8-1a Monosubstituted Ethylenes

8-1a-1 Site of Steric Isomerism

Isomerism is observed in the polymerization of alkenes when one of the carbon atoms of the double bond is monosubstituted. The polymerization of a monosubstituted ethylene, CH₂=CHR (where R is any substituent other than H), leads to polymers in which every tertiary carbon atom in the polymer chain is a stereocenter (or stereogenic center). The stereocenter in each repeating unit is denoted as C* in Ia and Ib. A stereocenter is an atom bearing substituents of such identity that a hypothetical exchange of the positions of any two substituents would convert one stereoisomer into another stereoisomer. Thus, an exchange of the R and H groups converts Ia into Ib and vice versa.

Each stereocenter C* is a site of steric isomerism in the polymerization of CH₂=CHR. Each such site in a polymer chain can exhibit either of two different configurations (Ia or Ib). Considering the main carbon—carbon chain of the polymer (CH₂CHR)ₙ to be stretched out in its fully extended planar zigzag conformation, two different configurations are possible for each stereocenter since the R group may be situated on either side of the plane of the carbon–carbon polymer chain. If the plane of the carbon–carbon chain is considered as being in the plane of this page, the R groups are located on one side or the other of this plane. The two configurations are usually referred to as R and S, although the Cahn–Ingold–Prelog priority rules cannot be applied strictly since that requires knowledge of the relative lengths of the two polymer chain segments. Without knowledge of the lengths of the polymer chain segments, designation of R and S configurations can be done only in an arbitrary manner. One of the configurations (Ia or Ib) is designated as R and the other as S. The lowercase designations, r and s, are often used in place of the uppercase letters to emphasize this aspect. (Other designations of the two configurations appear in the literature: d and l, d and l, + and −.)

There are two constitutional repeat units (Sec. 1-2c) from a stereochemical viewpoint, one with R configuration for the stereocenter and the other with S configuration for the stereocenter (corresponding to Ia and Ib). These are referred to as the two configurational base units and have an enantiomeric relationship [IUPAC, 1966, 1981, 1996].
The classification of a C* in the planar zigzag conformation as chirotopic or achirotopic presents difficulty. A stereocenter is chirotopic if it lies in a chiral environment [Eliel and Wilen, 1994; Mislow and Siegel, 1984]. A chiral environment is one that is not superposable on its mirror image. The literal definition of the term chirotopic would classify each C* as chirotopic since the two polymer chain segments, \(~\sim\) and \(\sim\sim\), are not equivalent. The non-equivalence of the two chain segments is due to differences in length. (There may also be differences in end groups depending on the modes of initiation and termination.) However, classification of C* as chirotopic implies optical activity, and this is clearly not true from a practical viewpoint. Optical activity is a short-range phenomenon with its magnitude determined by the differences in the groups attached to the stereocenter. The first few atoms of the two polymer chain segments attached to C* are the same and such stereocenters do not contribute measurably to the optical activity of the polymer. The only stereocenters with significant optical activity are those at the ends of the polymer chain, but their population is negligible for a high-molecular-weight polymer. The sum of contributions from all the stereocenters is such that optical activity is below the limits of detection. (This discussion of optical activity excludes optical activity arising from the existence of a polymer molecule exclusively in a chiral conformation, a very rare occurrence except for biological macromolecules; see Sec. 8-8b. A typical polymer in solution exists in the random-coil conformation. Many of the conformations are chiral, but on a time-average basis there are equal numbers of conformations of opposite rotation and the net rotation is zero.) Thus, it is more useful to classify stereocenters such as those in 1a and 1b as achirotopic.

The terms stereocenter, chirotopic, and achirotopic will be used in this text in line with the most recent terminology. However, other terms are found in the older literature. C* was previously referred to as a chiral or pseudochiral center. The term pseudochiral center is based on the same convention used to classify C* as achirotopic instead of chirotopic. The terms asymmetric and pseudoasymmetric center are found in much older literature.

**8-1a-2 Tacticity**

The regularity in the configurations of successive stereocenters determines the overall order (tacticity) of the polymer chain. If the R groups on successive stereocenters are randomly distributed on the two sides of the planar zigzag polymer chain, the polymer does not have order and is termed atactic. Two types of ordered or tactic structures or placements can occur: isotactic and syndiotactic. An isotactic structure occurs when the stereocenter in each repeating unit in the polymer chain has the same configuration. All the R groups will be located on one side of the plane of the carbon–carbon polymer chain—either all above or all below the plane of the chain. A syndiotactic polymer structure occurs when the configurations of the stereocenters alternate from one repeating unit to the next with the R groups located alternately on the opposite sides of the plane of the polymer chain. These different polymer structures are shown in Fig. 8-1. The various polymer structures are described by three different pictorial representations. The ones on the far left side of Fig. 8-1 show the polymer chain in the plane of this page with the H and R groups above (triangular bonds) and below (dotted bonds) that plane. The representations in the middle are the corresponding Fischer projections. Vertical lines in the Fischer projections correspond to bonds projecting behind the plane of this page; horizontal lines represent bonds projecting in front of the plane. This is the usual convention for Fischer projections [Bovey, 1982]. The configuration at each carbon atom in the polymer chain is drawn in the Fischer projection by imagining the rotation of each carbon–carbon bond in the polymer chain into an eclipsed conformations as opposed to the staggered conformation that actually exists. The
representations on the far right side of Fig. 8-1, recommended by IUPAC [1981], are obtained by rotating the previous Fischer projections 90° counterclockwise. The resulting Fischer projections do have the advantage of showing the polymer chain going in the same direction as the far-left representations. Their disadvantage is that one must always keep in mind that the usual Fischer convention for horizontal (forward) and vertical (back) bonds is reversed. These rotated Fischer projections will be used in the remainder of this chapter.

The Fischer projections show that isotactic placement corresponds to meso or $m$-placement for a pair of consecutive stereocenters. Syndiotactic placement corresponds to racemo (for racemic) or $r$-placement for a pair of consecutive stereocenters. The configurational
repeating unit is defined as the smallest set of configurational base units that describe the configurational repetition in the polymer. For the isotactic polymer from a monosubstituted ethylene, the configurational repeating unit and configurational base unit are the same. For the syndiotactic polymer, the configurational repeating unit is a sequence of two configurational base units, an \( R \) unit followed by an \( S \) unit or vice versa.

Polymerizations that yield tactic structures (either isotactic or syndiotactic) are termed stereoselective polymerizations. The reader is cautioned that most of the literature uses the term stereospecific polymerization, not stereoselective polymerization. However, the correct term is stereoselective polymerization since a reaction is termed stereoselective if it results in the preferential formation of one stereoisomer over another [IUPAC, 1996]. This is what occurs in the polymerization. A reaction is stereospecific if starting materials differing only in their configuration are converted into stereoisomeric products. This is not what occurs in the polymerization since the starting material does not exist in different configurations. (A stereospecific process is necessarily stereoselective but not all stereoselective processes are stereospecific.)

Stereoselective polymerizations yielding isotactic and syndiotactic polymers are termed isoselective and syndioselective polymerizations, respectively. The polymer structures are termed stereoregular polymers. The terms isotactic and syndiotactic are placed before the name of a polymer to indicate the respective tactic structures, such as isotactic polypropene and syndiotactic polypropene. The absence of these terms denotes the atactic structure; polypropene means atactic polypropene. The prefixes it- and st- together with the formula of the polymer, have been suggested for the same purpose: it-[CH\(_2\)CH(CH\(_3\))]\(_n\) and st-[CH\(_2\) CH(CH\(_3\))]\(_n\) [IUPAC, 1966].

Both isotactic and syndiotactic polypropenes are achiral as a result of a series of mirror planes (i.e., planes of symmetry) perpendicular to the polymer chain axis. Neither exhibits optical activity.

8-1b Disubstituted Ethylenes

8-1b-1 1,1-Disubstituted Ethylenes

For disubstituted ethylenes, the presence and type of tacticity depends on the positions of substitution and the identity of the substituents. In the polymerization of a 1,1-disubstituted ethylene, \( \text{CH}_2\text{=CRR'} \), stereoisomerism does not exist if the \( R \) and \( R' \) groups are the same (e.g., isobutylene and vinylidene chloride). When \( R \) and \( R' \) are different (e.g., \(-\text{CH}_3\) and \(-\text{COOCH}_3\) in methyl methacrylate), stereoisomerism occurs exactly as in the case of a monosubstituted ethylene. The methyl groups can be located all above or all below the plane of the polymer chain (isotactic), alternately above and below (syndiotactic), or randomly (atactic). The presence of the second substituent has no effect on the situation since steric placement of the first substituent automatically fixes that of the second. The second substituent is isotactic if the first is isotactic, syndiotactic if the first substituent is syndiotactic, and atactic if the first is atactic.

8-1b-2 1,2-Disubstituted Ethylenes

The polymerization of 1,2-disubstituted ethylenes, \( \text{RCH=CCHR'} \), such as 2-pentene (\( R = -\text{CH}_3, R' = -\text{C}_2\text{H}_5 \)), presents a different situation. Polymerization yields a polymer structure \( \Pi \) in which there are two different stereocenters in each repeating unit. Several possibilities of ditacticity exist that involve different combinations of tacticity for the two stereocenters. Various stereoregular structures can be defined as shown in Fig. 8-2. Diisotactic structures occur when placement at each of the two stereocenters is isotactic.
A disyndiotactic structure occurs when placement at each of the two different stereocenters is syndiotactic. Two diisotactic structures are possible. These are differentiated by the prefixes threo and erythro. The meaning of these prefixes corresponds to their use in carbohydrate chemistry. Considering the planar zigzag polymer chain, the erythro structure is the one in which like groups on adjacent carbons are anti to each other (i.e., R and R’ are anti to each other and H and H are anti to each other). The threo structure has an anti arrangement of unlike groups on adjacent carbons (i.e., R and H are anti and R’ and H are also anti). The difference between the erythro and threodisotactic structures can also be shown by Newman representations of the eclipsed conformation of two consecutive carbon atoms in the polymer chain. These are shown at the far right side of Fig. 8-2. Like groups are eclipsed on like groups (H on H, R on R’, polymer chain segment on polymer chain segment) in the erythro structure; unlike groups are eclipsed in the threo structure. For the threodisotactic polymer, the two stereocenters have opposite configurations. In the zigzag pictorial representation,
both R and R‘ are on the same side of the plane of the polymer chain. In the Fischer projection, R and R‘ are on opposite sides of the line representing the polymer chain. For the erthyrodiisotactic polymer, the configurations at the two stereocenters are the same.

The corresponding threodiszyndiotactic and erythrodiszyndiotactic polymers are drawn in Fig. 8-2. However, a close examination of the two diszyndiotactic structures shows that they are identical except for a difference in the end groups. Ignoring end groups, the two structures are superposable. Thus, from the practical viewpoint, there is only one diszyndiotactic polymer. The nomenclature for ditactic polymers follows in the same manner as for monotactic polymers. Thus the various stereoregular poly(2-pentene) polymers would be threodiisotactic poly(2-pentene), erythrodiiisotactic poly-(2-pentene), and diszyndiotactic poly(2-pentene) with the prefixes tit-, eit-, and st-, respectively, used before the formula [CH(CH₃)CH(C₂H₅)]ₙ.

The stereocenters in all three stereoregular polymers are achirotopic. The polymers are achiral and do not possess optical activity. The disosiotactic polymers contain mirror planes perpendicular to the polymer chain axis. The diszyndiotactic polymer has a mirror glide plane of symmetry. The latter refers to superposition of the diszyndiotactic structure with its mirror image after one performs a glide operation. A glide operation involves movement of one structure relative to the other by sliding one polymer chain axis parallel to the other chain axis.

It should be noted that other polymer structures can be postulated—those where one substituent is atactic while the other is either isotactic or syndiotactic or those where one substituent is isotactic while the other is syndiotactic. However, these possibilities are rarely observed since the factors that lead to ordering or disordering of one substituent during polymerization generally have the same effect on the other substituent. An exception is the formation of hemiisotactic polypropene where isotactic placements alternate with atactic placements [Coates, 2000].

8-1c Carbonyl and Ring-Opening Polymerizations

Several other types of monomers are capable of yielding stereoisomeric polymer structures. Ordered structures are possible in the polymerization of carbonyl monomers (RCHO and RCOOR') and the ring-opening polymerizations of certain monomers. Thus, for example, the polymers from acetaldehyde and propylene oxide can have isotactic and syndiotactic structures as shown in Figs. 8-3 and 8-4.
Polyacetaldehyde [IUPAC: Poly(oxy[methylmethylene])], like the systems described previously, contains stereocenters that are achirotopic. Both the isotactic and syndiotactic polymers are achiral and do not possess optical activity. The repeat unit (III) in poly(propylene oxide) [IUPAC: poly(oxy[1-methylethylene])], on the other hand, possesses stereocenters that are chirotopic since the two chain segments attached to C* are very different—one is attached via an oxygen and the other via a methylene. Isotactic poly(propylene oxide) contains no symmetry element, is not superposable on its mirror image, and possesses optical activity. The syndiotactic polymer is incapable of optical activity since it possesses a mirror glide plane of symmetry.

The stereochemistry of step polymerization is considered now. Bond formation during step polymerization almost never results in the formation of a stereocenter. For example, neither the ester nor the amide groups in polyesters and polyamides, respectively, possess stereocenters. Stereoregular polymers are possible when there is a chiral stereocenter in the monomer(s) [Oishi and Kawakami, 2000; Orgueira and Varela, 2001; Vanhaecht et al., 2001]. An example would be the polymerization of (R) or (S)-H₂NCHRCOOH. Naturally occurring polypeptides are stereoregular polymers formed from optically active α-amino acids.

8-1d 1,3-Butadiene and 2-Substituted 1,3-Butadienes

8-1d-1 1,2- and 3,4-Polymerizations

The polymerization of a 1,3-diene such as 1,3-butadiene, isoprene, and chloroprene can lead to cis and trans isomers when polymerization occurs by a 1,4-polymerization. On the
other hand, 1,2-polymerization through one or the other double bond can yield isotactic, syndiotactic, or atactic polymers, for example, for 1,3-butadiene

\[
\text{CH}_2=\text{CH}-\text{CH}=\text{CH}_2 \rightarrow \left[ \text{CH}_2-\underbrace{\text{CH}}_{n} \right]
\]

The situation is exactly analogous to the polymerization of monosubstituted alkenes; the various polymer structures would be those in Fig. 8-1 with \( R = -\text{CH}=_\text{CH}_2 \). With chloroprene and isoprene, the possibilities are enlarged since the two double bonds are substituted differently. Polymerizations through the 1,2- and 3,4-double bonds do not yield the same product as they would in 1,3-butadiene polymerization. There are, therefore, a total of six structures possible—corresponding to isotactic, syndiotactic, and atactic structures for both 1,2- and 3,4-polymerizations; for instance, for isoprene, one has the situation shown in Eq. 8-2 with polymers \( V \) and \( VI \) capable of exhibiting the structures in Fig. 8-1 with \( R = -\text{CH}=_\text{CH}_2 \) = \( \text{CH}_2 \) and \( -\text{C(CH}_3_)=\text{CH}_2 \), respectively.

\[
\text{CH}_3 \\
\text{CH}_2=\text{C}=_\text{CH}=\text{CH}_2 \\
\left[ \text{CH}_2-\underbrace{\text{CH}}_{n} \right]
\]

1,2-Polymerization

\[
\text{CH}_3 \\
\text{CH}_2=\text{C}=_\text{CH}=\text{CH}_2 \\
\left[ \text{CH}_2-\underbrace{\text{CH}}_{n} \right]
\]

3,4-Polymerization

\[ (8-2) \]

**8-1d-2 1,4-Polymerization**

From the practical viewpoint, the more important products from 1,3-dienes are those that occur by 1,4-polymerization of the conjugated diene system, for example, for isoprene, we obtain

\[
\text{CH}_3 \\
\text{CH}_2=\text{C}=_\text{CH}=\text{CH}_2 \\
\left[ \text{CH}_2=\underbrace{\text{C}=_\text{CH}=_\text{CH}_2} \right]_n
\]

1,4-Polymerization leads to a polymer structure (VII) with a repeating alkene double bond in the polymer chain. The double bond in each repeating unit of the polymer chain is a site of steric isomerism since it can have either a cis or a trans configuration. The polymer chain segments on each carbon atom of the double bond are located on the same side of the double
bond in the cis configuration (VIII) and on opposite sides in the trans configuration (IX), for example, for polyisoprene.

When all of the double bonds in the polymer molecule have the same configuration, the result is two different ordered polymer structures—transstactic and cistatic. Figure 8-5 shows the structures of the completely cis and completely trans polymers of isoprene. The stereochemistry of these polymers is indicated in their names. For example, the trans polymer (IX) is named as trans-1,4-polyisoprene or poly(E-1-methylbut-1-ene-1,4-diyl). The first name is the IUPAC-recommended trivial name; the second name is the IUPAC structure-based (Sec. 1-2c) [IUPAC, 1966, 1981, 1996].

It should be noted that both carbon atoms of the double bond in VIII and IX are achirrotopic stereocenters. Interchange of the groups attached to one or the other carbon of the double bond converts VIII into IX and vice versa.

8-1e 1-Substituted and 1,4-Disubstituted 1,3-Butadienes

8-1e-1 1,2- and 3,4-Polymerizations

The polymerizations of 1-substituted (X) and 1,4-disubstituted (XI) 1,3-butadienes involve several possibilities. 3,4-Polymerization of a 1-substituted 1,3-butadiene proceeds with the
same possibilities as the polymerization of a monosubstituted ethylene such as propene. 1,2-Polymerization of a 1-substituted 1,3-butadiene (Eq. 8-4) as well as 1,2- and 3,4-polymerizations of a 1,4-disubstituted 1,3-butadiene (Eqs. 8-5 and 8-6) proceed with the same possibilities as 1,2-disubstituted ethylene.

\[
\text{CH}_2=\text{CH} \rightarrow \text{CH}_2=\text{CH} \quad (8-4)
\]

\[
\text{CH}_2=\text{CH} \rightarrow \text{CH}_2=\text{CH} \quad (8-5)
\]

\[
\text{CH}_2=\text{CH} \rightarrow \text{CH}_2=\text{CH} \quad (8-6)
\]

**8-1e-2 1,4-Polymerization**

The 1,4-polymerization of a 1-substituted 1,3-butadiene can yield four stereoregular polymer structures. The double bond can have cis or trans configurations, and each of these can be combined with isotactic or syndiotactic placement of R groups. (Other polymer structures, not referred to as stereoregular polymers, are possible with either random placement of double bonds or atactic placement of R groups.)

The all-trans–all-isotactic and all-trans–all-syndiotactic structures for the 1,4-polymerization of 1,3-pentadiene are shown in Fig. 8-6. In naming polymers with both types of stereoisomerism, that due to cis–trans isomerism is named first unless it is indicated after the prefix poly. Thus, the all-trans–all-isotactic polymer is named as transisotactic 1,4-poly(1,3-pentadiene) or isotactic poly(E-3-methylbut-1-ene-1,4-diy1).

The \(sp^3\) stereocenter (i.e., \(C^*\)) in XII is chirotopic, like the case of poly(propylene oxide), since the first couple of atoms of the two chain segments are considerably different. The isotactic structures are optically active while the syndiotactic structures are not optically active.

The 1,4-polymerization of 1,4-disubstituted 1,3-butadienes leads to structure (XIII), which can exhibit tritacticycity since the repeating unit contains three sites of steric
isomerism—a double bond and the carbons holding R and R₀ substituents. Several different stereoregular polymers are possible with various combinations of ordered arrangements at the three sites. For example, polymer XIV possesses an erythrodiisotactic arrangement of R and R₀ groups and an all-trans arrangement of the double bonds. The polymer is named transerythrodiisotactic 1,4-poly(methyl sorbate) or diisotactic poly[erythro-3-(methoxycarbonyl)-4-E-methylbut-1-ene-1,4-diyl].

All four diisotactic polymers (cis and trans, erythro and threo) are chiral and possess optical activity. Each of the four disyndiotactic polymers possesses a mirror glide plane and is achiral. For symmetric 1,4-disubstituted 1,3-butadienes (R = R₀), only the cis and transthreo-diisotactic structures are chiral. Each of the erythrodiisotactic and threodisyndiotactic polymers has a mirror glide plane. Each of the erythrodisyndiotactic polymers has a mirror glide plane.

8-1f Other Polymers

The polymerization of the alkyne triple bond (Secs. 5-7d and 8-6c) and ring-opening metathesis polymerization of a cycloalkene (Secs. 7-8 and 8-6a) yield polymers containing double bonds in the polymer chain. Cis–trans isomerism is possible analogous to the 1,4-polymerization of 1,3-dienes.
Polymers containing rings incorporated into the main chain (e.g., by double-bond polymerization of a cycloalkene) are also capable of exhibiting stereoisomerism. Such polymers possess two stereocenters—the two atoms at which the polymer chain enters and leaves each ring. Thus the polymerization of cyclopentene to polycyclopentene [IUPAC: poly(cyclopentane-1,2-diyl)] is considered in the same manner as that of a 1,2-disubstituted ethylene. The four possible stereoregular structures are shown in Fig. 8-7. The erythro polymers are those in which there is a cis configuration of the polymer chain bonds entering and leaving each ring; the threo polymers have a trans configuration of the polymer chain bonds entering and leaving each ring. The threodiisotactic structure is chiral while the other three structures are achiral. The situation is different for an asymmetric cycloalkene such as 2-methylcyclopentene where both diisotactic structures are chiral, while both disyndiotactic structures are achiral.

Fig. 8-7 Stereoregular forms of polycyclopentene.
8-2 PROPERTIES OF STEREOREGULAR POLYMERS

8-2a Significance of Stereoregularity

The occurrence of stereoisomerism in polymers plays a major role in their practical utilization. There are very significant differences in the properties of unordered and ordered polymers as well as in the properties of ordered polymers of different types (cis versus trans, isotactic versus syndiotactic). The ordered polymers are dramatically different from the corresponding unordered structures in morphological and physical properties.

8-2a-1 Isotactic, Syndiotactic, and Atactic Polypropenes

The regularity or lack of regularity in polymers affects their properties by way of large differences in their abilities to crystallize. Atactic polymers are amorphous (noncrystalline), soft (“tacky”) materials with lower physical strength. The corresponding isotactic and syndiotactic polymers are usually obtained as highly crystalline materials. The ordered structures are capable of packing into a crystal lattice, while the unordered structures are not. Crystallinity leads to high physical strength and increased solvent and chemical resistance as well as differences in other properties that depend on crystallinity. The prime example of the industrial utility of stereoregular polymers is polypropene. Isotactic polypropene is a high-melting (165°C), strong, crystalline polymer, which is used as both a plastic and fiber (Sec. 8-11) [Juran, 1989; Lieberman and Barbe, 1988]. The annual United States production of isotactic polypropene was about 16 billion pounds in 2001. Atactic polypropene is an amorphous material with an oily to waxy soft appearance that finds use in asphalt blends and formulations for lubricants, sealants, and adhesives, but the volumes are minuscule compared to that of isotactic polypropene.

While the properties and applications of isotactic polymers have been extensively studied, those of syndiotactic polymers received less attention until relatively recently. The reason is the relative ease of forming isotactic polymers. Syndioselective polymerizations were less frequently encountered or proceeded with less efficiency compared to isoselective polymerizations. But the situation is changing fast as initiators and reaction conditions have been developed for syndioselective polymerizations. In the case of polypropene, the properties of the syndiotactic polymer have been examined [Youngman and Boor, 1967]. Syndiotactic polypropene, like its isotactic counterpart, is easily crystallized, but it has a lower $T_m$ by about 20°C and is more soluble in ether and hydrocarbon solvents.

8-2a-2 Cis- and Trans-1,4-Poly-1,3-Dienes

Stereoisomerism in 1,4-poly-1,3-dienes results in significant differences in the properties of the cis and trans polymers. The trans isomer crystallizes to a greater extent as a result of higher molecular symmetry and has higher $T_m$ and $T_g$ values (Table 8-1). These trends are

| Table 8-1 Glass Transition and Crystalline Melting Temperatures$^a$ |
|-----------------|-----|-----|
| Polymer         | Isomer | $T_g$ (°C) | $T_m$ (°C) |
| 1,4-Polybutadiene | Cis    | $-95$  | $6$    |
|                 | Trans  | $-83$  | $145$  |
| 1,4-Polyisoprene | Cis    | $-73$  | $28$   |
|                 | Trans  | $-58$  | $74$   |

$^a$ Data from Brandrup et al. [1999].
the same as for small molecules such as cis- and trans-2-butenes. The differences in the cis and trans polymers leads to major differences in their properties and utilization. Thus, cis-1,4-polyisoprene has very low crystallinity, has low $T_g$ and $T_m$ values, and is an excellent elastomer over a considerable temperature range, which includes ambient temperatures. About 2 billion pounds per year of cis-1,4-polyisoprene are used in the United State for tires, footwear, gloves, molded objects, adhesives, rubber bands, and other typical elastomer applications. trans-1,4-Polyisoprene is a much harder, much less rubbery polymer since it has relatively high $T_g$ and $T_m$ values and significant crystallinity. It is less an elastomer and more like a thermoplastic. trans-1,4-Polyisoprene has very good resistance to abrasion and is used in golf-ball covers and orthopedic devices. 1,4-Polyisoprene is found in nature in both the cis and trans forms. Hevea rubber, obtained from the Hevea brasiliensis tree (in Brazil, Indonesia, Malaysia, Sri Lanka), is the major naturally occurring 1,4-polyisoprene. It contains more than 98% of the double bonds in the cis configuration. (Over 90% of all cis-1,4-polyisoprene used commercially is the natural Hevea rubber.) cis-1,4-Polyisoprene is also found in the guayule bush. Other trees, mostly in Central America and Malaysia, yield gutta percha or balata rubber, which is predominantly the trans isomer.

8-2a-3 Cellulose and Amylose

The isomeric polysaccharides amylose (a component of starch) and cellulose also show the significance of stereoisomerism on polymer properties. Cellulose and amylose have the structures shown in Fig. 8-8. (Amylopectin, the other component of starch, has the same structure as amylose except that it is branched at carbon 6.) Both are polymers of glucose in which the
glucose units are joined together by glycoside linkages at carbons 1 and 4. The two polysaccharides differ only in the configuration at carbon 1.

In terms of the nomenclature used for stereoregular polymers, cellulose has a threodis syndiotactic structure while amylose is erythrodisotactic. In the nomenclature of carbohydrate chemistry, cellulose consists of β-1,4-linked D-glucopyranose chains and amylose of α-1,4-linked D-glucopyranose chains. The 1,4-linkage is trans (diequatorial) in cellulose and cis (equatorial–axial) in amylose. The difference in structure results in amylose existing in a random-coil conformation while cellulose exists in an extended-chain conformation. This leads to closer packing of polymer molecules with much greater intermolecular attractive forces and crystallinity in cellulose relative to amylose (and also amylpectin). Cellulose, compared to amylose, has good physical strength and mechanical properties, decreased solubility, and increased stability to hydrolysis. The result is that cellulose is used as a structural material both in nature (plants) and by people. Although starch is not useful as a structural material, it does serve important functions as a food source and storage form of energy for both plants and animals. The structure of each polysaccharide is uniquely fitted to its biological function in nature.

8-2b Analysis of Stereoregularity

Infrared spectroscopy has been used for quantitatively measuring the amounts of 1,2-, 3,4-, cis-1,4-, and trans-1,4-polymers in the polymerization of 1,3-diienes; its use for analysis of isotactic and syndiotactic polymer structures is very limited [Coleman et al., 1978; Tosi and Ciampelli, 1973]. Nuclear magnetic resonance spectroscopy is the most powerful tool for detecting both types of stereoisomerism in polymers. High-resolution proton NMR and especially $^{13}$C NMR allow one to obtain considerable detail about the sequence distribution of stereoisomeric units within the polymer chain [Bovey, 1972, 1982; Bovey and Mirau, 1996; Tonelli, 1989; Zambelli and Gatti, 1978].

Consider the description of the sequence distribution of isotactic and syndiotactic placements in the polymerization of a monosubstituted ethylene. The approach is general and can be applied with appropriate modification to the 1,4-polymerization of a 1,3-diene. **Dyad tacticity** is defined as the fractions of pairs of adjacent repeating units that are isotactic or syndiotactic to one another. The isotactic and syndiotactic dyads (XV) are usually referred to as meso and racemic dyads. The horizontal line in XV represents a segment of the polymer chain, and each vertical line represents the configuration at the stereocenter in a repeating unit. The fractions of isotactic and syndiotactic dyads are referred to as \( m \) and \( r \) or \( i \).
Triad tacticity describes isotactic, syndiotactic, and heterotactic triads (XVI) whose fractions are designated as \((mm)\), \((rr)\), and \((mr)\), or \(I\), \(S\), and \(H\), respectively.

These definitions are clarified by considering a portion of a polymer chain such as XVII. Chain segment XVII has a total of 9 repeating units but only 8 dyads and 7 triads. There are 6 meso dyads and 2 racemic dyads; \(\langle m \rangle = \frac{3}{4}\), \(\langle r \rangle = \frac{1}{4}\). There are 4 isotactic, 2 heterotactic, and 1 syndiotactic triads; \(\langle mm \rangle = \frac{4}{7}\), \(\langle mr \rangle = \frac{2}{7}\), \(\langle rr \rangle = \frac{1}{7}\).

The dyad and triad fractions each total unity by definition, that is

\[
\langle m \rangle + \langle r \rangle = 1 \tag{8-10}
\]

\[
\langle mm \rangle + \langle rr \rangle + \langle mr \rangle = 1 \tag{8-11}
\]

and the two are related by

\[
\langle m \rangle = \langle mm \rangle + 0.5\langle mr \rangle \tag{8-12}
\]

\[
\langle r \rangle = \langle rr \rangle + 0.5\langle mr \rangle \tag{8-13}
\]

It is clear that a determination of any two triad fractions allows a complete definition of both the triad and dyad structures of a polymer via Eqs. 8-10 through 8-13. An atactic polymer is one in which \(\langle r \rangle = \langle m \rangle = 0.5\) and \(\langle mm \rangle = \langle rr \rangle = 0.25\), \(\langle mr \rangle = 0.5\) with a random distribution of dyads and triads. The (all-) isotactic polymer has \(\langle m \rangle = \langle mm \rangle = 1\). The (all-) syndiotactic polymer is defined by \(\langle r \rangle = \langle rr \rangle = 1\). For random distribution with \(\langle m \rangle \neq \langle r \rangle \neq 0.5\) or \(\langle mm \rangle \neq \langle rr \rangle \neq 0.25\), one has different degrees of syndiotacticity or isotacticity. Isotacticity predominates when \(\langle m \rangle > 0.5\) and \(\langle mm \rangle > 0.25\) and syndiotacticity predominates when \(\langle r \rangle > 0.5\) and \(\langle rr \rangle > 0.25\). These polymers are random tactic polymers, containing random placement of isotactic and syndiotactic dyads and triads. When the distribution of dyads and triads is less than completely random, the polymer is a stereoblock polymer in which there are block (which may be short or long) of isotactic and syndiotactic dyads and triads.

The advent of high-resolution \(^{13}\text{C}\) NMR allows the determination of tetrad, pentad, and even higher sequence distributions in many polymers [Bovey, 1972; Bovey and Mirau, 1996; Farina, 1987]. The tetrad distribution consists of the isotactic sequence \(mm\), the syndiotactic sequence \(rr\), and the heterotactic sequences \(mrm\), \(mr\), \(rm\). The sum of the tetrad fractions is unity, and the following relationships exist:

\[
\langle mm \rangle = \langle mmm \rangle + 0.5\langle mmr \rangle \tag{8-14}
\]

\[
\langle rr \rangle = \langle rrr \rangle + 0.5\langle mrr \rangle \tag{8-15}
\]

\[
\langle mr \rangle = \langle mmr \rangle + 2\langle mrr \rangle = \langle mrr \rangle + 2\langle mmr \rangle \tag{8-16}
\]

The pentad distribution consists of the isotactic sequence \(mmmm\), the syndiotactic sequence \(rrrr\), and the heterotactic sequences \(mmmr\), \(mmrm\), \(mrrm\), \(rnrm\), \(rmrr\), \(mrrm\), \(rrmr\), \(mmrm\).
8-3 FORCES OF STEREOREGULATION IN ALKENE POLYMERIZATIONS

Consider the forces that actually operate for or against stereoselectivity in a polymerization. Alkene polymerizations are considered first. The extent of stereoselectivity in a polymerization depends on the relative rate at which an incoming monomer molecule is added with the same configuration as the preceding monomer unit compared to its rate of addition with the opposite configuration. Different forces determine the relative rates of the two modes of addition depending on whether the active end of a propagating chain is a free species (i.e., the chain end is free to rotate) or one that is coordinated (associated) with the initiator (or a component derived from the initiator). For free propagating species that are not coordinated, both modes of addition are possible. The stereoregularity of the polymer product is dependent primarily on the polymerization temperature, which determines the relative rates of the two modes of addition. The situation can be quite different when the propagating species is coordinated to the initiator. One or the other of the additions may be prevented or enhanced by the configuration of the coordination complex (usually consisting of the propagating chain end, initiator, and monomer). Under these circumstances coordination directs the mode of monomer addition in a stereoselective manner.

8-3a Radical Polymerization

Radical polymerizations involve free propagating species. The planar or nearly planar trigonal carbon atom does not have a specified configuration since there is free rotation about the terminal carbon–carbon bond (as indicated in Eq. 8-25 by the circular arrows). The configuration of a monomer unit in the polymer chain is not determined during its addition to the radical center but only after the next monomer unit adds to it. The situation can be depicted in Eq. 8-25 where the two placements—syndiotactic (Eq. 8-25a) and isotactic (Eq. 8-25b)—take place with the rate constants \( k_r \) and \( k_m \), respectively. Whether the same placement is propagated through successive additions of monomer units determines the stereoregularity of the final polymer molecule. The amount and type of stereoregularity are determined by the value of \( k_r/k_m \). Isotactic polymer is produced if this ratio is zero, syndiotactic polymer if it is infinity, and atactic polymer if it is unity. For \( k_r/k_m \) values between unity and infinity, the polymer is partially atactic and partially syndiotactic. For \( k_r/k_m \) values between zero and unity, the polymer is partially atactic and partially isotactic.

\[
\begin{align*}
\langle mnmr \rangle + 2\langle rmnr \rangle &= \langle mmrm \rangle + \langle mrrr \rangle \\
\langle mrrr \rangle + 2\langle mrmr \rangle &= \langle mmrm \rangle + \langle mmrr \rangle \\
\langle mmam \rangle &= \langle mmam \rangle + 0.5\langle mmnr \rangle \\
\langle mmr \rangle &= 0.5\langle mmrr \rangle + 0.5\langle mmrm \rangle \\
\langle rmr \rangle &= 2\langle mrmr \rangle + \langle mrrr \rangle = \langle mmrr \rangle + \langle rmrr \rangle \\
\langle rrr \rangle &= \langle rrrr \rangle + 0.5\langle mmrm \rangle \\
\end{align*}
\]
The value of $k_r/k_m$ is determined by the difference $\Delta \Delta G^\ddagger$ in the free energies of activation between the syndiotactic $\Delta G^\ddagger_r$ and isotactic $\Delta G^\ddagger_m$ placements

$$
\frac{k_r}{k_m} = \exp\left(\frac{-\Delta \Delta G^\ddagger}{RT}\right) = \exp\left\{\frac{\Delta \Delta S^\ddagger}{R} - \frac{\Delta \Delta H^\ddagger}{RT}\right\} \quad (8-26)
$$

with

$$
\Delta \Delta G^\ddagger = \Delta G^\ddagger_r - \Delta G^\ddagger_m \quad (8-27a)
$$

$$
\Delta \Delta S^\ddagger = \Delta S^\ddagger_r - \Delta S^\ddagger_m \quad (8-27b)
$$

$$
\Delta \Delta H^\ddagger = \Delta H^\ddagger_r - \Delta H^\ddagger_m \quad (8-27c)
$$

where $\Delta G^\ddagger_r$, $\Delta H^\ddagger_r$, $\Delta S^\ddagger_r$ respectively are the activation free energy, enthalpy, and entropy for syndiotactic placement and $\Delta G^\ddagger_m$, $\Delta H^\ddagger_m$, $\Delta S^\ddagger_m$ are the corresponding quantities for isotactic placement. Stereoregularity should be temperature-dependent with ordered structures favored at low temperatures [Huggins, 1944]. Calculations based on small molecules indicated that the differences in activation enthalpy $\Delta \Delta H^\ddagger$ and entropy $\Delta \Delta S^\ddagger$ between syndiotactic and isotactic placements are both expected to be small; $\Delta \Delta H^\ddagger$ is about $-4$ to $-8$ kJ mol$^{-1}$ and $\Delta \Delta S^\ddagger$ about $0$ to $-4$ J mol$^{-1}$ K$^{-1}$ [Fordham, 1959]. Syndiotactic placement is favored over isotactic placement primarily because of the enthalpy difference. The small energy differences between syndiotactic and isotactic placements have been confirmed for several monomers by studying the temperature dependence of tacticity [Bovey, 1972; Pino and Suter, 1976, 1977]. Thus, $\Delta \Delta H^\ddagger$ and $\Delta \Delta S^\ddagger$ are $-4.5$ kJ mol$^{-1}$ and $-4.2$ J mol$^{-1}$ K$^{-1}$, respectively, for methyl methacrylate and $-1.3$ kJ mol$^{-1}$ and $-2.5$ J mol$^{-1}$ K$^{-1}$, respectively, for vinyl chloride [Bovey et al., 1967; Fox and Schnecko, 1962].

The slight preference for syndiotactic placement over isotactic placement is a consequence of steric and/or electrostatic repulsions between substituents in the polymer chain. Repulsions between R groups, more specifically, between R groups on the terminal and penultimate units of the propagating chain, are minimized in the transition state of the propagation step (and also in the final polymer molecule) when they are located in the alternating arrangement of syndiotactic placement. The steric and electrostatic repulsions between R groups are maximum for isotactic placement. This mechanism (driving force) for syndioselective polymerization is referred to as polymer chain end control.
The difference in activation free energies for syndiotactic and isotactic placements leads to an increasing tendency toward syndiotacticity with decreasing polymerization temperature. Figure 8-9 shows the increase in the fraction of syndiotactic dyads, \((r)\), of poly(vinyl chloride) from 0.51 to 0.67 as the reaction temperature decreases from 120 to \(-78^\circ\text{C}\) [Talamini and Vidotto, 1967]. Corresponding data for methyl methacrylate show an increase in \((r)\) from 0.64 at 250\(^\circ\text{C}\) to 0.87 at \(-78^\circ\text{C}\) [Fox and Schnecko, 1962; Isobe et al., 2000; Otsu et al., 1966]. With decreasing temperature, the energy difference between syndiotactic and isotactic placements exerts a progressively increasing influence on the stereoselectivity of the polymerization; at high temperatures, their effects are progressively diminished.

Since radical polymerizations are generally carried out at moderately high temperatures, most of the resulting polymers are highly atactic. This does not mean that there is a complete absence of syndiotacticity. There is a considerable difference in the extent of syndiotacticity from one polymer to another. Thus, methyl methacrylate has a much greater tendency toward syndiotactic placement than vinyl chloride. Whereas the poly(vinyl chloride) produced at the usual commercial polymerization temperature (\(\sim 60^\circ\text{C}\)) is essentially completely atactic, that is, \((r) \simeq (m) \simeq 0.5\), this is not the case for poly(methyl methacrylate). The polymerization of MMA, usually carried out at temperatures up to 100\(^\circ\text{C}\), yields polymers with appreciable syndiotacticity—\((r)\) is 0.73 at 100\(^\circ\text{C}\). The difference is a consequence of the fact that MMA is a 1,1-disubstituted ethylene, leading to greater repulsions between substituents in adjacent monomer units.

There have been efforts to enhance stereoselectivity in radical polymerization by using fluoroalcohols or Lewis acids that complex with monomers such as MMA and vinyl acetate [Isobe et al., 2000, 2001a; Okamoto et al., 2002]. In almost all instances the effects are nil or very small. For example, the use of perfluoro-\(t\)-butyl alcohol as solvent instead of toluene changes \((rr)\) from 0.89 to 0.91 in the polymerization of MMA at \(-78^\circ\text{C}\). An exception is in the polymerization of acrylamide in the presence of some rare-earth Lewis acids such as ytterbium triflate. The polymer is atactic at 0\(^\circ\text{C}\), \((m) = 0.46\), in the absence of the Lewis acid, but significantly isotactic, \((m) = 0.80\), in the presence of the Lewis acid. The reason for this effect is unclear. More highly isoselective polymerization occurs in some radical polymerizations of MMA (Sec. 8-14b).
For ionic chain polymerizations in solvents with high solvating power where solvent-separated ion-pair- or free-ion-propagating species are involved, the factors governing the stereochemistry of the reaction are similar to those for radical polymerization. Syndiotactic polymerization is increasingly favored as the polymerization temperature is lowered. When polymerizations are carried out in solvents with poor solvating power, there is extensive coordination among the initiator, propagating chain end, and monomer, and the stereochemical result can be quite different. In the usual case, propagation is prevented from taking place by one or the other of the two placements (R- or S-) as coordination becomes the dominant driving force for stereoselectivity in the polymerization. The \( k_r/k_m \) ratio tends toward a value of zero, and isoselective polymerization occurs. Coordination can yield syndioselective polymerization in some systems. Table 8-2 shows some examples of the early stereoselective polymerizations. The MMA and isobutyl vinyl ether polymerizations involve initiators and reaction conditions discussed previously (Chap. 5) without consideration of stereochemistry.

The first reported instance of stereoselective polymerization was probably the cationic polymerization of isobutyl vinyl ether in 1947 [Schildknecht et al., 1947]. A semicrystalline polymer was obtained when the reaction was carried out at \(-80\) to \(-60^\circ\)C using boron trifluoride etherate as the initiator with propane as the solvent. The full significance of the polymerization was not realized at the time as the crystallinity was attributed to a syndiotactic structure. X-Ray diffraction in 1956 indicated that the polymer was isotactic [Natta et al., 1956a,b]. (NMR would have easily detected the isotactic structure, but NMR was not a routine tool in 1947.)

Stereoselective polymerization came into existence in the mid-1950s with the work of Ziegler in Germany and Natta in Italy. Ziegler was studying the reactions of ethylene catalyzed with trialkylaluminum at high temperatures and pressures. Both oligomerization to higher 1-alkenes and polymerization occurred. The highest polymer molecular weights achieved were 5000. The addition of a transition metal compound to trialkylaluminum had a dramatic effect on the polymerization. High-molecular-weight polyethylene (PE) was formed at low temperatures (50–100\(^\circ\)C) and low pressures [Ziegler, 1964; Ziegler et al., 1955]. This PE is much less branched and has property enhancements compared to PE

### Table 8-2 Stereoselective Polymerizations

<table>
<thead>
<tr>
<th>Monomer</th>
<th>Reaction Conditions</th>
<th>Polymer Structure</th>
</tr>
</thead>
<tbody>
<tr>
<td>Isobutyl vinyl ether</td>
<td>BF3 etherate in propane at (-80) to (-60^\circ)C</td>
<td>Isotactic</td>
</tr>
<tr>
<td>Methyl methacrylate</td>
<td>MgBr (30(^\circ)C) or (n)-C4H9Li ((-78) to (0^\circ)C in (\Phi)CH3)</td>
<td>Isotactic</td>
</tr>
<tr>
<td>Methyl methacrylate</td>
<td>(n)-C4H9Li in THF at (-78^\circ)C</td>
<td>Syndiotactic</td>
</tr>
<tr>
<td>Propene</td>
<td>TiCl4, (C2H5)3Al in (n)-heptane at 50(^\circ)C</td>
<td>Isotactic</td>
</tr>
<tr>
<td>Propene</td>
<td>VCl4, (C2H5)3Al, (\Phi)OCH3 in (\Phi)CH3 at (-78^\circ)C</td>
<td>Syndiotactic</td>
</tr>
</tbody>
</table>

\(^a\) Data from Schildknecht et al. [1947].
\(^b\) Data from Yuki et al. [1975].
\(^c\) Data from Natta et al. [1958].
\(^d\) Data from Zambelli et al. [1963].
produced by radical polymerization; see Sec. 8-11). Natta used Ziegler’s initiators to achieve stereoselective polymerizations (both isoselective and syndioselective) of propene and other 1-alkenes (α-olefins) [Natta, 1965]. This was a huge achievement since α-olefins cannot be polymerized to high-molecular-weight polymer by radical or other ionic initiators (Secs. 3-7c, 5-2b). The scientific and practical significance of their work earned Natta and Ziegler the joint award of the 1963 Nobel Prize in Chemistry [Mulhaupt, 2003].

The work of Ziegler and Natta led to the development of a very large number of two-component initiator systems consisting of an organometallic compound or hydride of a group I–III metal together with a halide or other derivative of a group IV–VIII transition metal [Pasquon et al., 1989]. The polymerizations are generally carried out in a hydrocarbon solvent such as n-hexane. The more important component of the initiator system is the transition metal compound. The function of the group I–III metal compound is to modify and activate the transition metal compound for initiation. Some of the compounds used as the group I–III metal component are triethylaluminum, diethylaluminum chloride, and diethylzinc; titanium trichloride or tetrachloride, vanadium trichloride, and chromium triacetylacetonate are examples of the transition metal component [Choi and Ray, 1985; Corradini et al., 1989; Pino et al., 1987; Tait, 1989]. These initiator systems are the traditional Ziegler–Natta initiators. The actual initiator species have not been isolated, and their structures are not well understood. One mixes the two components, perhaps adds some other compounds for enhancements in reactivity and/or stereoselectivity, and then adds the mixture (which usually is heterogeneous) to the monomer—the result is enormously useful stereoselective polymerizations. These were still the initiators used in more than 95% of commercial processes in 2002.

Since the mid-1980s there has been another revolution—the discovery and development of metallocene initiators—within the Ziegler–Natta revolution. Bis(cyclopentadienyl)titanium dichloride and bis(indenyl)zirconium dichloride are examples of simple metallocene initiators. More complex metallocenes have substituents on the organic ligands and the ligands are joined together through —CH₂CH₂— and other bridges. The metallocene initiators, unlike the traditional Ziegler–Natta initiators, are molecules that can be isolated, analyzed by techniques such as NMR, and purified. Metallocene initiators are also homogeneous in the reaction systems. They offer the potential for tailor-making initiators to perform highly stereoselective polymerizations of specific monomers. Utilization of the metallocene initiators requires the addition of a group I–III metal compound, as in the case of the traditional Ziegler–Natta initiators.

Some clarification is needed regarding terminology. The metallocene initiators are a type of Ziegler–Natta initiator, derived from a combination of a transition and group I–III metal compounds. However, the growing importance of metallocenes leads us to distinguish them from the traditional Ziegler–Natta initiators by using the term metallocene. All of these initiators can be considered as coordination initiators, initiators that perform stereoselectively due to coordination. This term includes initiators other than the Ziegler–Natta and metallocene initiators; examples are n-butyllithium, phenylmagnesium bromide, and boron trifluoride. Polymerizations brought about by coordination initiators are referred to as coordination polymerizations. The terms isoselective and syndioselective are used to describe initiators and polymerizations that produce isotactic and syndiotactic polymers, respectively.

8-3b-2 Mechanism of Stereoselective Placement

Coordination initiators perform two functions. First, they supply the species that initiates the polymerization. Second, the fragment of the initiator aside from the initiating portion has unique coordinating powers. Coordination of this fragment (which may be considered as
the counterion of the propagating center) with both the propagating chain end and the incoming monomer occurs so as to orient the monomer with respect to the growing chain end and bring about stereoselective addition. Many different mechanisms have been advanced to explain the usual isotactic placement obtained with coordination initiators [Corradini et al., 1989; Kuran, 2001; Tait and Watkins, 1989]. Stereoselective polymerization is a concerted, multicentered reaction. Figure 8-10 depicts the general situation for an anionic coordination polymerization proceeding with isotactic placement. The polymer chain end has a partial negative charge with the initiator fragment G (the counterion) having a partial positive charge. (Cationic coordination polymerization involves a similar mechanism except for reversal of the signs of the partial charges.) The initiator fragment G is coordinated with both the propagating chain end and the incoming monomer molecule.

Monomer is oriented and “held in place” by coordination during addition to the polymer chain. Coordination between the initiator fragment and the propagating center is broken simultaneously with the formation of bonds between the propagating center and the new monomer unit and between the initiator fragment and the new monomer unit. Propagation proceeds in the four-center cyclic transition state by the insertion of monomer between the initiator fragment and the propagating center. The initiator fragment essentially acts as a template or mold for the successive orientations and isotactic placements of the incoming monomer units. Isotactic polymerization occurs because the initiator fragment forces each monomer unit to approach the propagating center with the same face. This mechanism is referred to as catalyst (initiator) site control or enantiomorphic site control. For the polymerization described in Fig. 8-10, monomer approaches the propagating center with its re face facing the propagating center. The face of a monomer molecule is labeled as the re face if viewing that face of the molecule shows the groups attached to the CHR carbon decreasing in priority in a clockwise manner (=C > R > H). The opposite face is the si face, in which
priorities decrease in a counterclockwise manner when the face is viewed from the propagating center. The re and si faces of a monomer such as propene are enantiotopic; that is, the products formed by additions of a propagating center to the two faces have opposite configurations. (The term prochiral has been used for a carbon atom such as the CHR carbon of a monomer molecule to indicate additions to the si and re face yield, respectively, one enantiomer or the other of a pair of enantiomers.) The description in Fig. 8-10 for isotactic polymerization could also have been shown with the R and H groups of the last monomer unit in the polymer chain reversed (R in back and H in front), in which case isotactic propagation consists of monomer always approaching the propagating center with its si face.

The property of the initiator fragment that forces successive placements of monomer to occur with the same face is chirality. There is a stereochemical “fit” between initiator and monomer, which overrides the usual tendency toward moderate syndiotacticity. The initiator in isotactic polymerization is usually a racemic mixture of two enantiomers. One of the enantiomers yields isotactic polymer by forcing all propagations via the re face of monomer; the other enantiomer, via the si face. The isotactic polymer structures formed from the enantiomeric initiators are the same polymer; that is, they are superposable (ignoring the effects of end groups) for most monomers. (Exceptions are some ring-opening polymerizations, e.g., propylene oxide, and 1,4-polymerizations of some substituted 1,3-dienes, e.g., 1,3-pentadiene, where the two isotactic polymers are enantiomeric.) Isoselective initiators of the traditional Ziegler–Natta type are heterogeneous, with chirality attributable to the chiral crystal lattice in the vicinity of the initiator active center. The chirality of the homogeneous metallocene initiators resides in their molecular structures; thus, the initiator molecule is chiral.

Some chiral initiators have structures such that alternate monomer placements occur with opposite faces of the monomer to yield the syndiotactic polymer. This is syndioselective polymerization proceeding with catalyst site control and is usually observed only with some homogeneous initiators, both traditional Ziegler–Natta and metallocene.

When the initiator is achiral, the active sites can coordinate equally well (more or less) with either face of the incoming monomer. This generally results in either atactic or syndiotactic polymers depending on the specific interaction of the initiator fragment G, polymer chain end, and incoming monomer as well as the reaction temperature. Syndioselective polymerization occurs in systems where coordination accentuates the repulsive interactions between substituents on the polymer chain end and incoming monomer. The driving force for syndiotactic placement is similar to that previously described for low-temperature polymerizations with free propagating centers, but the initiator exaggerates the situation. Instead of obtaining a polymer with moderate syndiotacticity, say, 60% syndiotactic polymer, one may obtain 80% or 90% or higher syndiotacticity. The syndiotacticity increases with decreasing polymerization temperature.

The exact nature of the initiator needed for isoselective polymerization differs depending on the monomer. The ease of imposing catalyst site control on the entry of a monomer unit into the polymer chain increases with the ability of the monomer to coordinate with initiator and this depends on monomer polarity. Monomers, such as (meth)acrylates and vinyl ethers, with polar functional groups take a strong role in the coordination process. Ethylene, α-olefins, and other alkenes without polar functional groups have poorer coordinating power. The result is that nonpolar monomers require the use of initiators with very strong coordinating power for isoselective polymerization. For the traditional Ziegler–Natta initiators, this requires heterogeneous initiators to impose the most severe restriction on entry of a monomer into the propagating chain. Soluble traditional Ziegler–Natta initiators can yield only atactic and syndiotactic polymers. Heterogeneity is not required for isoselective polymerization with the metallocene initiators. The required level of coordination can be achieved through the appropriate structure of the metallocene.
For polar monomers, heterogeneity is seldom a requirement for isoselective polymerization with traditional Ziegler–Natta initiators; syndiotactic polymers are obtained only with the soluble initiators. Styrene and 1,3-dienes are intermediate in behavior between the polar and nonpolar monomer. These monomers undergo isoselective polymerization with both homogeneous and heterogeneous traditional Ziegler–Natta initiators.

8-4 TRADITIONAL ZIEGLER–NATTA POLYMERIZATION OF NONPOLAR ALKENE MONOMERS

Since the original discoveries of Ziegler and Natta, there have been many hundreds of different combinations of transition and group 1–III metal components, often together with an added electron donor, studied for use in alkene polymerizations. The resulting initiators exhibit a range of behaviors in terms of activity (reactivity) and stereoselectivity. Activity is often expressed as kg polymer formed per gram (or mole) of transition metal (or transition metal compound). Sometimes it is given as the activity per hour and sometimes it is given as the activity per polymerization run. The term productivity is often used as a synonym for activity.

Modification of an initiator system to increase activity has often come at the expense of stereoselectivity. The great utility of the Ziegler–Natta initiator system is the ability to change one or another of the components, or to add additional components (usually electron donors) to achieve very high stereoselectivity with high activity. The choice of the initiator components evolved in an empirical manner because of a less-than-complete understanding of the detailed structure of these initiators and the mechanism of their stereoselectivity.

8-4a Historical Development of Ziegler–Natta Initiators

Various mechanisms have been proposed to explain the stereoselectivity of Ziegler–Natta initiators [Boor, 1979; Carrick, 1973; Corradini et al., 1989; Cossee, 1967; Ketley, 1967a,b; Tait and Watkins, 1989; Zambelli and Tosi, 1974]. Most mechanisms contain considerable details that distinguish them from each other but usually cannot be verified. In this section the mechanistic features of Ziegler–Natta polymerizations are considered with emphasis on those features that hold for most initiator systems. The major interest will be on the titanium–aluminum systems for isoselective polymerization, more specifically, TiCl₃ with Al(C₂H₅)₂Cl and TiCl₄ with Al(C₂H₅)₃—probably the most widely studied systems, and certainly the most important systems for industrial polymerizations.

Before proceeding with the mechanistic consideration it is useful to review the evolution of the Ti-Al initiator system for industrial applications. The original initiator used by Ziegler for ethylene polymerization was obtained in situ as a precipitate on mixing the components TiCl₄ and Al(C₂H₅)₃ in a hydrocarbon solvent. The mixture was used directly for initiating polymerization. Natta, recognizing that the major product of the reaction was β-TiCl₃ (brown in color), explored various methods of preforming it outside the polymerization system, for example, by reduction of TiCl₄ with hydrogen, aluminum, and various alkylaluminum compounds. The stereoselectivity of these early initiator systems was low with isotactic indices of only 20–40% for polypropene. The isotactic index, a measure of the isotactic content of a polymer, is the percentage of the sample insoluble in a hydrocarbon solvent such as boiling n-heptane. This is not as informative a technique as high-resolution NMR since insoluble molecules may contain some syndiotactic and atactic sequences and soluble molecules may contain some isotactic sequences. It does, however, give a simple measure of isotactivity that is usually within about 10% of the value obtained from NMR, especially for highly isotactic samples.
There was a dramatic increase in stereoselectivity when the \( \alpha, \delta, \text{ or } \gamma \)-crystalline form of \( \text{TiCl}_3 \) (all violet in color) was used directly. The early generations of industrial processes used \( \text{TiCl}_3 \) together with \( \text{Al(C}_2\text{H}_5)_3 \) and/or \( \text{Al(C}_2\text{H}_5)_2\text{Cl} \). Over a two decade period starting in the late 1950s, the isotactic indices for polypropene increased to the low 90 percentile range. The initiator activity was enhanced by various ball milling and heat treatments of the initiator components before and after mixing. Ball milling involves mechanical grinding and not only increases surface area but also facilitates reactions between the initiator components. However, the activities were too low to allow the polymer products to be used without purification (by treatment with base or acid) to remove the residual metals, a process referred to as deashing. Also, optimization of the physical properties of the product often required removal of the atactic fraction. The initiator systems were inefficient with less than 1% of the Ti being active in polymerization. The later generations of initiators, starting in the late 1970s, increased initiator efficiency and activity without sacrificing stereoselectivity [Bohm, 2001; Busico and Cipullo, 2001; Cecchin et al., 2001; Chadwick, 2001; Chadwick et al., 2001; Chien et al., 1982; Hu and Chien, 1988]. The effective surface area of the active component of the initiator system was increased by close to 2 orders of magnitude by using \( \text{MgCl}_2 \) as a solid support in which \( \text{TiCl}_4 \) is finely dispersed. Stereoselectivity was kept high and actually increased by the addition of electron-donor additives.

A typical recipe for a present-day superactive or high-mileage initiator system involves ball milling of \( \text{MgCl}_2 \) (or the alkoxide) and \( \text{TiCl}_4 \) followed by the addition of \( \text{Al(C}_2\text{H}_5)_3 \) with an electron donor (such as dialkyl phthalate and alkoxysilane) usually added in each step of preparation. Activity is 50–200 kg polymer per gram of initiator system. Typically, the initiator system is no more than 2–4% Ti, which makes the activity about 1500–6000 kg polymer per gram of Ti. The high activity not only minimizes initiator and production costs but also avoids the costly task of initiator removal from the polymer product (except possibly for food- and medical-grade products). Isotactic indices for polypropene have been increased to 98% or higher with \( \text{mmmm} \) pentad fractions up to 98% and higher. This not only improves the product’s physical properties but also avoids the need to remove the atactic fraction.

### 8-4b Chemical Nature of Propagating Species

Some early polymerizations reported as Ziegler–Natta polymerizations were conventional free-radical, cationic, or anionic polymerizations proceeding with low stereoselectivity. Some Ziegler–Natta initiators contain components that are capable of initiating conventional ionic polymerizations of certain monomers, such as anionic polymerization of methacrylates by alkyllithium and cationic polymerization of vinyl ethers by \( \text{TiCl}_4 \).

Most Ziegler–Natta components participate in a complex set of reactions involving alkylolation and reduction of the transition-metal component by the group I–III component as shown below for \( \text{TiCl}_4 + \text{AIR}_3 \):

\[
\begin{align*}
\text{TiCl}_4 + \text{AIR}_3 & \rightarrow \text{TiCl}_3\text{R} + \text{AIR}_2\text{Cl} \quad (8-28) \\
\text{TiCl}_4 + \text{AIR}_2\text{Cl} & \rightarrow \text{TiCl}_3\text{R} + \text{AIRCl}_2 \quad (8-29) \\
\text{TiCl}_3\text{R} + \text{AIR}_3 & \rightarrow \text{TiCl}_2\text{R}_2 + \text{AIRCl}_2 \quad (8-30) \\
\text{TiCl}_3\text{R} & \rightarrow \text{TiCl}_3 + \text{R}\cdot \quad (8-31) \\
\text{TiCl}_3 + \text{AIR}_3 & \rightarrow \text{TiCl}_2\text{R} + \text{AIR}_2\text{Cl} \quad (8-32) \\
\text{R}\cdot & \rightarrow \text{combination} + \text{disproportionation} \quad (8-33)
\end{align*}
\]
Radicals produced in Eq. 8-31 are capable of initiating radical polymerizations with some monomers, for example, vinyl chloride.

The mechanism for the stereoselective polymerization of \( \alpha \)-olefins and other nonpolar alkenes is a \( \pi \)-complexation of monomer and transition metal (utilizing the latter’s \( d \)-orbitals) followed by a four-center anionic coordination insertion process in which monomer is inserted into a metal–carbon bond as described in Fig. 8-10. Support for the initial \( \pi \)-complexation has come from ESR, NMR, and IR studies [Burfield, 1984]. The insertion reaction has both cationic and anionic features. There is a concerted nucleophilic attack by the incipient carbanion polymer chain end on the \( \alpha \)-carbon of the double bond together with an electrophilic attack by the cationic counterion on the alkene \( \pi \)-electrons.

The anionic character of the polymerization is consistent with the polymerization rate decreasing in the order ethylene > propene > 1-butene [Bier, 1961; Boor, 1967]. The reverse order is expected for a polymerization involving the conversion of a monomer into the corresponding carbocation. For addition of a carbanion to the monomers, attack occurs at the \( \alpha \)-carbon to form the less substituted (and more stable) carbanion. Further, \( \alpha \)-substituents sterically hinder the approach of a carbanion and/or counterion with the result that reactivity decreases with increasing substituent size. Evidence for the anionic nature of propagation also comes from studies in which labeled methanol is used to terminate chain growth. The terminated polymer is radioactive when CH\( _3\)O\( _3\)H is used, while termination by \( ^{14}\)CH\( _3\)OH yields a nonradioactive polymer [Burfield and Savariar, 1979; Zakharov et al., 1977]. Additional verification comes from experiments with \( ^{14}\)CO and \( ^{14}\)CO\( _2\) [Mejzlik and Lesna, 1977].

8-4c Primary versus Secondary Insertion; Regioselectivity

The insertion reaction shown in Fig. 8-10 is primary insertion (or 1,2-addition)—the unsubstituted end of the double bond carries the partial negative charge and is attached to the counterion G. The other possibility is second insertion (or 2,1-addition) where the substituted end of the double bond becomes attached to G. The two modes of insertion are described by

\[
\begin{align*}
\text{primary insertion:} & \\
\text{second insertion:} & \\
\end{align*}
\]

Analysis for the mode of insertion involves the simultaneous determination of the degree of regioselectivity. \(^{13}\)C NMR analysis shows isoselective polymerization of propene to be very highly regioselective [Doi, 1979a,b; Doi et al., 1979; Natta et al., 1956a,b; Zambelli et al., 1979, 1982a,b]. There are no detectable regioirregular placements in the isotactic fractions (the fractions insoluble in boiling \( n \)-heptane). The soluble fractions, containing varying degrees of syndiotactic and atactic sequences, show 0.1–5% regioirregular placements. The insertion mode is determined by analysis of the monomer units adjacent to the polymer end group derived from the initiator. The NMR analysis, greatly enhanced by the use of \(^{13}\)C-enriched Al(\(^{13}\)CH\( _2\)CH\( _3\))\(_3\), shows that primary insertion occurs exclusively in isoselective polymerization. This is the expectation for a propagating carbanion—the less substituted carbanion is more stable.

Syndioselective polymerizations of propene are somewhat less regioselective than the isoselective reactions, with the typical highly syndiotactic polymer showing a few percent of the monomer units in head-to-head placement [Doi, 1979a,b; Doi et al., 1984a,b, 1985; Zambelli et al., 1974, 1987]. The mode of insertion is secondary, contrary to what is expected for a carbanion propagating center. Apparently, steric requirements imposed by the counterion derived from the initiator force propagation to proceed by secondary insertion.
8-4d Propagation at Carbon–Transition Metal Bond

Both the transition metal–carbon bond and the group I–III metal–carbon bond have been proposed as the site at which propagation occurs. However, the available evidence clearly points to propagation at the transition metal–carbon bond. The most significant evidence is that the group I–III metal component alone does not initiate polymerization, but the transition metal component alone does [Ballard, 1973; Giannini et al., 1970; Karol et al., 1978; Kohara et al., 1979; Matlack and Breslow, 1965; Soga and Yanagihara, 1988a,b; Soga et al., 1977]. Among the heterogeneous initiators that achieve polymerization of ethylene and ø-olefins are those obtained by ball milling of a transition metal alone or together with an alkyl halide, I₂, or H₂. Activity and stereoselectivity are low in the absence of the group I–III metal component.

The group I–III metal component increases activity and stereoselectivity by alkylation (often together with reduction) (Eqs. 8-28 through 8-32) of the transition metal component to form more active and stereoselective reaction sites. The group I–III metal component may also be involved in stabilizing the active transition metal sites by complexation and may be part of the counterion structure.

8-4e Mechanism of Isoselective Propagation

A variety of structures have been proposed for the active species in Ziegler–Natta initiator systems [Allegra, 1971; Arlman and Cossee, 1964; Corradini et al., 1989; Natta, 1960a,b; Patat and Sinn, 1958; Rodriguez and van Looy, 1966; Tait and Watkins, 1989]. Structure XX is generally considered as the active species formed from titanium chloride and alkylaluminum components. The □ in the structure represents an unoccupied (vacant) site of the octahedral titanium complex. XX represents an active titanium site at the surface of a TiCl₃ crystal after modification by reaction with the alkylaluminum component. The titanium atom shares four chloride ligands with its neighboring titanium atoms and has an alkyl ligand (incorporated via exchange of alkyl from the alkylaluminum for chloride) and a vacant orbital. There are molecular mechanics calculations that indicate dimeric Ti₂Cl₆ may be the active species instead of monomeric TiCl₃ [Monaco et al., 2000]. Other proposals for the active species include bimetallic species that contain both titanium and aluminum [Liu et al., 2002]. To simplify matters, our discussions will center on the monomeric and monometallic titanium species, especially since the mechanistic details of stereoselectivity and activity are essentially the same for both monomeric and dimeric titanium species as well as titanium–aluminum species.

The high-mileage supported initiators previously mentioned involve a species similar to XX as part of a mixed titanium–magnesium–chloride lattice, usually involving Mg–Cl–Ti bonds. Ti and Mg are interchangeable within the metal lattice.

Figure 8-11 shows the proposed mechanism for isoselective propagation. Monomer coordinates at the vacant site of titanium, resulting in a four-center transition state and subsequent insertion of monomer into the polymer–transition metal bond. The insertion is referred to as migratory insertion since the polymer chain migrates from its original site to that occupied...
by monomer. The whole polymer chain does not migrate, only the active end of the polymer chain migrates. This follows the principle of least nuclear motions. For the polymer chain to remain at its original coordination site after monomer insertion, all or at least most of the polymer chain atoms must move, specifically back away from the coordination site. For migratory insertion only the atoms of the first few repeat units move.

This regenerates a vacant site with its configuration opposite from the original vacancy. If propagation continued with this species, the result might be syndioselective propagation. Isoselective propagation requires migration of the polymer chain to its original position with regeneration of the original configuration of the vacant site, often referred to as back-skip or back-flip. The chain migrates twice for insertion of each monomer unit, and the overall process can also be regarded as a site epimerization. This mechanism, referred to as the
Cossee-Arlman mechanism, is based on the observed stereoselectivity and molecular modeling studies [Arlman and Cossee, 1964; Ewen, 1999; Rappe et al., 2000; Resconi et al., 2000]. A variation on this mechanism involves a lowering of the transition state barrier to insertion by an $\alpha$-agostic interaction, specifically, an attractive interaction between titanium and a hydrogen on the first carbon attached to Ti.

Isotactic polymerization depends intimately on the crystal structure of the initiator surface. For a coordination lattice, as opposed to a molecular crystal lattice, the crystal contains a number of ligand vacancies in order to achieve overall electrical neutrality of the crystal. $\alpha$-TiCl$_3$ crystals are made up of elementary crystal sheets of alternating titanium and chlorine layers aligned along the principal crystal axis [Natta et al., 1961a,b,c,d]. Figure 8-12 is a representation of a portion of the crystal [Corradini et al., 1989]. The titanium and chlorine atoms are represented by solid black and open spheres, respectively. The titaniums are at the octahedral interstices of the chlorine lattice while chlorines are hexagonally close-packed. Every third titanium in the lattice is missing, that is, there is a vacancy in between pairs of titanium atoms. Vacancies are represented by $\square$ in Fig. 8-12.

Polymerization occurs at active sites found on the edges (surfaces) of elementary sheets of the crystal and not in the basal planes. This is supported by microscopic observations of polymer growth at the crystal edges [Cossee, 1967; Kollar et al., 1968a,b; Rodriguez and van Looy, 1966]. A titanium atom at the surface is bonded to only five chlorines instead of six because of the imposed requirement of electroneutrality. Of the five chlorines, four are more strongly bonded since they are bridged to other titanium atoms. The fifth, nonbridged chlorine may be replaced by an alkyl group when the titanium component interacts with the group I–III component. The octahedral vacancy remains as a vacancy.

Neighboring metal atoms (bridged by two chlorines) have opposite chirality [Allegra, 1971]. The two enantiomeric titaniums can be represented as XXI and XXII where one of

![Diagram of XXI and XXII](image_url)
the chlorine ligands has been replaced by R via alkylation by the group I–III metal component. Propagation occurs by coordination of monomer at the vacancy, migratory insertion into the Ti–R bond, and migration of the newly formed bond to regenerate the vacancy in the original configuration. Considering either XXI or XXII, coordination of monomer can occur through either of the two monomer enantiofaces (si or re), which results in two diastereomeric transition states. The two diastereomeric states give rise to the two possible placements of monomer units in the polymer chain—meso and racemo [Corradini et al., 1984, 1985; Zambelli et al., 1978, 1980].

The driving force for isoselective propagation results from steric and electrostatic interactions between the substituent of the incoming monomer and the ligands of the transition metal. The chirality of the active site dictates that monomer coordinate to the transition metal vacancy primarily through one of the two enantiofaces. Actives sites XXI and XXII each yield isotactic polymer molecules through nearly exclusive coordination with the re and si monomer enantioface, respectively, or vice versa. That is, we may not know which enantioface will coordinate with XXI and which enantioface with XXII, but it is clear that only one of the enantiofaces will coordinate with XXI while the opposite enantioface will coordinate with XXII. This is the catalyst (initiator) site control or enantiomorphic site control model for isoselective polymerization.

The enantiomorphic site control model attributes stereoselectivity in isoselective polymerization to the initiator active site with no influence of the structure of the propagating chain end. The mechanism is supported by several observations:

1. $^{13}$C NMR of isotactic polypropene shows the main error is pairs of racemic dyads instead of isolated racemic dyads (Table 8-3) [Heatley et al., 1969; Resconi et al., 2000; Wolfsgruber et al., 1975]. A stereerrror in the addition of a monomer molecule is immediately corrected when stereocontrol is by the chiral active site. If stereocontrol was due to the propagating chain end, an error would continue to propagate in an isotactic manner to yield a polymer, referred to as an isotactic stereoblock, containing long isotactic all-R and all-S stereoblocks on each side of the error.

2. $^{13}$C NMR of ethylene-propene copolymers of low ethylene content produced by initiators that yield isotactic polypropene shows that the isotactic propene units on each side of an ethylene unit have the same configuration (i.e., all-R or all-S) [Zambelli et al., 1971, 1978, 1979]. For stereocontrol by the propagating chain end, the amount of polymer in which the polypropene blocks on either side of an ethylene unit have the same configuration would equal that in which the blocks have the opposite configuration.

3. Statistical analysis of the stereochemical sequence distributions (Table 8-3 and Sec. 8-16) also supports the enantiomorphic site control model.

Further insights into isoselective polymerization come from molecular mechanics studies showing that stereoselectivity is not due to direct interactions between monomer and the chiral active site [Corradini et al., 1979, 1982; Monaco et al., 2000]. The effect of the chiral active site is indirect, at least for propene polymerization—the mechanism is chiral orientation of the propagating polymer chain. The chiral active site forces the propagating polymer chain to assume a chiral orientation, which results in discrimination between the two enantiofaces of the monomer. Support for this mechanism comes from $^{13}$C NMR examination of the configuration of the first monomer unit inserted into the Ti–R active site [Ammendola et al., 1986; Tritto et al., 1986; Zambelli et al., 1982a,b]. The NMR analysis is enhanced by using $^{13}$C-enriched alkyl groups in the group I–III metal component. There is some minimum
amount of steric bulk required at the active site in order to observe high enantioselectivity between the two monomer faces. The monomer and various transition metal ligands contribute to the steric bulk at the active site. For propene polymerization, the enantioselectivity in the first monomer unit added is low for $R = \text{methyl}$, appreciable for $R = \text{ethyl}$, and very high for $R = \text{isobutyl}$ or phenyl. Enantioselectivity of the first addition is enhanced for larger-sized monomers such as styrene and vinylcyclohexane compared to propene and for larger-sized halogen ligands. The various steric effects act in a cooperative manner. Thus, addition of the first monomer unit for propene polymerization is as isoselective as all subsequent monomer units when TiI$_3$ is used instead of TiCl$_3$.

The Cossee–Arlman mechanism as originally proposed has a weakness—the back-flip is required to explain isoselective placement since the two active (coordination) sites are assumed to be enantiotopic. However, the structure of the traditional Ziegler–Natta heterogeneous initiators is not sufficiently understood to either support or reject the assumption of enantiotopic sites. Further, even if the sites are enantiotopic, there is no overwhelming reason why the polymer chain is more stable at one site than the other—which is the rationale for the back-flip. The mechanism of isoselectivity with various metalloocene initiators is much better understood since these are initiators whose molecular structures are well-established [Busico and Cipullo, 2001; Busico et al., 1997, 1999; Cavallo et al., 1998; Ewen, 1999; Rappe et al., 2000; Resconi et al., 2000]. Considerable advancements in understanding heterogeneous Ziegler–Natta initiators occur if one assumes that the active sites in these initiators mimic those in metalloocene initiators. Two types of metalloocene initiators offer possible models

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**TABLE 8-3 Stereoerrors versus Type of Stereocontrol**

<table>
<thead>
<tr>
<th>Isoselective Polymerization</th>
<th>Syndioselective Polymerization</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Catalyst site control</strong></td>
<td>Error</td>
</tr>
<tr>
<td>Error</td>
<td>Error</td>
</tr>
<tr>
<td>Only $mr$</td>
<td>Only $mr$</td>
</tr>
<tr>
<td>$(mr) = 2 (rr)$</td>
<td>$(mr) = 2 (rr)$</td>
</tr>
<tr>
<td>$(mmmr) = (mmrr) = 2 (mrrm)$</td>
<td>$(rrrm) = (mmmr) = 2 (mrrm)$</td>
</tr>
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for the isoselective active sites in heterogeneous Ziegler–Natta initiators, the $C_1$- and $C_2$-symmetric metallocenes. These will be discussed in greater detail in Secs. 8-5a-2 and 8-5a-4. The following gives a brief overview with specific application to the heterogeneous Ziegler–Natta initiators:

1. $C_1$-symmetric initiators have a pair of diastereotopic (nonequivalent) sites; one site is sterically crowded and enantioselective, and the other site is less crowded and nonselective. The propagating polymer chain always prefers the less crowded site, but monomer coordination and migratory insertion occur at the more crowded enantioselective site. The polymer chain then back-flips to the less crowded site. This model offers a rationale for the back-flip of the polymer chain—the polymer chain is less stable at the more crowded site.

2. $C_2$-symmetric initiators have a pair of equivalent homotopic sites, both of which prefer the same monomer enantioface, that is, both sites prefer the re enantioface or both prefer the si face. Isoselective propagation proceeds with or without migratory insertion since coordination and insertion of monomer at either site give the same stereochemical result.

8-4f Mechanism of Syndioselective Propagation

The synthesis of syndiotactic polymers by Ziegler–Natta initiators has been successful for propone, styrene, and some 1,3-dienes [Hagen et al., 2002; Pasquon et al., 1989; Youngman and Boor, 1967; Zambelli et al., 2001]. Only soluble initiators, almost exclusively limited to vanadium compounds, yield highly syndioselective polymerization. The level of syndiotacticity is not as high as the isotacticity achieved with the heterogeneous titanium–aluminum initiator systems. The maximum syndiotacticity, $(rr) = 0.9$, is achieved only at low temperatures (−78°C). (Metalloocene initiators produce more highly syndioselective polymerizations—Sec. 8-5.)

The initiator formed from $\text{VCl}_4$ and $\text{Al(C}_2\text{H}_5\text{)}_2\text{Cl}$ is one of the most efficient means for syndioselective polymerization of propene, especially in the presence of a Lewis base such as anisole (methoxybenzene) [Doi, 1979a,b; Natta et al., 1962; Zambelli et al., 1978, 1980]. Other vanadium compounds such as vanadium acetylacetonate and various vanadates [$\text{VO(OR)}_x\text{Cl}_{(3-x)}$, where $x = 1, 2, 3$] can be used in place of $\text{VCl}_4$ but are more limited in their stereoselectivity [Doi et al., 1979]. Trialkylaluminum can also be used as a coinitiator, but only for $\text{VCl}_4$. Syndiotacticity increases with decreasing temperature; most of these syndioselective polymerizations are carried out below −40°C and usually at −78°C. The initiators must be prepared and used at low temperatures since most of them undergo decomposition at ambient and higher temperatures. There is considerable reduction of V(III) to V(II) with precipitation of ill-defined products that are low in activity and do not produce syndiotactic polymer, when the initiators are prepared at or warmed to temperatures above ambient.

The driving force for syndiotactic placement with Ziegler–Natta initiators is similar to that (Sec. 8-3) for low-temperature radical and ionic, noncoordinated polymerizations—the repulsive interaction between substituents of the terminal unit of the propagating chain and incoming monomer. This is the polymer chain end control mechanism for stereocontrol. Figure 8-13 shows this model for syndiotactic placement with secondary insertion. (The original reference [Boor and Youngman, 1966] for this figure incorrectly showed propagation proceeding by primary insertion; see Sec. 8-4c.) The polymer chain end control model for syndiotactic placement is similar to the catalyst site control model for isotactic placement in the both are based on an octahedral transition metal complex that has an alkyl ligand as the propagating site and a coordination vacancy for complexing monomer. (A mechanism based
on pentacoordinated vanadium instead of hexacoordinated vanadium has also been proposed [Zambelli and Allegra, 1980]).

There are important differences between the catalyst site and polymer chain end control models. The homogeneous syndioselective initiator allows coordination of the monomer (and insertion into the polymer chain) via either of the monomer faces. The initiator achieves its stereoselectivity in essentially the same manner as lowered temperature in a noncoordination polymerization. Hindrance between the methyl group of the last unit of the propagating chain and the ligand(s) attached to vanadium prevent rotation about the transition metal–carbon bond. This brings into play the repulsive interaction between methyl groups of the terminal monomer unit and incoming monomer. Syndiotactic placement is energetically favored as methyl–methyl interactions force the monomer to be coordinated at its opposite face at each successive propagation step. On the other hand, monomer–monomer interactions are minimized with isoselective initiators by rotation about the transition metal–carbon bond.

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**Fig. 8-13** Polymer chain end control model for syndioselective polymerization. After Boor and Youngman [1966] (by permission of Wiley-Interscience, New York).
Isotactic placement occurs since only one configuration is favored for coordination and addition of monomer to the propagating chain. Isotactic placement proceeds with migration of the polymer chain to its original ligand position prior to the next propagation step. Syndiotactic propagation occurs alternately at the two ligand positions.

In summary, syndioselective initiators exaggerate the inherent tendency toward syndiotactic placement by accentuating the methyl–methyl repulsive interactions between the propagating chain end and incoming monomer. Isotactic placement occurs against this inherent tendency when chiral active sites force monomer to coordinate with the same enantioface at each propagation step.

The polymer chain end control model is supported by the observation that highly syndiotactic polypropene is obtained only at low temperatures (about $-78^\circ$C). Syndiotacticity is significantly decreased by raising the temperature to $-40^\circ$C [Boor, 1979]. The polymer is atactic when polymerization is carried out above $0^\circ$C. $^{13}$C NMR analysis of the stereoerrors and stereoch hemical sequence distributions (Table 8-3 and Sec. 8-16) also support the polymer chain end control model [Zambelli et al., 2001]. Analysis of propene–ethylene copolymers of low ethylene content produced by vanadium initiators indicates that a syndiotactic block formed after an ethylene unit enters the polymer chain is just as likely to start with an S- placement as with an R-placement of the first propene unit in that block [Bovey et al., 1974; Zambelli et al., 1971, 1978, 1979]. Stereocontrol is not exerted by chiral sites as in isotactic placement, which favors only one type of placement (either S- or R-, depending on the chirality of the active site). Stereocontrol is exerted by the chain end. An ethylene terminal unit has no preference for either placement, since there are no differences in repulsive interactions.

Not all syndioselective polymerizations proceed with polymer chain end control. Some metallocene initiators yield syndioselective polymerization through catalyst site control (Sec. 8-5).

### 8-4g Direction of Double-Bond Opening

A syn or cis addition to the carbon–carbon double bond is implied in the Ziegler–Natta mechanism. The effect of the mode of addition to the double bond has no effect on the stereochemical structure of the polymers from 1-substituted ethylenes. However, the ditacticity of polymers from 1,2-disubstituted ethylenes depends not only on the mode of addition but also on whether the monomer is a cis or trans monomer. For diisoselective polymerization, syn addition to a trans monomer would give the threo diisotactic structure. This is shown in Fig. 8-14, where it is proposed that the carbon–carbon bond in the monomer unit rotates after addition of the monomer to the polymer chain so as to avoid the 1,2-interactions in the fully eclipsed conformation [Goodman, 1967]. Syn addition to the cis monomer would yield the erythrodiisotactic polymer. Trans or anti addition to the two monomers would give the opposite results. Syn addition to the double bond in isotactic polymerization has been confirmed from studies with deuterium-labeled propenes [Miyazawi and Ideguchi, 1964; Natta et al., 1960; Zambelli et al., 1968]. The cis- and trans-1-d-propenes gave the erythro and threo diisotactic polymers, respectively.

The syn addition mechanism described in Fig. 8-14 for isoselective polymerization is based on monomer always approaching the propagating center with the same face (either always re or always si)—a reasonable assumption for a stereoeselective process leading to isotactic polymerization. It is also assumed that incoming monomer is aligned with the propagating chain end so as to minimize steric repulsions between the R group of the chain end and the R groups on the carbon of the double bond that bonds to the propagating chain end;
other words, the R groups are opposed to each other. Syn addition leads to syndioselective polymerization when successive monomer molecules alternate their two faces in approaching the propagating center. Syn addition in syndiotactic polymerization has been established, since copolymerizations of cis- and trans-1-d-propenes with perdeuteropropene yield the trans- and gauche-syndiotactic structures XXIII and XXIV, respectively [Zambelli et al., 1968]. Similar results have been observed in the syndioselective polymerization of styrene [Longo et al., 1988].

**Fig. 8-14** Syn addition to a trans 1,2-disubstituted ethylene to yield the threodiisotactic polymer. After Goodman [1967] (by permission of Wiley-Interscience, New York).

8-4h Effects of Components of Ziegler–Natta Initiator

The stereoselectivity and activity of Ziegler–Natta initiators vary considerably depending on the identity and relative amounts of the initiator components [Boor, 1979]. The interpretation
of experimental results is usually difficult. Changes in the initiator components often affect activity and stereoselectivity in opposite directions. The trends observed from one transition or group I–III metal component to another may be different. In spite of the difficulties in understanding much of the available data, empirical formulation of initiators to achieve high stereoselectivity with high activity has been successful on at least an empirical basis with much resultant commercial success. Some generalizations are presented below on the effects of changes in the initiator components on stereoselectivity. These are generally restricted to \( \alpha \)-olefins; they may not apply to other monomers such as 1,3-dienes.

8-4h-1 Transition-Metal Component

The most widely studied transition metal is titanium. At various times, all oxidation states of titanium (II, III, IV) have been proposed for the active site of titanium-based initiators. Most of the evidence points to titanium (III) as the most stereoselective oxidation state, although not necessarily the most active nor the only one [Chien et al., 1982]. (Data for vanadium systems indicate that trivalent vanadium sites are the syndioselective sites [Lehr, 1968].) Initiators based on the \( \alpha \)-, \( \gamma \)-, and \( \delta \)-titanium trihalides are much more stereoselective (iso-selective) than those based on the tetrahalide or dihalide. By itself, TiCl\(_2\) is inactive as an initiator but is activated by ball milling due to disproportionation to TiCl\(_3\) and Ti [Werber et al., 1968]. The overall stereoselectivity is usually \( \alpha \)-, \( \gamma \)-, \( \delta \)-TiCl\(_3\) > TiCl\(_2\) > TiCl\(_4\) > \( \beta \)-TiCl\(_3\) [Natta et al., 1957b,c].

The low stereoselectivity of \( \beta \)-TiCl\(_3\) relative to the \( \alpha \)-, \( \gamma \)-, and \( \delta \)-forms is a consequence of the different crystalline structure. While \( \alpha \)-, \( \gamma \)-, and \( \delta \)-TiCl\(_3\) are similar in that all contain a layered structure [Natta, 1960a,b; Natta et al., 1961a,b,c,d], in \( \gamma \)-TiCl\(_3\) the chlorines are cubic close-packed instead of hexagonal close-packed as in \( \alpha \)-TiCl\(_3\), \( \delta \)-TiCl\(_3\) has a mixed hexagonal and cubic close-packed layered structure, and \( \beta \)-TiCl\(_3\) consists of bundles of linear TiCl\(_3\) chains. The structure of \( \beta \)-TiCl\(_3\) results in a surface in which half the titanium atoms have two vacancies and the other half have one vacancy. The titanium sites containing two vacancies each are responsible for the low stereoselectivity of \( \beta \)-TiCl\(_3\). The two vacancies yield a site with a loose configuration of ligands since one of the chlorines and/or the growing polymer chain will be loosely bound. This is exactly opposite to the situation with the other titanium trichlorides (one vacancy per site) in which all chlorides and the polymer chain have fixed positions in a rigid configuration on the titanium site. That some isotactic polymer is formed with \( \beta \)-TiCl\(_3\) is a result of the presence of titanium sites that have only one vacancy each.

The oxidation state of the transition metal active sites is dependent not only on the transition-metal component but also on the group I–III metal component. For example, TiCl\(_4\) is usually used instead of TiCl\(_3\) in initiator recipes because it is a liquid and more conveniently handled but is usually employed under conditions (in combination with AlR\(_3\) or AlR\(_2\)Cl), which reduces a large fraction of titanium to the trivalent state. Further, the extent of reduction depends on the amount of the group I–III metal component relative to the transition metal [Kollar et al., 1968a,b; Schindler, 1968]. At Al/Ti ratios greater than 3, there is extensive reduction to divalent titanium and a significant decrease in stereoselectivity. The optimum ratio is usually near or less than 1. However, the situation is very different for the MgCl\(_2\)-supported initiators. The typical initiator contains about 0.5–2% Ti, and the optimum Al/Ti ratio is often as high as 10–100 [Chien et al., 1982; Dumas and Hsu, 1984].

Changes in the ligands of the transition metal component affect stereoselectivity [Natta et al., 1957a,b; Rishina et al., 1976]. For propene polymerization by titanium compounds in
combination with triethylaluminum, isotacticity follows the orders

\[ \alpha\text{-TiCl}_3 > \text{TiBr}_3 > \text{TiI}_3 \]

\[ \text{TiCl}_4 \simeq \text{TiBr}_4 \simeq \text{TiI}_4 \]  

(8-36)

\[ \text{TiCl}_4 > \text{TiCl}_2(\text{OC}_4\text{H}_9)_2 \gg \text{Ti}(\text{OC}_4\text{H}_9)_4 \simeq \text{Ti(OH)}_4 \]

Changes in the transition metal itself have a large effect. Titanium compounds are the most isoselective, while vanadium compounds are the most syndioselective.

Differences in initiator stereoselectivity and activity are greatest for the more stereoselective and active transition metal components (trivalent oxidation state). Initiators based on the less stereoselective and active transition metals (tetravalent oxidation state) are less affected by changes. Initiator stereoselectivity and activity are dependent on the crystal structure, steric size, ligands, and the electronegativity of the transition metal. Decreasing the electronegativity of the transition metal (leading to a more easily polarized metal growth bond) by changes in the transition metal, or its valence state, or its ligands, increases the stereoselectivity of the initiator. Increasing the size of the ligands decreases stereoselectivity probably because of a decreased coordinating ability. The quantitative interrelationship of these and other factors with the crystal structure of the transition metal and the active sites in determining stereoselectivity and activity are not clear.

8-4h-2 Group I–III Metal Component

Although the group I–III metal component is not an absolute necessity, its presence has a very significant effect on both activity and stereoselectivity [Boor, 1967, 1979; Coover et al., 1967; Diedrich, 1975; Natta, 1960a,b]. The group I–III metal component is required to obtain high stereoselectivity and high activity. Active initiators for ethylene and \( \alpha \)-olefin polymerizations have been found using Li, Na, and K from group I; Be, Mg, Zn, and Cd from group II; and Al and Ga from group III. Ziegler–Natta initiators based on other group I–III metals have far lower activity and stereoselectivity. Aluminum compounds are by far the most often used, a consequence of their ready availability and ease of handling (once in solution). Gallium is also active but expensive. Zinc and magnesium alkyls are the most thoroughly studied group II metal component [Greco et al., 1979]; beryllium compounds have received little attention because of their toxicity. Lithium, sodium, and potassium alkyls are the most studied group I metal component. They are generally not as attractive as the group II and III metals because of their lower solubility in the hydrocarbon solvents normally used. (Lithium alkyls, although soluble, are highly associated in hydrocarbon solvents.)

For initiators in which the group I–III metal is unchanged, isoselectivity generally decreases as the size of the organic group increases, although the opposite effect has also been reported. When titanium is the transition metal, the replacement of an alkyl group in AlR\(_3\) by any halogen other than fluorine results in increased stereoselectivity and decreased activity, where the effect of halogen is I > Br > Cl [Danusso, 1964; Doi and Keii, 1978]. The replacement of a second alkyl group in the aluminum component by halogen leads to a further decrease in activity as well as a moderate decrease in stereoselectivity. The behavior with vanadium compounds is very different. Trialkylaluminum yields isotactic polypropene [Chien et al., 1989], while AlR\(_2\)Cl yields syndiotactic polypropene. In fact, syndiotactic polypropene is obtained in high yield only with AlR\(_2\)Cl in combination with a soluble vanadium salt.
A variety of different compounds have been added to recipes for Ziegler–Natta initiators in attempts to enhance stereoselectivity and activity [Boor, 1979; Coover et al., 1967]. These are electron donors (Lewis bases) and include oxygen, water, inorganic and organic halides, phenols, ethers, esters, amines, phosphines, aromatics, carbon disulfide, and hexamethylphosphoramide. The effects of the third components vary considerably depending on the third component and the other two components of the initiator system. Some additives increase stereoselectivity and/or activity, while others have the opposite effect. Some increase stereoselectivity while decreasing activity or vice versa. Some additives such as oxygen and water have deleterious effects on both activity and stereoselectivity. Still other additives affect polymer molecular weight either exclusively or along with changes in initiator activity and stereoselectivity.

The high-mileage initiators achieve high activity by supporting (and finely dispersing) the transition metal component on MgCl\(_2\). High stereoselectivity is maintained and even increased by the Lewis base [Barbe et al., 1987; Chadwick, 2001; Chadwick et al., 2001; Chien and Hu, 1987; Chien and Bres, 1986; Chien et al., 1982; Galli et al., 1981; Pino and Mulhaupt, 1980; Soga et al., 1988, 1990]. Various mechanisms have been proposed for the action of Lewis bases in improving stereoselectivity—decreasing the reactivity of the less stereoselective sites (perhaps by altering the ligands) and increasing the number of stereoselective sites by assisting in their stabilization and/or dispersal in the support.

Both internal and external electron donors (Lewis bases) are used to produce the high-mileage initiators. An internal base is typically ball-milled with the support material and the transition metal component subsequently added with further mixing. This is followed by the addition of a mixture of the group I–III metal component with the external base. Previous recipes used the same base, usually an aromatic ester such as diisobutyl phthalate, as both internal and external bases. More recent recipes use an aromatic ester or diether as the internal base and an alkoxy silane, such as RR'Si(OCH\(_3\))\(_2\) or RSi(OCH\(_3\))\(_3\), as the external base. The external base is needed, especially when an ester is used as the internal base, because the addition of the group I–III metal component results in the loss of a large fraction of the internal base. Without replacement of the lost base by the external base, there is a loss of stereoselectivity [Chadwick et al., 2001]. An external base is seldom needed when a diether is used as the internal base. The loss of diether during the initiator preparation is much less than the loss of the ester.

### 8-4i Kinetics

#### 8-4i-1 Observed Rate Behavior

The kinetics of Ziegler–Natta polymerization are complex. The relatively few polymerizations that are homogeneous behave in a manner generally similar to noncoordination ionic polymerizations (Chap. 5). The heterogeneous systems usually exhibit complicated behavior as shown in Fig. 8-15 [Boor, 1979; Burfield, 1984; Burfield et al., 1976; Cooper, 1976; Keii, 1972; Tait and Watkins, 1989]. The behavior described by plot 1 is usually observed when the particle size of the transition metal component is relatively large. The particles of the transition metal component consist of aggregates of smaller crystals. The mechanical pressure of the growing polymer chains cleaves these aggregates with the result that the initiator surface area, number of active sites, and polymerization rate increase with time. After this initial period, referred to as a buildup or settling period, a steady-state rate is reached, which
corresponds to cleavage of the initial particles to the smallest-sized particles. When the initial particle size is decreased (by ball milling), the time required to reach the steady-state polymerization rate is decreased (plot 2). Other factors responsible for the buildup period include the time needed for the formation of the active sites by reaction of the two metal components, slow initiation, and the presence of impurities. Most of these factors are moderated for the typical situation where the initiator system is preformed and allowed to age prior to use in initiating polymerization. The superactive supported initiators often show very little or no buildup period [Busico et al., 1986; Chien and Hu, 1987].

Many polymerizations show a settling period with a relatively rapid rise in rate to a maximum value followed by a decay to the steady-state rate (plot 3). This behavior indicates the presence of active sites of differing activities with some of the active sites decaying with time. This behavior is avoided in some instances by aging the initiator. Ziegler–Natta polymerizations may exhibit a continuous rate decrease (plot 4) after the settling period (which may be of either type 1, 2, or 3) due to active site destruction. This can be due to thermal deactivation or further reduction of the transition metal by the group I–III metal component. Diffusion control of the propagation reaction has also been postulated. Diffusion of the monomer through the formed polymer to the propagation centers may become rate-determining at higher conversions. This has been substantiated in some systems where the polymerization rate increases with increased rate of stirring, but data in other systems indicate diffusion control to be absent [Chien et al., 1985].

8-4i-2 Termination

Ziegler–Natta polymerizations have the characteristics of living polymerizations with regard to active sites but not individual chains. (Some living polymerizations proceed with metallocene and other initiators—Sec. 8-9.) The lifetime of propagating chains is of the order of seconds or minutes at most, while active sites have lifetimes of hours or more. Each active site produces many polymer molecules. Propagating chains undergo a number of chain-breaking reactions:
1. β-Hydride transfer either directly to the transition metal

\[
\text{Ti} \rightarrow \text{CH}_2 \rightarrow \text{CH} \rightleftharpoons \text{CH}_3 \overset{k_s}{\rightarrow} \text{Ti} \rightarrow \text{H} + \text{CH}_2 \rightarrow \text{C} \rightleftharpoons \text{CH}_3
\]  

(8-37)

where Ti represents the transition metal active site at which propagation occurs.

or to monomer

\[
\text{Ti} \rightarrow \text{CH}_2 \rightarrow \text{CH} \rightleftharpoons \text{CH}_3 + \text{CH}_3 \text{CH} = \text{CH}_2 \overset{k_{\alpha,M}}{\rightarrow} \text{Ti} \rightarrow \text{CH}_2 \text{CH}_2 \text{CH}_3 + \text{CH}_2 \rightarrow \text{C} \rightleftharpoons \text{CH}_3
\]  

(8-38)

Both β-hydride transfers result in polypropene molecules with one vinylidene and one n-propyl end group. The two transfers are zero- and first-order, respectively, in monomer. β-Hydride transfer yields vinyl end groups in ethylene polymerization.

2. Chain transfer to the group I–III metal alkyl:

\[
\text{Ti} \rightarrow \text{CH}_2 \rightarrow \text{CH} \rightleftharpoons \text{CH}_3 + \text{Al(C}_2\text{H}_5)_3 \overset{k_{\alpha,A}}{\rightarrow} \text{Ti} \rightarrow \text{CH}_2 \text{CH}_3 + (\text{C}_2\text{H}_5)_2\text{Al} \rightarrow \text{CH}_2 \rightarrow \text{CH} \rightleftharpoons \text{CH}_3
\]  

(8-39)

Hydrolytic workup of the polymer cleaves the aluminium–polymer bond to yield an isopropyl end group.

3. Chain transfer to an active hydrogen compound such as molecular hydrogen:

\[
\text{Ti} \rightarrow \text{CH}_2 \rightarrow \text{CH} \rightleftharpoons \text{CH}_3 + \text{H}_2 \overset{k_{\alpha,H_2}}{\rightarrow} \text{Ti} \rightarrow \text{H} + \text{CH}_3 \rightarrow \text{CH} \rightleftharpoons \text{CH}_3
\]  

(8-40)

The β-hydride transfer reactions produce polymers with one saturated and one unsaturated end group. The other two transfers result in polymers with two saturated groups. The chain-breaking reactions limit the polymer molecular weight, but like typical chain-transfer reactions, they proceed with the reinitiation of new propagating chains. The extents to which the various chain-breaking reactions occur depend on the monomer, identity and concentrations of the initiator components, temperature, and other reaction conditions [Boor, 1979; Cooper, 1976; Longi et al., 1963]. The β-hydride transfer reactions are usually the predominant chain-breaking reaction in the absence of H₂ or other active hydrogen compound. H₂ is a highly effective chain-transfer agent and is used for molecular weight control in commercial polymerizations of ethylene and α-olefins. There are considerable differences in the extent of transfer to group I–III metal components. Trialkylaluminum is much less active a transfer agent compared to dialkylzinc [Natta et al., 1961a,b,c,d].

Chain transfer to molecular hydrogen not only affects polymer molecular weight, but unlike other transfer agents, also affects polymerization rate. Hydrogen often decreases the rate of ethylene polymerization, but increases the rate of propene polymerization [Chadwick,
2001; Kissin and Rishina, 2002; Kissin et al., 1999a]. The rate depression for ethylene is attributed to the high stability of the Ti–ethyl group, formed when transfer is followed by the addition of a monomer molecule, due to stabilization by a β-agostic coordination between a methyl hydrogen and Ti. The reactivity of a propagating chain in propene polymerization decreases whenever there is 2,1-insertion (secondary insertion). The resulting 2,1-chain ends are preferentially terminated by transfer to hydrogen; the overall result is replacement of 2,1-chain ends by more reactive 1,2-chain ends on reinitiation.

Termination is even more complicated than described, especially when polymerizations by metallocene initiators are considered [Beach and Kissin, 1986; Kissin et al., 1999b; Lehmus et al., 2000; Liu et al., 2001b; Resconi et al., 2000; Rossi et al., 1995, 1996; Thorshaug et al., 1998; Weng et al., 2000; Zhao et al., 2000]. A variety of different unsaturated end groups have been found in different polymerizations. Isomerization of propagating chain ends followed by β-hydride transfer (Eq. 8-41) results in trisubstituted double bond end groups in some α-olefin polymerizations and vinylene end groups in polyethylene (R = H). Trisubstituted double bonds are also produced in α-olefin polymerizations by chain transfer to vinylidene end groups [Rossi et al., 1995].

β-Hydride transfer from 2,1-chain ends produces vinylene end groups in α-olefin polymerization:

\[
\begin{align*}
\text{CH}_2\text{CHZr} & \quad \quad \text{Zr} \\
\quad & \quad \quad -\text{ZrH} \\
\text{CH} & \quad \quad \text{CH} \\
\quad & \quad \quad \text{R} \\
\end{align*}
\]

(8-41)

β-Alkyl transfer (R = CH₃, CH₂CH₂) produces polypropene and poly(1-butene) with vinyl end groups:

\[
\begin{align*}
\text{CH} & \quad \quad \text{CH}_2Zr \\
\quad & \quad \quad -\text{RZr} \\
\text{CH} & \quad \quad \text{CH} \\
\quad & \quad \quad \text{H} \\
\end{align*}
\]

(8-43)

8-4i-3 Rate and Degree of Polymerization

Homogeneous kinetics are applicable to some Ziegler–Natta polymerizations, when adsorption of initiator components or monomer is not important. The polymerization rate is expressed as

\[
R_p = k_p [C^*][M]
\]

(8-44)

where [C*] is the concentration of active sites expressed in moles per liter.

Adsorption phenomena are important in most Ziegler–Natta polymerizations, and this requires treatment by heterogeneous kinetics [Bohm, 1978; Boor, 1979; Chien and Ang, 1987; Chien and Hu, 1987; Cooper, 1976; Keii, 1972; Tait and Watkins, 1989]. The exact form of the resulting kinetic expressions differs depending on the specific adsorption
phenomena that are important in the particular reaction system. Consider a Langmuir–Hinschelwood model where reaction occurs only after monomer is adsorbed from solution onto the transition metal active sites. Further, we assume that the group I–III metal component is present in solution and competes with monomer for the same sites; that is, there is excess group I–III metal component over and above the amount needed to activate (reduce/alkylate) the transition metal sites. The fraction $\Theta_A$ and $\Theta_M$ of the transition metal sites covered with the group I–III metal component and monomer, respectively, are given by

$$\Theta_A = \frac{K_A[A]}{1 + K_A[A] + K_M[M]}$$  \hspace{1cm} (8-45)

$$\Theta_M = \frac{K_M[M]}{1 + K_A[A] + K_M[M]}$$  \hspace{1cm} (8-46)

where $[A]$ and $[M]$ are the concentrations of the group I–III metal component and monomer in solution, respectively, and $K_A$ and $K_M$ are the respective equilibrium constants for their adsorption [Atkins and dePaula, 2002].

Propagation occurs by reaction of adsorbed monomer at the active sites at a rate given by

$$R_p = k_p[C^*] \Theta_M$$  \hspace{1cm} (8-47)

Combination of Eqs. 8-45 to 8-47 yields the polymerization rate as

$$R_p = \frac{k_p K_M[M][C^*]}{1 + K_M[M] + K_A[A]}$$  \hspace{1cm} (8-48)

If the group I–III metal component does not compete with monomer for the active sites, then $K_A[A] = 0$ and Eq. 8-48 reduces to

$$R_p = \frac{k_p K_M[M][C^*]}{1 + K_M[M]}$$  \hspace{1cm} (8-49)

The degree of polymerization is obtained by dividing the propagation rate by the sum of all chain-breaking (transfer) reactions. For the simple situation where the only $\beta$-hydride transfer is that described by Eqs. 8-37 and 8-38 (which produce vinylidene end groups in polypropene) and no $\beta$-alkyl transfer occurs, the degree of polymerization is

$$\frac{1}{X_n} = \frac{k_{tr,M}}{k_p} + \frac{k_{tr,H_2}}{k_p K_M[M]} + \frac{k_{tr,A} K_A[A]}{k_p K_M[M]} + \frac{k_{tr,H_2} [H_2]}{k_p K_M[M]}$$  \hspace{1cm} (8-50)

For the more complex situation with other $\beta$-hydride transfers, additional terms would be needed to account for those reactions. An alternate approach is to use Eq. 8-50 with $k_i$ and $k_{tr,M}$ redefined as composite rate constants for the sum of all $\beta$-hydride transfers.

The derivations of Eqs. 8-48 through 8-50 assume that transfer to hydrogen does not involve adsorption of hydrogen at the active sites prior to transfer. If hydrogen competes with monomer and the group I–III metal component for adsorption at the active sites, the treatment described above requires modification of $\Theta_A$ and $\Theta_M$ and the introduction of $\Theta_{H_2}$.

8-4i-4 Values of Kinetic Parameters

Evaluation of the various kinetic parameters requires a determination of the active-site concentration. $[C^*]$ is usually determined from experiments in which the active sites are
quenched (made inactive) with CH$_3$O$_3$H, $^{14}$CO, or $^{14}$CO$_2$ [Jaber and Fink, 1989; Mejzlik et al., 1986, 1988; Tait and Watkins, 1989; Vozka and Mejzlik, 1990]. Other methods include the use of number-average molecular weight (combined with polymer yield) and $^{14}$C-labeled group I—III metal component. Each of the techniques has limitations that require care if reliable results are to be obtained. For example, quenching with CH$_3$O$_3$H gives high values for [C*] since the polymer chains terminated by chain transfer to the group I–III metal component are reactive toward methanol. Values of [C*] obtained at different conversions need to be extrapolated to zero conversion.

Literature values of the active-site concentrations range from tenths or hundredths of a percent to tens of percents of the transition metal concentration [Lieberman and Barbe, 1988; Tait and Watkins, 1989]. Much of this is indicative of the range of activity of different initiators, especially when comparing older initiators to the recent high-mileage initiators. However, some of the variation is due to the problems inherent in measurement of [C*]. Literature values of $k_p$ and other rate constants also show a considerable range.

Both rate and molecular weight data are often interpreted in terms of multicenter models, in which the initiator contains both selective (either iso- or syndioselective) and nonselective (aselective) active sites [Chien and Hu, 1987; Kissin, 2001a, 2002; Liu et al., 2001b]. Table 8-4 shows various kinetic parameters in propene polymerization (0.65 M in n-heptane) using a TiCl$_4$/Al(C$_2$H$_5$)$_3$ initiator ([Ti] = 0.0001 M) supported on MgCl$_2$ with ethyl benzoate and methyl-$p$-toluate as internal and external Lewis bases. The concentrations of isoselective and aselective active sites were obtained by a combination of quenching experiments for the total concentration of active sites and ESR (as well as isotactic index) measurements for the isoselective active sites. The amounts of isoselective and aselective active sites as percentages of total titanium are expressed by (C*)$_I$ and (C*)$_A$, respectively. $k_{pl}$ and $k_{pa}$ represent the propagation rate constants for isoselective and aselective active sites, respectively. The external base is critical to achieving a highly isoselective polymerization. With an internal base but no external base, isoselective polymerization is favored over aselective by a factor of 2.1 because (C*)$_I$/(C*)$_A$ favors aselective polymerization by a factor of 4, while $k_{pl}/k_{pa}$ favors isoselective polymerization by a factor of 8.3. With both internal and external bases present, the concentration of aselective active sites decreases, as does their reactivity while there is negligible effect on the isoselective sites. Isoselective polymerization

<table>
<thead>
<tr>
<th>Kinetic Parameter$^b$</th>
<th>Internal Base Only</th>
<th>Internal and External Bases</th>
</tr>
</thead>
<tbody>
<tr>
<td>(C*)$_I$</td>
<td>6.0</td>
<td>2.3</td>
</tr>
<tr>
<td>[C*]$_I$</td>
<td>$6.0 \times 10^{-6}$</td>
<td>$2.3 \times 10^{-6}$</td>
</tr>
<tr>
<td>(C*)$_A$</td>
<td>24</td>
<td>2.4</td>
</tr>
<tr>
<td>$k_{pl}$</td>
<td>138</td>
<td>133</td>
</tr>
<tr>
<td>$k_{pa}$</td>
<td>16.6</td>
<td>5.1</td>
</tr>
<tr>
<td>Isotactic index</td>
<td>68.2</td>
<td>96.0</td>
</tr>
<tr>
<td>$k_{tr,A}$</td>
<td>$4.0 \times 10^{-4}$</td>
<td>$1.2 \times 10^{-4}$</td>
</tr>
<tr>
<td>$k_{tr,M}$</td>
<td>$9.1 \times 10^{-3}$</td>
<td>$7.2 \times 10^{-3}$</td>
</tr>
<tr>
<td>$k_c$</td>
<td>$8.2 \times 10^{-3}$</td>
<td>$9.7 \times 10^{-3}$</td>
</tr>
</tbody>
</table>

$^a$ Data from Chien and Hu [1987].

$^b$ Units: (C*) = % of Ti; [C*]$_I$ = mol L$^{-1}$; $k_i$ = s$^{-1}$; all other rate constants = L mol$^{-1}$ s$^{-1}$; isotactic index = percent of sample insoluble in refluxing n-heptane.

$^c$ Values are for the isoselective sites.
becomes favored by a factor of 25. The isotactic index increases from 68.2 to 96.0% when an external base is present together with the internal base. The $k_{tr,A}$, $k_{tr,M}$, and $k_s$ values in Table 8-4 are those for the isoselective active sites. These are lower than $k_p$ by a factor of $10^4$–$10^6$, which results in high polymer molecular weights ($M_n = 2.0 \times 10^5$ and $1.5 \times 10^5$, respectively, with and without external base). Lower molecular weights are achieved only in the presence of H$_2$ whose rate constant for transfer is much higher. The aselective active sites yield lower molecular weights ($M_n = 1.1 \times 10^5$ and $0.9 \times 10^5$, respectively, with and without external base) than do the isoselective active sites.

The molecular weight distributions obtained with heterogeneous Ziegler–Natta initiators vary considerably depending on the initiator. $X_w/X_n$ is slightly above 3 for the polymerization in Table 8-4, but most literature reports show values in the 5–30 range. The broader distributions, found for the less isoselective polymerizations, are the result of initiators with multicenters. The analysis of the system in Table 8-4 is based on a two-center model, but there are indications of the presence of more than two types of active centers for some initiators. For example, resolution of the GPC molecular weight data in an ethylene polymerization by a titanium–magnesium initiator system supported on silica indicated five different molecular weight distributions, which were interpreted in terms of five different active sites of different activities [Kissin, 2001a, 2003]. Homogeneous Ziegler–Natta polymerizations typically have narrower distributions than the heterogeneous systems since there is a narrower distribution of active sites of differing reactivities.

The overall activation energies for the rates of most Ziegler–Natta polymerizations fall in the range 20–70 kJ mol$^{-1}$. $E_R$ is a composite of the activation energy for propagation and the heat of adsorption of monomer. Although polymerization rates increase with temperature, reaction temperatures above 70–100°C seldom are employed. High temperatures result in loss of stereoselectivity, a decrease in polymer molecular weight, as well as lowered polymerization rates due to the decreased stability of the initiator.

### 8-4j Transition Metal Oxide Initiators

Various supported transition metal oxides, such as CrO$_3$ and MoO$_3$, initiate the polymerization of ethylene. The most active initiator is chromium oxide [Beach and Kissin, 1986; Pino et al., 1987; Ruddick and Badyal, 1998; Tait, 1989; Tait and Watkins, 1989; Thune et al., 2001; Witt, 1974]. Silica (SiO$_2$) or aluminosilicates (mixed SiO$_2$/Al$_2$O$_3$) are used as the support material. The support is sometimes modified with titania (TiO$_2$). The CrO$_3$ catalyst, referred to as a Phillips catalyst or initiator, is prepared by impregnating the finely divided support with an aqueous solution of CrO$_3$. The chromium loading is in the range 0.5–5 wt%, typically 1 wt%. The initiator is fixed on the support surface by heating at 500–800°C and higher. This probably results in the reaction of surface hydroxyl groups in the support material with CrO$_3$ to form chromate (XXV) and dichromate (XXVI) species.

\[
\begin{align*}
\text{Si}-\text{O-Si} + \text{CrO}_3 & \rightarrow \text{Si}-\text{O}+\text{Cr}_2\text{O}_7 \\
\text{Si}-\text{O-Si} & \rightarrow \text{Si}-\text{O-Si}
\end{align*}
\]

\[
\text{(8-51)}
\]

Initiation by the Phillips catalyst is not well understood. Both Cr(II) and Cr(III) have been proposed as the active oxidation state of chromium. Initiation involves the formation
of chromium–carbon bonds by reaction of ethylene with the active sites. Initiation is accelerated by carrying out the heat treatment of the catalyst in a reducing atmosphere of CO, H₂, or metal hydride or treatment with AlR₃ or Al(OR)₃. The Phillips catalyst is highly active for ethylene polymerization and is used to produce about one-quarter to one-third of all high-density PE and linear low-density PE (Sec. 8-11). However, the Phillips catalyst is not useful for the homopolymerization of propene and other α-olefins since it does not bring about a stereoselective polymerization.

8-5 METALLOCENE POLYMERIZATION OF NONPOLAR ALKENES MONOMERS

Metallocenes of the general formula LL'MtX₂ have received enormous attention for the stereoselective polymerization of a range of monomers [Togni and Halterman, 1998]. In 2002, the polymer literature contained more papers on metallocenes than any other subject; the second most published topic was free radical living polymerization. L and L' are η⁵-cyclopentadienyl ligands, which may be the same or different. Among the most studied ligands are η⁵-cyclopentadienyl (Cp) and various substituted cyclopentadienyls, including alkyl-substituted η⁵-cyclopentadienyls, 1-indenyl (Ind), 4,5,6,7-tetrahydro-1-indenyl (H₄Ind), and 9-fluorenyl (Flu) ligands. Mt is a group 4 transition metal, usually zirconium, but also titanium and to a lesser extent hafnium. Some group 3 transition metals (Sc, Y, La) have also been studied. X is usually Cl, but also CH₃.

The initial interest in metallocenes was to study soluble initiator systems as models to better understand the heterogeneous isoselective initiators. However, it soon became apparent that metallocenes offered several advantages over the traditional Ziegler–Natta initiators. Many metallocenes are up to 100-fold more active because the initiators are homogeneous and each (or nearly each) atom of the transition metal is active. Stereoselectivity can be controlled and varied to produce different stereoregular products by appropriate choice of the metallocene ligands and reaction conditions. The metallocene initiators are single-site initiators, unlike the multisite traditional Ziegler–Natta initiators, since each metal resides in the same coordination environment. This results in polymers with narrower distributions of molecular weight, regiochemistry, and stereochemistry.

Titanocene and zirconocene dichlorides (Cp₂MtCl₂ with Mt = Ti, Zr) were the first metallocenes studied [Breslow and Newburg, 1957; Natta et al., 1957a]. The metallocene initiators, like the traditional Ziegler–Natta initiators, require activation by a Lewis acid coinitiator, sometimes called an activator. AlRCl₂ and AlR₃ were used initially, but the result was initiator systems with low activity for ethylene polymerization and no activity in α-olefin polymerization. The use of methylaluminoxane (MAO), [Al(CH₃)₂O]ₙ, resulted in greatly improved activity for ethylene polymerization [Sinn and Kaminsky, 1980]. The properties of MAO are discussed in Sec. 8-5g. MAO has two functions: alkylation of a transition metal–chloride bond followed by abstraction of the second chloride to yield a metallocenium
cation with a vacant coordination site (XXVII):

\[
\text{C}_2\text{H}_5\text{C}l_2 \xrightarrow{\text{MAO}} \text{C}_2\text{H}_5\text{Cl} \xrightarrow{\text{MAO}} \text{C}_2\text{H}_5\text{Cl} - (\text{ClMAO})^- \quad (8-52)
\]

Propagation proceeds in a manner similar to that described for the traditional Ziegler–Natta initiators. The transition metal has two active sites—the polymer chain is held at one site (the one occupied by a methyl group in XXVII) and monomer at the other site (shown as the vacancy □). The reactivity of the active sites is high because the counteranion, which is either (ClMAO)\(^-\) or (CH\(_3\)MAO)\(^-\) or a mixture of the two, is a weakly coordinating anion. Reactivity is decreased when the counterion is strongly coordinating.

The positive charge on the transition metal in XXVII is a consequence of the tetravalent oxidation state of the transition metal in Cp\(_2\)TiCl\(_2\). The active sites in traditional Ziegler–Natta polymerizations may be neutral because the transition metal is trivalent in those initiators (Secs. 8-4e, 8-4h-1). The group 3 metallocene initiators have neutral metal centers because those metals are trivalent.

### 8-5a Metallocene Symmetry

The activating effect of MAO on Cp\(_2\)TiCl\(_2\) results in the polymerization of propene but the reaction rates and molecular weights are modest, and more importantly, the reaction does not proceed in a stereoselective manner. Stereoselective polymerization with high reaction rates and molecular weights occurs generally when the metallocene initiator is both chiral and stereorigid. Chiral and stereorigid metallocenes bear appropriately substituted \(\eta^5\)-cyclopentadienyl ligands that are linked together by a bridging group. Bridged-metallocenes are referred to as *ansa metallocenes*.

Table 8-5 shows the structures and properties of the propagating species for ansa metallocenes with different types of molecular symmetry. The \(\eta^5\)-cyclopentadienyl ligands represent the unsubstituted and various substituted \(\eta^5\)-cyclopentadienyl ligands such as 1-indenyl, 4,5,6,7-tetrahydro-1-indenyl, or 9-fluorenyl. R represents an alkyl or aromatic group. E is the bridging group, usually CH\(_2\)CH\(_2\), CH\(_2\), Si(CH\(_3\))\(_2\), or C(CH\(_3\))\(_2\). The transition metal atom (Mt) has two active sites, one holds the propagating polymer chain P and the other is shown with a vacancy (□) to which monomer coordinates prior to insertion into the polymer chain. The stereochemistry of the polymerization depends on whether the active sites are nonchiral or chiral, and if chiral, the stereochemical relationship between the two sites. As always the stereochemical outcome of the polymerization also depends on reaction variables such as temperature. The unbridged versions of many of the metallocene initiators in Table 8-5 have also been examined. Certain bridged metallocene initiators direct highly stereoselective polymerization because one or both of the transition metal active sites is (are) in a chiral environment. With few exceptions, the corresponding unbridged initiators do not achieve highly stereoselective polymerizations because free rotation of the \(\eta^5\)-cyclopentadienyl ligands results in achiral environments at the active sites. The bridge locks in the symmetry of the metallocene initiator.

The type of symmetry present in each type of metallocene initiator (\(C_2\), \(C_2\), \(C_4\), \(C_1\)) is listed in Table 8-5. The symmetry elements (axis and plane) for each type is indicated. An axis is a \(C_2\) axis of symmetry when rotation of 180\(^\circ\) about that axis yields a structure indistinguishable from the original structure. The stereoselectivity of each of the two coordination
<table>
<thead>
<tr>
<th>Metallocene</th>
<th>Symmetry</th>
<th>Axis</th>
<th>Planes</th>
<th>Coordination Sites&lt;sup&gt;a&lt;/sup&gt;</th>
<th>Polymer Structure&lt;sup&gt;b&lt;/sup&gt;</th>
</tr>
</thead>
<tbody>
<tr>
<td>XXVIII</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>XXIX</td>
<td>C&lt;sub&gt;2v&lt;/sub&gt;</td>
<td>C&lt;sub&gt;2&lt;/sub&gt;</td>
<td>2</td>
<td>Homotopic NS, NS</td>
<td>Atactic (variable) CEC</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>XXX</td>
<td>C&lt;sub&gt;2&lt;/sub&gt;</td>
<td>C&lt;sub&gt;2&lt;/sub&gt;</td>
<td>None</td>
<td>Homotopic E, E</td>
<td>Isotactic CSC</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>XXXI</td>
<td>Meso C&lt;sub&gt;s&lt;/sub&gt;</td>
<td>None</td>
<td>1</td>
<td>Diastereotopic NS, NS</td>
<td>Atactic CEC</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>XXXII</td>
<td>C&lt;sub&gt;s&lt;/sub&gt;</td>
<td>None</td>
<td>1</td>
<td>Enantiotopic E, E</td>
<td>Syndiotactic CSC</td>
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<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>C&lt;sub&gt;1&lt;/sub&gt;</td>
<td>None</td>
<td>None</td>
<td>Diastereotopic E, NS or E, E</td>
<td>Variable CSC</td>
</tr>
</tbody>
</table>

<sup>a</sup> E = enantioselective, NS = nonselective.

<sup>b</sup> CEC = chain end control, CSC = catalyst site control.
(active) sites of the transition metal is indicated, a site is either enantioselective (i.e., one of the two monomer faces is preferentially inserted) or nonselective. The relationship of the stereoselectivities of the two active sites of a metallocene initiator, namely homotopic, enantiotopic, or diastereotopic, determines the stereoregularity of the polymer and the type of stereocontrol (chain end control or catalyst site control) [Alt and Koppl, 2000; Busico and Cipullo, 2001; Coates, 2000; Ewen, 1999; Grisi et al., 1998; Kaminiski, 2001; Resconi et al., 2000].

The geometry of the group 4 metallocenes is shown in XXXIII. The metallocenes are often referred to as bent metallocenes because the planes of the two \( \eta^5 \)-cyclopentadienyl ligands are not parallel to each other. The angle between the ligands, \( \beta \), often referred to as the bite angle, is in the range 60–75°; the exact value depends on the identity of the \( \eta^5 \)-ligands and the transition metal. The transition metal is pseudotetrahedral with \( \alpha \) in the range 115–125°. \( \delta \) is a few degrees less than 90°.

![XXXIII](image)

The ansa metallocene initiators are synthesized in a relatively straightforward manner (Eq. 8-53). Cyclopentadiene or a substituted analog such as an alkyl-substituted cyclopentadiene, indene, 4,5,6,7-tetrahydroindene, or fluorene (CpH\(_2\)) is reacted with butyllithium to form the cyclopentadienyl (aromatic) anion, which is then reacted with ECl\(_2\) to form the bridged biscyclopentadienyl derivative E(CpH\(_2\)). Reaction with butyllithium forms the bis-cyclopentadienyl dianion, which is reacted with ZrCl\(_4\) (or other transition metal halide) to form the bridged zirconocene dichloride E(Cp\(_2\))ZrCl\(_2\). [E(Cp\(_2\))Zr(CH\(_3\)_2 can be obtained from the dichloride by reaction with methyllithium.]

8-5b \( C_{2v} \)-Symmetric Metallocenes

Both bridged and unbridged \( C_{2v} \)-symmetric metallocenes, mostly the unsubstituted biscoyclopentadienyl initiators, but also others such as (CH\(_3\)_2SiFlu\(_2\))ZrCl\(_2\), have been studied. These initiators are achiral, and their two coordination (active) sites are both achiral and homotopic. The result is that atactic polymer is formed via chain end control. Modest tendencies toward slight isotactic or syndiotactic placement are observed for some initiators, depending on the temperature and other reaction conditions.

8-5c \( C_2 \)-Symmetric Metallocenes

The \( C_2 \)-symmetric ansa metallocenes possess a \( C_2 \) axis of symmetry, are chiral, and their two active sites are both chiral. The two sites are equivalent (homotopic) and enantioselective for the same monomer enantioface. The result is isoselective polymerization. \( C_2 \) ansa metallocenes are one of two classes of initiators that produce highly isotactic polymer, the other class being the \( C_1 \) ansa metallocenes (Sec. 8-5e). \( C_2 \) ansa metallocenes generally produce the most isoselective polymerizations.
A $C_2$-symmetric ansa metallocene is a racemic mixture of an enantiomeric pair—an example is $\text{rac-}(\text{dimethylsilyl})\text{bis(1-indenyl)}\text{zirconium dichloride (XXXIV), abbreviated as rac-}(\text{CH}_3)_2\text{SiInd}_2\text{ZrCl}_2$. The enantiomers are designated as $(R, R)$ and $(S, S)$ to describe the two coordination sites in each enantiomer. Actually, the synthesis of a $C_2$ ansa metallo-
cene usually produces a mixture of the racemic pair plus the meso compound $(R, S)$. The
meso compound, which is a diastereomer of the racemic pair, can be separated from the race-
cmic mixture by physical techniques such as recrystallization. The meso stereoisomer poss-
sesses $C_S$ symmetry, and its stereoselectivity is very different from that of the
enantiomeric pair (Sec. 8-5a-3).

The stereoselectivity of the propagating species derived from $C_2$ ansa metallocenes, as
well as other metallocenes, is described by molecular mechanics studies [Busico and Cipullo,
2001; Cavallo et al., 1998; Monaco et al., 2000; Resconi et al., 2000]. The steric environment
at the active site, consisting of the $\eta^3$-ligands and the polymer chain, determines which enan-
tioface of the incoming monomer is coordinated to the transition metal vacancy. The effect of
the chiral active site is indirect, at least for propene polymerization—the mechanism is chiral
orientation of the propagating polymer chain. The chiral active site forces the propagating
polymer chain to assume an orientation that minimizes steric interaction with one of the
$\eta^5$-ligands and this results in discrimination between the two enantiofaces of the monomer.
The first C–C bond of the polymer chain is bent to one side, which favors 1,2-insertion of
propene with the enantioface that results in the methyl group anti to the first C–C bond. This
corresponds to the re face for the $(R, R)$-propagating species and the si face for the $(S, S)$-
propagating species. Polymerization is highly regioselective since 2,1-insertion is less
favored because it involves steric interactions between the methyl group of monomer and
the $\eta^5$-ligands.

Migratory insertion of monomer places the propagating chain in the coordination site pre-
viously occupied by monomer, a result of the principle of least nuclear motion (Sec. 8-4e).
The next monomer molecule coordinates at the site previously occupied by the propagating
chain and then reacts by migratory insertion. There is back-and-forth migratory insertion
between the two coordination sites. Isotactic polymer is produced because the two coordina-
tion sites are homotopic with the same enantioselectivity. Both enantiomers of the initiator
produce isotactic polymer. Successive propagations with one enantiomer occur only through
the re face and the other enantiomer, only through the si face. Catalyst site control of pro-
pagation is verified by $^{13}$C NMR analysis of the stereoerrors with $(mnmr) = (mmrr) =
2(mrrm)$ as expected (Table 8-3).

8-5c-1 Effect of Initiator Structure

$C_2$ ansa metallocenes are inherently isoselective, but the degree of isoselectivity as well
as activity and polymer molecular weight vary considerably depending on the specific
$\eta^5$-ligands, substituents on the ligands, transition metal, bridge, and reaction conditions [Busico and Cipullo, 2001; Coates, 2000; Resconi et al., 2000]. The structural variables interact in a complex manner to change the course of the polymerization by altering the bite angle and stereorigidity of the initiator and its derived propagating species. One assumes that there is an optimum bite angle and stereorigidity that maximizes the imposition of the initiator’s chirality on the propagating species and coordinated monomer. If the bite angle is too large and the stereorigidity too low, isoselectivity is decreased because the propagating chain and monomer are too loosely held in place. If the bite angle is too small and the stereorigidity too high, isoselectivity is decreased because the propagating chain and monomer have difficulty coordinating to the active site and/or do have the necessary mobility to rapidly undergo migratory insertion. Although the exact interrelationship between the various structural parameters is not clear, a number of generalizations have been established:

1. Metalloccenes based on zirconium (referred to as zirconocenes) are the most widely studied and useful at present. Hf metalloccenes are generally less active but produce higher molecular weights than do Zr metalloccenes. Ti metalloccenes are less active and less stereoselective than Zr and Hf. Zr metalloccenes are the most useful because they are the most active and have been optimized by appropriate structural variations to yield very high stereoselectivity coupled with high polymer molecular weight and high activity at useful temperatures (>50°C). Some examples are given in Table 8-6.

2. Substituents in the 3- and 4-positions of Cp ligands have the greatest effect for increasing isoselectivity, activity, and polymer molecular weight. Substituents in the 2- and 5-positions have a positive but lesser effect. The 6-membered ring plays the role of 4- and 5-substituents in Ind and H4Ind ligands. H4Ind ligands generally increase isoselectivity with some decrease in activity, and sometimes also a decrease in polymer molecular weight.

![Cyclopentadienyl](image1.png)

![Indenyl](image2.png)

**TABLE 8-6 Propene Polymerization with rac-Zirconocene/MAO**

<table>
<thead>
<tr>
<th>Initiator</th>
<th>T (°C)</th>
<th>A$^a$</th>
<th>$(\text{mmmm})$</th>
<th>$M^b$ ($\times 10^{5}$)</th>
<th>PDI</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\text{Me}_2\text{Si}(3$-$\text{Me}$-$\text{Cp})_2\text{ZrCl}_2$</td>
<td>30</td>
<td>16.3</td>
<td>0.93</td>
<td>0.17</td>
<td>2.3</td>
</tr>
<tr>
<td>$\text{C}_2\text{H}_4(3$-$\text{Me}$-$\text{Cp})_2\text{ZrCl}_2$</td>
<td>40</td>
<td>5.8</td>
<td>0.92</td>
<td>0.20</td>
<td>2.3</td>
</tr>
<tr>
<td>$\text{Me}_2\text{Si}(2,3,5$-$\text{Me}_3\text{Cp})_2\text{ZrCl}_2$</td>
<td>50</td>
<td>207</td>
<td>0.96</td>
<td>1.8</td>
<td>1.9</td>
</tr>
<tr>
<td>$\text{Me}_2\text{Si}(2$-$\text{Me}$-$4$-$\text{C}_6\text{H}_5$-$\text{Ind})_2\text{ZrCl}_2$</td>
<td>70</td>
<td>755</td>
<td>0.95</td>
<td>7.3</td>
<td>—</td>
</tr>
<tr>
<td>$\text{Me}_2\text{C}(3$-$\text{t}$-$\text{Bu}$-$\text{Ind})_2\text{ZrCl}_2$</td>
<td>50</td>
<td>125</td>
<td>0.95</td>
<td>0.89</td>
<td>—</td>
</tr>
<tr>
<td>$\text{CH}_2(3$-$\text{t}$-$\text{Bu}$-$\text{Ind})_2\text{ZrCl}_2$</td>
<td>50</td>
<td>37</td>
<td>0.97</td>
<td>2.4</td>
<td>—</td>
</tr>
<tr>
<td>$\text{Me}_2\text{Si}(4$-$\text{[1}$-$\text{naphthyl}]$-$\text{Ind})_2\text{ZrCl}_2$</td>
<td>50</td>
<td>875</td>
<td>0.99</td>
<td>9.2</td>
<td>—</td>
</tr>
<tr>
<td>$\text{Me}_2\text{C}(\text{Ind})_2\text{ZrCl}_2$</td>
<td>50</td>
<td>66</td>
<td>0.81</td>
<td>0.11</td>
<td>—</td>
</tr>
<tr>
<td>$\text{Me}_2\text{C}(\text{H}_4\text{Ind})_2\text{ZrCl}_2$</td>
<td>50</td>
<td>37</td>
<td>0.96</td>
<td>0.25</td>
<td>—</td>
</tr>
</tbody>
</table>

$^a$ Activity in units of kg PP (nmol Zr)$^{-1}$ h$^{-1}$.

$^b$ Either $M_w$ or $M_v$.

$^c$ Data from Coates [2000]. All other data from Resconi et al. [2000].
3. The effect of the bridge between ligands differs depending on the ligands. For the unsubstituted indenyl ligand, isoselectivity and molecular weight increase in the order CH₂ < CH₂CH₂ < (CH₃)₂C < Si(CH₃)₂. However, for the 3-t-butylindenyl ligand, CH₂ and (CH₃)₂C are highly isoselective, and more so than CH₂CH₂ and Si(CH₃)₂. The bite angle and stereorigidity of the system are affected differently by the bridge depending on the ligands. Initiators with bridges longer than two atoms are not useful. Markedly decreased isoselectivity and activity is observed with the CH₂CH₂CH₂ bridge. Bulkier or longer bridges such as (CH₃)₂SiCH₂CH₂Si(CH₃)₂ and (CH₃)₂SiOSi(CH₃)₂ yield initiators inactive for propene polymerization. Various other types of bridges have been studied with poor results. This includes bridges through the 6-membered rings in Ind and H₄Ind systems and two bridges in Cp systems.

4. The introduction of heteroatoms into the ligands via alkoxy and trisubstituted amino groups has been explored to improve initiator performance through electronic effects. This approach is not promising as initiator performance deteriorates with very few exceptions. The exceptions do not result in performance enhancements; at best, performance is unaffected.

5. Bisfluorenyl zirconocenes generally are neither highly active nor highly isoselective.

6. Polymerizations are highly regioselective with regioirregular placement generally in the range 0.3–1.0%, but regioselectivity is very sensitive to the ligands. At the extremes, there is less than 0.002% regioerrors with rac-CH₂(3-t-Bu-Ind)₂ZrCl₂/MAO, but 20% with rac-CH₂CH₂(2,4-Me₂-H₄Ind)₂ZrCl₂/MAO. C₂ metallocenes generally are less regioselective than the metallocenes that are syndioselective or aselective.

Some 3,1-placements (CH₂CH₂CH₂) are observed in propene polymerization, a result of isomerization after a 2,1-placement [Busico and Cipullo, 2001].

8-5c-2 Effect of Reaction Variables
Polymerization at higher temperature increases the reaction rate but decreases isoselectivity, regioselectivity, and polymer molecular weight. For example, (mmmm) decreases from 0.92 to 0.83 for polymerization of liquid propene with rac-C₂H₄(Ind)₂ZrCl₂/MAO when the temperature is increased from 20 to 70°C. \( M_w \) decreases from 56,000 to 19,600, and the regioirregular fraction increases from 0.4 to 0.7%. Similar effects were observed in the polymerization of 1-hexene by Me₂Si(H₄Ind)₂ZrCl₂/MAO [Zhao et al., 2000]. Increased temperature affects the polymerization by decreasing the rigidity of the initiator and propagating species (increased fluxionality). The result is epimerization of the propagating chain end, specifically, scrambling the chirality of the last monomer unit inserted into the propagating chain (the first monomer unit attached to the transition metal atom). The greater the inherent stereorigidity of the initiator, the less the effect of increased temperature on polymerization. 

Isoselectivity decreases with decreasing monomer concentration. Epimerization of the propagating chain end is a unimolecular process, unaffected by monomer concentration. Propagation is slowed by decreased monomer concentration, allowing time for epimerization to occur. The effect varies considerably depending on the initiator. For rac-C₂H₄(Ind)₂ZrCl₂/MAO, (mmmm) decreases from 0.87 to 0.55 when the monomer concentration is decreased from 11 to 0.4 mol L⁻¹. The same effect is observed in the polymerization of 1-hexene by Me₂Si(H₄Ind)₂ZrCl₂/MAO [Zhao et al., 2000]. In the extreme case of very high dilution, the polymer molecular weight decreases enormously and the polymer becomes atactic. The polymerization is less sensitive to monomer concentration for the more stereorigid rac-Me₂Si
(2-Me-4-C₆H₅-Ind)₂ZrCl₂/MAO. The \( (m) \) fraction decreases from 0.97 to 0.93 when the monomer concentration is decreased from 1.5 to 0.1 mol L\(^{-1}\).

Isoselectivity also varies with the initiator and coinitiator concentrations. Isoselectivity decreases with increasing zirconocene and MAO concentrations in the polymerization of 1-hexene by Me₂Si(H₄Ind)₂ZrCl₂/MAO [Zhao et al., 2000]. For polymerization at 50°C with \([M] = 8.0 \text{ mol L}^{-1}\), \((mmm)\) decreases from 0.90 to 0.76 when the zirconocene concentration increases from 5.2 to 104 \(\mu\)M with [MAO] kept constant at 62 mM. When [MAO] is increased from 4.0 to 62 mM with [zirconocene] constant at 52 \(\mu\)M, \((mmm)\) decreases from 0.92 to 0.84. Polymerization at higher initiator and coinitiator concentrations at constant monomer concentration is essentially equivalent to polymerization at lower monomer concentrations at constant initiator and coinitiator concentrations. The amount of monomer available per propagating species decreases, there is more time available for epimerization, and isoselectivity decreases.

The effects of temperature and reactant concentrations on regioselectivity generally mirror the effects on isoselectivity. Regioselectivity decreases with increasing temperature. For example, 2,1-placements increase from 0.4 to 0.7% and from 2.5 to 4.3% for liquid propene polymerizations with rac-C₂H₄(Ind)₂ZrCl₂/MAO and rac-C₂H₄(4,7-Me₂-1-Ind)₂ZrCl₂/MAO, respectively, when the polymerization temperature is increased from 20 to 70°C [Resconi et al., 2000]. Similar effects were observed for the polymerization of 1-hexene by Me₂Si(H₄Ind)₂ZrCl₂/MAO [Zhao et al., 2000]. Regioselectivity also decreases with decreasing monomer concentration. Additionally, the isomerization of 2,1-units to 3,1-units increases with increasing temperature and decreasing monomer concentration. For the polymerization of 1-hexene by Me₂Si(H₄Ind)₂ZrCl₂/MAO, regioselectivity decreases with increasing concentrations of zirconocene and MAO, although the effects are small [Zhao et al., 2000].

In summary, it is important to emphasize that the course of the polymerization depends not only on the initiator structure but also quite strongly on reaction variables such as temperature and reactant concentrations.

8-5d C₅-Symmetric Metallocenes

There are two types of C₅-symmetric metallocenes, XXX and XXXI (Table 8-5). Both types contain a mirror plane of symmetry—a horizontal plane in XXX, a vertical plane in XXXI. Both are achiral molecules, but they differ very significantly in stereoselectivity. XXX produces atactic polymer, while XXXI usually forms syndiotactic polymer.

The XXX type of C₅-symmetric metallocene is the meso diastereomer of a corresponding pair of enantiomers. For example, meso-(CH₃)₂SiInd₂ZrCl₂ is the meso diastereomer of rac-(CH₃)₂SilInd₂ZrCl₂ (XXXIV). The meso type of C₅ metallocene is referred to as meso C₅;
the other type of C₅ metalocene is not a meso compound and is referred to simply as a C₅ metalocene. The two types are distinguished by the presence or absence of the meso prefix.

The two coordination (active) sites of a meso C₅ metalocene are diastereotopic and nonequivalent, but achirrotopic. Each site resides in an achiral environment and polymerization produces a highly atactic polymer, although the regioselectivity is very high, even higher than the best C₂ metalocenes. Unlike some C₂ᵥ metalocenes, there are no reported cases of even modest stereoselective polymerization, either syndioselective or isoselective, due to chain end control.

C₅ metalocenes such as Me₂C(Cp) (Flu)ZrCl₂ are very different from the meso C₅ metalocenes. The two active sites are chirotopic, specifically enantiotopic, because the two ligands are symmetric but different. Each active site has a preference for the opposite monomer face, one site for the re face and the other for the si face, and the outcome is syndioselective polymerization. The mechanism of stereoselectivity is catalyst site control as shown by NMR analysis of stereoerrors, namely, \((rrrr) = (mmrr) = 2(rmmr)\) (Table 8-3). Highly syndiotactic polymer with \((rrrr)\) greater than 0.90, some as high as 0.95 and even slightly higher, have been observed with a number of initiators [Busico and Cipullo, 2001; Busico et al., 2003c; Grisi et al., 1998; Resconi et al., 2000]. The best of these syndioselective initiators are not quite as stereoselective as the best of the C₂ isoselective initiators. Highly syndiotactic polymer is generally achieved only at relatively low temperature and high monomer concentration. For example, \((rrrr)\) decreases from 0.94 at 0°C to 0.88 at 50°C in liquid propene polymerization with Me₂C(Cp) (Flu)ZrCl₂/MAO. Higher temperature and lower monomer concentration decrease stereoselectivity due to epimerization of the propagating chain end and/or by allowing back-flip (site epimerization) of the propagating chain to the other coordination site.

The effect of the transition metal is similar to that in the C₂ metalocenes. However, the differences between different metals are greater for the C₅ metalocenes; for example, titanium metalocenes do no yield even modestly syndioselective polymerization under any conditions of temperature and monomer concentration.

Polymerizations with C₅ metalocenes are highly regioselective, even more so than the C₂ metalocenes.

8-5e C₁-Symmetric Metalocenes

C₁-symmetric metalocenes possess no element of symmetry, neither a plane nor axis of symmetry. A C₅ metalocene becomes a C₁ metalocene when one of the ligands is unsymmetric; for instance, compare XXXII with XXXI in Table 8-5. Many different C₁ metalocenes have been studied, including Me₂C(3-R-Cp) (Flu)ZrCl₂ and Me₂C(Cp) (2-R-3-R’-Ind)ZrCl₂.

\[
\begin{align*}
\text{Me}_2\text{C}(3-R-\text{Cp}) \ (\text{Flu})\text{ZrCl}_2 & \quad \text{Me}_2\text{C}(\text{Cp}) \ (2-R-3-R'-\text{Ind})\text{ZrCl}_2 \\
\end{align*}
\]

The two coordination sites are chirotopic—each site is in a chiral environment. The two sites are diastereotopic, not enantiotopic. Thus, one might expect both sites to be
enantioselective, but not necessarily for the same monomer enantioface. Further, not all chiralotopic sites are highly enantioselective. The degree of enantioselectivity as well as activity and polymer molecular weight vary considerably depending on the specific \( \eta^5 \)-ligands, substituents on the ligands, transition metal, bridge, and reaction conditions (Sec. 8-5c-1). C\(_1\) metallocenes show a wider range of behaviors—from hemisotactic to moderate syndiotactic to moderate isotactic to highly isotactic polymer—which offers the possibility of obtaining a range of polymer products from elastomeric amorphous or low crystallinity polypropene to crystalline thermoplastics [Busico and Cipullo, 2001; Busico et al., 1997; Coates, 2000; Gomez and Waymouth, 2002; Kukral and Rieger, 2002; Kukral et al., 2000; Leino et al., 2001; Miller and Bercaw, 2002; Resconi et al., 2000; Rieger et al., 2002]. C\(_1\) metallocenes are often referred to as dual-side metallocenes because of the range of stereoselectivities of the two coordination sites.

Consider the Me\(_2\)C(3-R-Cp)(Flu)ZrCl\(_2\) system. Highly hemiisotactic (hit) polypropene is obtained when \( R = \) methyl for polymerization at \(-20^\circ\text{C}\) and \([M] = 1.8 \text{ mol L}^{-1}\); \( \langle mmmm \rangle = 0.16 \), theoretical value \( = 0.1875 \). Hemiisotactic polymerization corresponds to one of the two coordination sites being isoselective and the other site being aselective. The isoselective site is probably the more crowded site, the site on the side with the \( R \) group [Coates, 2000]. The aselective site is aselective even though it is chirotopic. Chirotopic sites are not stereoselective when there are difficulties of fit of the monomer and/or propagating chain at the site. The fit depends on the structure of the ligands, transition metal, and reaction parameters (Sec. 8-5c-1). Hemiisotacticty occurs under conditions of polymer chain migratory propagation (low temperature and high \([M]\)), specifically, propagation alternates at the two coordination sites. When polymerization occurs at higher temperature and lower monomer concentration, hemiisotacticty decreases and the reaction becomes more isoselective.

The trend toward isoselective polymerization increases with increasing bulk of the \( R \) group. Moderate isotactic polymer occurs with \( R = \) isopropyl, \( \langle mmmm \rangle = 0.64 \) at 60°C. The trend becomes dominant for \( R = t\)-butyl, \( \langle mmmm \rangle \) increases to 0.88 at 50°C and 0.95 at 30°C [Coates, 2000; Resconi et al., 2000]. The \( \langle mmmm \rangle \) fraction is even greater for the corresponding metallocene bridged by Me\(_2\)Si instead of Me\(_2\)C. Me\(_2\)Si(2-Me-Ind)(2-Me-4-C\(_6\)H\(_5\)-Ind)ZrCl\(_2\) is another highly isoselective C\(_1\) metallocene. The general mechanism for isoselectivity, indicated from molecular mechanics calculations, involves propagation occurring exclusively at one coordination site—the sterically more hindered site. The propagating chain coordinates at the less hindered side, whereas monomer coordinates at the more hindered side. Propagation involves polymer chain migratory insertion. However, the polymer chain is not highly stable at the more hindered side and it back-flips to the less hindered side, and the overall process repeats. Isoselectivity increases with increasing temperature and decreasing \([M]\), trends that are opposite those for isoselective C\(_2\) metallocenes. Higher temperature and lower \([M]\) facilitate the back-flip (site epimerization) of the polymer chain to the less hindered site. An alternate mechanism that may be responsible for isoselective polymerization with some C\(_1\) metallocenes is that both coordination sites are isoselective and propagation occurs by alternating monomer insertion at the two sites. Isoselective C\(_1\) metallocenes are highly regioselective, with the total of 2,1- and 3,1-units generally below 0.5%. The most isoselective C\(_1\) metallocenes are less isoselective than the most isoselective C\(_2\) metallocenes.

Some C\(_1\) metallocenes produce moderately syndiotactic polymer. For example, Me\(_2\)C(Cp)(2-R-3-R'-Ind)ZrCl\(_2\)/MAO with \( R = \) methyl and \( R' = \) CH\(_2\)SiMe\(_3\) yields polypropene with \( \langle rrrr \rangle = 0.74 \) for polymerization at 20°C [Gomez and Waymouth, 2002]. There is a report of much higher syndioselectivity with a C\(_1\) metallocene. Ph\(_2\)C(Cp)(2,3-R\(_2\)-Flu)ZrCl\(_2\)/MAO yields polypropene with \( \langle r \rangle > 0.98 \) [Miller, 2000].
Unbridged metallocenes rarely achieve highly stereoselective polymerizations because free rotation of the \( \eta^5 \)-ligands results in achiral environments at the active sites. An exception occurs when there is an appreciable barrier to free rotation of the \( \eta^5 \)-ligands. *Fluxional* (conformationally dynamic) metallocenes are initiators that can exist in different conformations during propagation. Stereoconvergent copolymers are possible when the conformations differ in stereoselectivity and each conformation has a sufficient lifetime for monomer insertion to occur prior to conversion to the other conformation(s). Isotactic–atactic stereoconvergent polymers would result if one conformation were isoselective and the other, aselective. An isotactic–atactic stereoconvergent polymer has potential utility as a thermoplastic elastomer in which the isotactic crystalline blocks act as physical crosslinks.

Bis(2-arylindene)zirconium dichlorides have been studied for the purpose of synthesizing isotactic–atactic stereoconvergent polymers [Busico et al., 2001; Lin et al., 2000; Lin and Waymouth, 2002; Nele et al., 2000]. Without the phenyl substituents, bisindenylzirconium dichloride yields atactic polypropene because there is rapid rotation of the \( \eta^5 \)-ligands. The 2-phenyl substituents in bis(2-arylindene)zirconium dichloride interfere with each other sufficiently that rotation is slowed to produce isotactic–atactic stereoconvergent polypropene. Three conformational isomers (conformers) are possible in this metallocene (Eq. 8-54). There is one syn conformer that has a meso-like structure analogous to the meso-\( C_5 \) ansa metallocenes and two anti enantiomeric conformers that together have a rac-like structure analogous to the rac-\( C_2 \) ansa metallocenes. The mechanism originally proposed to explain the formation of isotactic–atactic stereoconvergent polymer involved a slow rate of interconversion of the anti (rac) and syn (meso) conformers, a rate slower than the propagation rate, but faster than the chain breaking reactions. During the lifetime of a propagating chain, the propagating species alternates between the anti (rac) and syn (meso) conformers. The conformers are chiral and achiral, respectively, analogous to the corresponding isoselective rac-\( C_2 \) ansa metallocene and aselective meso \( C_5 \) ansa metallocene. The result is a stereoconvergent polymer with alternating isotactic and atactic blocks.

The \((m)\) fraction is in the range 0.6–0.7 for polymerization at high monomer concentration in the temperature range \(-25\) to \(25^\circ C\) [Resconi et al., 2000]. Substituents on the phenyl groups of the 2-phenylindene ligands, especially meta substituents, slow down the conformational interconversion, and this increases the isotacticity of the polymerization. Both steric and electronic factors operate to affect the interconversion of conformers. Bis(2-phenylindene)zirconium dichloride/MAO yields polypropene with \((mmm) = 0.33\) for polymerization of liquid propene at \(20^\circ C\). 3,5-Di-\( t \)-butyl and 3,5-difluoromethyl substituents increase \((mmmm)\) above 0.70 [Lin and Waymouth, 2002; Wilmes et al., 2002a,b].
More recent work indicates that the conformational equilibrium is not between rac and meso conformers, but between the two enantiomeric anti conformers of the rac mixture [Busico et al., 2002]. The prime support for this interpretation is the nature of the stereoeerrors in the isotactic sequences of the polymer. The stereoeerrors are \( \text{XXXV} \) instead of \( \text{XXXVI} \). The isotactic sequences consist of all-\( R \) isotactic blocks alternating with all-\( S \) isotactic blocks.

Polymerization with oscillating metallocenes is complicated because solvent fractionation of the polymer product shows separate fractions—highly atactic, mostly isotactic, and isotactic–atactic stereoblock. The mechanism of this phenomenon is not clear. It may result from the initiators not being perfectly single-site initiators. There is some evidence that a metallocene initiator may consist of more than one species, and that each species produces a different stereochemical result (Sec. 8-5g-1, 8-5h-1).

8-5g Coinitiators

8-5g-1 Methylaluminoxane (MAO)

MAO, the most widely used Lewis acid coinitiator (activator) (Eq. 8-52), is obtained by a “controlled” hydrolysis of trimethylaluminum (TMA). In spite of considerable research, the detailed structure of MAO remains unclear [Chen and Marks, 2000; Kissin and Brandomlini, 2003; Pedeutour et al., 2001; Wang et al., 2001; Ystenes et al., 2000]. MAO is probably a mixture of linear, cyclic, and three-dimensional structures containing the repeat unit \( \text{XXXVII} \) with \( n = 5–20 \).

\[
\left[ \frac{\text{CH}_3}{\text{Al}} \right]_n \quad \text{XXXVII}
\]

The exact composition in terms of the relative amounts of linear, cyclic, and three-dimensional structures and molecular weight probably varies with the detailed method of preparation. Most workers favor a three-dimensional spherical cagelike structure as the structure responsible for MAO’s coinitiator property. However, this may be an oversimplification, and more than one structure may be responsible for the observed activation of metallocenes by MAO. After activation of a metallocene initiator, MAO forms the basis of the counterion, \( (\text{ClMAO})^- \) or \( (\text{CH}_3\text{MAO})^- \). MAO normally contains TMA in two forms: free TMA and
associated TMA. Free TMA is undesirable since it decreases initiator activity and polymer molecular weight and also changes the kinetic profile from decay to buildup (behaviors 4 and 1-3, respectively, in Fig. 8-15). Free TMA can be removed by vacuum drying. It is very difficult to remove the associated TMA and MAO preparations almost always contain associated TMA. In fact, associated TMA may be important in the overall role of MAO as a coinitiator.

MAO is needed in large excess relative to the metallocene initiator, usually $10^2$–$10^4 : 1$, to achieve high activities and stable kinetic profiles. MAO is usually added first in a polymerization system, and a portion may actually serve the function of destroying deleterious impurities prior to the addition of the metallocene initiator. Otherwise, the impurities would destroy the metallocene if the metallocene were added first.

The structure of MAO is poorly defined and varies with preparation conditions, but it performs well in activating the metallocene initiator. The use of MAO is complicated by its lack of long-term storage stability. It is usually supplied by manufacturers as a cloudy solution of MAO in toluene; MAO has very low solubility in aliphatic solvents. Precipitation is often observed on long standing, especially if the container is frequently opened and exposed to moisture and oxygen. This precipitation, if not too extensive, may not affect the utility of the MAO as a coinitiator. A modified MAO, known as MMAO, offers some improvement in storage stability and improved solubility in aliphatics. MMAO is prepared by controlled hydrolysis of a mixture of trimethylaluminum and triisobutylaluminum.

The poorly defined structure of MAO leads to a corresponding lack of understanding of the actual initiating species formed by reaction between MAO and a metallocene. The usual description of these systems shows the initiating species as \(\text{XXVII}\) (Eq. 8-52), a monometallic species. Bimetallic species such as \(\text{XXXVIII}\) and \(\text{XXXIX}\) have also been proposed.

The actual initiating species in any polymerization system may be different, depending on the concentrations (both absolute and relative) of metallocene and MAO. The presence of more than one type of initiating species cannot be ruled out, which would mean that metallocenes do not necessarily always act as single-site initiators. The simultaneous presence of more than one type of initiating specis may also result from the presence of more than a single MAO (and corresponding counterion) structure.

\[\text{XXXVIII}\]

\[\text{XXXIX}\]

8-5g-2 Boron-Containing Coinitiators

Other Lewis acids have been considered as alternatives to MAO for two reasons: (1) one might avoid the cost of the large excess of MAO required to activate the metallocene; and (2) simpler systems, which allow isolation of the product(s) from reaction of metallocene and coinitiator, would be useful to obtain a better understanding of metallocene-initiated polymerizations.

Boron-based Lewis acids are useful coinitiators for metallocenes [Chen and Marks, 2000; Chen et al., 1998; Pedeutour et al., 2001; Zhou et al., 2001]. Organoboranes such as
tris(pentafluorophenyl)borane and organoborates such as trityl tetrakis(pentafluorophenyl)borate react with dimethyl metalallocenes to produce very active initiating metalloconium borates for olefin polymerization:

\[
\text{Cp}_2\text{Zr(CH}_3\text{)}_2 + \text{B(C}_6\text{F}_5\text{)}_3 \rightarrow [\text{Cp}_2\text{Zr(CH}_3\text{)}]^{+} [(\text{CH}_3\text{)}\text{B(C}_6\text{F}_5\text{)}_3]^{-}
\]

(8-55)

\[
\text{Cp}_2\text{Zr(CH}_3\text{)}_2 + (\text{C}_6\text{H}_5\text{)}_3\text{C}^+\text{B(C}_6\text{F}_5\text{)}_3^{-} \rightarrow [\text{Cp}_2\text{Zr(CH}_3\text{)}]^{+} [\text{B(C}_6\text{F}_5\text{)}_4]^{-} + (\text{C}_6\text{H}_5\text{)}_3\text{CCH}_3
\]

(8-56)

Unlike the case for MAO, one needs only an equimolar amount of the coinitiator to activate the initiator. In some reaction systems, higher polymerization activity is observed with an excess of initiator relative to coinitiator. Maximum activity is observed in some polymerization systems at a 2 : 1 initiator : coinitiator ratio, which indicates that bimetallic species such as XXXVIII are the actual initiating species [Wang et al., 2003]. A unique feature of the use of organoboranes and organoborates is that the complexes, both monometallic such as XL and XLI and the corresponding bimetallic complexes, have been isolated and characterized in a number of systems.

The high activity of these systems results from having a large, weakly coordinating anion to stabilize the metalloconium cation. The anion must be sufficiently weak in coordinating to the cationic active site so as not to compete with monomer for coordination to the active site. The order of coordinating ability for anions is [CH\(_3\)MAO]\(^-\) > [(CH\(_3\))B(C\(_6\)F\(_5\))\(_3\)]\(^-\) > [B(C\(_6\)F\(_5\))\(_4\)]\(^-\). [B(C\(_6\)H\(_5\))\(_4\)]\(^-\) is too strong a coordinating anion to allow initiation and propagation. Polymerization activity and polymer molecular weight generally increase in the opposite order. Deviations from this order are observed, indicating specific interactions between some initiators and anions. Also, the effect of anion structure cannot be considered independent of reaction variables such as reactant concentrations and temperature. The effect of anion structure on stereoselectivity is not so clear. Stereoselectivity often decreases with increasing activity, but the trend is not universal and can be circumvented by alterations in the initiator symmetry and ligands as well as reaction variables.

8-5h Kinetics

8-5h-1 Rate of Polymerization

The rate of polymerization is derived in a straightforward manner. The following derivation describes polymerization with a zirconocene (Zr) and MAO, but is general and applies to any metalloconocene coupled with any coinitiator. Reaction between the initiator zirconocene and MAO forms the active initiating species I*, which subsequently adds monomer to yield the initial propagating species M*:

\[
\text{Zr} + \text{MAO} \xrightleftharpoons[K_1]{K_2} \text{I*}
\]

(8-57)

\[
\text{I*} + \text{M} \xrightleftharpoons[K_3]{K_4} \text{M*}
\]

(8-58)
Propagation proceeds by successive additions of monomer to the propagating species:

\[ M^* + M \xrightarrow{k_p} M^* \]  

(8-59)

For the case where Reaction 8-58 is irreversible and fast (i.e., \([M^*] = [I^*]\)), the polymerization rate is

\[ R_p = K_1 k_p [Zr][MAO][M] \]  

(8-60)

which shows first-order dependencies of \(R_p\) on zirconocene, MAO, and monomer.

If Reaction 8-58 is reversible and slow, \([M^*] \neq [I^*]\), the polymerization rate is

\[ R_p = K_1 K_2 k_p [Zr][MAO][M]^2 \]  

(8-61)

and the dependence of \(R_p\) on monomer increases to second-order.

For a polymerization using an isolated metallocenium borate (I*), there is no equilibrium corresponding to Eq. 8-57, and the \(R_p\) expressions become

\[ R_p = k_p [I^*][M] \]  

(8-62)

and

\[ R_p = K_2 k_p [I^*][M]^2 \]  

(8-63)

in place of Eqs. 8-60 and 8-61, respectively.

Various studies with different metallocenes and coinitiators show a range of behaviors from first- to second order dependence of \(R_p\) on monomer for the polymerization of propene and other 1-alkenes [Frauenrath et al., 2001a; Herfert and Fink, 1993; Jungling et al., 1995; Liu et al., 2001c; Resconi et al., 2000; Zhao et al., 2000]. The observation of an intermediate order such as \(\frac{3}{2}\) may indicate two types of propagating species: thus, metallocenes are not simple single-site initiators. One possibility is propagation by a combination of tight and loose ion pairs. This possibility is supported by the effect of solvent on polymerization. Polymerization is faster in methylene chloride than in toluene. (Free-ion-propagating species are excluded from consideration by the absence of a common ion effect on rate.) A different possibility is a decrease in reactivity of a propagating species after a 2,1-addition of monomer, with reactivity subsequently restored by a 1,2-addition. If the two propagating species show different dependencies on monomer concentration, such as first- and second-order, the overall effect is an intermediate order of dependence of \(R_p\) on monomer. The observation that the dependence of \(R_p\) on monomer for the polymerization of 1-hexene by rac-Me2Si(H4Ind)2ZrCl2/MAO changes from first-order to 1.4-order in going from 0 to 50°C adds support for either of the possible mechanisms [Zhou et al., 2001].

The dependence of \(R_p\) on zirconocene is observed as first-order in a range of polymerization systems, in line with both Eqs. 8-60 and 8-62. The order of dependence of \(R_p\) on MAO is unclear. There is a minimum [MAO]/[Zr] ratio below which polymerization is not observed and a maximum [MAO]/[Zr] ratio above which no changes in \(R_p\) are observed. The minimum may correspond to the amount of MAO required to destroy deleterious impurities. The
maximum may correspond to the amount of MAO that completely converts the metallocene to the metallocenium cation. Thus, an observation of the effect of polymerization rate on MAO can be carried out only in the concentration range between the minimum and maximum. The minimum and maximum \( [MAO]/[Zr] \) ratios are 150 and 600 for the polymerization of 1-hexene by rac-Me_2Si(H_4Ind)_2ZrCl_2/MAO. This narrow range limits the precision and accuracy of kinetic experiments, but within these limits \( R_p \) was approximately first-order in MAO.

Activation energies are generally in the range 40–60 kJ mol\(^{-1}\); some lower values have been observed, in a range similar to that for traditional Ziegler–Natta initiators.

8-5h-2 Degree of Polymerization

The degree of polymerization is given by the same expression that described traditional Ziegler–Natta polymerizations (Eq. 8-50).

In the absence of H_2 and other transfer agents, polymer molecular weight is limited by various \( \beta \)-hydride transfers—from normal (1,2-) and reverse (2,1-) propagating centers, before and after rearrangement [Lehmus et al., 2000; Resconi et al., 2000; Rossi et al., 1995, 1996; Zhou et al., 2001] (Sec. 8-4i-2). Vinylidene, vinylene, and trisubstituted double-bond end groups are formed in 1-alkene polymerizations, vinyl and vinylene in ethylene polymerization. Vinyl groups are also produced in some 1-alkene polymerizations, not by \( \beta \)-hydride transfer, but by \( \beta \)-alkyl transfer (Sec. 8-4i-2).]

The relative amounts of the different double-bond end groups vary with the metallocene and reaction conditions. For example, consider the polymerization of 1-hexene by rac-Me_2Si(H_4Ind)_2ZrCl_2/MAO [Zhou et al., 2001]. The polymer molecular weight decreases steeply with increasing temperature because transfer activation energies are greater than propagation activation energies. Simultaneously, the vinylene content decreases and the vinylidene content increases with increasing temperature. Vinylene double bonds constitute about 85% of all double bonds at 0°C; vinylidene constitutes about 75% at 80°C. The trisubstituted double-bond content is low (8–10%) and unaffected by temperature.

The double-bond composition varies in a complex manner with changes in metallocene and monomer concentrations because the orders of dependence of the various \( \beta \)-hydride transfer reactions on monomer and metallocene are not the same [Liu et al., 2001c; Zhou et al., 2001]. Vinylidene content decreases with increasing monomer concentration, but increases with increasing metallocene. The trends for vinylene content are the opposite, while trisubstituted double-bond content is relatively unaffected by monomer and metallocene concentrations.

Extreme differences in double-bond end groups are sometimes observed with some initiators. Small amounts of vinyl end groups are found in polypropenes obtained with most initiators, metallocenes as well as traditional Ziegler–Natta initiators, under a range of reaction conditions. However, atactic polypropene with vinyl groups constituting 90% or more of the double-bond end groups are reported for sterically hindered metallocenes such as [(CH_3)_5Cp]_2MtCl_2 and those containingacenaphthyl substituents on the cyclopentadienyl ligands [Repo et al., 1997; Resconi et al., 1992]. Isotactic polypropene with vinyl groups constituting up to 80% of the double-bond end groups is obtained with rac-Me_2Si(2-Me-4-C_6H_3)ZrCl_2 at 75–120°C [Weng et al., 2000].

Molecular weight distributions in metallocene polymerizations are generally in the range of 2–5. PDI is often broadened at higher polymerization temperatures, which may indicate that more than one type of propagating species is present. In general, the more
stereoselective polymerizations yield narrower molecular weight distributions. Metallocene polymerizations yield narrower PDI polymers compared to traditional Ziegler–Natta polymerizations.

Molecular weight is a major determinant of the mechanical properties of a polymer at its use temperature while molecular weight distribution is indicative of its rheological properties, which relate to ease of polymer processing. A high-molecular-weight polymer has high strength, but processability is more difficult, especially if it has a narrow PDI. A broader PDI polymer is easier to process because it has better flow behavior. The molecular weight distributions of many metallocene polymers are sufficiently narrow, about 2, that processability is affected.

Various methods are available to broaden the PDI of a polymer [Alt et al., 2001; Beigzadeh et al., 2001; de Souza and Casagrande, 2001]. One method is the physical blending of different-molecular-weight polymers. Another method is a tandem polymerization—polymerization with two different operating conditions (different initiator, temperature, hydrogen pressure, or monomer concentration). This can be carried out in two different reactors whereby polymerization is performed in one reactor under one set of reaction conditions, and the resulting reaction mixture transported into a second reactor with polymerization continued under a second set of reaction conditions. It can also be performed in one reactor by changing conditions at some point in the overall process. A variation on the one-reactor process involves the simultaneous use of two different initiators (that produce different molecular weight polymers) in the reactor with all other reaction conditions the same.

8-5h-3 Supported Metallocenes

Commercial processes for traditional Ziegler–Natta polymerizations use supported initiators in slurry (suspension) and gas-phase processes. Replacement of the traditional Ziegler–Natta initiator by a metallocene initiator in a commercial process is most economically accomplished by drop-in technology—the existing process is essentially unchanged except for using a different initiator and adjusting reaction parameters such as temperature and reactant concentrations. This necessitates the fixing of a metallocene initiator on a support.

Various methods have been studied for obtaining supported metallocenes, with silica, \((\text{SiO}_2)_n\), as the most-used support material [Fink et al., 2000, 2001; Hlatky, 2000; Kaminsky, 2001; Tannous and Soares, 2002]. The methods differ in the sequence used for reaction of support, initiator, and coinitiator. The “coinitiator first” method is the most commonly used method. Silica is treated with MAO or with TMA followed by water to fix MAO on silica. The metallocene initiator is then added to produce the supported metallocenium species

\[
\begin{align*}
\text{Si-OH} & \underset{\text{MAO}}{\longrightarrow} \text{Si-O-MAO} \\
\text{Si-O-MAO} & \underset{\text{Cp}_2\text{ZrCl}_2}{\longrightarrow} \text{Si-O-MAOCl}^- \\
\text{Si-O-MAOCl}^- & \underset{\text{Cp}_2\text{Zr(CH}_3)_3}{\longrightarrow}\text{Cp}_2\text{Zr(CH}_3)_3^+
\end{align*}
\]

(Eq. 8-64). The equivalent species is formed by adding the metallocene first to silica followed by MAO or adding silica to premixed metallocene and MAO.

Supported metallocenes generally have lower activity than do homogeneous metallocenes because of steric hindrance by the support. At the same time, less MAO is required because
Deactivation processes are also hindered. Polymer molecular weight and stereoselectivity are either unaffected or increased, depending on the specific reaction system.

8-5i Branching in Metallocene Polymerizations

Long-chain branching (LCB), generally less than 0.1 branch per 1000 carbons, has been observed in some metallocene polymerizations of ethylene and propene [Nele and Soares, 2002; Soares, 2002; Weng et al., 2002]. The presence of even small amounts of LCB improves melt strength and melt processability of narrow PDI polymers. Thus, it is often useful to choose conditions, such as the metallocene, temperature, and other reaction conditions, that deliberately introduce long chain branching.

LCB results from the copolymerization of ethylene or propene with vinyl-terminated polymer formed during the polymerization. Since vinyl double bonds are more reactive in copolymerization than other types of double-bond end groups, LCB is increased under conditions that generate higher vinyl contents. This can be accomplished by choice of initiator and reaction conditions. Tandem polymerization is also useful, such as by using two initiators, one of which produces a vinyl-terminated oligomer (referred to as a macro-monomer or macromer) [Komon and Bazan, 2001; Quijada et al., 2001; Wang et al., 2000].

Short branches, specifically ethyl branches up to about 2 mol%, are formed in the polymerization of ethylene by meso–ansa zirconocenes containing unsubstituted cyclopentadienyl and indenyl ligands [Melillo et al., 2002]. Ethyl branches form by an isomerization process in which the usual β-hydride transfer to monomer is immediately followed by reinsertion of the vinyl-terminated polymer into the formed ethyl–zirconium bond.

8-6 OTHER HYDROCARBON MONOMERS

Traditional Ziegler–Natta and metallocene initiators polymerize a variety of monomers, including ethylene and α-olefins such as propene, 1-butene, 4-methyl-1-pentene, vinylcyclohexane, and styrene. 1,1-Disubstituted alkenes such as isobutylene are polymerized by some metallocene initiators, but the reaction proceeds by a cationic polymerization [Baird, 2000]. Polymerizations of styrene, 1,2-disubstituted alkenes, and alkynes are discussed in this section; polymerization of 1,3-dienes is discussed in Sec. 8-10. The polymerization of polar monomers is discussed in Sec. 8-12.

8-6a 1,2-Disubstituted Alkenes; Cycloalkenes

With a few exceptions, 1,2-disubstituted alkenes are not polymerized because of steric hindrance. The exceptions include 1-deuteropropene (Sec. 8-4g) and cycloalkenes. Polymers are obtained from some 1,2-disubstituted alkenes, but the reactions involve isomerization of the monomer to a 1-alkene prior to polymerization, e.g., 2-butene yields poly(1-butene) [Endo et al., 1979]. There is one report of polymerization of trans-2-butene to poly(trans-2-butene) using the α-diimine nickel initiators described in Sec. 8-8b [Leatherman and Brookhart, 2001].

Cycloalkenes undergo facile polymerization because ring strain is relieved on polymerization. Polymerization occurs using both traditional Ziegler–Natta and metallocene initiators [Boor, 1979; Coates, 2000; Dall’Asta et al., 1962; Ittel et al., 2000; Kaminsky, 2001; Natta...
et al., 1966; Pasquon et al., 1989]. Two possible routes are possible, ring-opening metathesis polymerization (ROMP) (Sec. 7-8) and polymerization through the double bond, for example, for cyclobutene.

\[
\begin{align*}
&\text{CH} \equiv \text{CH} \\
&\text{CH}_2 \text{CH}_2
\end{align*}
\]  

(8-65) 

\[
\begin{align*}
&\text{CH} \equiv \text{CH} \\
&\text{CH}_2 \text{CH}_2
\end{align*}
\]  

(8-66) 

Four different stereoisomers are possible for polymer XLII, poly(cyclobutane-1,2-diyl) (Sec. 8-1f). Cis and trans isomers are possible for polymer XLIII, poly(but-1-ene-1,4-diyl). (XLIII is the same polymer obtained by the 1,4-polymerization of 1,3-butadiene—Sec. 8.10). Traditional Ziegler–Natta initiators based on vanadium and metallocene initiators yield polymerizations almost exclusively through the double bond. Titanium, tungsten, and ruthenium initiators yield predominantly ROMP with varying amounts of cis and trans placements.

Cyclopentene yields mixtures of ROMP and double-bond polymerization with some Ti and V initiators. ROMP occurs exclusively with molybdenum and tungsten initiators, as well as Re, Nb, and Ta initiators. The relative amounts of cis and trans structures vary with the initiator and temperature [Dall’Asta et al., 1962; Pampus and Lehnert, 1974]. Metallocene initiators polymerize cyclopentene through the double bond, but the polymer structure consists of cis 1,3-placement (Coates, 2000; Kaminsky, 2001; Kelly et al., 1997]. 1,3-Placement occurs through an isomerization process similar to that responsible for 3,1-placement in propene polymerization (Sec. 8-5c-1). 1,3-Placement is also observed with nickel and palladium \(\alpha\)-diimine initiators [Sacchi et al., 2001] (Sec. 8-8b). 1,3-Placement has not been reported for other cycloalkene polymerizations.

Cyclohexene does not polymerize by either route except when it is part of a bicyclic structure as in norbornene. Stereochemistry in the ROMP of norbornene is complicated since the polymer, LXVI in Sec. 7-8, has possibilities of isomerism at both the ring and the double bond. Most polymerizations by the typical ROMP initiators yield cis stereochemistry at the cyclopentane ring with varying amounts of cis and trans placements at the double bond [Ivin, 1987]. Metallocene initiators yield predominantly double-bond polymerization with 1,2-placement [Janiak and Lassahn, 2001].

Little is known about the R/S isomerism (i.e., erythro and threo ditactic structures are possible) at the stereocenters that result from double-bond polymerization. Cycloheptene and higher cycloalkenes undergo only ROMP; double-bond polymerization does not occur because the larger rings can accommodate the double bond without being highly strained.

8-6b Styrene

Styrene is slightly polar compared to ethylene and \(\alpha\)-olefins. The lack of a strongly polar functional group allows styrene to undergo highly (>95–98%) isoselective polymerization
with many of the heterogeneous traditional Ziegler–Natta initiators effective for \(\alpha\)-olefins [Longo et al., 1990; Pasquon et al., 1989; Soga et al., 1988].

Highly (>95–98%) syndiotactic polystyrene is obtained using a variety of soluble titanium initiators such as CpTiCl\(_3\) and Cp\(_2\)TiCl\(_2\), and various substituted cyclopentadienyl analogs with MAO [Coates, 2000; Ishihara et al., 1988; Minieri et al., 2001a,b; Pellecchia et al., 1987; Po and Cardi, 1996; Schellenberg and Tomotsu, 2002; Schwecke and Kaminsky, 2001; Zambelli et al., 1989]. Zirconium initiators are also useful, but their activity is lower than that of the titanium initiators.

Partially isotactic polystyrenes are obtained with \(n\)-butyllithium in toluene at \(-40^\circ\text{C}\) and the heterogeneous \textit{alfin initiator} (allylsodium + sodium isopropoxide + NaCl) in hexane at \(-20^\circ\text{C}\) [Braun et al., 1960; Kern, 1960]. Partially syndiotactic polystyrenes are obtained with many different initiators, including \(n\)-butyllithium in toluene at \(-25^\circ\text{C}\) and higher temperatures and cesium naphthalene in toluene at \(0^\circ\text{C}\) or THF at \(-78^\circ\text{C}\) [Kawamura et al., 1982]. There is little tendency toward stereoselectivity with cationic initiators, although polymerizations of \(\alpha\)-methylstyrene by BF\(_3\), SnCl\(_4\), and other Lewis acids give moderate syndioselectivity [Wicke and Elgert, 1977].

8-6c Alkynes

Acetylene is polymerized to polyacetylene [IUPAC: poly(ethene-1,2-diyl)] by Ziegler–Natta initiators such as titanium tetraisobutoxide with triethylaluminum [Ito et al., 1974; Shelburne and Baker, 1987; Shirakawa, 2001; Theophilou and Naarman, 1989]. Polymerization at \(-18^\circ\text{C}\) yields a polymer with 90% cis content; polymerization at \(100^\circ\text{C}\) yields a polymer with >90% trans content. Polyacetylene, doped with an oxidant or a reductant, showed promise as a polymeric semiconductor [Chien, 1984]. That promise was not realized because of the oxidative instability of polyacetylene and emergence of cheaper and more stable polymer systems (Sec. 2-14j). Various substituted acetylenes such as phenylacetylene have also been studied [Kanki et al., 2002; Misumi et al., 2000].

8-7 COPOLYMERIZATION

Statistical copolymerization occurs among ethylene and various \(\alpha\)-olefins [Baldwin and Ver Strate, 1972; Cooper, 1976; Pasquon et al., 1967; Randall, 1978]. The reactivities of monomers in copolymerization generally parallel their homopolymerization behavior: ethylene > propene > 1-butene > 1-hexene [Soga et al., 1989]. Table 8-7 shows monomer reactivity ratios for several comonomer pairs.

Monomer reactivity ratios vary somewhat with the identity of the initiator in some systems, but the available data are insufficient to understand the general trends [Dankova and Waymouth, 2003; Fan et al., 2001; Kaminsky and Freidank, 2002; Wigum et al., 2000]. Among the structural parameters that might affect \(r_1\) and \(r_2\) are differences in monomer accessibilities to the initiator sites and differences that result from steric or electronic factors. One might also anticipate that \(r_1\) and \(r_2\) are affected by solvent polarity whereby a coordinat- ing solvent competes preferentially with one of the monomers for the initiator sites [Forlini et al., 2002; Sacchi et al., 2003].
Copolymerization of ethylene with a cycloalkene, especially a bulky one such as norbornene, yields an alternating copolymer if the comonomer feed is rich in the cycloalkene [Wendt et al., 2002].

8-8 POSTMETALLOCENE: CHELATE INITIATORS

The search for new initiators continues past the metallocenes. There is always the desire to produce polymers with different structures in a controlled manner by selective choice of the initiator. New initiators might produce polymers with structures different from those obtained by the metallocenes, such as branched instead of unbranched structures or different stereo-regularity or different molecular weight. Finally, commercial interests require a continuing search for new initiators that have not yet been patented. Several of the newer classes of stereoselective initiators are described below. They are referred to here by the general terms **postmetallocene** or **chelate initiators**.

### 8-8a ansa-Cyclopentadienyl–Amido Initiators

The **ansa-cyclopentadienyl–amido initiators** (CpA), often referred to as **constrained-geometry initiators**, retain one cyclopentadienyl ring of the metallocenes, but replace the other ring with a nitrogen substituent that coordinates with the metal center, usually a group 4 metal.
(Zr or Ti) [Busico et al., 2003a; Gibson and Spitzmesser, 2003; McKnight and Waymouth, 1998; Shapiro et al. 1990]. X is chlorine or methyl, and R is usually a bulky alkyl group such as \( t \)-butyl or an aryl group.

The absence of a second cyclopentadienyl ring coupled with the short bridge gives a very open environment at the metal site. This allows easier access for bulky monomers, including 1-alkenes and norbornene, compared to polymerization with metallocenes. CpA initiators yield ethylene copolymers not easily available with metallocenes. Copolymers containing significant amounts of comonomers such as styrene, norbornene, and \( \alpha \)-olefins from 1-hexene to 1-octadecene are easily obtained with CpA, but not with metallocene or traditional Ziegler–Natta initiators.

Long-chain branching via the in situ formation of vinyl macromonomers is also accessible with CpA initiators. A key feature of CpA initiators is that polymerizations can be carried out at higher temperatures (>100°C) to generate the vinyl macromonomer without loss of activity.

The open nature of the metal site limits catalyst site control by CpA initiators. Polymerization of propene proceeds with weak chain end control at low temperatures. The highest stereoselectivity reported is \( (\text{mmm})m = 0.77 \) using Me\(_2\)Si(Flu)(N-\( t \)-Bu)ZrCl\(_2\).

CpA initiators show high activity for ethylene homo- and copolymerizations, and high molecular weights are easily achieved. The activity, polymer molecular weight, and percent comonomer incorporation are dependent on the initiator structure. Activity, polymer molecular weight, and 1-octene incorporation increase for the Cp ligand in the order Me\(_4\)Cp > Cp > Ind. Larger bite angle, (Me\(_2\)Si)\(_2\) > Me\(_2\)Si, increases activity and 1-octene incorporation. Ti is slightly less active than Zr, decreases polymer molecular weight, but increases 1-octene incorporation. Activity with organoborate coinitiators is greater than with MAO.

**8-8b \( \alpha \)-Diimine Chelates of Late Transition Metals**

The high oxophilicity of the early transition metallocenes (Zr, Ti, Cr) prevents their use with polar monomers. Initiators based on late transition metals such as Ni and Pd would be useful because those metals are less oxophilic. Previous initiators based on late transition metals had low activity and were useful only for producing dimers and oligomers because of extensive \( \beta \)-hydride transfer. The use of bulky \( \alpha \)-diimine ligands favors monomer insertion over \( \beta \)-hydride transfer and gives access to polymers [Busico and Cipullo, 2001; Gates et al., 2000; Gibson and Spitzmesser, 2003; Ittel et al., 2000; Kunrath et al., 2002; Mecking, 2001].

Nickel and palladium \( \alpha \)-diimine chelates in the presence of MAO polymerize ethylene to polymers with weight-average molecular weights of \( 10^3 \text{–} 10^6 \). Palladium initiators yield higher molecular weights than do Ni initiators. Unlike Ni and Pd, platinum shows no activity.
The polyethylene produced with these initiators is different from other polyethylenes. There is considerable branching, mostly methyl branches, up to 100 branches per 1000 methylenes for Pd initiators. Branching is less for Ni initiators, 5–50 branches per 1000 methylenes. Branching occurs by the process described by Eqs. 8-68 and 8-69. Normal propagation involves the formation of XLIV with continued insertion of monomer. Methyl branching occurs when XLIV undergoes extensive β-hydride transfer to the metal center with the formation of vinyl-terminated polymer that remains coordinated at the metal site (XLV). Reinsertion of the vinyl-terminated polymer at the metal–hydride bond forms XLVI with a methyl branched polymer chain. More complex branching patterns have been observed, indicative of hydride transfer from positions further down the polymer chain than the β-position. Some long-chain branching has also been observed.

\[
\begin{align*}
\text{C}_2\text{H}_4\text{MAO} & \quad \text{Ni}^+ \quad \text{N} \quad \text{N} \quad \text{CH}_3 \\
& \quad \text{Ni}^+ \quad \text{N} \quad \text{N} \\
& \quad \text{NiBr}_2 \quad \alpha\text{-Diimine chelate}
\end{align*}
\]

The effect of initiator structure and reaction variables on polymer structure have been studied in detail for nickel initiators [Gates et al., 2000; Ittel et al., 2000]. Palladium initiators have been less studied. Polymer molecular weight is decreased by steric bulk in the R groups and ortho substituents in the Ar groups for both Pd and Ni initiators. Branching with Ni initiators is also reduced with these substitutions, but the tendency toward branching is so strong in Pd initiators that it is unaffected. Branching is increased by decreasing ethylene pressure. Increased reaction temperature results in increased branching coupled with a moderate decrease in polymer molecular weight. Polymer molecular weight is increased by using less coordinating anions, borates instead of MAO.
Both Ni and Pd initiators polymerize propene to give a combination of different microstructures, including 1,2- and 3,1-placements as well as methyl branches (via 2,3-placement) and long-chain branching. Room-temperature polymerizations with both Ni and Pd initiators yield atactic polypropene. Low temperature polymerizations proceed by chain end control to yield moderate syndioselectivity, \((rr)\) as high as 0.8, but usually less [Busico and Cipullo, 2001; McCord et al, 2001; Pappalardo et al., 2000; Zambelli et al., 2001].

Ni and Pd initiators polymerize cycloalkenes through the double bond with cis 1,3-placement (Sec. 8-6a). The only reported polymerization of an acyclic 2-alkene, specifically \(\text{trans-2-butene}\), involves the use of an \(\alpha\)-diimine initiator [Leatherman and Brookhart, 2001].

Pd initiators are very tolerant of oxygen-containing compounds, including air, water, and esters. Monomers such as acrylates polymerize very slowly, too slowly for practical purposes. Copolymerization of ethylene–acrylate has been achieved, but high acrylate comonomer feeds are needed to incorporate even small amounts of acrylate. The acrylate is incorporated mostly at the branch ends, and acrylate greatly slows down the reaction. Nickel initiators are even less efficient than the Pd initiators. Nitrogen-containing compounds, including amines, amides, and nitriles, completely inhibit polymerization by preferentially complexing with the initiator. Palladium initiators yield alternating copolymerizations between carbon monoxide and alkenes such as ethylene and propene [Coates, 2000; Drent and Budzelaar, 1996; Jiang and Sen, 1995; Sen, 1993].

Fe, Co, Cu, Rh, and Ru initiators are much less studied. They are not as active as the Ni and Pd initiators, but this can be altered in some cases by appropriate ligands.

Many other chelates of Ni and Pd have been studied, including the phosphorus and alkoxide chelate \(\text{XLVII}\) [Gibson and Spitzmesser, 2003; Mecking, 2001].

\[\text{XLVII}\]

### 8-8c Phenoxy–Imine Chelates

A variation on the \(\alpha\)-diimine ligand is the phenoxy–imine ligand, which has been studied mostly with the group 4 metals Ti and Zr [Ittel et al., 2000; Makio et al., 2002; Milano et al., 2002; Mitani et al., 2003; Saito et al., 2001, 2002; Tian and Coates, 2000]. A typical phenoxy–imine initiator is shown below, where \(R^1\) is usually a phenyl or substituted phenyl group.

\[
\begin{array}{c}
\text{Phenoxy–imine initiator} \\
\end{array}
\]

Ethylene is polymerized with good activity by both Zr and Ti phenoxy–imines to high molecular weight polymer, \(M_v = 10^4–10^6\). Activity increases with increasing steric bulk at
the R² group. Activity increases with increasing temperature from 0 to 40°C and then decreases due to initiator decomposition. Initiator stability is increased by electron-donating substituents on both the main phenyl ring and R¹. Molecular weight increases and branching decreases when R¹ contains a bulky alkyl group at the ortho position. Ortho-halogen groups on R¹ increase branching. Titanium initiators have lower activity and yield higher polymer molecular weights compared to zirconium initiators.

The stereoselectivity of polymerization depends on the transition metal and the structure of the initiator. Syndioselective polymerization is more common than isoselective polymerization. Some titanium phenoxy–imine initiators yield highly syndioselective polymerization by chain end control. For example the initiator with R² = R³ = t-butyl yields polypropene with (rr) = 0.92 [Tian and Coates, 2000]. The initiator with R² = t-butyl and R¹ = C₆F₅ yields polypropene with (rr) = 0.98 [Saito et al., 2001; Tian et al., 2001]. Moderately iso-selective polymerization is obtained with some zirconium and hafnium phenoxy–imine initiators [Saito et al., 2002].

8-9 LIVING POLYMERIZATION

Living polymerizations are useful for producing block copolymers and functionalized polymers. Facile chain-breaking reactions such as β-hydride transfer greatly limit the possibility of living polymerization for most of the polymerizations described in this chapter, but there are significant differences between the different types of initiators:

1. Living polymerization does not occur with traditional Ziegler–Natta isoselective heterogeneous initiators.

2. Traditional Ziegler–Natta syndioselective homogeneous vanadium initiators such as vanadium(III) acetylacetonate with Al(C₂H₅)₂Cl yield living polymerizations at low temperatures (≥−60°C) [Doi, 1986; Hagen et al., 2002].

3. There are very few reports of living polymerization by metallocene initiators. Living polymerization is reported for propene polymerization with Cp₂ZrMe₂ at −78°C or Cp₂HfMe₂ at −50°C using B(C₆F₅)₃ plus Al(OC₈H₁₇)₃ as coinitiator [Fukui et al., 1999]. Isoselective living polymerization of 1-hexene proceeds with rac-C₂H₄(Ind)₂ZrMe₂ and B(C₆F₅)₃ at −78°C.

4. The postmetallocene initiators offer the greatest potential for producing block copolymers and functionalized polymers. Many ansa-cyclopentadienyl–amido, α-dimine chelate, phenoxy–imine chelate, and related initiators produce living, stereoselective polymerizations [Busico et al., 2003b; Fujita and Coates, 2002; Gottfried and Brookhart, 2001; Hagihara et al., 1998; Hasan et al., 2001; Ittel et al., 2000; Jayaratne and Sita, 2000; Kawabe and Murata, 2001; Makio et al., 2002; Mehrkhodavandi and Schrock, 2001; Mitani et al., 2003; Saito et al., 2001; Tian et al., 2001; Tshuva et al., 2000]. Some of these polymerizations require low temperatures, others proceed as living polymerizations at 0°C and higher.

8-10 POLYMERIZATION OF 1,3-DIENES

8-10a Radical Polymerization

The polymerization of 1,3-dienes is more complicated than that of alkenes because of the greater number of possible stereoisomers (Secs. 8-1d and 8-1e). Table 8-8 shows the
polymers obtained in radical polymerization of 1,3-butadiene, isoprene, and chloroprene (2-chloro-1,3-butadiene). 1,4-Polymerization occurs in preference to 1,2- or 3,4-polymerization and trans 1,4-polymerization occurs in preference to cis 1,4-polymerization. (Both 1,2- and 3,4-polymerizations yield the same polymer for the symmetric 1,3-butadiene.) The temperature dependence of the structure of polybutadiene shows trans 1,4-addition to have a more favorable enthalpy of activation by about 12 kJ mol\(^{-1}\) relative to the cis-1,4-addition, although the latter has a more favorable entropy of activation by about 29 J mol\(^{-1}\) K\(^{-1}\). Trans 1,4-addition is favored over 1,2-addition by an enthalpy of activation of about 4 kJ mol\(^{-1}\) with no difference in the entropies of activation.

The polymerization of a 1,3-diene involves delocalization of the radical over carbons 2 and 4 of the terminal monomer unit (XLVIII). The predominance of 1,4-propagation over 1,2-propagation is primarily a consequence of the lower steric hindrance at carbon 4 relative to carbon 2 for bonding to an incoming monomer molecule. The difference increases as the 2-position becomes substituted with the result that 1,4-polymerization is even more favored in the polymerizations of isoprene and chloroprene (Table 8-8). The stability of the polymer is probably also a factor, since the 1,4-polymer (a 1,2-disubstituted alkene) is generally more stable than the 1,2-polymer (a monosubstituted alkene).

Several factors favor the preference of trans 1,4-polymerization over cis 1,4-polymerization. 1,3-Butadiene exists predominately in the transoid or s-trans conformation (ILa) as opposed to the cisoid or s-cis conformation (ILb). This is probably also the situation for...
isoprene [Craig et al., 1961; Hsu et al., 1969]. The conformation of the monomer need not translate into polymer stereochemistry since isomerization is possible after the \( s \)-trans or \( s \)-cis conformer adds to a propagating center. However, one expects predominance of the trans configuration of the allyl propagating radical (XLVIII) since the cis configuration involves steric hindrance to overlap among the \( p \)-orbitals of the carbon atoms of the allyl radical. Another factor is the greater stability of the trans 1,4-polymer over the cis 1,4-polymer. The configuration of the last monomer unit in the propagating chain is determined (with trans favored over cis) when the next monomer unit adds.

The stereochemistry of the 1,3-diene units in copolymerization is expected to be the same as in homopolymerization of 1,3-dienes. This expectation has been verified in styrene-1,3-butadiene copolymerizations at polymerization temperatures of \(-33\) to \(100^\circ\text{C}\) [Binder, 1954].

8-10b Anionic Polymerization

The anionic polymerization of 1,3-dienes yields different polymer structures depending on whether the propagating center is free or coordinated to a counterion [Morton, 1983; Quirk, 2002; Senyek, 1987; Tate and Bethea, 1985; Van Beylen et al., 1988; Young et al., 1984] Table 8-9 shows typical data for 1,3-butadiene and isoprene polymerizations. Polymerization of 1,3-butadiene in polar solvents, proceeding via the free anion and/or solvent-separated ion pair, favors 1,2-polymerization over 1,4-polymerization. The anionic center at carbon 2 is not extensively delocalized onto carbon 4 since the double bond is not a strong electron acceptor. The same trend is seen for isoprene, except that 3,4-polymerization occurs instead of 1,2-polymerization. The 3,4-double bond is sterically more accessible and has a lower electron density relative to the 1,2-double bond. Polymerization in nonpolar solvents takes place with an increased tendency toward 1,4-polymerization. The effect is most pronounced with

<table>
<thead>
<tr>
<th>Counterion</th>
<th>Solvent</th>
<th>Cis 1,4</th>
<th>Trans 1,4</th>
<th>3,4</th>
<th>1,2</th>
</tr>
</thead>
<tbody>
<tr>
<td>1,3-Butadiene (at 0°C)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Li</td>
<td>( n )-Pentane</td>
<td>35</td>
<td>52</td>
<td>13</td>
<td></td>
</tr>
<tr>
<td>Na</td>
<td>( n )-Pentane</td>
<td>10</td>
<td>25</td>
<td>65</td>
<td></td>
</tr>
<tr>
<td>K</td>
<td>( n )-Pentane</td>
<td>15</td>
<td>40</td>
<td>45</td>
<td></td>
</tr>
<tr>
<td>Rb</td>
<td>( n )-Pentane</td>
<td>7</td>
<td>31</td>
<td>62</td>
<td></td>
</tr>
<tr>
<td>Cs</td>
<td>( n )-Pentane</td>
<td>6</td>
<td>35</td>
<td>59</td>
<td></td>
</tr>
<tr>
<td>Li</td>
<td>THF</td>
<td>0</td>
<td>4</td>
<td>96</td>
<td></td>
</tr>
<tr>
<td>Na</td>
<td>THF</td>
<td>0</td>
<td>9</td>
<td>91</td>
<td></td>
</tr>
<tr>
<td>K</td>
<td>THF</td>
<td>0</td>
<td>18</td>
<td>82</td>
<td></td>
</tr>
<tr>
<td>Rb</td>
<td>THF</td>
<td>0</td>
<td>25</td>
<td>75</td>
<td></td>
</tr>
<tr>
<td>Isoprene (at 25°C)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Li</td>
<td>( n )-Hexane</td>
<td>93</td>
<td>0</td>
<td>7</td>
<td>0</td>
</tr>
<tr>
<td>Na</td>
<td>( n )-Hexane</td>
<td>0</td>
<td>47</td>
<td>45</td>
<td>8</td>
</tr>
<tr>
<td>Cs</td>
<td>None</td>
<td>4</td>
<td>51</td>
<td>37</td>
<td>8</td>
</tr>
<tr>
<td>Li</td>
<td>THF</td>
<td>0</td>
<td>30</td>
<td>54</td>
<td>16</td>
</tr>
<tr>
<td>Na</td>
<td>THF</td>
<td>0</td>
<td>38</td>
<td>49</td>
<td>13</td>
</tr>
</tbody>
</table>

\(^a\) Data from Tobolsky and Rogers [1959], Rembaum et al. [1962].
lithium ion, which has the greatest coordinating power of the counterions. Further, there is a strong tendency toward cis 1,4-polymerization over trans 1,4-polymerization with lithium even though the trans 1,4-polymer is more stable than the cis 1,4-polymer. This effect is much stronger for isoprene than 1,3-butadiene. The addition of small amounts of Lewis base such as \( N,N,N,N \)-tetramethylethylenediamine (TMEDA) to a polymerization in a non-polar solvent changes the stereochemistry to that observed in a polar solvent [Quirk, 1995, 2002]. 1,2-/3,4-Polymerization dominate over 1,4-polymerization due to solvation of the propagating species by the Lewis base.

There is no mechanism that adequately explains all features of the anionic polymerization of 1,3-dienes. NMR data indicate the presence of \( \pi \)- and \( \sigma \)-bonded propagating chains (\( \text{L} \) and \( \text{LI} \)). When reaction occurs in polar solvents, the carbanion center is delocalized as both anionic and cationic centers are solvated. Delocalization also occurs in nonpolar solvent when the counterion does not form a strong covalent bond to carbon. The situation is different for lithium counterion in nonpolar solvent. The allyl carbanion becomes localized in the absence of solvation as long as the counterion (lithium) forms a strong covalent bond to carbon. Localization yields \( \text{LI} \) instead of \( \text{LII} \). \( \text{LI} \) is the more stable carbanion—it is a primary carbanion and also contains the more substituted double bond. The formation of \( \text{LI} \) results in 1,4-polymerization in nonpolar solvent when lithium is the counterion. The predominance of cis 1,4-polymerization over trans 1,4-polymerization has been ascribed to the greater reactivity of cis-\( \text{LI} \), i.e., \( \text{LI} \) is formed as a mixture of cis and trans isomers (which are in equilibrium), but the cis isomer is more reactive [Van Beylen et al., 1988]. The preference for 1,2-polymerization of 1,3-butadiene indicates that the delocalized species \( \text{L} \) is preferentially attacked by monomer at carbon 2 instead of carbon 4. The reason for this is not evident.

The relative extents of the different structural units in 1,3-diene polymerization are not strongly dependent on polymerization temperature in the range −20 to 50°C [Morton, 1983]. Table 8-10 shows other features of 1,3-diene polymerization in nonpolar solvent.

TABLE 8-10  Effect of Solvent and Initiator Concentration on Stereochemistry in Anionic Polymerization of Isoprene at 20°C

<table>
<thead>
<tr>
<th>Solvent</th>
<th>[RLi] (mol L⁻¹)</th>
<th>Cis 1,4</th>
<th>Trans 1,4</th>
<th>3,4</th>
<th>1,2</th>
</tr>
</thead>
<tbody>
<tr>
<td>None</td>
<td>(8 \times 10^{-6})</td>
<td>96</td>
<td>0</td>
<td>4</td>
<td>0</td>
</tr>
<tr>
<td>None</td>
<td>(3 \times 10^{-3})</td>
<td>77</td>
<td>18</td>
<td>5</td>
<td>0</td>
</tr>
<tr>
<td>(n)-Hexane</td>
<td>(1 \times 10^{-5})</td>
<td>86</td>
<td>11</td>
<td>3</td>
<td>0</td>
</tr>
<tr>
<td>(n)-Hexane</td>
<td>(1 \times 10^{-2})</td>
<td>70</td>
<td>25</td>
<td>5</td>
<td>0</td>
</tr>
<tr>
<td>Benzene</td>
<td>(4 \times 10^{-5})</td>
<td>70</td>
<td>24</td>
<td>6</td>
<td>0</td>
</tr>
<tr>
<td>Benzene</td>
<td>(9 \times 10^{-3})</td>
<td>69</td>
<td>25</td>
<td>6</td>
<td>0</td>
</tr>
</tbody>
</table>

\(^a\)Data from Morton [1983].
with lithium counterion. The extent of cis 1,4-placement is greatest in the absence of solvent and at low initiator concentration [Worsfold and Bywater, 1978]. Isomerization of cis-Li to the more stable trans-Li increases faster than propagation of cis-Li with an increase in initiator concentration since propagation proceeds only through unassociated species while isomerization proceeds through both associated and unassociated species. Increasing the concentration of initiators such as alkyl lithium increases the concentration of associated species much more than unassociated species (Sec. 5-3d-5). The decrease in cis 1,4-placement observed for polymerization in a solvent relative to the neat polymerization is a consequence of the effect of monomer concentration. Increased monomer concentration increases the polymerization rate without any effect on isomerization. The extent of isomerization of cis-Li to trans-Li relative to propagation of cis-Li decreases with increasing monomer concentrations.

A variety of other initiators have been studied for the stereoselective polymerization of 1,3-dienes [Coates, 2000; Cooper, 1979; Endo and Hatakeyama, 2001; Ikai et al., 1999; Nath et al., 2002; Pasquon et al., 1989; Peluso et al., 1997; Porri and Giarrusso, 1989; Ricci et al., 1996; Senyek, 1987; Tate and Bethea, 1985; Visseaux et al., 2001]. Traditional Ziegler–Natta, metallocene, and other initiators yield remarkable results, surpassing the stereoselectivity by alkyl lithium initiators. Table 8-11 shows the polymer structures obtained

<table>
<thead>
<tr>
<th>Initiator</th>
<th>Polymer Structure</th>
</tr>
</thead>
<tbody>
<tr>
<td>1,3-Butadiene</td>
<td></td>
</tr>
<tr>
<td>TiCl₄/AlR₃: Al/Ti = 1.2</td>
<td>50% cis 1,4, 45% trans 1,4</td>
</tr>
<tr>
<td>TiCl₄/AlR₃: Al/Ti = 0.5</td>
<td>91% trans 1,4</td>
</tr>
<tr>
<td>Ti₄/AlR₃:b</td>
<td>95% cis 1,4</td>
</tr>
<tr>
<td>VCl₃ or VCl₄/AlR₃ or AlR₂Cl₆</td>
<td>94–98 trans 1,4</td>
</tr>
<tr>
<td>(η⁴-allyl)NiCl₂:</td>
<td>95% cis 1,4</td>
</tr>
<tr>
<td>(η⁴-allyl)NiCl₂:</td>
<td>95% cis 1,4</td>
</tr>
<tr>
<td>Rh(NO₃)₃:d</td>
<td>99% trans 1,4</td>
</tr>
<tr>
<td>Ni(octanoate)₂/AlR₃/HF:e</td>
<td>97% cis 1,4</td>
</tr>
<tr>
<td>CoCl₃/AlR₂Cl/pyridine:</td>
<td>98% cis 1,4</td>
</tr>
<tr>
<td>Co(acetylacetonate)₃/AlR₃/CS₂:e</td>
<td>99–100% st 1,2</td>
</tr>
<tr>
<td>CoCl₃/MAO:f</td>
<td>98–99% cis 1,4</td>
</tr>
<tr>
<td>Co(acetylacetonate)₃/MAO:g</td>
<td>94–97% cis 1,4</td>
</tr>
<tr>
<td>Me₂C(Cp)₂Sm(η⁴-allyl)₂Li:h</td>
<td>95% trans 1,4</td>
</tr>
</tbody>
</table>

| Isoprene |
|-----------|------------------|
| TiCl₄/AlR₃ or AlH₃:e | 96% cis 1,4 |
| VCl₃/AlR₃:e | 97% trans 1,4 |
| Ti(OR)₃/AlR₃:e | 60–70% 3,4 |

---

[a] Data from Natta et al. [1959a,b,c].
[b] Data from Moyer [1965].
[c] Data from Taube et al. [1987].
[d] Data from Tate and Bethea [1985].
[e] Data from Porri and Giarrusso [1989].
[f] Data from Nath et al. [2002].
[g] Data from Endo and Hatakeyama [2001].
[h] Data from Visseaux et al. [2001].
from 1,3-butadiene and isoprene using different initiators. The exceptional stereoselectivity and chemoselectivity of the initiators is even more evident here than in the polymerizations of propene and other 1-alkenes. Four different stereoregular polymers (cis 1,4-, trans 1,4-, st 1,2-, it 1,2-) are possible for 1,3-butadiene. Table 8-11 shows that except for the it 1,2-polymer, each of the other three polymers have been obtained in high stereoselectivity by appropriate choice of initiator. For isoprene, the cis 1,4- and trans 1,4-products are obtained in high stereoselectivity, but not the various 3,4- and 1,2-products.

Stereoselectivity in a polymerization with some initiator cannot always be considered independent of the reaction conditions. For example, the polymerization of 1,3-butadiene by vanadium(III) acetylacetonate and MAO is sensitive to temperature and polar additives [Endo and Yamanaka, 2001]. The polymer structure is 64% cis 1,4-, 14% trans 1,4-, and 22% 1,2- when polymerization is performed in toluene at 40°C, but becomes 9% cis 1,4-, 87% trans 1,4-, and 4% 1,2- at −18°C. The polymer becomes 11% cis 1,4-, 9% trans 1,4-, and 80% 1,2- at 40°C when triethylamine is present. On the other hand, the polymer structure is 94–97% cis 1,4- and independent of temperature for the corresponding polymerization by cobalt(III) acetylacetonate and MAO in the range 60 to −78°C [Endo and Hatakeyama, 2001].

Some work has also been reported on the polymerizations of various 1-substituted and 1,4- and 2,4-disubstituted 1,3-butadienes. Many more different stereoregular structures are possible for these monomers (Sec. 8-1e). The result is that very few of the completely stereoregular polymers have been obtained in high yield coupled with high stereoregularity. For example, (E)-2-methyl-1,3-pentadiene (LIII) was polymerized by neodymium(III) octanoate to a polymer consisting of 98–99% cis 1,4-structure but different fractions differed in isotacticity [Cabassi et al., 1988]. Similar results were found for other monomers [Pasquon et al., 1989; Porri and Giarrusoso, 1989; Takasu et al., 2001].

\[
\begin{align*}
\text{CH}_2=\overset{\text{I}}{\text{C}}=\text{CH}\equiv\text{CH}\equiv\text{CH}_3 & \quad \text{CH}_2=\overset{\text{I}}{\text{C}}=\text{CH}\equiv\text{CH}(\text{CH}_3)\overset{\text{I}}{\text{C}} \\
\text{LIII} &
\end{align*}
\]

Mechanisms have been proposed to explain stereoselectivity in 1,3-diene polymerizations, but these processes are less understood than the polymerization of ethylene and 1-alkenes [Peluso et al., 1997]. The ability to obtain cis 1,4-, trans 1,4-, and st 1,2-polymers from 1,3-butadiene, each in very high stereoregularity, by using different initiators has great practical utility for polymer synthesis even if it is not well understood why a particular initiator gives a particular stereoregular polymer.

8-10c Cationic Polymerization

The cationic polymerization of 1,3-dienes is not of practical interest as the products are usually low-molecular-weight with cyclized structures [Cooper, 1963; Kennedy, 1975]. Polymerizations have been carried out with conventional cationic initiators as well as Ziegler–Natta initiators under conditions (usually high ratio of transition metal to group I–III metal) where the latter act as cationic initiators. There is a general tendency toward 1,4-polymerization with trans 1,4 favored over cis 1,4. Cyclization occurs during propagation with the extent of unsaturation in the product varying from about 80% to almost zero depending on initiator, monomer, and reaction conditions [Delfour et al., 2003; Gaylord and Svestka, 1969; Gaylord et al., 1968; Hasegawa and Asami, 1978; Hasegawa et al., 1977].

Various mechanisms have been proposed to account for cyclization of 1,3-dienes. Cyclization probably occurs by attack of the propagating carbocation on trans 1,4-double bonds,
Extensive cyclization could occur by a corresponding sequential process

\[ \begin{align*}
R^+ & \quad \text{LIV} \\
\end{align*} \]

where \( R^+ \) is either an initiator species or the propagating carbocation LIV.

8-10d Other Polymerizations

There have been various attempts to achieve stereoselective polymerization of 1,3-dienes and also alkenes by imposing physical restraints on the monomer by means other than the initiator, including polymerizations of crystalline monomer, monomer monolayers, canal complexes, and liquid crystals [Allcock and Levin, 1985; Audisio et al., 1984; Bowden et al., 1978; DiSilvestro et al., 1987; Finkelmann et al., 1978; Miyata et al., 1977; Naegle and Ringsdorf, 1977; Nagahama and Matsumoto, 2001]. However, these polymerizations have generally been less stereoselective than those achieved using the traditional Ziegler–Natta, metallocene, and other initiators.

8-11 COMMERCIAL APPLICATIONS

The importance of coordination polymerization of alkenes and dienes is evident when it is noted that more than 40 billion pounds of polymers were produced by this route in the United States in 2001. This corresponds to 35–40% of the total industrial production of polymers from monomers containing carbon–carbon double bonds.

8-11a Process Conditions

Commercial polymerizations of ethylene, propene, and other \( \alpha \)-olefins are carried out as slurry (suspension) and gas-phase processes [Beach and Kissin, 1986; Diedrich, 1975; Lieberman and Barbe, 1988; Magovern, 1979; Vandenberg and Repka, 1977; Weissermel et al., 1975]. Solution polymerization has been used in the past for ethylene polymerization at 140–150°C, pressures of up to \( \sim 8 \) MPa (1 MPa = 145 psi = 9.869 atm), using a solvent such as cyclohexane. The solution process with its higher temperatures was employed for polymerization with the relatively low efficiency early Phillips initiators. (Polyethylene, but not the initiator, is soluble in the reaction medium under the process conditions.) The development of a variety of high-efficiency initiators has allowed their use in lower-temperature suspension and gas-phase processes, which are more advantageous from many
viewpoints (energy consumption, product workup). Solution polymerization is limited at present to producing low-molecular-weight polyethylene.

Both traditional Ziegler–Natta and metal oxide Phillips-type initiators are used in suspension polymerizations (Secs. 8-4a, 8-4j) [Kaminsky, 2001]. Both types of initiators are used for ethylene, but only the traditional Ziegler–Natta initiators are used for propene since Phillips-type initiators do not yield stereoselective polymerizations.

The use of gas-phase processes has increased greatly since their initial use in 1968 for ethylene polymerization. The process has been extended to ethylene copolymers and to propylene. The absence of solvent accomplished major economies for the gas-phase process relative to suspension polymerization. Pressures of about 2–3 MPa and temperatures in the range 70–105°C are employed in both fluidized-bed and stirred-bed reactors [Brockmeier, 1987]. The reaction medium is a well-stirred mixture of initiator and polymer powders together with gaseous monomer. After emerging from the reactor, polymer is separated from unreacted monomer, and the latter is recycled. Temperature control and temperature homogeneity throughout the reactor are critically important. The temperature must be maintained below the softening temperature of the polymer to prevent agglomeration of the polymer product into large lumps. Agglomeration leads to an inability to control reactor temperature, and this results in deterioration of the product as well as reactor shutdown. Highly active initiators based on both chromium and titanium are employed. For ethylene polymerization titanium-based initiators yield narrower molecular weight distributions than do chromium-based initiators [Karol, 1989].

Metallocene initiators reached commercialization near the beginning of the twenty-first century. These initiators probably accounted for about 5% of the total production of HDPE, LLDPE, and PP in 2002. The relative importance of metallocene initiators compared to the traditional Ziegler–Natta and Phillips–type initiators will increase in the future.

8-11b High-Density Polyethylene

Polyethylene produced by traditional Ziegler–Natta and Phillips-type initiators differs structurally from that obtained by radical polymerization (Sec. 3-14a) in having a much lower degree of branching (0.5–3 vs. 15–30 methyl groups per 500 monomer units). The two polyethylenes are often referred to as linear and branched polyethylenes, respectively. The lower degree of branching results in higher crystallinity (70–90% vs. 40–60%), higher density (0.94–0.96 vs. 0.91–0.93 g mL⁻¹), and higher crystalline melting temperature (133–138 vs. 105–115°C) for linear polyethylene. The polyethylenes produced by coordination and radical polymerizations are also referred to as high-density (HDPE) and low-density (LDPE) polyethylene, respectively. Compared to LDPE, HDPE has increased tensile strength, stiffness, chemical resistance, and upper use temperature combined with decreased low-temperature impact strength, elongation, permeability, and resistance to stress cracking. About 14 billion pounds of HDPE were produced in the United States in 2001. The two polyethylenes complement each other as about 8 billion pounds of LDPE were also produced.

Most HDPEs have number-average molecular weights of 50,000–250,000. These materials are used in a wide range of applications [Beach and Kissin, 1986; Juran, 1989]. The largest market (40%) consists of blow-molded products such as bottles (milk, food, detergent), housewares, toys, and pails. Injection-molded objects similar to those produced by blow molding constitute about 30% of the total market. Extruded products make up most of the remainder of the market for HDPE. This includes film for producing grocery and merchandise bags and food packaging, sheet for truck bed liners and luggage, pipe, tubing, and wire
and cable. Very-low-molecular-weight (several thousand) polyethylenes are used as wax substitutes in paper and spray coatings, crayons, and polishes.

Various specialty HDPEs are produced by polymerization to higher molecular weights. Increased molecular weight results in increased tensile strength, elongation, low-temperature impact resistance, and stress crack resistance, although processing is more expensive because of increased melt viscosity. High-molecular-weight high-density polyethylene (0.25–1.5 million molecular weight) is used for pressure piping in mining, industrial, sewer, gas, oil, and water applications. Other uses include large blow-molded parts such as shipping containers and bulk storage tanks and blown film for grocery and merchandise bags and can liners. Ultra-high-molecular-weight high-density polyethylene (>1.5 million molecular weight) has very high abrasion resistance and impact strength, the highest of any thermoplastic material. It can be processed without additives and stabilizers because the longer chains are resistant to mechanical scission, and even when chain scission occurs the molecular weight is sufficiently high to retain mechanical strength. Applications include low-speed bearings, gears for snowmobile drives, impellers for snow blowers, and the sliding surfaces in chutes and hoppers in the mining and freight industries as well as in agricultural and earthmoving machinery.

8-11c Linear Low-Density Polyethylene

Coordination copolymerization of ethylene with small amounts of an α-olefin such as 1-butene, 1-hexene, or 1-octene results in the equivalent of the branched, low-density polyethylene produced by radical polymerization. The polyethylene, referred to as linear low-density polyethylene (LLDPE), has controlled amounts of ethyl, n-butyl, and n-hexyl branches, respectively. Copolymerization with propene, 4-methyl-1-pentene, and cycloalkanes is also practiced. There was little effort to commercialize linear low-density polyethylene (LLDPE) until 1978, when gas-phase technology made the economics of the process very competitive with the high-pressure radical polymerization process [James, 1986]. The expansion of this technology was rapid. The utility of the LLDPE process limits the need to build new high-pressure plants. New capacity for LDPE has usually involved new plants for the low-pressure gas-phase process, which allows the production of HDPE and LLDPE as well as polypropene. The production of LLDPE in the United States in 2001 was about 8 billion pounds, the same as the production of LDPE. Overall, HDPE and LLDPE, produced by coordination polymerization, comprise two-thirds of all polyethylenes.

8-11d Polypropene

Isotactic polypropene (PP) has the lowest density (0.90–0.91 g mL⁻¹) of the major plastics and possesses a very high strength : weight ratio. It has a high crystalline melting point of 165–175°C and is usable to 120°C; both temperatures are higher than the corresponding values for HDPE. Sixteen billion pounds of PP were produced in the United States in 2001. About 20% of this production consists of copolymers, mostly copolymers containing 2–5% ethylene, which imparts increased clarity, toughness, and flexibility. Injection-molded products account for about 40% of the total polypropene usage [Juran, 1989; Lieberman and Barbe, 1988]. This includes durable goods (housings and parts for small and large appliances, furnitute and office equipment, battery cases, automobile interior trim, and airducts) and semirigid packaging (yogurt and margarine containers, caps and closures for medicines).
Packaging films (extruded, blown, and cast) are used in pressure-sensitive tapes and electrical applications and as replacements for cellophane and glassine films in liners for cereal boxes, wraps for snack foods, cigarettes, bread, and cheese. Blow-molded containers are used in applications where the higher use temperature of polypropene is needed (compared to HDPE), such as in packaging of syrups that are hot-filled.

Fiber products account for about 15% of polypropene consumption. The products range from continuous filaments for carpeting and rope to melt-blown fibers for nonwoven goods. Specific applications include outdoor carpets, yarns for upholstery and automobile seats, and replacements for canvas in luggage and shoes, disposable goods (diapers, surgical gowns), ropes, and cords.

8-11e Ethylene–Propene Elastomers

Copolymers and terpolymers of ethylene and propene, commonly known as EPM and EPDM polymers, respectively, are useful elastomers [Ver Strate, 1986]. EPM and EPDM are acronyms for ethylene-propene monomers and ethylene–propene–diene monomers, respectively. The terpolymers contain up to about 4 mol% of a diene such as 5-ethylidene-2-norbornene, dicyclopentadiene, or 1,4-hexadiene. A wide range of products are available, containing 40–90 mol% ethylene. The diene, reacting through one of its double bonds, imparts a pendant double bond to the terpolymer for purposes of subsequent crosslinking (Sec. 9-2b).

More than 800 million pounds of EPM and EPDM polymers were produced in the United States in 2001. Their volume ranks these materials fourth behind styrene-1,3-butadiene copolymers, poly(1,4-butadiene), and butyl rubber as synthetic rubbers. EPM and EPDM polymers have good chemical resistance, especially toward ozone. They are very cost-effective products since physical properties are retained when blended with large amounts of fillers and oil. Applications include automobile radiator hose, weather stripping, and roofing membrane.

8-11f Other Polymers

Isotactic poly(1-butene) and poly(4-methyl-1-pentene) are useful in applications which take advantage of their higher melting and use temperatures compared to polypropene and high-density polyethylene. Poly(1-butene) is used as hot- and cold-water plumbing pipe (both commercial and residential) and large-diameter pipe for transporting abrasive materials at high temperatures in the mining, chemical, and power generation industries. Poly-(4-methyl-1-pentene) is used to produce various laboratory and medical ware, cook-in containers for both hot-air and microwave ovens, and various other items for the lighting, automobile, appliance, and electronics industries. Syndiotactic polystyrene has recently been commercialized as an engineering thermoplastic. It is a highly crystalline polymer ($T_m = 270{\text{°C}}$) with very good strength properties, and a fast crystallization rate. Isotactic polystyrene also has many good properties but its slow crystallization rate make it uneconomical to commercialize.
8-11g Polymers from 1,3-Dienes

Several polymers based on 1,3-dienes are used as elastomers. These include styrene–1,3-butadiene (SBR), styrene–1,3-butadiene terpolymer with an unsaturated carboxylic acid (carboxylated SBR), acrylonitrile–1,3-butadiene (NBR or nitrile rubber) (Secs. 6-8a, 6-8e), isobutylene–isoprene (butyl rubber) (Sec. 5-2i-1), and block copolymers of isoprene or 1,3-butadiene with styrene (Sec. 5-4a).

\textit{cis}-1,4-Polyisoprene is produced using alkyllithium and Ti/Al Ziegler–Natta initiators. About 100 million pounds are produced annually in the United States to supplement the 2 billion pounds of natural rubber that are used. \textit{trans}-1,4-Polyisoprene is a specialty material produced in small amounts by means of V/Al Ziegler–Natta initiators. The uses for these materials were discussed in Sec. 8-2a-2.

About 1.5 billion pounds of \textit{cis}-1,4-poly(1,3-butadiene) were produced in the United States in 2001. This polymer has a lower $T_g$ and, therefore, higher resilience but poorer tear resistance and tensile strength than does natural rubber. For this reason, \textit{cis}-1,4-polybutadiene is not used alone but is blended with either natural rubber or SBR to produce tires for trucks and passenger automobiles. Considerable amounts of \textit{cis}-1,4-polybutadiene are also used in producing ABS materials (Sec. 6-8a).

More than 100 million pounds of polychloroprene (trade name: Neoprene) are produced annually in the United States by the radical (emulsion) polymerization of chloroprene. Polychloroprene, highly trans 1,4 in structure, is surpassed in oil and fuel resistance only by nitrile rubber, while its strength is superior to all except \textit{cis}-1,4-polyisoprene. The high cost of polychloroprene limits its use to applications requiring its unique combination of properties. It is used for wire and cable coatings and jackets, industrial belts and hoses, seals for buildings and highway joints, roof coatings, adhesives, gloves, and coated fabrics.

8-12 POLYMERIZATION OF POLAR VINYL MONOMERS

Polar monomers such as methacrylates and vinyl ethers undergo stereoselective polymerization when there is an appropriate balance between monomer, initiator, solvent, and temperature. Under conditions where the propagating species is free (uncoordinated), syndiotactility is increasingly favored with decreasing reaction temperature (Sec. 8-3). This is the case for all radical polymerizations and for those ionic polymerizations that take place in highly solvating media. Isoselective polymerization can occur in poorly solvating media where the propagating species is coordinated to the counterion. Many of the homogeneous polymerizations described in Chap. 5 result in stereoselective polymerization, although the degree of stereoselectivity generally is less than that observed in polymerizations with the traditional Ziegler–Natta, metalloocene, and chelate initiators.

8-12a Methyl Methacrylate

The stereoselective polymerization of various acrylates and methacrylates has been studied using initiators such as alkyllithium [Bywater, 1989; Pasquon et al., 1989; Quirk, 1995, 2002]. Table 8-12 illustrates the effects of counterion, solvent, and temperature on the stereochemistry of the anionic polymerization of methyl methacrylate (MMA). In polar solvents (pyridine and THF versus toluene), the counterion is removed from the vicinity of the propagating center and does not exert an influence on entry of the next monomer unit. The tendency is toward syndiotactic placement via chain end control. The extent of syndiotacticity
decreases in the order Li > Na > K, corresponding to the relative extents of solvation of different ions. The smallest ion Li\(^{+}\) is the most highly solvated and furthest removed from the propagating center. (This is analogous to the effect of polar solvent on propagation rate constants for anionic polymerization of styrene with different counterions. The ion-pair propagation rate constant for styrene is largest for Li and smallest for Cs, which is the reverse of the order in less polar solvent—Sec. 5-3d-2-b.) The extent of syndiotacticity increases with decreasing temperatures, as is evident in the data for polymerization with cesium as the counterion. The level of syndioselectivity is similar to that observed in radical polymerization of MMA, \((rr) = 0.79\) at \(-55\)°C [Hatada et al., 1988].

When nonpolar solvents are employed, polymerization proceeds by an anionic coordination mechanism. The counterion directs isotactic placement of entering monomer units into the polymer chain. The extent of isotactic placement increases with the coordinating power of the counterion (Li > Na ≫ K, Cs). The small lithium ion has the greatest coordinating power and yields the most stereoselective polymerization. Increased reaction temperature decreases the isoselectivity.

Mechanisms proposed to explain the isoselective polymerization of methyl methacrylate involve rigidification of the enolate propagating species by coordination of counterion with the terminal monomer unit (and possibly also the penultimate monomer unit) [Braun et al., 1962; Leitereg and Cram, 1968; Wiles and Bywater, 1965]. The rigid propagating chain end imposes stereoselectivity on monomer insertion in a manner analogous to that for a traditional Ziegler–Natta, metallocene, or chelate propagating species in alkene polymerizations.

The delicate nature of this stereoselectivity is evident when noting that the presence of triethylaluminum coinitiator changes the \(t\)-C\(_4\)H\(_9\)Li polymerization of MMA in toluene from

### TABLE 8-12 Effect of Counterion, Solvent, and Temperature of Polymerization of Methyl Methacrylate

<table>
<thead>
<tr>
<th>Solvent</th>
<th>Counterion</th>
<th>Temperature (°C)</th>
<th>((mm))</th>
<th>((mr))</th>
<th>((rr))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Toluene(^a)</td>
<td>Li</td>
<td>0</td>
<td>0.72</td>
<td>0.17</td>
<td>0.11</td>
</tr>
<tr>
<td>Pyridine(^a)</td>
<td>Li</td>
<td>0</td>
<td>0.08</td>
<td>0.32</td>
<td>0.60</td>
</tr>
<tr>
<td>Toluene(^b)</td>
<td>Li</td>
<td>−78</td>
<td>0.87</td>
<td>0.10</td>
<td>0.03</td>
</tr>
<tr>
<td>Toluene(^b)</td>
<td>Mg</td>
<td>−78</td>
<td>0.97</td>
<td>0.03</td>
<td>0</td>
</tr>
<tr>
<td>Toluene(^b)</td>
<td>Mg</td>
<td>−78</td>
<td>0.23</td>
<td>0.16</td>
<td>0.61</td>
</tr>
<tr>
<td>THF(^b)</td>
<td>Li</td>
<td>−85</td>
<td>0.01</td>
<td>0.15</td>
<td>0.84</td>
</tr>
<tr>
<td>THF(^b)</td>
<td>Li</td>
<td>−78</td>
<td>0.05</td>
<td>0.33</td>
<td>0.61</td>
</tr>
<tr>
<td>Toluene(^c)</td>
<td>Li</td>
<td>−78</td>
<td>0.78</td>
<td>0.16</td>
<td>0.06</td>
</tr>
<tr>
<td>Toluene(^d)</td>
<td>Li(^d)</td>
<td>−78</td>
<td>0</td>
<td>0.10</td>
<td>0.90</td>
</tr>
<tr>
<td>Toluene(^e)</td>
<td>Na</td>
<td>0</td>
<td>0.57</td>
<td>0.31</td>
<td>0.12</td>
</tr>
<tr>
<td>Pyridine(^e)</td>
<td>Na</td>
<td>0</td>
<td>0.12</td>
<td>0.46</td>
<td>0.42</td>
</tr>
<tr>
<td>Toluene(^e)</td>
<td>K</td>
<td>0</td>
<td>0.35</td>
<td>0.42</td>
<td>0.23</td>
</tr>
<tr>
<td>Pyridine(^e)</td>
<td>K</td>
<td>0</td>
<td>0.14</td>
<td>0.53</td>
<td>0.33</td>
</tr>
<tr>
<td>THF(^e)</td>
<td>Cs</td>
<td>20</td>
<td>0.10</td>
<td>0.56</td>
<td>0.34</td>
</tr>
<tr>
<td>THF(^e)</td>
<td>Cs</td>
<td>−100</td>
<td>0</td>
<td>0.40</td>
<td>0.60</td>
</tr>
</tbody>
</table>

\(^d\) Initiator = \(t\)-C\(_4\)H\(_9\)Li + Al(C\(_2\)H\(_5\))\(_3\).

\(^\text{a}\) Data from Braun et al. [1962].
\(^\text{b}\) Data from Bywater [1989].
\(^\text{c}\) Data from Kitayama et al. [1989].
\(^\text{d}\) Initiator = \(t\)-C\(_4\)H\(_9\)Li + Al(C\(_2\)H\(_5\))\(_3\).
\(^\text{e}\) Data from Muller et al. [1977], Kraft et al. [1980a,b].
isoselective, \( (mm) = 0.87 \), to syndioselective, \( (rr) = 0.90 \). This is also the reason for the two apparently divergent entries for Mg counterion in Table 8-12, one entry shows isoselectivity and the other shows syndioselectivity. Sterically hindered Grignard reagents give different results depending on whether the actual initiator present is \( t\text{-C}_4\text{H}_9\text{MgBr} \) or \( (t\text{-C}_4\text{H}_9)_2\text{Mg} \) and whether the Grignard reagent is free of trace amounts of ether [Bywater, 1989; Hatada et al., 1986; Quirk, 1995, 2002].

Metallocene initiators are also useful for methacrylate and acrylate polymerizations [Bandermann et al., 2001; Boffa and Novak, 2000; Bolig and Chen, 2001; Cameron et al., 2000; Chen et al., 1998; Collins and Ward, 1992; Collins et al., 1994; Deng et al., 1995; Frauenrath et al., 2001a,b; Holscher et al., 2002; Ihara et al., 1995; Jiang and Hwu, 2000; Karanikolopoulos et al., 2001; Li et al., 1997; Nguyen et al., 2000; Shiono et al., 1998; Soga et al., 1994; Yasuda, 2001; Yasuda et al., 1993]. Metallocenes based on both groups 3 and 4 transition metals initiate polymerization, although the group 3 metallocenes (Sc, Y, La) are somewhat more active than the group 4 metallocenes. Table 8-13 shows various initiators and their stereoselectivity in MMA polymerization. Studies on initiators other than the metallocenes have recently begun—the last entry in Table 8-13 is for an \( \text{ansa} \)-cyclopentadienyl–amido initiator. High stereoselectivity, both isoselective and syndioselective, are observed depending on the initiator. The level of stereoselectivity is somewhat less than that observed with \( \alpha \)-olefins, but this may be due only to the much smaller effort expended to date for MMA.

Propagation proceeds through an enolate species in the bimetallic mechanism described by Eq. 8-73 in which two metallocene species are involved—one is a neutral enolate, and the other is the corresponding metalloccenium cation [Collins et al., 1994; Li et al., 1997]. In LV, the propagating chain is coordinated at the neutral transition metal center (\( \text{Zr}^2 \)) and monomer

### TABLE 8-13 Metallocene Polymerization of Methyl Methacrylate

<table>
<thead>
<tr>
<th>Initiator</th>
<th>( T (\text{°C}) )</th>
<th>Polymer</th>
<th>PDI</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \text{SmH}[(\text{Me}_5\text{Cp})_2]_2 )</td>
<td>0</td>
<td>( (rr) = 0.95 )</td>
<td>1.1</td>
</tr>
<tr>
<td>( \text{Cp}_2\text{YCl(MTHF)/MAO}^{a,d} )</td>
<td>( -60 )</td>
<td>( (rr) = 0.90 )</td>
<td>—</td>
</tr>
<tr>
<td>( \text{rac}-\text{C}_2\text{H}_4(H_2\text{Ind})_2\text{ZrMe}_2/\text{Bu}_3\text{NHBPh}_4^{c} )</td>
<td>0</td>
<td>( (mm) &gt; 0.90 )</td>
<td>1.5</td>
</tr>
<tr>
<td>( \text{Cp}_2\text{ZrMe}_2/\text{Et}_3\text{NHBPh}_4^{e} )</td>
<td>0</td>
<td>( (rr) = 0.80 )</td>
<td>1.2–1.4</td>
</tr>
<tr>
<td>( \text{rac}-\text{C}_2\text{H}_4(H_2\text{Ind})_2\text{ZrMe}_2/\text{Bu}_3\text{NHBPh}_4^{f} )</td>
<td>40</td>
<td>( (mm) = 0.94 )</td>
<td>1.3</td>
</tr>
<tr>
<td>( \text{Cp}(\text{Flu})\text{ZrMe}_2/\text{Bu}_3\text{NHBPh}_4^{g} )</td>
<td>0</td>
<td>( (rr) = 0.74 )</td>
<td>1.2</td>
</tr>
<tr>
<td>( {\text{rac}-\text{Me}_2\text{Si(Ind)}_2\text{ZrMe}}_2 \text{MePBB}^{-b,h} )</td>
<td>0</td>
<td>( (mm) = 0.93 )</td>
<td>—</td>
</tr>
<tr>
<td>( \text{Me}_2\text{CCp(Ind)ZrMe(TTHF)+BPh}_4^{-i} )</td>
<td>( -20 )</td>
<td>( (mm) = 0.94 )</td>
<td>1.2</td>
</tr>
<tr>
<td>( \text{Me}_2\text{CCp}_2\text{ZrMe}(\text{TTHF})^+\text{BPh}_4^{-j} )</td>
<td>( -45 )</td>
<td>( (rr) = 0.89 )</td>
<td>1.3</td>
</tr>
<tr>
<td>( \text{Me}_2\text{Si(Me}_4\text{Cp})/(N-t\text{-Bu})\text{ZrL}_2^{2-}\text{Bar}_4^{-j,k} )</td>
<td>( -40 )</td>
<td>( (mm) = 0.96 )</td>
<td>1.2</td>
</tr>
</tbody>
</table>

\( ^a \text{ZnEt}_2 \) is also present.

\( ^b \text{PBB} = \text{tris(2,2’-2”,2’”-perfluorobiphenyl)borane.} \)

\( ^c \) Data from Yasuda et al. [1993].

\( ^d \) Data from Jiang and Hwu [2000].

\( ^e \) Data from Collins and Ward [1992], Collins et al. [1994].

\( ^f \) Data from Deng et al. [1995].

\( ^g \) Data from Shiono et al. [1998].

\( ^h \) Data from Chen et al. [1998].

\( ^i \) Data from Frauenrath et al. [2001a].

\( ^j \) \( L = \text{Me}_2\text{C}(\text{OR})\text{O}, L = \text{THF}, \text{Ar} = 3,5-(\text{CF}_3)_2\text{C}_6\text{H}_3. \)

\( ^k \) Nguyen et al. [2000].
at the transition metal cation center ($Z^b_b$). Monomer insertion into the polymer chain proceeds with the electron flow indicated by the arrow in LV. The result is LVI with an empty coordination site, ready to coordinate the next monomer unit and facilitate subsequent monomer insertion. The roles of the neutral and cationic metallocenes alternate with each monomer insertion. The rationale for the bimetallic mechanism, instead of a monometallic mechanism, is that a group 4 transition metal may not be sufficiently electropositive for one metal center to coordinate with two different oxygens (one from the enolate species and one from monomer). A monometallic mechanism is assumed for MMA polymerization with group 3 metallocenes since the group 3 metals are larger and more electropositive than group 4 transition metals [Boffa and Novak, 2000].

Metalocene polymerization of MMA proceeds with differences compared to polymerizations of ethylene and $\alpha$-olefins. A moderately coordinating anion such as $[\text{B}(\text{C}_6\text{H}_5)_4]^-$ can be used with MMA because the polar MMA can displace it from the initiator’s coordination site. Alkene monomers are generally unable to displace $[\text{B}(\text{C}_6\text{H}_5)_4]^-$ and polymerization does not proceed. The polarity of MMA and, more specifically, its Lewis base character prevents polymerization if the monomer and coinitiator are mixed together prior to the addition of monomer [Cameron et al., 2000]. Monomer coordinates strongly to the coinitiator and renders the coinitiator ineffective for reaction with the metallocene. Polymerization is accomplished by mixing the metallocene and coinitiator together to form the active initiating species prior to the addition of monomer. Another approach involves the addition of a large excess of another Lewis acid such as diethylzinc to displace the coinitiator from monomer prior to addition of initiator.

There is a strong interest in copolymerization of alkenes with polar monomers to alter the characteristics of a nonpolar polymer such as polyethylene or polypropene by introduction of polar functional groups. The polar groups would allow control over properties such as adhesion, compatibility with other polymers, solvent resistance, and rheological behavior. However, there is an inherent problem to achieving this goal for MMA and other (meth)acrylates by use of metallocene, traditional Ziegler–Natta, or any other type of anionic initiator. These monomers polymerize through enol intermediates, whereas alkenes polymerize through carbanion intermediates. Even more important is the big difference in the interaction of the nonpolar and polar monomers with metal centers in the initiator. To date there has been no success in finding metallocene or other initiator systems that allow a back-and-forth crossover between the two mechanisms. Thus, random copolymerization is not possible except in the rare cases of monomers with protected functional groups [Boffa and Novak, 2000].

Block copolymers have been successfully synthesized because many metallocene polymerizations of MMA proceed as living polymerizations, and it is possible to have a single one-way crossover from carbanion (alkene) polymerization to MMA (enolate) polymerization with metallocene and related initiators, especially when group 3 transition metal initiators are used [Boffa and Novak, 2000; Desurmont et al., 2000a,b; Jin and Chen, 2002; Yasuda et al., 1992].
8-12b Vinyl Ethers

The isotactic polymerization of a vinyl ether requires a cationic coordination process. The cationic process is analogous to the anionic coordination process except that the propagating center is a carbocation instead of a carbanion and the counterion is an anion instead of a cation. Various initiators, of both the homogeneous and heterogeneous types, yield varying degrees of isotactic placement [Ketley, 1967a,b; Ouchi et al., 1999, 2001; Pasquon et al., 1989]. This includes boron trifluoride and other Lewis acids, including components (sometimes only one, sometimes both of the two different metal components) used in Ziegler–Natta formulations. Some of the polymerizations proceed with very high isoselectivity, for example, ethylaluminum dichloride and diethylaluminum chloride yield 96–97% isotactic polymer for polymerization of isobutyl vinyl ether at −78°C in toluene, whereas aluminium tribromide yields mostly atactic polymer [Natta et al., 1959a,b,c]. Not all vinyl ethers give the same result with the same initiator. Thus, the polymerization of t-butyl vinyl ether is only mildly isoselective under the same conditions described above for the highly isoselective polymerization of isobutyl vinyl ether. In general, the effects of solvent, temperature, and other reaction conditions on the extent of isoselectivity are similar to those previously described for other types of monomers.

Highly syndiotactic polymers have been obtained in only a few instances—with some monomers containing bulky substituents, such as α-methylvinyl methyl ether, trimethylvinyl-oxysilane, and menthyl vinyl ether, in polar solvents under homogeneous conditions [Goodman and Fan, 1968; Ledwith et al., 1979; Murahashi et al., 1966]. That less hindered monomers in polar solvents do not yield highly syndiotactic polymers may be indicative of the involvement of ether monomers in intramolecular solvation of propagating centers. The polar solvents such as THF may not be sufficiently polar to displace monomer as a solvating species to yield the highly solvated, relatively free propagating centers that lead to syndiotactic placement. One of the mechanisms proposed to explain isotactic placement of vinyl ethers is consistent with this consideration [Cram and Kopecky, 1959]. Propagation involves a 6-membered cyclic propagating chain end (LVII) formed by the antepenultimate (the second repeat unit behind the last unit) ether group of the propagating chain solvating the carbocation center:

\[
\text{LVII}
\]

There are some isolated reports of metallocenes and phenoxy-imines as effective initiators for the polymerization of vinyl ethers, but the reactions do not proceed in a stereoselective manner [Baird, 2000; Kawaguchi et al., 2002].

8-13 ALDEHYDES

The isoselective polymerization of acetaldehyde has been achieved using initiators such as zinc and aluminum alkyls, Grignard reagents, and lithium alkoxides [Kubisa et al., 1980; Pasquon et al., 1989; Pregaglia and Binaghi, 1967; Tani, 1973; Vogl, 2000]. The isoselectivity is high in some systems with isotactic indices of 80–90%. Cationic initiators such as BF₃...
etherate are less isoselective, with isotactic dyads of 70% being the maximum achieved in any polymerization. There are few reports of other aldehydes undergoing stereoselective polymerization, the one exception being chloral (Sec. 8-14b).

8-14 OPTICAL ACTIVITY IN POLYMERS

Optically active polymers are rarely encountered. Most syndiotactic polymers are optically inactive since they are achiral. Most isotactic polymers, such as polypropene and poly(methyl methacrylate), are also inactive (Sec. 8-1a-1). Optically active polymers have been obtained in some situations and these are discussed below.

8-14a Optically Active Monomers

Ioselective polymerization of one enantiomer or the other of a pair of enantiomers results in an optically active polymer [Ciardelli, 1987; Delfini et al., 1985; Pino et al., 1963]. For example, polymerization of $(S)$-3-methyl-1-pentene yields the all-$S$ polymer. The optical activity of the polymer would be maximum for the 100% isotactic polymer. Each racemic placement of the $S$-monomer decreases the observed optical activity in the polymer.

$$\text{CH}_2=\text{CH} \quad \text{CH}_2-\text{CH}_2$$

$$\text{CH}_3-\text{C}-\text{H} \quad \text{CH}_3-\text{C}-\text{H}$$

$$\text{C}_2\text{H}_5 \quad \text{C}_2\text{H}_5$$

(8-75)

8-14b Chiral Conformation

There are a few instances of polymer optical activity arising from a chiral conformation. Many isotactic polymers; for instance polypropene, are composed of equimolar amounts of right- and left-handed helices, since the initiator is composed of equal numbers of the two enantiomeric states. This is also the case for polymerization of chloral (trichloroacetaldehyde) in hexane solution at 58°C with an achiral initiator such as lithium t-butoxide. The bulky CCl₃ group forces monomer units placed in the meso arrangement in the first few propagation steps to form a helical conformation; the helical conformation is subsequently propagated throughout the isoselective polymerization. The product is optically inactive since there is an equal probability of propagating via right- and left-handed helices.

Polymerization of the bulky monomer chloral yields an optically active product when one uses a chiral initiator, e.g., lithium salts of methyl $(+)$- or $(-)$-mandelate or $(R)$- or $(S)$-octanoate [Corley et al., 1988; Jaycox and Vogl, 1990; Qin et al., 1995; Vogl, 2000]. The chiral initiator forces propagation to proceed to form an excess of one of the two enantiomeric helices. The same driving force has been observed in the polymerization of triphenylmethyl methacrylate at $-78°C$ in toluene by initiating polymerization with a chiral complex formed from an achiral initiator such as $n$-butyllithium and an optically active amine such as $(+)$-1-(2-pyrrolidinylmethyl)pyrrolidine [Isobe et al., 2001b; Nakano and Okamoto, 2000; Nakano et al., 2001]. Such polymerizations that proceed in an unsymmetrical manner to form an excess of one enantiomer are referred to as asymmetric polymerizations [Hatada et al., 2002]. Asymmetric polymerization has also been observed in the radical
polymerization of the bulky monomer (1-methylpiperidine-4-yl) diphenylmethyl methacrylate with an achiral initiator if polymerization is carried out in the presence of an optically active additive such as (−)-menthol [Nakano et al., 2001]. (−)-Menthol complexes with the achiral, bulky monomer and induces asymmetric polymerization.

8-14c Enantiomer-Differentiating Polymerization

The isoselective polymerization of a racemic mixture of monomers can proceed in two ways depending on initiator, monomer, and reaction conditions. Racemate-forming enantiomer-differentiating polymerization involves both the R and S monomers polymerizing at the same rate but without any cross-propagation [Hatada et al., 2002]. A racemic monomer mixture polymerizes to a racemic mixture of all-R and all-S polymer molecules [Pino, 1965; Sigwalt, 1976, 1979; Tsuruta, 1972]. This is consistent with the mechanism for isoselective polymerization that attributes steric control to the initiator. The initiator contains R and S enantiomeric polymerization sites in equal numbers such that R sites polymerize only R monomer and S sites polymerize only S monomer. If the isoselectivity of R and S sites is less than complete, there is some cross-propagation of the two enantiomeric monomers and a decrease in the overall isotacticity of the reaction product.

As discussed in Sec. 8-14a, an optically active polymer sample, composed of either all-R or all-S polymer molecules, can be synthesized by isoselective polymerization of a pure enantiomer, the pure R or pure S monomer, respectively. The direction of optical rotation of the polymer is usually the same as the corresponding monomer.

Asymmetric enantiomer-differentiating polymerization occurs when one of the enantiomers polymerizes faster than the other. This type of process has also been referred to as stereoelection. In the extreme case, one enantiomer (e.g., the R monomer) is unreactive and polymerization of racemic monomer yields the optically active all-S polymer with the optically active R monomer left unreacted. This does not occur unless the initiator is an (optically active) enantiomer itself. An optically active Ziegler–Natta initiator is obtained by using an optically active group I–III metal compound in combination with the transition metal compound, such as Zn[(S)-2-methyl-1-butyl]2 plus TiCl4. The use of a chiral electron donor in a Ziegler–Natta initiator has also been used to achieve asymmetric enantiomer-differentiating polymerization [Carlini et al., 1977]. Such polymerizations have also been studied with vinyl ethers, acrylates and methacrylates [Okamoto et al., 1979; Villiers, et al., 1978]. For example, the S monomer is preferentially consumed in the polymerization of (R, S)-1,2-diphenylethyl methacrylate at −75°C in toluene using C3H7MgBr(−)-sparteine as the initiator [Okamoto et al., 1984].

Asymmetric enantiomer-differentiating polymerization results from the presence of only one (either R or S) of two enantiomeric polymerization sites in the initiator—a consequence of using a chiral initiator component. One of the enantiomeric monomers is able to propagate at a faster rate. The reactive monomer is usually the enantiomer having the same absolute configuration as the initiator in terms of the ordering of similar groups. Similar groups are those having similar steric and polar effects. This may not always correspond to both monomer and initiator having the same Cahn–Ingold–Prelog designation. (Polymerizations in which the reactive enantiomer has the configuration opposite that of the initiator are known.) Asymmetric enantiomer-differentiating polymerization is highly sensitive to the
positions of chiral centers in both monomer and initiator [Carlini et al., 1974; Chiellini and Marchetti, 1973; Pino et al., 1967]. The maximum effect occurs when the chiral centers are as close as possible to the bonds (in both monomer and initiator) through which reaction takes place. Asymmetric enantiomer-differentiating polymerization is maximum for a monomer (e.g., 3-methyl-1-hexene) when the chiral center is in the $\alpha$-position to the double bond, decreases sharply when the chiral carbon is in the $\beta$-position (e.g., 4-methyl-1-pentene), and essentially disappears when the chiral carbon is in the $\gamma$-position (e.g., 5-methyl-1-heptene). Asymmetric enantiomer-differentiating polymerization seldom occurs if the chiral carbon in the initiator is in the $\gamma$-position to the metal instead of in the $\beta$-position.

If the polymerization sites are not prefectly isoselective, the result is a modified asymmetric enantiomer-differentiating polymerization behavior with some cross-propagation of the two enantiomeric monomers and a decrease in the overall isotacticity of the reaction product.

The extent of asymmetric enantiomer-differentiating polymerization in an isoselective process is evaluated by measuring the optical activity of unreacted monomer \(a\) as a function of the extent of reaction \(p\) [Zhong et al., 2003]. The rates of reaction of \(R\) and \(S\) enantiomers are given by

\[
\begin{align*}
\frac{-d[R]}{dt} &= k_r[C^*][R] \quad (8-78) \\
\frac{-d[S]}{dt} &= k_s[C^*][S] \quad (8-79)
\end{align*}
\]

where \(k_r\) and \(k_s\) are the rate constants for reaction of \(R\) and \(S\) enantiomers and \([C^*]\) is the concentration of polymerization sites. This treatment assumes that differentiation between \(R\) and \(S\) enantiomers is not dependent on whether the last monomer added to the propagating chain is \(R\) or \(S\).

Dividing Eq. 8-78 by Eq. 8-79 followed by integration yields

\[
\frac{[R]}{[R]_0} = \left(\frac{[S]}{[S]_0}\right)^r \quad (8-80)
\]

where \(r = k_r/k_s\) and the 0 subscripts indicate initial concentrations.

The variables \(\alpha\) and \(p\) are related to various concentration terms by

\[
\begin{align*}
\alpha &= \frac{[S] - [R]}{[S] + [R]} \quad (8-81) \\
p &= 1 - \frac{[S] + [R]}{[S]_0 + [R]_0} \quad (8-82)
\end{align*}
\]

where \(\alpha_0\) is the absolute value (without sign) of \(\alpha\) for the pure enantiomer.

Combination of Eqs. 8-80 through 8-82 yields

\[
(1 - p)^{(r-1)} = \left(1 - \frac{\alpha}{\alpha_0}\right) \frac{2^{(r-1)} [S]_0^r}{[R]_0 ([R]_0 + [S]_0)^{(r-1)}} \quad (8-83)
\]

which simplifies to

\[
(1 - p)^{(r-1)} = \left(1 - \frac{\alpha}{\alpha_0}\right) \frac{2^{(r-1)} [S]_0^r}{[R]_0 ([R]_0 + [S]_0)^{(r-1)}} \quad (8-84)
\]

for the case where the starting monomer mixture is racemic, that is, \([R]_0 = [S]_0\).
8-14d  Asymmetric Induction

A special case of asymmetric enantiomer-differentiating polymerization is the isoselective copolymerization of optically active 3-methyl-1-pentene with racemic 3,7-dimethyl-1-octene by TiCl₄ and diisobutylzinc [Ciardelli et al., 1969]. The copolymer is optically active with respect to both comonomer units as the incorporated optically active 3-methyl-1-pentene directs the preferential entry of only one enantiomer of the racemic monomer. The directing effect of a chiral center in one monomer unit on the second monomer, referred to as asymmetric induction, is also observed in radical and ionic copolymerizations. The radical copolymerization of optically active α-methylbenzyl methacrylate with maleic anhydride yields a copolymer that is optically active even after hydrolytic cleavage of the optically active α-methylbenzyl group from the polymer [Kurokawa and Minoura, 1979]. Similar results were obtained in the copolymerizations of mono- and di-l-menthyl fumarate and (−)-3-(β-styrlyloxy)menthane with styrene [Kurokawa et al., 1982].

8-15  RING-OPENING POLYMERIZATION

The stereochemistry of ring-opening polymerizations has been studied for epoxides, episulfides, lactones, cycloalkenes (Sec. 8-6a), and other cyclic monomers [Pasquon et al., 1989; Tsuruta and Kawakami, 1989]. Epoxides have been studied more than any other type of monomer. A chiral cyclic monomer such as propylene oxide is capable of yielding stereo-regular polymers. Polymerization of either of the two pure enantiomers yields the isotactic polymer when the reaction proceeds in a regioselective manner with bond cleavage at bond 1.

\[ \begin{array}{c}
\text{O} \\
\text{CH₃} \\
\text{H} \\
\end{array} \]

This is generally the case for the typical polymerization of epoxides as well as other cyclic monomers, although the regioselectivity is not 100%. The degree of isoselectivity is generally decreased in proportion to the extent of ring opening at bond 2. There are no initiator systems that are even moderately isoselective subsequent to bond cleavage at bond 2. The extent of regioselectivity at bond 1 is greater than 90% for many anionic polymerizations. It is very difficult to give a generalization that holds up well in this respect. In a number of polymerizations significant amounts of cleavage at bond 2 have been reported, such as propylene oxide polymerizations by Zn(C₂H₅)₂ or Al(C₂H₅)₃ with H₂O or Zn(C₂H₅)₂ with CH₃OH, and styrene oxide polymerization by aluminum isopropoxide [Tsuruta and Kawakami, 1989]. The extent of regioselectivity depends markedly on reaction conditions in some systems. Thus, polymerization by Zn(C₂H₅)₂/H₂O proceeds exclusively by cleavage at bond 1 in many polymerizations but significant extents of cleavage occur at bond 2 in other polymerizations with the differences depending on the relative amounts of Zn(C₂H₅)₂ and H₂O. Cationic polymerizations of epoxides are significantly less regioselective and isoselective compared to anionic polymerizations.

Polymerization of racemic propylene oxide proceeds differently depending on the initiator. Polymerization by potassium hydroxide or alkoxide proceeds with better than 95% regioselectivity of cleavage at bond 1, but the product is atactic [Tsuruta and Kawakami, 1989]. Both (R)- and (S)-propylene oxide react at the same rate as shown by the invariance
of the optical rotation of unreacted monomer with conversion in a polymerization where the initial ratio of the two enantiomers was unequal. The atacticity of the product indicates that the initiator is unable to distinguish between the \( R \) and \( S \) enantiomers of propylene oxide and both enantiomers react at the same rate with complete cross-propagation. Polymerizations by \( \text{Zn(OCH}_3\text{)}_2 \) and \( \alpha, \beta, \gamma, \delta \)-tetraphenylporphyrin (structure VI in Sec. 7-2a-1) proceed in a completely regioselective manner (cleavage at bond 1), but with only modest isoselectivity (67% and 68% isotactic dyads, respectively) [Le Borgne et al., 1988; Tsuruta, 1981]. For polymerization by \( \alpha, \beta, \gamma, \delta \)-tetraphenylprophyrin, the degree of isotacticity varied with the ratio of \((R)\)- and \((S)\)-propylene oxide in the feed. Polymerization proceeds as an asymmetric enantiomer-differentiating polymerization but with significant cross-propagation. The highest isoselectivity reported, \( \langle \text{imm} \rangle = 0.81 \), for a propylene oxide polymerization was achieved with an initiator derived from dialkylzinc and methanol [Hasebe and Tsuruta, 1988; Tsurata, 1986; Tsuruta and Kawakami, 1989; Yoshino et al., 1988].

The stereochemistry of ring-opening polymerizations of episulfides, lactones, lactides, \( N \)-carboxy-\( \alpha \)-amino acid anhydrides, and other monomers has been studied but not as extensively as the epoxides [Boucard et al., 2001; Chatani et al., 1979; Duda and Penczek, 2001; Elias et al., 1975; Guerin et al., 1980; Hall and Padias, 2003; Imanishi and Hashimoto, 1979; Inoue, 1976; Ovitt and Coates, 2000; Spassky et al., 1978; Zhang et al., 1990].

8-16 STATISTICAL MODELS OF PROPAGATION

The polymer stereosequence distributions obtained by NMR analysis are often analyzed by statistical propagation models to gain insight into the propagation mechanism [Bovey, 1972, 1982; Doi, 1979a,b, 1982; Ewen, 1984; Farina, 1987; Inoue et al., 1984; Le Borgne et al., 1988; Randall, 1977; Resconi et al., 2000; Shelden et al., 1965, 1969]. Propagation models exist for both catalyst (initiator) site control (also referred to as enantiomorphic site control) and polymer chain end control. The Bernoullian and Markov models describe polymerizations where stereochemistry is determined by polymer chain end control. The catalyst site control model describes polymerizations where stereochemistry is determined by the initiator.

8-16a Polymer Chain End Control

8-16a-1 Bernoullian Model

The Bernoullian model (also referred to as the zero-order Markov model) assumes that only the last monomer unit in the propagating chain end is important in determining polymer stereochemistry. Polymer stereochemistry is not affected by the penultimate unit or units further back. Two different propagation events are possible—meso or racemic (Eqs. 8-85, 8-86). Equations 8-85 and 8-86 are general in representing two cases: (1) where the stereochemistry of the polymer chain end units is determined relative to the penultimate unit when...
the next monomer unit adds and (2) where the stereochemistry of the polymer chain end unit is determined relative to the incoming monomer unit when the latter adds.

Probabilities \( P_m \) and \( P_r \), the *transition or conditional probabilities* of forming meso and racemic dyads, respectively, are defined by

\[
P_m = \frac{R_m}{R_m + R_r} \quad P_r = \frac{R_r}{R_m + R_r} \quad P_m + P_r = 1
\]

(8-87)

where \( R_m \) and \( R_r \) are the rates of meso and racemic dyad placements, respectively.

Probabilities \( P_m \) and \( P_r \) are synonymous with the dyad tactic fractions \((m)\) and \((r)\) defined in Sec. 8-2b. Triad probabilities, synonymous with the triad fractions, follow as

\[
(mm) = P_m^2 \quad (mr) = 2P_m(1 - P_m) \quad (rr) = (1 - P_m)^2
\]

(8-88)

The probability of forming a particular triad is the product of the probabilities of forming the two dyads making up the triad. The coefficient of 2 for the heterotactic triad is required since the heterotactic triad is produced in two ways; thus, \( mr \) is produced as \((mr)\) and \((rm)\).

Tetrad probabilities are given by

\[
(mmm) = P_m^3 \quad (mrm) = P_m^2(1 - P_m)
\]

\[
(mm) = 2P_m(1 - P_m) \quad (rrm) = 2P_m(1 - P_m)^2
\]

and pentad probabilities by

\[
(mmm) = P_m^3 \quad (mrm) = 2P_m^2(1 - P_m)^2
\]

\[
(mm) = 2P_m(1 - P_m)^2 \quad (rrm) = P_m^2(1 - P_m)^2
\]

\[
(mm) = 2P_m^2(1 - P_m)^2 \quad (rr) = (1 - P_m)^3
\]

(8-89)

and pentad probabilities by

\[
(mmm) = P_m^3 \quad (mrm) = 2P_m^2(1 - P_m)^2
\]

\[
(mm) = 2P_m(1 - P_m)^2 \quad (rrm) = P_m^2(1 - P_m)^2
\]

\[
(mm) = 2P_m^2(1 - P_m)^2 \quad (rrr) = (1 - P_m)^3
\]

(8-90)

**8-16a-2 First-Order Markov Model**

The first-order markov model describes a polymerization where the penultimate unit is important in determining subsequent stereochemistry. Meso and racemic dyads can each react in two ways:
Meso (isotactic) and racemic (syndiotactic) triads result from Reactions 8-91 and 8-94, respectively. Reactions 8-92 and 8-93 yield the heterotactic triad.

Four probabilities, $P_{mr}, P_{mr}, P_{rm},$ and $P_{rr},$ characterize this model for propagation with the conservation relationships

$$P_{mr} + P_{mm} = 1 \quad P_{rm} + P_{rr} = 1$$  \hfill (8-95)

The dyad fractions are given by

$$(m) = \frac{P_{rm}}{P_{mr} + P_{rm}} \quad (r) = \frac{P_{mr}}{P_{mr} + P_{rm}}$$  \hfill (8-96)

The triad fractions are given by

$$(mm) = \frac{(1 - P_{mr})P_{rm}}{P_{mr} + P_{rm}} \quad (mr) = \frac{2P_{mr}P_{rm}}{P_{mr} + P_{rm}}$$  \hfill (8-97)

$$(rr) = \frac{(1 - P_{rm})P_{nr}}{P_{nr} + P_{rm}}$$

The tetrad fractions are given by

$$(mmm) = \frac{P_{rm}(1 - P_{mr})^2}{P_{mr} + P_{rm}} \quad (mrr) = \frac{2P_{mr}P_{rm}(1 - P_{rm})}{P_{mr} + P_{rm}}$$

$$(mrm) = \frac{P_{mr}P_{rm}^2}{P_{nr} + P_{rm}} \quad (rrr) = \frac{P_{mr}(1 - P_{rm})^2}{P_{mr} + P_{rm}}$$

The pentad fractions are given by

$$(mmmm) = \frac{P_{rm}(1 - P_{mr})^3}{P_{mr} + P_{rm}} \quad (rmrm) = \frac{2P_{mr}P_{rm}^2}{P_{mr} + P_{rm}}$$

$$(mmmr) = \frac{2P_{mr}P_{rm}(1 - P_{rm})^2}{P_{mr} + P_{rm}} \quad (rrmr) = \frac{2P_{mr}P_{rm}^2(1 - P_{rm})}{P_{mr} + P_{rm}}$$

$$(rrmr) = \frac{P_{mr}P_{rm}^2(1 - P_{rm})}{P_{mr} + P_{rm}} \quad (mmrr) = \frac{P_{mr}P_{rm}(1 - P_{rm})^2}{P_{mr} + P_{rm}}$$

$$(mmrr) = \frac{2P_{mr}P_{rm}(1 - P_{rm})(1 - P_{mr})}{P_{mr} + P_{rm}} \quad (rrrr) = \frac{P_{mr}(1 - P_{rm})^3}{P_{mr} + P_{rm}}$$

A second-order Markov model has also been described to show the effect on stereochemistry of the monomer unit behind the penultimate unit [Bovey, 1972].
8-16b Catalyst (Initiator) Site Control

Isoselective polymerization by traditional Ziegler–Natta, metallocene, and other initiators is described by the catalyst (initiator) site control model. The initiator has enantiomeric propagation sites, \( R \) and \( S \) sites, at which propagation occurs through the re and si faces of monomer (\( R \) and \( S \) monomer, respectively, if the monomer is optically active). The model is described in terms of the single parameter \( \sigma \) [Doi, 1979a,b, 1982; Farina, 1987; Inoue et al., 1984; Le Borgne et al., 1988; Shelden et al., 1965, 1969]. Parameter \( \sigma \) is the probability of an \( R \) or re monomer unit adding at the \( R \) site; \( \sigma \) is also the probability of an \( S \) or si monomer unit adding at the \( S \) site.

The dyad fractions are given by

\[
(m) = \sigma^2 + (1 - \sigma)^2 \quad (r) = 2\sigma(1 - \sigma)
\]

The triad fractions are given by

\[
(mm) = 1 - 3\sigma(1 - \sigma) \\
(mr) = 2\sigma(1 - \sigma) \\
(rr) = \sigma(1 - \sigma)
\]

The tetrad fractions are given by

\[
(mmnn) = 2\sigma^4 - 4\sigma^3 + 6\sigma^2 - 4\sigma + 1 \\
(mmrr) = (mrr) = -4\sigma^4 + 8\sigma^3 - 6\sigma^2 + 2\sigma \\
(mrmr) = (rmrr) = 2\sigma^4 - 4\sigma^3 + 2\sigma^2
\]

The pentad fractions are given by

\[
(mmmm) = 5\sigma^4 - 10\sigma^3 + 10\sigma^2 - 5\sigma + 1 \\
(mmrm) = -3\sigma^4 + 6\sigma^3 - 4\sigma^2 + \sigma \\
(mmrr) = (mrrm) = -6\sigma^4 + 12\sigma^3 - 8\sigma^2 + 2\sigma \\
(mrrm) = (rmrr) = \sigma^4 - 2\sigma^3 + \sigma^2
\]

Syndioselective polymerization by a \( C_7 \) metallocene such as \( \text{Me}_2\text{C}($\text{Cp})($\text{Flu})\text{ZrCl}_2 \) proceeds by catalyst site control. A statistical model for syndioselective catalyst site control has been described in terms of the parameter \( \rho \) [Resconi et al., 2000]. Parameter \( \rho \) is the probability of a monomer with a given enantioface inserting at one site of the initiator; \( \rho \) is also the probability of the monomer with the opposite enantioface inserting at the other site of the initiator. The pentad fractions are given by

\[
(mmmm) = \rho^4 - 2\rho^3 + \rho^2 \\
(mmrm) = (mmrm) = (rmrr) = (mrrm) = 2\rho^4 - 4\rho^3 + 2\rho^2 \\
(mmrr) = -3\rho^4 + 6\rho^3 - 4\rho^2 + \rho \\
(mmnr) = -6\rho^4 + 12\rho^3 - 8\rho^2 + 2\rho \\
(rrrr) = 5\rho^4 - 10\rho^3 + 10\rho^2 - 5\rho + 1 \\
(rrrm) = -6\rho^4 + 12\rho^3 - 8\rho^2 + 2\rho \\
(mrrm) = \rho^4 - 2\rho^3 + \rho^2
\]
8-16c Application of Propagation Statistics

Experimentally obtained sequence distributions in a particular polymerization are used to determine whether the polymerization follows the Bernoullian, Markov, or catalyst site control models. The general approach is to fit data on the dyad, triad, and higher sequence fractions to the appropriate equations for the different models. One needs to recognize the difference between fitting and testing of data. Fitting of data involves calculating the value(s) of the appropriate probability term(s) from the sequence distributions. Testing involves determining that the sequence data are consistent or inconsistent with a particular model. All the models can be fitted but not tested with dyad data. The Bernoullian and catalyst site control models require triad data as a minimum for testing; the first-order Markov model requires tetrad data. The appropriate level of sequence data tests a model by showing the consistency or inconsistency of the $P_m$ values (Bernoullian model) or $P_{mr}$ and $P_{rm}$ values (first-order Markov), or $\sigma$ (or $\rho$) values (catalyst site control models).

There are alternate criteria for testing the different models [Bovey, 1972; Chujo, 1967; Inoue et al., 1971, 1984]. The Bernoullian model requires

\[
\frac{4(mm)(rr)}{(mr)^2} = 1 \quad (8-105)
\]

The term on the left is extremely sensitive, and this criterion should be used only with sufficiently accurate triad data. This is especially important if the polymer is very highly isotactic or syndiotactic, that is, with very small value of either $(rr)$ or $(mm)$. The term $4(mm)(rr)/(mr)^2$ is considerably larger than one for the Markov and catalyst site control models.

The first-order Markov model requires

\[
\frac{4(mmm)(rmm)}{(mmr)^2} = 1 \quad \text{and} \quad \frac{4(mrm)(rrr)}{(mrr)^2} = 1 \quad (8-106)
\]

while the catalyst site control models have the criteria

\[
\frac{2(rr)}{(mr)} = 1 \quad \text{and} \quad 1 - \frac{4}{(mr) + 2(rr)} + \frac{1}{(rr)} = 1 \quad (8-107)
\]

Having established that a particular polymerization follows Bernoullian or first-order Markov or catalyst site control behavior tells us about the mechanism by which polymer stereochemistry is determined. The Bernoullian model describes those polymerizations in which the chain end determines stereochemistry, due to interactions between either the last two units in the chain or the last unit in the chain and the entering monomer. This corresponds to the generally accepted mechanism for polymerizations proceeding in a noncoordinated manner to give mostly atactic polymer—ionic polymerizations in polar solvents and free-radical polymerizations. Highly isoselective and syndioselective polymerizations follow the catalyst site control model as expected. Some syndioselective polymerizations follow Markov behavior, which is indicative of a more complex form of chain end control.

More sophisticated experimental and theoretical analysis of isoselective polymerizations have been performed by using a two-site model for propagation [Inoue et al., 1984; Wu et al., 1990]. The polymer product is fractionated into the highly isotactic, insoluble and atactic,
soluble fractions, and the respective stereosequence determinations are usually found to fit the catalyst site control and Bernoullian models.

Although the treatment described above has been limited to polymerizations proceeding by meso and racemic placements, the various models can also be adopted to describe the stereochemistry of 1,4-propagation in 1,3-dienes.

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### PROBLEMS

**8-1** Show by structural drawings the various (if any) stereoregular polymers that might possibly we obtained from each of the monomers.

a. \( \text{CH}_2=\text{CH}=\text{CH}_3 \)
b. \(CH_2=\text{C}(CH_3)_2\)

c. \(CH_3-\text{CH}=\text{CH} \quad \text{CH}_3\)

d. \(CH_2=\text{C}(\text{CH}_3)(\text{C}_2\text{H}_5)\)

e. \(CH_3-\text{CH}=\text{CH} \quad \text{C}_2\text{H}_5\)

f. \(\text{CH}_2=\text{CH} \quad \text{CH} \quad \text{CH}=\text{CH}_2\)

g. \(CH_3-\text{CH}=\text{CH} \quad \text{CH} \quad \text{CH}=\text{CH}_2\)

h. \(\text{CH}_2=\text{C}(\text{CH}_3) \quad \text{CH} \quad \text{CH}=\text{CH}_2\)

i. \(CH_3-\text{CH}=\text{C}(\text{Cl}) \quad \text{CH} \quad \text{CH}=\text{CH}_2\)

j. \(\text{CH}_3-\text{CH}=\text{CH} \quad \text{C}(\text{CH}_3)=\text{CH}_2\)

k. \(\text{CH}_3-\text{CH}=\text{CH} \quad \text{CH} \quad \text{CH}=\text{CH}_2\)

l. \(\text{CH}_2=\text{C}(\text{CH}_3)-\text{C}(\text{CH}_3)=\text{CH}_2\)

m. \(\text{H}_2\text{N}\)-(\text{CH}_2)_6-\text{NH}_2 \quad + \quad \text{HO}_2\text{C}-(\text{CH}_2)_4-\text{CO}_2\text{H}\)

n. \(\text{CH}_2=\text{CH} \quad \text{CH} \quad \text{CH}_3\)

o. \(\text{CH}_3-\text{CH} \quad \text{CH} \quad \text{CH} \quad \text{CH}_3\)

p. \(\text{CH}_3-\text{CH} \quad \text{CH} \quad \text{C}_2\text{H}_5\)

q. \(\text{CH}_3-\text{CHO}\)

r. \((\text{CH}_3)_2\text{CO}\)

s. \(\text{CH}_3-\text{CO}-\text{CCl}_3\)

t. 

u. 

v. 

Name the various polymer structures using the nomenclature described in this chapter.

8-2 What are the mechanisms for syndiotactic and isotactic placements in propene polymerization? Describe the reaction conditions that favor each type of stereoselective placement.

8-3 Discuss the use of homogeneous versus heterogeneous reaction conditions for the coordination and traditional Ziegler–Natta polymerizations of propene, isoprene, styrene, methyl methacrylate, and \(n\)-butyl vinyl ether.

8-4 What reaction conditions determine the relative amounts of 1,2-, cis 1,4-, and trans 1,4-polymerization in the radical and anionic polymerizations of 1,3-butadiene? Indicate
the effect of solvent and counterion in these polymerizations. What polymer structures are obtained using traditional Ziegler–Natta and metallocene initiators?

8-5 Which of the stereoregular polymer structures in question 8-1 are capable of exhibiting optical activity? How would you synthesize optically active polymers of these structures? Explain the inability of certain stereoregular polymers to exhibit optical activity.

8-6 The polymerization cis-1-d-propene by traditional Ziegler–Natta initiators in hydrocarbon solvents yields the erythrodiisotactic structure, while under similar solvent conditions anionic polymerization of cis-β-d-methyl acrylate yields the threodiisotactic polymer. Explain the factor(s) responsible for this difference.

8-7 The polymerization of optically pure propylene oxide by FeCl₃-derived initiators yields an optically active polymer. E. J. Vandenberg [J. Polym. Sci., A-1(7), 525 (1969)] attempted to gain insight into the mechanism by polymerizing the 2,3-epoxybutanes. The optically active trans-2,3-epoxybutane was polymerized to an optically inactive crystalline polymer. Evaluate this result and discuss its implications on the propagation mechanism for propylene oxide polymerization.

8-8 Briefly explain each of the following:

a. There is only one disyndiotactic structure for \((\text{CHRCHR'})_n\), whereas there are erythro- and threodiisotactic structures.

b. Addition of aluminum trialkyl to a traditional Ziegler–Natta polymerization system (e.g., β-TiCl₃, propene) increases the polymerization rate up to a maximum after which \(R_p\) either remains constant or decreases.

c. Hydrogen lowers the molecular weight of polyethylene and polypropene synthesized using traditional Ziegler–Natta and metallocene initiators.

d. Low temperatures enhance syndioselective polymerization.

e. Metal–polymer bonds are sometimes found in polymers synthesized using traditional Ziegler–Natta and metallocene initiators.

8-9 ¹³C NMR analysis of polypropene sample A showed \((m) = 0.78, (r) = 0.22, (nm) = 0.62, (nr) = 0.33, (rr) = 0.05, (nmnm) = 0.44, (nmnr) = 0.27, (rnrm) = 0.06, (rrnm) = 0.04, (rmrm) = 0.13, (rrr) = 0.01\). Polypropene sample B showed \((m) = 0.80, (r) = 0.20, (nm) = 0.71, (nr) = 0.19, (rr) = 0.10\). What type of propagation mechanism (Bernoulli, first-order Markov, catalyst site control) is indicated for the synthesis of samples A and B?

8-10 Methyl methacrylate polymerization was carried out using \(\text{rac-C}_2\text{H}_4(\text{Ind})_2\text{ZrMe}_2\) with \(\text{C(C}_6\text{H}_5)_3\text{B(C}_6\text{F}_5)_4\) in the presence of triisobutylaluminum at 0°C [H. Deng, T. Shiono, and K. Soga, Macromolecules, 28, 3067 (1995)]. ¹³C NMR of the polymer showed the pentad structure \((mmmm) = 0.869, (nmnr) = 0.0155, (rnrm) = 0.0014, (nmrm) = 0.0005, (rrnm) = 0.0027, (nmnr) = 0.0177, (rrmr) = 0.0165, (nmrm) = 0.0089, (rrrn) = 0.0165, (rrrr) = 0.0510\). Show by analysis of the stereorerrors whether polymerization occurred by chain end control or catalyst site control.

8-11 Consider each of the following metallocene initiators:

a. \(\text{C}_2\text{H}_4(\text{Cp})_2\text{ZrCl}_2\)
b. rac-$\text{Me}_2\text{Si}(\text{H}_4\text{Ind})_2\text{ZrCl}_2$

c. meso-$\text{Me}_2\text{Si}(\text{H}_4\text{Ind})_2\text{ZrCl}_2$

d. $\text{Me}_2\text{C}(\text{Cp})(\text{Flu})\text{ZrCl}_2$

e. $\text{Me}_2\text{Si}(3\text{-isopropyl-Cp})(\text{Flu})\text{Zr}_2$

For each initiator, indicate the (1) type of symmetry, (2) symmetry elements, and (3) stereochemistry of polymer produced.
The preceding chapters dealt with the synthesis of polymers by polymerization reactions. This chapter describes the synthesis of new polymers by modification of existing polymers using a variety of chemical reactions [Allen and Bevington, 1990; Fettes, 1964a,b; Moore, 1973]. These include the esterification of cellulose, crosslinking of polyisoprene, hydrolysis of poly(vinyl acetate), and chlorination of polyethylene. A second aspect of polymer reactions is the use of a polymer as a carrier or support for some component of a reaction system [Benham and Kinstle, 1988; Manecke and Storck, 1978; Mathur et al., 1980]. Examples include polymeric brominating and Wittig reagents, the Merrifield solid-phase synthesis of polypeptides, and polymeric catalysts.

9-1 PRINCIPLES OF POLYMER REACTIVITY

Polymers undergo the same reactions as their low-molecular-weight homologs. Acetylation of the hydroxyl groups of cellulose is basically the same reaction as acetylation of ethanol, chlorination of polyethylene follows the same mechanism as chlorination of \( n \)-hexane. It is usually assumed that the reactivity of a functional group in a polymer and a small organic molecule are the same. This is the familiar concept of functional group reactivity independent of molecular size (Sec. 2-1), which is the basis for analyzing polymerization kinetics. However, in many instances, the reaction rates and maximum conversions observed in the reactions of polymer functional groups differ significantly from those for the corresponding low-molecular-weight homolog. Polymer reaction rates and conversions are usually lower, although higher rates are also found in some reactions [Morawetz, 1975; Plate, 1976;
Rempp, 1976. The reaction conditions under which polymer reactivity differs from that of a low-molecular-weight homolog are discussed below.

9-1a Yield

Yield or conversion in reactions of polymers means something quite different from that in small-molecule reactions when the conversion is less than 100%. For example, 80% yield in the hydrolysis of methyl propanoate has no effect on the purity of the propanoic acid that can be obtained assuming the appropriate techniques are available to separate starting material and product. The 80% yield simply limits the maximum amount of pure propanoic acid that can be obtained to 80% of the theoretical yield. However, 80% yield in the corresponding hydrolysis of poly(methyl acrylate) does not result in 80% yield of poly(acrylic acid) with 20% unreacted poly(methyl acrylate). The product contains copolymer molecules, each of which, on the average, contains 80% acrylic acid repeating units and 20% methyl acrylate units randomly placed along the polymer chain. Unlike the corresponding small molecule reaction, the unreacted ester groups cannot be separated from the product since both are part of the same molecule.

9-1b Isolation of Functional Groups

When a polymer reaction involves the random reaction of a pair of neighboring functional groups (either with each other or simultaneously with a common small molecule reagent), the maximum conversion is limited due to the isolation of single functional groups between pairs of reacted functional groups. This effect was studied for the dechlorination of poly(vinyl chloride) when heated in the presence of zinc. The maximum conversion for irreversible reactions has been calculated as 86%, which is in excellent agreement with that observed in most systems [Alfrey et al., 1951; Flory, 1939]. This limitation applies equally to polymers in which the functional groups react with each other, such as anhydride formation in poly(acrylic acid) or with a small reactant, for example, acetal formation in poly(vinyl alcohol) by reaction with an aldehyde. The conversions are higher for reversible reactions but the reaction times required for complete conversion may be quite long.

9-1c Concentration

The reaction of a polymer in solution involves a considerably higher local concentration of functional groups than that indicated by the overall polymer concentration. Polymer molecules are generally present in solution as random-coil conformations. The concentration of functional groups is high within the polymer coils and zero outside [Alexandratos and Miller, 2000]. The difference between the overall and local concentrations can be illustrated by considering a 1% solution of poly(vinyl acetate) of molecular weight $10^6$. The overall concentration of acetate groups is about 0.11 $M$, while the local concentration is estimated as being fivefold higher [Elias, 1984]. The high local concentration of polymer functional groups gives a high local rate for the reaction of a polymer with a small molecule reactant. The reaction rate outside the polymer coils is zero since the concentration of polymer functional groups is zero. The observed overall reaction rate is an average of the rates inside and outside.
the polymer coils [Sherrington, 1988]. The overall rate may be the same, higher, or lower than the corresponding reaction with a low-molecular-weight homolog of the polymer depending on the concentration of the small molecule reactant inside the polymer coils relative to its concentration outside.

The concentrations of the small-molecule reactant inside and outside are the same for soluble polymers unless there is some special effect responsible for attracting or repulsing the reactant from the polymer coils. Such situations are described in the remainder of Sec. 9-1. The concentration of a small molecule reactant inside the polymer coils can be lower than outside when one uses a poor solvent for the polymer. This results in lower local and overall reaction rates. In the extreme, a poor solvent results in reaction occurring only on the surfaces of a polymer. Surface reactions are advantageous for applications requiring modification of surface properties without affecting the bulk physical properties of a polymer, such as modification of surface dyeability, biocompatibility, adhesive and frictional behavior, and coatability [Ward and McCarthy, 1989].

9-1d Crystallinity

The reactions of semicrystalline (and crystalline) polymers proceed differently depending on the reaction temperature and solvent. When reaction proceeds under conditions where portions of the polymer remain crystalline, the product is heterogeneous since only functional groups in the amorphous regions are available for reaction [Stoeva and Vlaev, 2002]. Such behavior has been observed in many systems, including the chlorination of polyethylene, acetylation of cellulose, and aminolysis of poly(ethylene terephthalate). The functional groups in the crystalline regions are generally inaccessible to chemical reagents, and reaction is limited to the amorphous regions. Thus the rate of chlorosulfonation of different polyethylenes increases directly with the amorphous content of the polymer [Bikson et al., 1979]. The reaction of a polymer is exactly like its low-molecular-weight homolog only when carried out under homogeneous conditions by the appropriate choice of temperature and/or solvent.

The situation is not so clear-cut in some polymer reactions. Reaction often occurs at crystal surfaces, and this leads to subsequent penetration of a small reactant into the crystalline regions. Complete penetration of the crystalline regions occurs if the reaction times are sufficiently long, although the extent of reaction may be lower in the crystalline regions compared to the amorphous regions.

Although homogeneous polymer reactions are generally more desirable than heterogeneous reactions, this is not necessarily always the case. The properties of the products of heterogeneous and homogeneous reactions will clearly be different. For example, homogeneous chlorination of polyethylene yields a less crystalline product with lower $T_g$ and stiffness than heterogeneous chlorination [Fettes, 1964a,b]. Whether one product or the other is more desirable depends on the specific application. Heterogeneous reaction is more suited for applications requiring modification of surface properties without alteration of bulk properties.

9-1e Changes in Solubility

Abnormal behavior can occur in the reaction of an initially homogeneous system if there is a change in the physical nature of the system on reaction of the polymer. Partial reaction may yield a polymer that is no longer soluble in the reaction medium or that forms a highly viscous system. The solubility changes can be quite complex, as shown in the chlorination of polyethylene when carried out in solution using aliphatic or aromatic hydrocarbon solvents.
The polymer solubility increases with extent of chlorination until about 30% by weight of chlorine has been added and then decreases with further chlorination. After 50–60% chlorination, solubility again increases with further chlorination. Such solubility behavior presents problems in carrying out a polymer reaction. As a minimum, one must take into account the rate changes accompanying the solubility changes when planning the synthesis. In the extreme case, insolubility of a polymer may limit the maximum conversion if the small-molecule reagent cannot diffuse into and through the polymer.

Enhanced reaction rates have also been observed in some instances of decreased polymer solubility with conversion when the precipitating polymer absorbs the small-molecule reactant. Adsorption results in an increased concentration of the reactant at the actual polymerization site (the polymer coils). Similar effects are observed if a catalyst is adsorbed onto the precipitating polymer [Beresniewicz, 1959].

**9-1f Crosslinking**

A consideration of the effect of crosslinking on polymer reactivity is important since some polymer reactions are performed to achieve crosslinking for specific applications (Sec. 9-2), while other polymer reactions are carried out on previously crosslinked polymers (Secs. 9-10 through 9-13). For crosslinked polymers, the concentration of small molecule reactant inside the polymer domains can be lower than outside because of a low degree of swelling. This results from a high degree of crosslinking and/or the use of a poor solvent for the polymer. The diffusion coefficients for solvent and small-molecule reactant often also decrease under these conditions. The effects of different solvents on polymer reactivity can be quite dramatic. For the S_N2 reaction of pyridine with various alkyl halides, the ratios of the reaction rates in 2-pentanone, toluene, and n-heptane are approximately 7:2:1. This is the expected order for an S_N2 reaction between neutral substrate and reactant molecules, where increased solvent polarity assists in the development of charge separation in the transition state. For the corresponding reaction of crosslinked poly(4-vinylpyridine), the 2-pentanone : toluene : n-heptane reaction rate ratio is approximately 10:10:1 [Grieg and Sherrington, 1978]. The high reactivity in toluene is a consequence of this solvent being a good solvent (as is 2-pentanone) for poly(4-vinylpyridine), while n-heptane is a poor solvent. The extent of swelling of the crosslinked polymer is high in 2-pentanone and toluene, which results in higher local concentrations of the small molecule reactant in the polymer domains. Presumably, the diffusion coefficients are also higher in these solvents relative to n-heptane.

The rate of epoxidation of cyclohexene with perbenzoic acid decreases with increasing solvent polarity. The epoxidation by poly(peracylic acid) shows the opposite trend. A polar solvent causes the polar polymer to swell to a greater extent and the reaction rate is increased due to a higher local concentration of cyclohexene [Takagi, 1975].

High crosslink densities may severely depress polymer reactivity as a result of large decreases in swelling and diffusion rate within the polymer. Diffusion control in a polymer reaction can be detected by the inverse dependence of rate on polymer particle size (radius for spherical particle, thickness for film or sheet) [Imre et al., 1976; Sherrington, 1988].

**9-1g Steric Effects**

Polymer reactivity can be sterically hindered under certain conditions—when the functional group is close to the polymer chain or in a sterically hindered environment or reaction involves a small molecule reactant that is bulky. Several examples illustrate this effect:
1. The α-chymotrypsin-catalyzed hydrolysis of the \( p \)-nitroanilide group in acrylamide copolymers with monomer I proceeds with a rate comparable to that of the monomer when \( n = 5 \). The rate decreases sharply with decreasing value of \( n \) as the reactive site becomes progressively closer to the polymer backbone and less accessible to the bulky α-chymotrypsin catalyst [Fu and Morawetz, 1976]. The reaction rate is not, however, affected by the molecular weight of the copolymer [Drobnik et al., 1976].

2. Hydrogenation of cyclododecene using the polymeric rhodium catalyst II occurs at a rate 5 times slower than does cyclohexene [Mathur and Williams, 1976; Mathur et al., 1980]. The low-molecular-weight homolog III shows no difference in catalytic activity toward the two cycloalkenes.

3. Compounds \( n-C_4H_9I \) and \( n-C_{18}H_{37}I \) react at the same rate with pyridine, but \( n-C_4H_9I \) is almost fourfold more reactive than \( n-C_{18}H_{37}I \) toward poly(4-vinylpyridine) [Grieg and Sherrington, 1978].

### 9-1h Electrostatic Effects

Polymer reactions involving the conversion of uncharged functional groups to charged groups often exhibit a decrease in reactivity with conversion. Thus the quaternization of poly(4-vinylpyridine) becomes progressively slower with increasing conversion, since reaction proceeds with the buildup and concentration of charge on the polymer molecule [Noah et al., 1974; Sawage and Loucheux, 1975]. An unreactive pyridine group is less reactive by a factor of 3 when neighboring pyridine groups have reacted. This autoretardation behavior is not observed for the small molecule homolog, such as 4-ethylpyridine, since unreacted molecules are separated from reacted 4-ethylpyridine by solvent.
The same phenomenon is responsible for the decrease in the ionization constant of a polymeric acid such as poly(acrylic acid) with increasing degree of ionization [Kawaguchi et al., 1990, 1992; Morawetz and Wang, 1987]. This effect is somewhat moderated for acrylic acid–ethylene copolymers, since charge density on the ionized polymer is decreased. The basicity

\[
\begin{align*}
\text{COOH} & \quad \text{CH} \quad \text{CH}_2 \quad \text{CH} \quad \text{CH}_2 \quad \text{CH} \quad \text{COOH} \\
\text{COOH} & \quad \text{CH} \quad \text{CH}_2 \quad \text{CH} \quad \text{CH}_2 \quad \text{CH} \quad \text{COOH} \\
\hline
\text{COO}^- & \quad \text{H}^+ \quad \text{COO}^- \\
\end{align*}
\]

of a polymeric base such as poly(4-vinylpyridine) or poly(vinyl amine) decreases with increasing protonation of nitrogen [Lewis et al., 1984; Satoh et al., 1989]. These autoretardation effects are partially alleviated by the addition of salts that shield the charge on the polymer.

Charge on a polymer molecule can also affect reactivity by altering the concentration of the small molecule reactant within the polymer domains. The reaction of a charged polymer with a charged reactant results in acceleration for oppositely charged species and retardation when the charges are the same. For example, the rate constant for the KOH saponification of poly(methyl methacrylate) decreases by about an order of magnitude as the reaction proceeds [Plate, 1976]. Partially reacted poly(methyl methacrylate) (IV) repels hydroxide ion, while unreacted polymer does not. The concentration of OH\(^-\) within the polymer domains decreases progressively with increasing conversion. Acceleration of reactivity is observed for the S\(_{N2}\) reaction of poly(4-vinylpyridine) and \(\alpha\)-bromoacetate ion when the polymer is partially protonated [Ladenheim et al., 1959]. The positive charge on the polymer attracts and concentrates \(\alpha\)-bromoacetate ion within the polymer domains.

\[
\begin{align*}
\text{CH}_3 & \quad \text{CH}_3 \\
\text{COO}^- & \quad \text{COOCH}_3 \\
\end{align*}
\]

Polymers can also affect polymer reactivity toward neutral reagents. The nucleophilic reactivity of the carboxylate anions of a partially ionized poly(methacrylic acid) toward \(\alpha\)-bromoacetoamide decreases with increasing charge on the polymer when the reaction is carried out in water [Ladenheim and Morawetz, 1959]. Water is preferentially concentrated within the polymer coils with the partial exclusion of the neutral reagent, resulting in a decreased reaction rate. Similar retardation is observed when partially protonated poly(4-vinylpyridine) acts as the catalyst in hydrolysis of 2,4-dinitrophenyl acetate [Letsinger and Savereide, 1962]. These retardation effects are decreased or eliminated when reaction is carried out in an organic solvent where there is less tendency for preferential concentration of the solvent within the polymer domains.

Related phenomena include the effect of a polymer on the reaction between two small reactants. Acceleration occurs when the polymer attracts both reactants (both reactants
have the same charge and both are opposite in sign to the charge on the polymer backbone. An example is the redox reaction performed in the presence of poly(sodium vinyl sulfonate).

\[
\text{Co(NH}_3\text{)}_3\text{Cl}^{2+} + \text{Hg}^{2+} + \text{H}_2\text{O} \rightarrow \text{Co(NH}_3\text{)}_3\text{H}_2\text{O}^{3+} + \text{HgCl}^+ \quad (9-5)
\]

The rate increases with polyanion concentration, reaches a maximum, and then decreases with further increase in polyanion concentration [Morawetz and Vogel, 1969]. Retardation occurs for reactions between ions of opposite charge because the polymer attracts one ion but repels the other.

### 9-1i Neighboring-Group Effects

The reactivity of a functional group on a polymer is sometimes affected directly by an adjacent neighboring group. (The effects described in the beginning of Sec. 9-1h are indirect effects of neighboring groups.) Thus, the saponification of poly(methyl methacrylate) and related polymers proceeds with autoacceleration when carried out with weak bases such as pyridine or low concentrations of strong bases [Gaetjens and Morawetz, 1961; Kheradmand et al., 1988]. (Saponifications at high OH\textsuperscript{−} concentrations involve retardation due to hydroxide–carboxyl anion repulsions as described in Sec. 9-1h). After the initial formation of some carboxylate anions, subsequent hydrolysis of ester groups occurs not directly by hydroxide ion but by neighboring carboxylate anions. The reaction proceeds by the sequence in Eq. 9-6 with the intermediate formation of a cyclic acid anhydride. Direct rate enhancement by a neighboring group, referred to as anchimeric assistance, occurs primarily when the cyclic anhydride intermediate is the favored 5- or 6-membered ring. Such effects are also encountered in low-molecular-weight bifunctional compounds, as in succinic esters.

![Neighboring-Group Effects Diagram](image)

Neighboring-group effects are dependent not only on the functional group and reaction involved but also on the stereochemistry of the neighboring groups. Thus, whereas there is a rate enhancement of 1–2 orders of magnitude in the saponification of isotactic poly(methyl methacrylate) by pyridine–water at 145°C, no effect is observed for the syndiotactic polymer [Barth and Klesper, 1976; Plate, 1976]. The isotactic structure has neighboring functional groups in the optimum orientation for interaction with each other to form the cyclic anhydride intermediate. The difference between the two stereoisomers is evident even for saponification with strong base as the reaction rate constant for syndiotactic PMMA falls much more rapidly with conversion compared to isotactic PMMA.

### 9-1j Hydrophobic Interactions

Hydrophobic attractive interactions between a polymer and a small-molecule reactant often occur in reactions carried out in aqueous media [Imanishi, 1979; Morawetz, 1975; Overberger and Guterl, 1978, 1979]. Acid catalysis of ester hydrolysis by polysulfonic acids is most
effective when either the ester or polysulfonic acid contains hydrophobic groups. The reaction rate increases because the small reagent becomes concentrated within the polymer domains where there is a high local hydrogen ion concentration. Similar hydrophobic effects have been observed in the hydrolysis of p-nitrophenyl acetate by quaternized poly(4-vinyl pyridine) and the aminolysis of poly(methyl acrylate) by n-hexylamine [Kirsh et al., 1968; Royer and Klotz, 1969; Spetnagel and Klotz, 1977; Yu and Brown, 1994].

Overberger and coworkers carried out an interesting study on the hydrolysis of various 3-nitro-4-acyloxybenzoic acid substrates (V) catalyzed by imidazole (VI) and poly[4(5)-vinylimidazole] (VII) in ethanol–water mixtures [Overberger et al., 1973].

The reaction rate constant is independent of the size of the alkyl group (i.e., value of n) in the substrate for the imidazole-catalyzed reaction. Catalysis by poly[4(5)-vinylimidazole] (PVIm) is more effective than by imidazole, and its effectiveness increased sharply with the hydrophobicity of the substrate. Thus, the PVIm-catalyzed reaction rate for n = 11 is 30-fold larger than for n = 1 and almost 400-fold larger than for the imidazole-catalyzed reaction. Hydrophobic attraction between the imidazole group and the alkyl group of the substrate increases the substrate concentration within the polymer domains. Such hydrophobic attractions decrease considerably and even disappear if the water content of the reaction medium is sufficiently decreased. When the solvent and substrate have similar polarities, there is no preferential attraction of the polymer for substrate. Hydrophobic interactions have been the subject of considerable study with polymers containing the imidazole group [Overberger and Meenakshi, 1984; Overberger and Smith, 1975; Septnagel and Klotz, 1977]. PVIm has received attention as a model for a biological enzyme.

9-1k Other Considerations

Some other considerations relative to polymer reactivity are as follow:

1. Morawetz and coworkers have discussed the reaction between functional groups on different polymer molecules [Cho and Morawetz, 1973; Morawetz, 1975]. Reaction occurs only if the two polymers are sufficiently similar that there is interpenetration of the two polymer coils. However, most polymers do not fall in this category, polymer mixing is quite endothermic, and reactions of functional groups do not occur. Reaction occurs with dissimilar polymers only when polymer mixing is highly exothermic, for example, an acidic polymer with a basic polymer [Letsinger and Wagner, 1966].

2. Polymer reactivity can also be affected by the conformation of polymer chains [Imanishi, 1979; Overberger et al., 1973; Overberger and Morimoto, 1971; Pshezetsky et al., 1968]. Whether the polymer chain exists in a tight or expanded coil can influence the accessibility of polymer functional groups and the local concentration of a small-molecule reactant.

3. The functional groups in a number of polymers are not of the same reactivity. For example, the hydroxyl groups in cellulose (VIII) are of different reactivities. The hydroxyl at C-2 is reported to be slightly more reactive than that at C-6, which is about
4 times more reactive than the hydroxyl at C-3 [Lenz, 1960]. Reaction of cellulose leads to a nonuniform distribution of reacted groups. Another report shows no reactivity difference between the secondary hydroxyls at C-2 and C-3 [Jain et al., 1985]. The situation is more complicated. For xanthation of hydroxyl groups (Sec. 9-3a), the hydroxyls at C-2 and C-3 are reported to be favored kinetically but the hydroxyl at C-6 is favored thermodynamically [Turbak, 1988].

9-2 CROSSLINKING

A number of crosslinking reactions have been discussed—crosslinking of monomers with functionality greater than 2 (Sec. 2-10), including the crosslinking of prepolymer such as epoxy prepolymer (Sec. 2-12d) and unsaturated polyester (Sec. 6-8c) and crosslinking via copolymerization of vinyl-divinyl systems (Sec. 6-6). The crosslinking of high-molecular-weight polymers such as 1,4-polyisoprene and polyethylene will be discussed in this section. The reaction by which a polymer is converted into a cross-linked structure is usually difficult to analyze kinetically because of the insolubility of the network system. Decreased reaction rates are encountered at high crosslink densities.

9-2a Alkyds

Unsaturated polyesters in which the alkene double bond resides in a fatty acid component such as oleic (IX) and linoleic (X) acids are referred to as alkyds or alkyd resins (Sec. 2-12a),

\[
\text{CH}_3(\text{CH}_2)_7\text{CH}=[\text{CH}(\text{CH}_2)_2]\text{COOH} \quad \text{IX}
\]

\[
\text{CH}_3(\text{CH}_2)_7\text{CH}=[\text{CHCH}]=\text{CH}(\text{CH}_2)_2\text{COOH} \quad \text{X}
\]

Alkyds are crosslinked via oxidation by atmospheric oxygen [Marshall et al., 1987; Solomon, 1967]. The process is usually referred to as drying or air-drying. Varnishes and other surface coatings based on these polymers are crosslinked by standing in air.

The crosslinking process is different depending on whether the unsaturation is an unconjugated double bond as in oleic acid or a conjugated double bond as in linoleic acid. Unconjugated double bonds undergo crosslinking by the initial formation of an allylic hydroperoxide

\[
\text{CH}_2=\text{CH}=[\text{CH}]=\text{CH} \quad \underbrace{\text{O}}_{\text{OOH}} \quad \text{(9-7)}
\]
followed by decomposition of the hydroperoxide. The reaction sequence involves:

\[
\begin{align*}
\sim\text{OOH} & \rightarrow \sim\text{O}^- + \text{HO}^- \\
2\sim\text{OOH} & \rightarrow \sim\text{O}^- + \sim\text{OO}^- + \text{H}_2\text{O} \\
\text{HO}^- + \sim\text{H} & \rightarrow \sim\text{HO}^- + \text{H}_2\text{O} \\
2\sim\text{HO}^- & \rightarrow \sim\text{HO}^- \\
\sim\text{HO}^- + \sim\text{HO}^- & \rightarrow \sim\text{O}^- \sim \\
2\sim\text{O}^- & \rightarrow \sim\text{O}^- \sim \sim\text{O}^- \\
\sim\text{CH}═\text{CH}═\text{CH}═\sim & \stackrel{\text{H}_{2}\text{O}}{\longrightarrow} \sim\text{CH}═\text{CH}═\text{CH}═\sim
\end{align*}
\]

where \(\sim\text{OOH}\) and \(\sim\sim\text{H}\) represent the oxidized and unoxidized polymer molecules. In order to achieve practical crosslinking rates, the reaction is catalyzed by hydrocarbon-soluble salts (usually octanoates, naphthenates, and linoleates) of metals (cobalt, lead, and manganese). The metal ions accelerate hydroperoxide decomposition in a manner analogous to the redox initiator systems discussed in Sec. 3-4b. The relative amounts of carbon–carbon (Eq. 9-12), ether (Eq. 9-13), and peroxide (Eq. 9-14) crosslinks depend on the reaction conditions.

Crosslinking of alkyds containing conjugated double bonds results in more carbon–carbon bonds in the crosslinks than in the alkyds containing unconjugated double bonds. The crosslinking mechanism involves the formation and decomposition of cyclic peroxides, to yield radicals that initiate crosslinking by 1,4-polymerization of the polymer molecules.

9-2b Elastomers Based on 1,3-Dienes

Various homo- and copolymers of 1,3-dienes make up the large bulk of polymers used as elastomers. Crosslinking is an absolute requirement if elastomers are to have their essential property of rapidly and completely recovering from deformations. The term \textit{vulcanization} is used synonymously with crosslinking in elastomer technology. Crosslinking or vulcanization can be achieved by using sulfur, peroxides, other reagents, or ionizing radiation [Alliger and Sjothun, 1964; Bateman, 1963; Coran, 1978; Engels et al., 2002; Morrison and Porter, 1984; Roberts, 1988]. Heating with sulfur is used almost exclusively for the commercial crosslinking of most elastomers based on 1,3-dienes. This includes 1,4-polyisoprene (synthetic and natural), 1,4-poly(1,3-butadiene), ethylene–propene–diene terpolymer (EPDM), 1,3-butadiene copolymers with styrene (SBR) and acrylonitrile (nitrile rubber or NBR), and isobutylene–isoprene copolymer [butyl rubber (BR)]. Poly(Oct-1-ene-1,8-diyl) and polynorbornene are also vulcanized by sulfur.
9-2b-1 Sulfur Alone

Although sulfur vulcanization has been studied since its discovery in 1839 by Goodyear, its mechanism is not well understood. Free-radical mechanisms were originally assumed but most evidence points to an ionic reaction [Bateman, 1963]. Neither radical initiators nor inhibitors affect sulfur vulcanization and radicals have not been detected by ESR spectroscopy. On the other hand, sulfur vulcanization is accelerated by organic acids and bases as well as by solvents of high dielectric constant. The ionic process can be depicted as a chain reaction involving the initial formation of a sulfonium ion (XI) by reaction of the polymer with polarized sulfur or a sulfur ion pair. The sulfonium ion reacts with a polymer molecule by hydride abstraction to yield the polymeric (allylic) carbocation XII, which undergoes crosslinking by reacting with sulfur followed by addition to a polymer double bond. A subsequent reaction with polymer by hydride abstraction regenerates the polymer carbocation as shown in the sequence:

\[
\begin{align*}
S_8 & \overset{\text{heat}}{\rightarrow} S_{m}^+ + S_n^- \\
\sim & \text{CH}_2-\text{CH} \rightarrow \text{CH} \sim \text{CH}_2 \sim \leftrightarrow S_{m}^+ + S_n^- \\
\sim & \text{CH}_2-\text{CH} \rightarrow \text{CH} \rightarrow \text{CH}_2 \sim \leftrightarrow S_m^- \quad (9-16)
\end{align*}
\]

\[
\begin{align*}
\sim & \text{CH}_2-\text{CH} \rightarrow \text{CH} \rightarrow \text{CH}_2 \sim + S_m^- \\
\text{pol} & \rightarrow \sim \text{CH}_2-\text{CH} \rightarrow \text{CH} \rightarrow \text{CH}_2 \sim + S_m^- \\
\sim & \text{CH}_2-\text{CH} \rightarrow \text{CH} \rightarrow \text{CH}_2 \sim + \sim \text{CH} \rightarrow \text{CH} \rightarrow \text{CH}_2 \sim \quad (9-17)
\end{align*}
\]

\[
\begin{align*}
\sim & \text{CH}_2\text{CH} \rightarrow \text{CH} \rightarrow \text{CH}_2 \sim \overset{S_8}{\rightarrow} \sim \text{CH}_2\text{CH} \rightarrow \text{CH} \rightarrow \text{CH}_2 \sim \\
\text{pol} & \rightarrow \sim \text{CH}_2\text{CH} \rightarrow \text{CH} \rightarrow \text{CH}_2 \sim + S_m^- \\
\sim & \text{CH} \rightarrow \text{CH} \rightarrow \text{CH}_2 \sim + \sim \text{CH}_2\text{CH} \rightarrow \text{CH} \rightarrow \text{CH}_2 \sim \quad (9-18a)
\end{align*}
\]

\[
\begin{align*}
\sim & \text{CH}_2\text{CH} \rightarrow \text{CH} \rightarrow \text{CH}_2 \sim \overset{S_8}{\rightarrow} \sim \text{CH}_2\text{CH} \rightarrow \text{CH} \rightarrow \text{CH}_2 \sim \\
\text{pol} & \rightarrow \sim \text{CH}_2\text{CH} \rightarrow \text{CH} \rightarrow \text{CH}_2 \sim + S_m^- \\
\sim & \text{CH}_2\text{CH} \rightarrow \text{CH} \rightarrow \text{CH}_2 \sim + \sim \text{CH}_2\text{CH} \rightarrow \text{CH} \rightarrow \text{CH}_2 \sim \quad (9-18b)
\end{align*}
\]
9-2b-2 Accelerated Sulfur Vulcanization

Vulcanization by heating with sulfur alone is a very inefficient process with approximately 40–50 sulfur atoms incorporated into the polymer per crosslink. Sulfur is wasted by the formation of long polysulfide crosslinks (i.e., high values of $m$ in XIV), vicinal crosslinks (XIV), and intramolecular cyclic sulfide structures (XV). (Structures XIV and XV do not contribute significantly to the physical properties of the polymer.)

Commercial sulfur vulcanizations are carried out in the presence of various additives, referred to as accelerators, which greatly increase the rate and efficiency of the process [Kuczkowski, 1988; Morrison and Porter, 1989]. The most used accelerators are sulfenamide derivatives of 2-mercaptobenzothiazole (XVI). Actually, the use of accelerators alone usually gives only small increases in crosslinking efficiency. Maximum efficiency is achieved by using accelerators together with a metal oxide and fatty acid. The latter substances are referred to as the activator. Zinc oxide and stearic acid are the most commonly used. The fatty acid solubilizes the zinc oxide by forming the zinc carboxylate salt. Vulcanization is achieved in minutes using the accelerator–activator combination compared to hours for sulfur alone. Analysis of the crosslinked product shows a large decrease in the extent of the wastage reactions. The crosslinking efficiency in some systems is increased to slightly less than two sulfur atoms per crosslink. Most of the crosslinks are monosulfide or disulfide with very little vicinal or cyclic sulfide units.

Studies with model alkenes indicate that the action of accelerators is to increase the extent of sulfur substitution (crosslinking) at the allylic positions of the diene polymer [Skinner, 1972]. The mechanism of vulcanization by XVI involves the initial formation of 2,2'-dithiobisbenzothiazole (XVII) via cleavage of XVI to 2-mercaptobenzothiazole followed by oxidative coupling. 2,2'-Dithiobisbenzothiazole reacts with sulfur to form the accelerator

$$\text{N} \begin{array}{c} \text{S} \end{array} \text{S-NHR}$$

$$\text{XVI}$$

$$\text{C-S-S-C'} \quad \text{XVII} \quad \text{XVIII} \quad \text{S}_s$$

(9-19)
polysulfide (XVIII). The accelerator polysulfide reacts with the polydiene at an allylic hydrogen in a concerted process to form a rubber polysulfide (XIX):

Crosslinking occurs by the corresponding reaction between XIX and the polydiene:

The action of zinc in increasing the efficiency and rate of crosslinking is thought to involve chelation of zinc with the accelerator as well as species XVIII and XIX. Zinc polysulfide compounds such as XX are also likely intermediates. Zinc chelated to sulfur or as zinc sulfide bonds probably facilitate cleavage of sulfur–sulfur bonds in the concerted reactions described by Eqs. 9-20 and 9-21.

The second important class of accelerators are zinc dialkyldithiocarbamates (XXI). These are more active with faster vulcanization rates than the 2-mercaptobenzothiazole sulfenamides. Also, activators are not usually needed since the zinc is incorporated into the accelerator molecule. Tetraalkylthiuram disulfides (XXII) in combination with activators
give equivalent vulcanization rates. 1,3-Diarylguanidines (XXIII) are sometimes used as secondary accelerators in combination with the 2-mercaptobenzothiazole sulfenamides to obtain increased vulcanization rates.

It should be noted that all elastomers, prior to the vulcanization step, are compounded (mixed) with a reinforcing agent such as carbon black or silica (in addition to the crosslinking agents) in industrial applications. The reinforcing agents increase the strength and elastic properties of the final crosslinked product (often referred to as a vulcanizate).

### 9-2b-3 Other Vulcanizations

Polydiene rubbers can also be crosslinked by heating with \( p \)-dinitrosobenzene, phenolic resins, or maleimides [Coran, 1978; Gan and Chew, 1979; Gan et al., 1977, 1978; Sullivan, 1966]. The crosslinking mechanism is similar to that for accelerated sulfur vulcanization, for example, for vulcanization by \( p \)-dinitrosobenzene

\[
\begin{align*}
\text{NO} & \quad \text{C} \quad \text{H} \quad \text{C} \\
& \quad \text{CH}_2 \quad \text{NHO} \quad \text{CH} \quad \text{CH}_2 \\
\text{H} & \quad \text{O=N} \quad \text{CH}_2 \quad \text{C} \\
& \quad \text{H} \quad \text{C} \quad \text{H} \\
\end{align*}
\]

These products find use in specialty applications requiring better thermal stability than available in the sulfur vulcanized elastomers. Other processes are also used to crosslink polydiene rubbers (Secs. 9-2c and 9-2d).

### 9-2c Peroxide and Radiation Crosslinking

Many polymers are crosslinked by compounding with a peroxide such as dicumyl peroxide or di-\( t \)-butyl peroxide and then heating the mixture [Alliger and Sjothun, 1964; Coran, 1978; Emami et al., 2002; Keller, 1988; Peacock, 1987; Ratzsch et al., 2002; Yamazaki and Seguchi, 2000]. Peroxide crosslinking of diene polymers works with all except butyl rubber, which undergoes chain scission. The crosslinks formed via peroxides are more thermally stable than those formed via sulfur vulcanization. However, peroxide crosslinking is not economically competitive with sulfur crosslinking because of the high cost of peroxides. Peroxide crosslinking is primarily used for those polymers that cannot be easily crosslinked by sulfur, such as polyethylene and other polyolefins, ethylene–propene (no diene) rubbers (EPM), and polysiloxanes. Crosslinking of polyethylene increases its strength properties and extends the upper temperature limit at which this plastic can be used. Uses include electrical wire and cable insulation, pipe, and hose. For EPM and polysiloxanes, crosslinking is essential to their use as elastomers.
Peroxide crosslinking involves the formation of polymer radicals via hydrogen abstraction by the peroxy radicals formed from the thermal decomposition of the peroxide. Crosslinking occurs by coupling of the polymer radicals

\[
\begin{align*}
ROOR & \rightarrow 2RO \cdot \\
RO \cdot + \sim \sim \text{CH}_2\text{CH}_2 & \rightarrow \text{ROH} + \sim \sim \text{CH}_3\text{CH} \sim \sim \\
2 \sim \sim \text{CH}_3\text{CH} & \rightarrow \sim \sim \text{CH}_2\text{CH} \sim \sim 
\end{align*}
\]

(9-23) (9-24) (9-25)

The maximum crosslinking efficiency in this process is one crosslink per molecule of peroxide decomposed—far less than that of a chain polymerization where one radical converts large numbers of monomer molecules to product. Further, the actual crosslinking efficiency is often considerably less than one because of various side reactions of the initiator (Sec. 3-4g-2) and the polymer radical. Thus, if a polymer is not formed in the close vicinity of another polymer radical, crosslinking may be impaired since the process takes place in a highly viscous system. Side reactions such as chain scission, hydrogen atom abstraction, or expulsion, and combination with initiator radicals become possible. These considerations, together with the high cost of peroxides, limit the practical utility of the peroxide crosslinking process.

The crosslinking efficiency of the peroxide process can be increased for some systems by incorporating small amounts of a comonomer containing vinyl groups into the polymer. This approach is used for polysiloxanes by copolymerization with small amounts of vinyltrimethylsilanol

\[
\begin{align*}
\text{CH}_2 & \quad \text{CH} \\
\text{HO} & \quad \text{Si} \quad \text{OH} \\
\text{CH}_3 & \quad \text{CH}_3
\end{align*}
\quad \begin{align*}
\text{CH}_2 & \quad \text{CH} \\
\text{O} & \quad \text{Si} \quad \text{O} \\
\text{CH}_3 & \quad \text{CH}_3
\end{align*}
\]

(9-26)

Peroxide crosslinking of the copolymer is more efficient than that of the homopolymer (Table 9-1). The process becomes a chain reaction (but with short kinetic chain length) involving polymerization of the pendant vinyl groups on the polysiloxane chains in combination with coupling of polymeric radicals. The crosslinking of EPDM rubbers is similarly more efficient when compared to EPM rubbers since the former contain double bonds in the polymer chain.

**TABLE 9-1 Efficiency of Crosslinking of Polydimethylsiloxane by Bis(2,4-dichlorobenzoyl) Peroxide**

<table>
<thead>
<tr>
<th>Vinyl Comonomer Content (mol %)</th>
<th>Number of Crosslinks per Peroxide Molecule Decomposed for Peroxide Concentration of 0.74%</th>
<th>1.47%</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.0</td>
<td>0.31</td>
<td>0.19</td>
</tr>
<tr>
<td>0.1</td>
<td>0.80</td>
<td>0.42</td>
</tr>
<tr>
<td>0.2</td>
<td>1.0</td>
<td>0.63</td>
</tr>
</tbody>
</table>

aData from Bobear [1967].
Radiation crosslinking of various polymers has been studied [Chapiro, 1962; McGinniss, 1986; Pappas, 1989; Shyichuk et al., 2001; Wilson, 1974]. The reaction is essentially the same as in peroxide crosslinking except that polymer radicals are formed by the interaction of ionizing radiation (Sec. 3-4d) with polymer. Ultraviolet radiation can also be used but is more limited in that the depth of penetration of a sample by UV is considerably less than by ionizing radiation. Radiation crosslinking has found commercial utilization in the crosslinking of polyethylene, other polyolefins, and poly(vinyl chloride) for electrical wire and cable insulation and heat-shrinkable products (tubing, packaging film, and bags). Curing of coatings and adhesives are other applications of radiation crosslinking. The efficiency of radiation crosslinking is increased by the presence of a multifunctional monomer such as allyl methacrylate or trimethylolpropane triacrylate [Odian and Bernstein, 1964; Ratnam, 2001].

Ultraviolet and ionizing radiation play a major role in integrated-circuit technology. For negative resists, a pattern is formed in a polymer placed on a substrate such as silicon by a controlled electron beam or using a masking technique with UV radiation. The portion of the polymer exposed to radiation undergoes crosslinking, and the corresponding image can be developed by dissolving away the unexposed, uncrosslinked polymer with an appropriate solvent. The pattern is etched into the silicon substrate by treatment with acid. The portions of the silicon covered with polymer are protected during the etching process. [Positive resists use a polymer, such as poly(methyl methacrylate), which undergoes degradation on irradiation.] The same principle is used in photoimaging applications.

9-2d Other Crosslinking Processes

Many other crosslinking reactions are used in commercial applications. A variety of halogen-containing elastomers are crosslinked by heating with a basic oxide (e.g., MgO or ZnO) and a primary diamine [Labana, 1986; Schmiegel, 1979]. This includes poly(epichlorohydrin) (Sec. 7-2b-6); various co- and terpolymers of fluorinated monomers such as vinylidene fluoride, hexafluoropropene, perfluoro(methyl vinyl ether), and tetrafluoroethylene (Sec. 6-8e); and terpolymers of alkyl acrylate, acrylonitrile, and 2-chloroethyl vinyl ether (Sec. 6-8e).

Crosslinking involves dehydrohalogenation followed by addition of the diamine to the double bond (Eq. 9-27) with the metal oxide acting as an acid acceptor. Some vulcanizations employ a dithiol instead of a diamine. Elastomeric terpolymers of alkyl acrylate, ethylene, and alkenoic acid (Sec. 6-8b) are vulcanized by addition of diamine.
The vulcanization of polychloroprene (Neoprene) is carried out in different ways. Vulcanization by sulfur, even with an accelerator, is not practiced to a large extent. Vulcanizations by metal oxides (without diamine), either alone or in combination with sulfur (sometimes together with an accelerator), give the best physical properties for the crosslinked product. Halogenated butyl rubber is crosslinked in a similar manner. The mechanism for crosslinking by metal oxide alone is not established [Stewart et al., 1985; Vukov, 1984].

Cellulosic fibers (cotton, rayon) are crosslinked by reaction of the hydroxyl groups of cellulose with formaldehyde, diepoxides, diisocyanates, and various methylol compounds such as urea–formaldehyde prepolymer, \(N,N'\)-dimethylol-\(N,N'\)-dimethylene urea, and trimethylolmelamine [Marsh, 1966]. Crosslinking imparts crease and wrinkle resistance and results in iron-free fabrics.

9-3 REACTIONS OF CELLULOSE

Cellulose is an abundant naturally occurring polysaccharide, whose repeat unit is derived from \(\beta\)-glucose. About one-third of all plant matter is made up of cellulose. Although found widely in nature, commercial cellulose is derived almost entirely from cotton and wood [Arthur, 1989; Bikales and Segal, 1971; Billmeyer, 1984; Brydson, 1999; Ott et al., 1954, 1955]. Cotton, the hairs on the seed of the cotton plant, is composed of about 89% cellulose and 7% water, and the remaining portion consists mostly of waxes, pectic and other organic acids, and protein. The seed hairs contain both long fibers (cotton or lint) and short fibers (linters). The long fibers are used directly to manufacture cotton textiles with more than 40 billion pounds produced annually worldwide. Cotton fabrics hold up well to laundering and have an excellent feel on the human body. The latter is a consequence of cotton possessing high moisture absorption and heat conduction. The short fibers, after treatment with 2–5% aqueous sodium hydroxide to remove most impurities, are used as a source of cellulose (99% pure) for producing a variety of polymeric materials as described below.

Wood contains about 40–50% cellulose with the remaining being lignin and lower-molecular-weight polysaccharides. Treatment of wood pulp with acid and steam followed by basic sodium sulfide yields a product that is 92–98% cellulose.

The properties of the cellulose obtained from cotton short fibers and wood are such that it cannot be directly formed into useful products. It is highly crystalline and insoluble and decomposes at high temperatures without flowing or melting—all a consequence of the extremely strong hydrogen bonding present. However, cellulose is used in large quantities for both fiber and plastics applications by employing various chemical reactions to impart processability.

9-3a Dissolution of Cellulose

Cellulose (VIII) is spun into fiber or cast into film by using a chemical reaction to convert it into a soluble xanthate derivative (Turbak, 1988). This is achieved by treating cellulose with 18–20% aqueous sodium hydroxide solution at 25–30°C for about 0.5–1 h. Much of the sodium hydroxide is physically absorbed into the swollen polymer; some of it may be in the form of cellulose alkoxides. The excess alkali is pressed out of the cellulose pulp and the mass aged to allow oxidative degradation of the polymer chains to the desired molecular weight. The alkali cellulose is then treated with carbon disulfide at about 30°C and the resulting mass dissolved in dilute sodium hydroxide to form the sodium
The degree of xanthation for the commercial process is about 0.5 xanthate group per repeat unit. This is sufficient to solubilize the cellulose. (Although XXIV shows the xanthate group only at C-6, it should be understood that there is a distribution of xanthate groups among C-2, C-3, and C-6 as per the discussion in Sec. 9-1k.) Fibers or films are produced by spinning or casting the viscous cellulose sodium xanthate solution into a coagulation bath containing about 10% sulfuric acid at 35–40°C. The acid hydrolyzes the sodium xanthate derivative to the xanthic acid (XXV), which is unstable and decomposes (without isolation). This regenerates cellulose that is insoluble in the aqueous medium, and the result is a solid cellulose fiber or film product, referred to as viscose rayon and cellophane, respectively. Both products are also referred to as regenerated cellulose. Viscose rayon is not as good a fiber as cotton (sometimes referred to as native cotton). The mechanical strength is lower as a result of a somewhat lower crystallinity and lower molecular weight (chain scission occurs during the various processing steps). However, it is an important fiber with about 4 billion pounds produced annually worldwide. Cellophane is widely used in packaging applications (wrap for food and tobacco products).

An alternate procedure used in a few specialty applications is the cuprammonium process. This involves stabilization of cellulose in an ammonia solution of cupric oxide. Solubilization occurs by complex formation of cupric ion with ammonia and the hydroxyl groups of cellulose. Regeneration of cellulose, after formation of the desired products, is accomplished by treatment with acid. The main application of the cuprammonium process is for the synthesis of films and hollow fibers for use in artificial kidney dialysis machines. The cuprammonium process yields products with superior permeability and biocompatibility properties compared to the xanthation process. Less than 1% of all regenerated cellulose is produced by the cuprammonium process.

A more recent process for producing regenerated cellulose involves the use of N-methylmorpholine-N-oxide, a highly polar solvent, at about 130°C to dissolve cellulose [Rosenu et al., 2001]. About 5% of all regenerated cellulose is produced by this method.
9-3b Esterification of Cellulose

Acetate, mixed acetate–propionate and acetate–butyrate, and nitrate esters of cellulose are produced commercially [Brewer and Boagan, 1985; Heinze and Liebert, 2001]. Most products fall into either of two categories—about 2.4 or close to 3 ester groups per repeat unit. As a result of decreased hydrogen bonding and crystallinity relative to cellulose, these esters are thermoplastic (i.e., they flow when heated) and can be manufactured into products by extrusion, molding, and similar processes. All cellulose esters except the triacetate generally require plasticization to achieve the required flow behavior. Plasticization is insuffi- cient for the triacetate and processing is usually carried out in solutions of methylene chloride–methanol.

Cellulose acetate is the most important ester derivative of cellulose. It is produced by acetylation of cellulose using acetic anhydride in acetic acid in the presence of a strong acid catalyst (usually sulfuric acid). In Eq. 9-29 the symbol $\overline{P}$ is a general means of representing a polymer molecule minus the functional group of interest and $\overline{P}$—OH specifically represents the cellulose molecule, although it could also represent poly(vinyl alcohol) or any other polymer containing a hydroxyl group.

Partially acetylated cellulose (i.e., cellulose with less than three ester groups per repeat unit) is produced by an indirect route. Direct synthesis yields an inhomogeneous product due to insolubility of cellulose in the reaction mixture. Some chains are completely acetylated while others may be completely unreacted. A partially acetylated product is usually produced by controlled hydrolysis of the triacetate. The triacetate is soluble in the reaction mixture and complete solubility ensures that the final product will be more homogeneous. Hydrolysis of the triacetate is carried out by controlled reversal of the esterification reaction by the addition of water or dilute acetic acid.

Cellulose acetate and other esters are tough, strong materials with good optical clarity. The acetate has the best strength and hardness while the acetate–butyrate is better in weatherability, dimensional stability, and low-temperature impact strength. The acetate–propionate has properties in between the other two materials. The largest-volume application of cellulose acetate is as a fiber for textiles (clothes, draperies, and bedspreads) and cigarette filters. Plastic applications for cellulose acetate and the mixed ester derivatives include eyeglass frames, photographic film, combs, brush handles, film and sheet for decorative signs, and lacquers and protective coatings for automobiles and wood furniture. Cellulose nitrate is used for lacquer finishes (automobiles, wood furniture), explosives, and propellants.

9-3c Etherification of Cellulose

Various ether derivatives of cellulose, including some that are water-soluble, are important [Heinz and Liebert, 2001; Just and Majewicz, 1985; Zhang, 2001]. Methyl cellulose and carboxymethyl cellulose ($R = \text{CH}_3$ and $\text{CH}_2\text{COOH}$, respectively) are synthesized by reaction of cellulose with sodium hydroxide followed by the appropriate alkyl halide:

$$
\overline{P} - \text{OH} + \text{HOCCCH}_3 \rightarrow \overline{P} - \text{OCCH}_3 + \text{H}_2\text{O} \quad (9-29)
$$
Hydroxyethyl cellulose is produced by using ethylene oxide in place of the halide. Applications for these products include lacquers, additives for detergents, food, drilling muds, and paints.

9-3d Chitin

Chitin is a polysaccharide similar to cellulose except that the OH at C–2 is replaced by an acetamido group (CH$_3$CONH). Chitin is the main component of the hard external covering (exoskeleton) of crustaceans such as lobsters, crabs, and shrimp. Like cellulose, the processing of chitin into polymeric products is limited by its insolubility and decomposition without melting. The availability in huge quantities has encouraged many attempts to find commercial applications of chitin, but very few have been found to be economically feasible.

9-4 REACTIONS OF POLY(VINYL ACETATE)

In addition to its use as a plastic, poly(vinyl acetate) is used to produce two polymers that cannot be synthesized directly since their monomers do not exist. Poly(vinyl alcohol) is obtained by alcoholysis of poly(vinyl acetate) with methanol:

\[
\begin{align*}
\text{CH}_3 & \quad \text{CO} \\
\sim\text{CH}_2\sim \text{CH} & \quad \xrightarrow{\text{CH}_3\text{OH}} \quad \sim\text{CH}_2\sim \text{CH} \sim
\end{align*}
\]

Both acids and bases catalyze the reaction, but base is usually employed because of the more rapid rates and freedom from side reactions.

Reaction of poly(vinyl alcohol) with an aldehyde yields the corresponding poly(vinyl acetal):

\[
\begin{align*}
\sim\text{CH}_2\sim \text{CH} & \quad \xrightarrow{\text{RCHO}} \quad \sim\text{CH}_2\sim \text{CH} \sim \\
\text{OH} & \quad \xrightarrow{-\text{H}_2\text{O}} \quad \sim\text{CH}_2\sim \text{CH} \sim
\end{align*}
\]

The reaction is usually carried out with an acid catalyst. Acetal formation does not proceed to completion because of isolation of single hydroxyl groups between pairs of acetal structures. The two most important acetals are the formal and butyral (R = H and C$_3$H$_7$, respectively). The applications of poly(vinyl alcohol) and its acetals are described in Sec. 3-14c-2.

Reaction of poly(vinyl alcohol) with cinnamoyl chloride yields polymers that produce photocrosslinked resists for microelectronic applications.

9-5 HALOGENATION

9-5a Natural Rubber

Chlorination and hydrochlorination of natural rubber are industrial processes carried out on solutions of uncrosslinked rubber in chlorinated solvents [Allen, 1972; Ceresa, 1978;
Subramaniam, 1988]. Hydrochlorination, usually carried out at about 10°C, proceeds by electrophilic addition to give the Markownikoff product with chlorine on the tertiary carbon (Eq. 9-33) [Golub and Heller, 1964; Tran and Prud’homme, 1977]. Some cyclization of the intermediate carbocation (XXVI) also takes place (Sec. 9-7). The product, referred to as rubber hydrochloride, has low permeability to water vapor and is resistant to many aqueous solutions (but not bases or oxidizing acids). Applications include packaging film laminates with metal foils, paper, and cellulose films, although it has been largely replaced by cheaper packaging materials such as polyethylene.

\[ \text{CH}_3\text{CH}_2\text{C} \equiv \text{CH} - \text{CH}_2 \text{Cl} \text{H}^+ \rightarrow \text{CH}_2\text{C} \equiv \text{CH}_2 - \text{CH}_2 \text{Cl} \text{H}^+ \]

\[ \text{CH}_3 \]

XXVI

\[ \text{CH}_2\text{C} \equiv \text{CH}_2 - \text{CH}_2\text{Cl} \text{Cl}^- \]

(9-33)

Chlorination of natural rubber (NR) is carried out with chlorine in carbon tetrachloride solution at 60–90°C to yield a chlorinated rubber containing about 65% chlorine, which corresponds to 3.5 chlorine atoms per repeat unit. The process is complex and includes chlorine addition to the double bond, substitution at allylic positions, and cyclization. Chlorinated rubber has high moisture resistance and is resistant to most aqueous reagents (including mineral acids and bases). It is used in chemical- and corrosion-resistant paints, printing inks, and textile coatings. Bromination of butyl rubber is also practiced [Parent et al., 2002].

Butyl rubber, containing only 0.5–2.5% isoprene units, is not efficiently crosslinked by sulfur. Chlorination of butyl rubber is carried out to improve its vulcanization efficiency by allowing a combination of sulfur and metal oxide vulcanizations.

9-5b Saturated Hydrocarbon Polymers

The chlorination of polyethylene, poly(vinyl chloride), and other saturated polymers has been studied [Favre et al., 1978; Lukas et al., 1978; McGuchan and McNeil, 1968; Stoeva and Vlaev, 2000]. The reaction is a free-radical chain process catalyzed by radical initiators.

\[ \text{CH}_3\text{CH}_2\text{CHO} + \text{Cl}^- \rightarrow \text{CH}_3\text{CH}_2\text{CHO} + \text{HCl} \]

\[ \text{Cl}^- \]

(9-34)

\[ \text{CH}_3\text{CH}_2\text{CO} + \text{Cl}_2 \rightarrow \text{CH}_3\text{CH}_2\text{CO} + \text{Cl}^- \]

(9-35)

Chlorinated poly(vinyl chloride) (CPVC) has increased $T_g$ compared to PVC, and this increases its upper use temperature. Applications include hot- and cold-water pipe as well as pipe for the handling of industrial chemical liquids. Chlorinated polyethylene (CPE) finds use as roofing and other vapor barrier membranes, as pond liners, and as an additive to improve the impact strength of PVC.
The reaction of polyethylene with chlorine in the presence of sulfur dioxide yields an elastomer containing both chloro and chlorosulfonyl groups:

\[ \text{CH}_2\text{CH} \rightarrow \text{Cl} \text{SO}_2\text{Cl} \]

The commercial products contain one chlorine atom per 2–3 repeat units and about one chlorosulfonyl group per 70 repeat units. The chlorosulfonyl groups allow the elastomer to be vulcanized with metal oxides such as lead or magnesium oxide by the formation of metal sulfonate linkages:

\[ \text{SO}_2\text{Cl} \text{PbO}_2 \rightarrow \text{CH}_2\text{CH} \text{SO}_2 \text{O} \text{Pb} \text{O} \text{SO}_2 \text{CH}_2\text{CH} \]

Additional curing is often achieved with sulfur, peroxide, or maleimide formulations. Chlorosulfonated polyethylene has improved resistance to oil, ozone, and heat compared to many other elastomers. Applications include barrier membranes and liners, surface coatings on fabrics, automobile air-conditioner hose, electrical cable insulation, and spark-plug boots [Andrews and Dawson, 1986].

9-6 AROMATIC SUBSTITUTION

Aromatic electrophilic substitution is used commercially to produce styrene polymers with ion-exchange properties by the incorporation of sulfonic acid or quaternary ammonium groups [Brydson, 1999; Lucas et al., 1980; Miller et al., 1963]. Crosslinked styrene–divinylbenzene copolymers are used as the starting polymer to obtain insoluble final products, usually in the form of beads and also membranes. The use of polystyrene itself would yield soluble ion-exchange products. An anion-exchange product is obtained by chloromethylation followed by reaction with a tertiary amine (Eq. 9-38) while sulfonation yields a cation-exchange product (Eq. 9-39):

\[ \text{ClCH}_2\text{OCH}_3 \rightarrow \text{CH}_2\text{Cl} \rightarrow \text{CH}_2\text{NR}_3 \]

\[ \text{H}_2\text{SO}_4 \rightarrow \text{SO}_3\text{H} \]

\[ \text{NR}_3 \]

\[ \text{Cl}^- \]
Natural rubber and other 1,4-poly-1,3-diene polymers are cyclized by treatment with strong protonic acids or Lewis acids [Golub, 1969; Subramaniam, 1988]. The reaction involves protonation of the double bond (Eq. 9-40) followed by cyclization via attack of the carbocation on the double bond of an adjacent monomer unit (Eq. 9-41). Some bicyclic and polycyclic fused-ring structures are formed by propagation of the cyclization reaction through more than two successive monomer units. However, the average number of fused rings in a sequence is only 2–4 because of the steric restrictions involved in the polymer reaction as well as competing transfer reactions and the isolation of unreacted monomer units between pairs of cyclized units. Cyclized rubbers have been used for shoe soles and heels, adhesives, hard moldings, and coatings.

Cyclization is a key reaction in the production of carbon fibers from polyacrylonitrile (PAN) (acrylic fiber; see Sec. 3-14d-2). The acrylic fiber used for this purpose usually contains no more than 0.5–5% comonomer (usually methyl acrylate or methacrylate or methacrylic acid). Highly drawn (oriented) fibers are subjected to successive thermal treatments—initially 200–300°C in air followed by 1200–2000°C in nitrogen [Riggs, 1985]. PAN undergoes cyclization via polymerization through the nitrile groups to form a ladder structure (XXVII). Further reaction results in aromatization to the polyquinizarine structure (XXVIII) while some of the rings remain as hydrogenated polyquinizarine structures (XXIX). Further heating at temperatures above 2500°C in nitrogen or argon for brief periods eliminates all elements except carbon to yield carbon fibers with graphitelike morphology. The carbon
fibers are subjected to a final oxidizing atmosphere such as a mixture of gaseous nitrogen and oxygen at 350–1100°C to oxidize the surface for purposes of imparting adhesive properties. The process for producing carbon fibers is expensive because of the large energy expenditures required as well as the need to treat the volatile by-products (which include toxic HCN).

Carbon fibers combine ultrahigh strength and low density when used in composite formulations with epoxy and other resins. More than 50% of carbon fiber use is in air and spacecraft applications where weight and fuel savings are achieved without sacrificing performance. A variety of components of air and spacecraft are fabricated from carbon fiber–epoxy composites. Carbon fiber–epoxy composites have been used to produce the entire aircraft structure of a business jet (Lear 2100) and the payload bay doors of a space shuttle. Carbon fibers combined with higher-performance matrix materials such as polyimides or polybenzimidazole offer the potential for further improvements. Civilian applications include sporting goods—golf-club shafts, tennis racquets, fishing rods, and boat masts. The lighter weight of the carbon fiber composite (compared to the metal component it replaces) allows a redesign of the item for improved performance. The lighter golf-club shaft allows a heavier head design. Other applications include high-quality loudspeakers and various medical applications, including artificial limbs and surgical implants.

Other polymers undergo cyclization, but there are no commercial applications. Poly(methacrylic acid) cyclizes by anhydride formation and poly(methyl vinyl ketone) by condensation (with dehydration) between methyl and carbonyl groups.

9-8 OTHER REACTIONS

Hydrogenation of double bonds is practiced with some elastomers such as SBR and NBR to increase high temperature and oxidative resistance [Hsieh, 1998; Hsieh and Quirk, 1996, Wrana et al., 2001]. Only partial hydrogenation is performed since some double bonds are required to achieve the subsequent crosslinking required to achieve elastic behavior.

Epoxidation of double bonds in poly(1,3-dienes) yield epoxy resins that are subsequently crosslinked (Sec. 2-12d).

9-9 GRAFT COPOLYMERS

Graft and block copolymers contain long sequences of each of two different monomers in the copolymer chain. A block copolymer contains the sequences of the two monomers in a continuous arrangement along the copolymer chain while a graft copolymer contains a long sequence of one monomer (often referred to as the backbone polymer) with one or more branches (grafts) of long sequences of a second monomer (Secs. 2-13a, 6-1b). A variety of techniques for synthesizing such structures have been studied.

Most methods of synthesizing graft copolymers involve radical polymerization, but ionic graft polymerizations are also possible [Battaerd and Tregear, 1967; Ceresa, 1973, 1976; Dreyfuss and Quirk, 1986; Gnanou, 1996; Gnanou and Taton, 2002; Rempp and Lutz, 1989]. Graft polymerizations are carried out in heterogeneous as well as homogeneous systems.

Three methods exist for synthesizing graft copolymers. Grafting onto involves the reaction between functional groups on two different polymers:

\[
\text{A} + \text{B} \rightarrow \text{AB}
\]
Graft polymerization can be synthesized with different densities of graft chains attached to the backbone polymer. Higher graft densities are achieved in the grafting-onto and grafting-from methods by using a backbone polymer with a higher density of A groups. The grafting density in the grafting-through method is controlled by the ratio of macromonomer to comonomer. The graft copolymer is essentially the equivalent of a star polymer when there are only a few graft chains. The terms comb polymer and brush polymer are used to describe a graft copolymer with a high density of graft chains. The term brush polymer is the more correct description because of the conformational freedom allowed the graft chains as well as the backbone polymer. The graft polymer resembles a brush used in the laboratory to clean the inside of a test tube or bottle.

9-9a Radical Graft Polymerization

9-9a-1 Vinyl Macromonomers

There are various routes to vinyl macromonomers [Gnanou and Taton, 2002]. For example, the reaction of an HO-terminated polymer such as polysiloxane, polycaprolactone, or polytetrahydrofuran with acryloyl chloride

\[
\text{HO} + \text{CH}_2=\text{CH}-\text{CO-Cl} \rightarrow \text{HO-CH-CH}_2
\]

or using vinyl chloroacetate as the initiator in ATRP

\[
\text{CH}_2=\text{CH-OCH}_2\text{Cl} \xrightarrow{\text{CuCl}} \text{CH}_2=\text{CH-OCH}_2\text{Cl} (\text{M}_n\text{Cl})
\]
polymerization (Sec. 3-6e), the formation of unsaturated end groups in cationic polymerization of isobutylene, and the traditional Ziegler–Natta and metallocene polymerizations of ethylene and propene; see also Sec. 5-4b.

Vinyl macromonomers can be polymerized by any of the methods of radical polymerization to produce graft polymers. Ionic polymerization is also possible for some macromonomers.

9-9a-2 Chain Transfer and Copolymerization

In the presence of a dissolved polymer, the radical polymerization of a monomer by thermal decomposition of an initiator results in a mixture of homopolymerization and graft polymerization [Brydon et al., 1973, 1974; Ludwico and Rosen, 1975, 1976; Pham et al., 2000; Russell, 2002]. Polymer radicals (XXX), formed by chain transfer between the propagating radical and polymer, initiate graft polymerization of styrene. The product (XXXI) consists of polystyrene grafts on the 1,4-poly-1,3-butadiene backbone. Polymer radicals are also formed by attack on polymer by primary radicals from the initiator. Although chain transfer usually involves hydrogen abstraction, some polymers contain more labile atoms; for instance, chlorine atom abstraction occurs with chlorinated rubber [Kaleem et al., 1979].

For polymers containing double bonds as in 1,4-poly-1,3-butadiene, graft polymerization also involves copolymerization between the polymerizing monomer and the double bonds of the polymer in addition to grafting initiated by chain transfer. The relative amounts of the two processes depend on the identity of the double bond. Grafting via chain transfer predominates for 1,4-poly-1,3-dienes containing relatively unreactive 1,2-disubstituted double bonds. Grafting via copolymerization of the double bond predominates when the double bond is more reactive, such as polybutadienes with high contents of vinyl groups (produced by 1,2-polymerization).

Although this method yields a mixture of homopolymer and graft copolymer, and probably also ungrafted backbone polymer, some of the systems have commercial utility. These are high-impact polystyrene (HIPS) [styrene polymerized in the presence of poly(1,3-butadiene)], ABS and MBS [styrene–acrylonitrile and methyl methacrylate–styrene, respectively, copolymerized in the presence of either poly(1,3-butadiene) or SBR] (Sec. 6-8a).

The chain transfer to polymer process that produces long-chain branching is also a graft polymerization process (Sec. 3-6d).
Polymer radicals can also be produced by the irradiation of a polymer–monomer mixture with ionizing radiation. Thus, the interaction of ionizing radiation with polyethylene–styrene produces radical centers on polyethylene, and these initiate graft polymerization of styrene to produce poly(ethylene-graft-styrene) [Rabie and Odian, 1977].

Most radiation graft polymerizations are carried out as heterogeneous reactions. The polymer is swollen by monomer but does not dissolve in the monomer. (For semicrystalline polymers, swelling and grafting take place only in the amorphous regions.) The typical reaction system involves equilibration of polymer with monomer followed by irradiation of the monomer-swollen polymer while immersed in excess monomer. Whether graft polymerization occurs uniformly throughout the volume of the polymer or mainly at its surfaces depends on the rate of monomer diffusion into the polymer relative to the grafting rate [Cardona et al., 2002; Imre and Odian, 1979; Odian et al., 1980]. For reaction systems with slow diffusion rates and/or fast grafting rates, the overall process becomes diffusion-controlled, with the observed grafting rate limited by the rate of diffusion of monomer into polymer. Anomalous kinetic behavior is observed under these reaction conditions; for example, the reaction rate becomes greater than first-order in monomer, less than half-order in initiation rate, and inversely dependent on the thickness of the polymer sample.

Most graft polymerizations, irrespective of the initiation process, yield mixtures of the graft copolymer, ungrafted backbone polymer, and homopolymer of the monomer. The relative amounts of the three species depend on the monomer–polymer combination and the initiation process. For initiation by chain transfer, the efficiency of the grafting reaction relative to homopolymerization is dependent on the tendency of a propagating radical to transfer to polymer compared to propagation. A consideration of $C_p$ values (Sec. 3-6d) indicates that the extent of homopolymerization will be very significant during graft polymerization. The grafting efficiency of the irradiation process is often discussed in terms of the relative extents of radical formation in the polymer and monomer. Combinations of a polymer such as polyethylene (relatively susceptible to radiolytic bond cleavage) and a monomer such as styrene (relatively resistant to radiolytic bond cleavage) are generally considered to involve minimal homopolymerization relative to graft polymerization. However, this conclusion is somewhat naive as it assumes that hydrogen atoms formed in the radiolytic initiation step (Eq. 9-51) will mostly form molecular hydrogen. This is unlikely in the presence of monomer, which should scavenge at least some of the hydrogen radicals. The extent of homopolymerization equals that of graft polymerization if all hydrogen radicals initiate homopolymerization [Machi and Silverman, 1968].

The range of radiation grafting systems studied is enormous; almost all of the more common monomers such as styrene, methyl methacrylate, vinyl chloride, and acrylonitrile have been grafted to most of the commercially available addition and condensation polymers [Chapiro, 1962; Wilson, 1974]. One commercial application of radiation processing is the curing of wood impregnated with monomers for high-performance commercial flooring.

\[
\begin{align*}
\text{radiation} & \quad \rightarrow \quad \text{radicalization} \\
\text{CH}_2\text{CHCH}_2\text{H} & \quad \rightarrow \quad \text{CH}_2\text{CH} \cdot + \text{H}^+ \\
\text{CH}_2\text{CH} & \quad + \quad n\text{CH}_2\text{═CH} \phi & \quad \rightarrow \quad \text{CH}_2\text{CH} \cdot \quad (\text{CH}_2\text{CH} \phi)_n \cdot
\end{align*}
\]
The product involves a combination of homopolymerization and graft polymerization of a monomer such as methyl methacrylate to wood.

Graft polymerization can also be achieved by irradiation with ultraviolet radiation, often in the presence of a photosensitizer such as benzophenone or benzoin [Guthrie et al., 1979; Tazuke and Kimura, 1978]. Photolytic grafting is similar to radiation grafting, except that the depth of penetration by UV is far less than by ionizing radiation.

9-9a-4 Redox Initiation

Redox initiation is often an efficient method for graft polymerization. Hydroxyl-containing polymers such as cellulose and poly(vinyl alcohol) undergo redox reaction with ceric ion or other oxidizing agents to form polymer radicals capable of initiating polymerization [Graczyk and Hornof, 1988; Leza et al., 1990; Odian and Kho, 1970; Storey and Goff, 1989]. Redox initiation usually results in grafting with a minimum of homopolymerization since only the polymer radical is formed. It is, however, limited to polymers containing the necessary functional group. There are some reports of polymers with amide, urethane, and nitrile groups undergoing redox initiation [Feng et al., 1985; Lee et al., 1976; Nayak et al., 1979a,b; Sengupta and Palit, 1978].

9-9a-5 Living Radical Polymerization

Living radical polymerization (LRP) by NMP and ATRP (Sec. 3-15) has been extensively studied for producing graft copolymers using both the grafting-from and grafting-through methods [Davis and Matyjaszewski, 2002; Gnanou and Taton, 2002; Hawker et al., 2001; Matyjaszewski and Xia, 2001].

LRP offers the potential for producing graft polymers in which the lengths of the graft chains are controlled much better than in other radical polymerizations. Also unlike the other methods of radical polymerization, it is possible to have graft chains that are block copolymers by using a sequential addition of different monomers. For example, ATRP yields graft copolymers via the grafting from method when a polymer with halogen-containing side groups is used (Eq. 9-54). If only monomer M_1 is used, the product is a graft copolymer with polyM_1 graft chains. If monomers M_1 and M_2 are sequenced, the graft chains are poly-M_1–poly-M_2 block copolymers. The graft chains contain statistical placements of M_1 and M_2 units if a mixture of the two monomers is used. Block copolymer graft chains offer interesting possibilities for producing core–shell cylindrical brushes in which the core blocks have properties very different from those of the shell blocks, such as hard versus soft morphologies [Borner et al., 2001; Cheng et al., 2001]. Such materials may be useful for synthesis of nanoscale channels and other devices. In one application, the core was loaded with HAuCl₄, which was then reduced with UV, light, or chemical reducing agents to deposit gold in the core–resulting in a metal nanowire [Djalali et al., 2002].
Various halogenated polymers are used as the polymeric initiator for ATRP, for example, vinyl chloride–vinyl chloroacetate and styrene–p-chloromethylstyrene copolymers, brominated butyl rubber, and chlorosulfonated polyethylene [Borner and Matyjaszewski, 2002; Coskun and Temuz, 2003]. (The vinyl chloride units have much lower reactivity for ATRP compared to the vinyl chloroacetate units because of steric reasons.) The density of grafting is adjusted by varying the copolymer composition.

The grafting-through method has also been studied for ATRP. Vinyl chloroacetate is used as the initiator in ATRP of a monomer such as styrene to produce a macromonomer. Vinyl chloroacetate does not significantly copolymerize with styrene, and the result is a polystyrene vinyl macromonomer, which is then polymerized to a brush polymer [Davis and Matyjaszewski, 2002].

Using the grafting-from method with NMP requires the synthesis and (co)polymerization of monomers that contain the nitroxide group [Hawker et al., 2001]. A halogen-containing monomer such as vinyl chloroacetate or p-chloromethylstyrene is reacted with an HO-containing alkoxyamine to yield a vinyl alkoxyamine, which is used as a NMP initiator to produce a vinyl macromonomer. Subsequent (co)polymerization of the vinyl macromonomer produces the graft copolymer. Alternately, the HO-containing alkoxyamine is reacted with a halogen-containing polymer such as vinyl chloride–vinyl chloroacetate to place alkoxyamine sites on the polymer. These sites are subsequently used to initiate graft polymerization by NMP.

RAFT has also been used to produce graft polymers. The grafting from method is achieved by reacting a halogen-containing polymer such as styrene–p-chloromethylstyrene copolymer with sodium dithiobenzoate to obtain a polymeric dithioester, which is an initiator in RAFT polymerization (Sec. 3-15d) [Quinn et al., 2002].

\[
\text{CH}_2\equiv\text{CHO-COCH}_2\text{Cl} + \text{HO-}R^1\text{O-}NR^2R^3 \rightarrow \text{CH}_2\equiv\text{CHO-COCH}_2\text{O-}R^1\text{O-}NR^2R^3
\]

(9-55)

The grafting-through method has been used to graft polymers onto solid surfaces such as silica, gold, and polymers via the NMP and ATRP techniques [Davis and Matyjaszewski, 2002]. The solid surfaces include those on flat wafers and spherical particles. Appropriate reagents are used to introduce functional groups that initiate NMP or ATRP. For example, a thiol reacts with gold surfaces through sulfide formation. If the thiol reagent also contains a halogen or alkoxyamine group, ATRP or NMP can be achieved. Alternately, the thiol contains a functional group that is reacted with some other reagent to attach a halogen or alkoxyamine group to the surface. A chlorosilane is used to introduce functional groups onto silica surfaces [Zhao and Brittain, 2000].

9-9b Anionic Graft Polymerization

Metallation of a polymer by treatment with strong base, for example, t-butyllithium, yields polymeric anions that initiate the grafting of monomers such as styrene, acrylonitrile, and...

\[
\text{BuLi} \quad \text{CH}_2\text{CH}=\text{CHCH}_2 \quad \rightarrow \quad \text{BuLi} \quad \text{CH}_2\text{CH}=\text{CHCH}_2
\] (9-57)

Polymers with carboxylate anionic groups (COOH and COOR are precursors) initiate graft polymerization [Harris and Sharkey, 1986; Sundet, 1978].

\[
\text{COO}^- + \text{O} \quad \rightarrow \quad \text{COO(}\text{CH}_2\text{CH}_2\text{COO})_n
\] (9-58)

Coupling of polymers to form graft copolymers is accomplished by nucleophilic reaction between living polystyryl carbanion and various chlorine-containing polymers such as poly(vinyl chloride) [Kucera et al., 1983, 1985; Majid et al., 1982]. Elimination is a side reaction, and the overall yield is also limited by steric hindrance.

### 9-9c Cationic Graft Polymerization

Polymeric carbocations have been formed from a chlorine-containing polymer such as chlorinated SBR and polystyrene, poly(vinyl chloride), and polychloroprene, by reaction with \((\text{C}_2\text{H}_5)_2\text{AlCl}\), for example

\[
\text{Cl} \quad \text{CH}_2\text{CH} \quad \rightarrow \quad \text{Cl} \quad \text{CH}_2\text{CH}
\] (9-60)

The polymeric carbocation initiates polymerization of isobutylene, styrene, tetrahydrofuran, and other monomers [Cai and Yan, 1987; Cameron and Sarmouk, 1990; Kennedy and Ivan, 1992; Martinez et al., 2001; Pi and Kennedy, 2001].

A hydroxy-containing polymer can be coupled with living polytetrahydrofuran carbocation [Cameron and Duncan, 1983]:

\[
\text{HO} + \text{O} \quad \rightarrow \quad \text{HO} \quad \text{O}
\] (9-61)

### 9-9d Other Approaches to Graft Copolymers

Nonionic coupling reactions between appropriate polymers is another approach to graft copolymers. An example is the use of a telechelic polymer such as polystyrene containing one carboxyl end group per molecule. Graft copolymers are formed by coupling of carboxyl groups with the pendant epoxy groups of a copolymer of methyl methacrylate and glycidyl methacrylate [Miyauuchi et al., 1988]. The carboxyl-terminated polystyrene can be obtained by living anionic polymerization followed by reaction with carbon dioxide or radical polymerization in the presence of a chain-transfer agent such as 3-mercaptopropionic acid.
A telechelic polystyrene containing two carboxyl groups at one end of a polymer can be used as a macromonomer in a step polymerization with a diol or diamine to yield a polyester or polyamide containing graft chains of polystyrene. The required telechelic polymer is obtained by radical polymerization of styrene in the presence of 2-mercaptosuccinic acid.

Macromonomers containing a norbornene group have been polymerized by ROMP (Sec. 7-8) to form graft copolymers [Breunig et al., 1995; Heroguez et al., 1997].

ROMP combined with living anionic polymerization produces an interesting architecture referred to as a *double-brush polymer* by using compound $\text{XXXII} \ [R = (\text{CH}_2)_{10}\text{OCH}_2]$, which contains both norbornene and 1,1-diphenylethylene (DPE) groups [Cheng et al., 2002]. ROMP of $\text{XXXII}$ through the norbornene group produces a polymer $\text{XXXIII}$ with pendant DPE groups. Reaction of $\text{XXXIII}$ with living polystyryl anions produces $\text{XXXIV}$, a polymer with polystyrene graft chains. Subsequent reaction of $\text{XXXIV}$ with monomer $M_2$ ($\varepsilon$-caprolactam, ethylene oxide, or hexamethylcyclotrisiloxane) yields the double-brush polymer $\text{XXXV}$, in which there is one brush of polystyrene graft chains and a second brush of poly$M_2$ graft chains.

$$\text{XXXII} \xrightarrow{\text{ROMP}} \text{XXXIII} \xrightarrow{\text{PS}^-} \text{PSCH}_2\text{PhR} \xrightarrow{M_2} \text{PSCH}_2\text{PhR} = \text{PM}_2\text{Ph} \xrightarrow{(9-62)} \text{XXXV}$$

**9-10 BLOCK COPOLYMERS**

Most of the methods for synthesizing block copolymers were described previously. Block copolymers are obtained by step copolymerization of polymers with functional end groups capable of reacting with each other (Sec. 2-13c-2). Sequential polymerization methods by living radical, anionic, cationic, and group transfer propagation were described in Secs. 3-15b-4, 5-4a, and 7-12e. The use of telechelic polymers, coupling and transformations reactions were described in Secs. 5-4b, 5-4c, and 5-4d. A few methods not previously described are considered here.

Block copolymers have been obtained from polymeric radicals, which—unlike those employed for graft polymerization—have the radical centers at the ends of the polymer chains. This can be achieved by breaking chemical bonds in the polymer backbone by mastication (mixing) of the polymer [Ceresa, 1973, 1976, 1978; Sakaguchi and Sohma, 1978].
the shearing forces are sufficiently high during mastication, their concentration at individual bonds in the polymer chain results in bond rupture. Block copolymers are obtained by the mastication of either a mixture of two homopolymers

\[
\begin{align*}
\sim M_1M_1 \sim & \quad \text{milling} \quad \sim M_1, \\
\sim M_2M_2 \sim & \quad \rightarrow \quad \sim M_2,
\end{align*}
\]

or a mixture of a polymer and a monomer

\[
\begin{align*}
\sim M_1M_1 \sim & \quad \text{milling} \quad \sim M_1, \\
M_2 & \quad \rightarrow \quad \sim M_1M_2 \sim
\end{align*}
\]

The former gives a mixture of the block copolymer with the two homopolymers since the polymer radicals combine randomly. The latter yields the block copolymer along with the homopolymer of M_1.

Treatment of polyisobutylene (which contains terminal double bonds) with ozone followed by thermolysis produces polymeric radicals. Isobutylene–styrene block copolymer is formed when thermolysis is performed in the presence of styrene, but the process is not efficient because polystyrene and polyisobutylene homopolymers constitute more than half of the product [Cunliffe et al., 2001].

The synthesis of special initiators is another route to block copolymers. Reaction of XXXVI with an HO-terminated polyester or polyether yields a polymeric azonitrile, which initiates polymerization of a monomer such as styrene [Laverty and Gardland, 1977; Walz and Heitz, 1978].

\[
\begin{align*}
\text{CH}_3 & \quad \text{CH}_3 \\
\text{Cl} & \quad \text{CO(CH}_2)_2\text{C} & \quad \text{N} \equiv \text{N} \equiv \text{CO} \text{Cl} \\
\text{CN} & \quad \text{CN}
\end{align*}
\]

XXXVI

9-11 POLYMERS AS CARRIERS OR SUPPORTS

The use of a polymer as a carrier or support for some component of a reaction system is discussed in the remainder of this chapter. Three classes of polymer supports are encountered—polymer reagents, polymer catalysts, and polymer substrates [Kirschning et al., 2001; Sherrington, 2001]. Polymers that serve as reagents, catalysts, or substrates are functional polymers; that is, they contain a functional group that performs a particular chemical function. The term reactive polymer is also used. A polymer reagent is a polymer containing a functional group that acts as the reagent to bring about a chemical transformation on some small (i.e., low-molecular-weight) molecule. A polymer substrate has an attached molecule on which some transformation is carried out using a small-molecule reagent. A polymer catalyst contains a group that performs a catalytic function in some reaction—usually a reaction between small molecules.
There are two general approaches to the synthesis of a polymer reagent, catalyst, or substrate [Hodge, 1978; Mathur et al., 1980; Neckers, 1978; Sherrington, 1980, 1988]. In the functionalization of polymer approach the required functional group, which is to perform the reagent, catalyst, or substrate function, is attached to a readily available polymer by an appropriate reaction. The attachment is usually through a covalent bond, but ionic bonding has also been employed. In the functionalization of monomer approach an appropriate monomer with the desired functional group is synthesized and then polymerized or copolymerized.

**9-11a-1 Functionalization of Polymer**

This approach can be illustrated by describing the preparation of the polymer rhodium catalyst II (Sec. 9-1g). The synthesis is based on a nucleophilic substitution reaction of chloromethylated polystyrene [Grubbs and Kroll, 1971]:

\[
P\text{CH}_2\text{Cl} \xrightleftharpoons{\Phi\text{PLi}}^{\text{THF}} \xrightarrow{\text{RhCl(PO}}_3)\_3\_2 \quad \text{II} \quad (9-65)
\]

The chloromethylated polystyrene is usually obtained by chloromethylation of polystyrene (Eq. 9-38), although polymerization of p-vinyl benzyl chloride has also been used [Arshady et al., 1976]. A less desirable variation of this approach is the physical entrapment of a catalyst, substrate, or reagent within a polymer.

There are a number of considerations in the choice of the polymer to be used as a support—availability and cost, mechanical, thermal, and chemical stability, porosity, and compatibility with reagents and solvents. The use of a commercially available, inexpensive polymer is clearly preferable to a more expensive polymer or one that must be specifically synthesized for the purpose. The support polymer must be chemically and thermally inert under the conditions necessary for its functionalization and subsequent use. Heterogeneous polymer catalysts, reagents, and substrates require the support to possess a reasonable degree of mechanical strength. Some degree of crosslinking is usually employed for this purpose. The physical form of the functionalized polymer is also a consideration in terms of its application. The polymer support as well as the functionalized polymer should be porous to allow access of the reagent(s) and solvent(s), if any, to achieve a homogeneously active polymer. A polymer reagent, catalyst, or substrate with only surface activity would result if the polymer were nonporous. Compatibility of the functionalized polymer (more specifically, the regions in the vicinity of the functional groups) with reagents and solvents is also needed to achieve high reaction rates and high yields.

Polystyrene is presently the overwhelming choice as the polymer support [Frechet and Farrall, 1977; Frechet et al., 1988; Messing, 1974]. The polystyrene used is a crosslinked polymer prepared by copolymerization of styrene with divinylbenzene (DVB). (The divinylbenzene is usually the commercially available mixture containing the meta and para isomers
Crosslinked polystyrene fulfills many of the requirements of a support—it is an inexpensive, readily available polymer with good mechanical, chemical, and thermal stability. Very importantly, polystyrene can be functionalized by many routes, such as chloromethylation, lithiation, carboxylation, acylation, and sulfonation. The chloromethyl and lithio derivatives are the most useful. The two complement each other by reacting with nucleophilic and electrophilic reagents, respectively, to yield a wide range of functionalized polystyrenes. For example, ammonium, carboxylate, aldehyde, thiol, cyanide, and diphenylphosphine groups can be introduced by reacting chloromethylated polystyrene (Sec. 9-6) with an amine, RCOOK, NaHCO₃, RSK, KCN, and LiP₂, respectively. Lithiated polystyrene can be obtained by direct lithiation of polystyrene with n-butyllithium in the presence of tetramethylethylenediamine (or indirectly by reaction of brominated polystyrene with n-butyllithium):

\[
\begin{align*}
\text{CH}_2\text{CH}_2\text{Li} & \quad \text{TMEDA} \\
& \quad \text{Li}
\end{align*}
\]

The lithio derivative of polystyrene offers a route to polystyrenes containing OH, COOH, B(OH)₂, RSnCl₂, and P₂Cl₂ groups by reaction with ethylene oxide, CO₂, B(OR)₃, MgBr₂ followed by RSnCl₃, and P₂PCl₂, respectively.

The usual polystyrene support contains 1–2% DVB, as this yields a mechanically strong support that is microporous; that is, it is highly swollen by solvents for polystyrene. Swelling is accompanied with a significant expansion in volume. Much higher degrees of crosslinking, up to and sometimes exceeding 20% DVB, yield rigid polymers that are macroporous or macroreticular. They are produced by carrying out the copolymerization of styrene–DVB in the presence of significant amounts of diluent. This keeps the polymer in an expanded form during preparation and results in the macroporous structure. The diluents used are always solvents for the monomers but may or may not be solvents for the polymer. The macroporous structure allows a macroreticular resin to take up solvent with little or no change in volume. Microporous supports offer certain advantages relative to macroreticular supports. Microporous supports are less fragile, require less care in handling, react faster in the functionalization and applications reactions, and possess higher loading capacities. Macroreticular supports are less frequently employed but do have certain advantages, including ease of removal from a reaction system (due to greater rigidity) and the lack of diffusional limitations on reaction rates (since the pore sizes are usually larger and there is no microporosity). Macroreticular supports can be used with almost any solvent irrespective of whether it is a good solvent for the uncrosslinked polymer. The behavior of microporous supports varies considerably depending on the solvent used. Solvents for polystyrene are optimal; examples are benzene, toluene, dioxane, tetrahydrofuran, chloroform, and methylene chloride. Although the overwhelming majority of supports used are based on polystyrene, polystyrene has the significant limitation of not being optimally suitable for use with systems involving polar or hydrophilic reactants or solvents. Other polymers studied as supports include poly(acrylic acid), polyamides, bisphenol A-epichlorohydrin copolymer, polyacrylamide, poly(ethylene oxide), cellulose, dextran, poly(glycidyl methacrylate), and polymaleimide copolymers. Inorganic polymers such as silica have also been used; organic groups are attached via hydroxyl groups on the inorganic surface.
9-11a-2  Functionalization of Monomer

The approach of synthesizing a monomer containing the desired functional group followed by (co)polymerization can be illustrated for the poly[4(5)-vinylimidazole] catalyst (VII) described in Sec. 9-1j. Synthesis involves the sequence of reactions starting from histidine (XXXVII) to yield 4(5)-vinylimidazole (XXXVIII), which is subsequently polymerized by radical initiation [Overberger and Vorchheimer, 1963].

\[ \begin{align*}
\text{NH}_3^+\text{Cl}^- & \quad \xrightarrow{\text{HNO}_2} \quad \text{Cl}^- \\
\text{HOOC-CH-CH}_2 & \quad \text{N} \quad \text{N} \quad \text{HN} \\
\text{H} & \quad \text{N} \\
\text{HOOC-CH-CH}_2 & \quad \text{N} \quad \text{N} \\
\end{align*} \]

XXXVII

\[ \begin{align*}
\text{H}_2\text{C}=\text{CH} & \quad \xrightarrow{200^\circ} \quad \text{CO}_2 \\
\text{HOOC-CH=CH} & \quad \text{N} \\
\end{align*} \]

XXXVIII

The key to the utility of this approach is whether the required functional group can be incorporated into a monomer that undergoes polymerization. Two methods have been used. One is the synthesis of a unique monomer such as 4(5)-vinylimidazole that contains the required functional group with an attached polymerizable linkage. The second method involves the incorporation of the required group as part of one of the more common types of monomers. The most successfully employed have been functional derivatives of acrylic and methacrylic esters and styrene where the functional group is part of the ester group and aromatic ring, respectively. Monomers suitable for step polymerizations have been much less frequently employed.

9-11a-3  Comparison of the Two Approaches

The two approaches are complementary. The functionalization of a polymer may be more advantageous for a particular system due to the availability of the appropriate polymer and the ease of accomplishing the required functionalization reaction in high yield with a minimum of side reactions. It may be completely unsuitable for a system where the appropriate polymer is not readily available and/or the required functionalization reaction does not proceed cleanly to high yield. The polymerization of a functional monomer will be advantageous for a system if synthesis of the required monomer can be accomplished in high yield and purity and polymerization or copolymerization proceeds to yield a high polymer of the required mechanical strength with good thermal and chemical resistance. The approach may be impractical if either monomer synthesis or polymer formation does not proceed satisfactorily. For any specific polymer reagent, catalyst, or substrate, one approach may be more suitable than the other.

The functionalization of polymer approach is used much more often than the functionalization of monomer approach at present because functional polymers such as chloromethylated polystyrene are readily available with different porosities and degrees of chloromethylation. There are relatively few situations where less work is needed to use the functionalization of monomer approach. Also, many practitioners of polymer reagents,
catalysts, and substrates are organic chemists, not polymer chemists, and there is a hesitancy in performing polymerization reactions.

9-11b Advantages of Polymer Reagents, Catalysts, and Substrates

Polymer reagents, catalysts, and substrates have practical advantages compared to their small molecule analogs. An insoluble polymer reagent, catalyst, or substrate can be easily separated from the other (i.e., the small molecule) components of a reaction system by filtration. This ease of separation allows the synthesis of high-purity products and the recovery of the polymeric species, with resulting economies. Reactions with functional polymers are sometimes advantageously carried out in a manner similar to that for column chromatography. The polymeric species is packed in a column and the small molecule species poured through the column. Some of the more specific details are described in Secs. 9-12 through 9-14.

When the polymer reagent, catalyst, or substrate is easily recoverable, it can be economically used in large excess to achieve high yields in a reaction. Small-molecule reagents, catalysts, or substrates that are highly reactive, toxic, or malodorous can be handled much more safely and easily in the form of the corresponding polymers. Other advantages of functional polymers may arise from the enhancement of rate or equilibrium due to factors discussed in Sec. 9-1. These factors may also lead to negative effects in some systems.

There are disadvantages that limit the commercial utilization of polymer reagents, catalysts, and substrates at this time. Functional polymers are more expensive than their small-molecule analogs. Many applications that work well in the laboratory fail the economics of industrial use. One needs large-scale uses where one or another of the advantages of functional polymers cannot be achieved by other means. Filtration of a polymer reagent, catalyst, or substrate is often not easy. Fine particles slough off from larger beads or ground resin because of the stresses resulting from mechanical stirring or shaking. These “fines” interfere with filtration by clogging the filters. For a few functional polymers, the functional group(s) of importance may not be permanently anchored; in other words, the functionalization reaction is reversible. This is the case with some polymer catalysts containing transition metal groups. The transition metal components leach out with time. Organic supports are of lesser stability than inorganic supports.

The advantages of functional polymers are best realized when used in two situations—multistep sequential reactions and automated parallel combinatorial synthesis to produce libraries of compounds. In both situations there is a large savings in the time and expense of carrying out the many chemical reactions and their corresponding handling and purification steps.

Insoluble polymer reagents, catalysts, and reagents have received the most attention, but there is increasing work with soluble polymer reagents, catalysts, and reagents [Bergbreiter, 2001, 2002; Osburn and Bergbreiter, 2001; Toy and Janda, 2000]. Insoluble functional polymers have some deficiencies. They are difficult to characterize and monitoring of the progress of reaction is also difficult. Insoluble functional polymers often show low reactivity and altered selectivity (chemo-, regio-, and stereoselectivity compared to the corresponding small-molecule reactions). Soluble reagents, catalysts, and reagents are easy to characterize, and their chemical behavior is much closer to that of the small-molecule reactions. This makes it easier to make the transition from small-molecule reactions to using soluble polymer reagents, catalysts, and reagents.

Poly(ethylene glycol) (PEG) is extensively used as a soluble polymer support. It is a low molecular weight poly(ethylene oxide) with hydroxyl groups at both chain ends. The terminal hydroxyl groups allow for attachment of a wide range of other functional groups that
perform reagent, catalyst, and substrate functions. PEG is soluble in water and many organic solvents, but insoluble in hexane, ether, and cold isopropanol.

Soluble polymer supports, like their insoluble counterparts, offer the advantage of ease of separation. After carrying out a chemical process, the polymer reagent, catalyst, or substrate can be isolated by adding a nonsolvent, for instance, by adding isopropanol for PEG supports.

## 9-12 POLYMER REAGENTS

A wide range of polymer reagents have been studied [Akelah and Sherrington, 1983; Blossey and Ford, 1989; Ford, 1986a; Kirschning et al., 2001]. The epoxidation of an alkene by a polymer peracid illustrates the use of a polymer reagent [Frechet and Haque, 1975]. Chloromethylated polystyrene is treated with potassium bicarbonate in dimethylsulfoxide to yield

$$
\begin{align*}
\text{CH}_2\text{Cl} & \quad \xrightarrow{\text{KHCO}_3} \quad \text{CHO} \\
\text{and} & \quad \xrightarrow{\text{H}_2\text{O}_2, \text{H}^+} \quad \text{CO}_3\text{H}
\end{align*}
$$

the formylated derivative which is then oxidized to the peracid (Eq. 9-68). The polymer peracid is used to epoxidize an alkene by the scheme shown in Fig. 9-1. A mixture of the

![Scheme for utilization of a polymer reagent. The epoxidation of an alkene by a polymer peracid.](image-url)

**Fig. 9-1** Scheme for utilization of a polymer reagent. The epoxidation of an alkene by a polymer peracid.
polymer reagent (peracid) and low-molecular-weight substrate (alkene), often with a solvent for the latter, are allowed to react and then filtered. Solvent is evaporated from the filtrate to yield the low-molecular-weight product (epoxide); purification steps such as distillation may also be involved. From the economic viewpoint, it is desirable if the polymer reagent can be regenerated from the polymer by-product (polymer acid). This is easily accomplished in the particular example as the polymer acid yields the peracid on treatment with hydrogen peroxide. It is not possible to obtain the economy of polymer regeneration in all polymer reagent systems. Polymer peracids have also been used for the oxidation of sulfides to sulfoxides and sulfones [Grieg et al., 1980; Harrison and Hodge, 1976].

Oxidation of alcohols to aldehydes or ketones is accomplished with chromate bound to an anion-exchange resin (XXXIX with $A^- = HCrO_4^{-}$) [Frechet et al., 1981; Taylor, 1986]. Other oxidants include polymers functionalized with $ClO_4^-$, $ClCrO_4^-$, and $RuO_4^-$ [Kirschning et al., 2001]:

![XXXIX](image1) ![XXXX](image2)

Polymer reducing agents for reducing aldehydes and ketones to alcohols are obtained by complexing $AlH_3$ or $BH_3$ with a nitrogen-containing polymer such as poly(4-vinylpyridine) (e.g., XXXX) [Boga et al. 1989; Menger et al., 1980]. Another useful reducing reagent is XXXIX with $A^- = BH_4^-$, which involves ionic bonding of boron hydride anion to a quaternary ammonium polymer [Sande et al., 1984].

The use of a chiral polymer instead of the achiral polymers in XXXIX and XXXX allows an asymmetric synthesis. An example is the stereoselective reduction of acetophenone to $(R)$-1-phenylethanol in 76–97% enantiomeric excess by using the indicated chiral support (Eq. 9-69) [Itsuno et al., 1985]:

![XXXI](image3)

Pyridinium bromide, useful for bromine addition to alkenes and $\alpha$-substitution on aldehydes and ketones, is dangerous to handle. The polymer analog (XXXXI) is easy to handle and accomplishes the same reaction as does the small-molecule reagent [Frechet et al., 1977; Johar et al., 1982]. Similar halogenating reagents are obtained from XXXIX (e.g.,
A\(^-\) = Br\(_3\), BrCl\(_2\), ICl\(_2\) [Sket and Zupan, 1984]. An ethylene-\(N\)-bromomaleimide copolymer has been used for bromine substitution at allylic and benzyl positions [Yaroslavsky et al., 1970].

Polymer Wittig reagents are useful for the conversion of an aldehyde or ketone to an alkene according to the sequence in Eq. 9-70 [Ford, 1986a,b].

\[
\begin{align*}
P &\xrightarrow{\text{1. } RR'\text{CHX}} P\xrightarrow{\phi} P=\text{CRR}' & &\xrightarrow{\text{2. base}} & P\xrightarrow{\phi} P=O + RR'C=\text{CR''R'''}
\end{align*}
\tag{9-70}
\]

Other polymer reagents have been studied for performing nucleophilic substitution, alkylation, acylation, deprotonation, and other reactions [Kirschning et al., 2001].

Polymer scavengers are used to remove excess reactants and/or by-products from a chemical reaction. For example, nucleophiles are removed by polymer electrophiles and bases are removed with polymer acids.

Several applications of functional polymers for achieving chemical separations have been described. Ion-complexing polymers allow the removal of ions from solution for analytical, purification, or preparative purposes [Akelah and Sherrington, 1983; Braun and Farag, 1974; Lundgren and Schilt, 1977]. For example, polymers containing the 8-hydroxyquinoline group (XXXXII) are useful for chelating nickel, cobalt, and copper ions. Chelation occurs through the hydroxyl and nitrogen functions. The metal is separated by filtration of the polymer and can be recovered from the polymer by changing the pH. Other chelating polymers have been studied for removal of pertechnetate ion, TcO\(_4\), from contaminated groundwater at nuclear reactor facilities [Alexandratos and Natesan, 1999; Bonnesen et al., 2000]. Polymers containing crown ether or cryptand macrocyclic ligands bind and separate various cations [Jaycox and Smid, 1981; Mathias and Al-Jumah, 1980].

Polymers containing chiral groups are useful for resolving racemic mixtures into the individual enantiomers [Kiniwa et al., 1987; Mathur et al., 1980; Wulff et al., 1980]. For example, the copper(II) complex of XXXXIII (either the R- or S-enantiomer) resolves racemates of amino acids [Sugden et al., 1980]. The separation is based on the formation of a pair of diastereomeric complexes from the reaction of the polymer reagent with the two enantiomers. One of the enantiomers is complexed more strongly than the other and this achieves separation of the enantiomers.

A polymer drug can be synthesized by the covalent bonding of a drug to a polymer or the synthesis and (co)polymerization of a monomer containing the drug moiety [Çallant and Schacht, 1990; Donaruma and Vogl, 1978; Hsieh, 1988; Levenfeld et al., 1990; Ottenbrite
and Sunamoto, 1986]. (Ionic bonding or complexing of a drug to the polymer are other approaches.) Polymer drugs are of interest since they offer a number of potential advantages relative to the corresponding low-molecular-weight drugs. The action of a polymer drug usually depends on in vivo hydrolytic or enzymatic cleavage of the drug moiety from the polymer. This gives the advantage of a delayed and sustained release of the drug over a longer time period with a corresponding decrease in side effects such as irritation, intolerance, and toxicity. There is the potential to tailor-make a polymer drug with a specific required solubility, rate of diffusion, and increased or decreased activity by appropriate choice of the polymer and drug. Other possibilities include the synthesis of polymer drugs with negligible absorptivity for situations where localized drug action is desired (e.g., skin treatment), the ability to design drugs capable of getting to a specific organ (via appropriate affinity groups) in the desired amounts at the required time, and the coupling of two or more drugs onto the same polymer to achieve enhanced or synergistic activity. The term polymer drug also includes the physical encapsulation of a low-molecular-weight drug by a polymer. Drug action requires the hydrolytic or enzymatic degradation of the polymer. Such materials can show many of the advantages of polymer drugs in which the drug is chemically bound to a polymer. Also of interest are polymer drugs that do not depend on release of a low-molecular-weight drug moiety for activity but possess activity as polymers.

Polymeric agricultural chemicals such as polymer herbicides, fertilizers, and insecticides have also been studied [Lohmann and d’Hondt, 1987; Scher, 1977; Shambhu et al., 1976]. Controlled and slow release of the herbicide, fertilizer, or insecticide moiety has the advantages of prolonged action and decreased indiscriminant pollution of the environment. Other polymer reagents of interest include polymer antioxidants, flame retardants, and UV stabilizers as additives to polymers [Scott, 1987, 1989; Vogl et al., 1985]. The advantage of the polymeric additive is decreased migration or leaching from the polymer compared to the corresponding low-molecular-weight additive.

9-13 POLYMER CATALYSTS

Some examples of polymer catalysts have previously been described—hydrogenation by the polymer rhodium catalyst (II) (Sec. 9-1g) and ester hydrolysis by poly[4(5)-vinylimidazole] (VII) (Sec. 9-1j). Many other types of polymer catalysts have been described [Akelah and Sherrington, 1983; Bergbeiter, 2001, 2002; Blossey and Ford, 1989; Corma and Garcia, 2002; Fan et al., 2002; Hodge and Sherrington, 1980; Leadbeater and Marco, 2002; Mathur et al., 1980; McNamara et al., 2002; Sherrington, 2001]. The physical method of carrying out a reaction using a polymer catalyst is the same as the scheme described in Fig. 9-1, with the exception that two low-molecular-weight substances, instead of only one, are usually involved. Many of the general advantages of polymer catalysts have been described (Sec. 9-11b). Polymer catalysts are often easier to handle, less toxic, and more stable toward moisture and atmospheric contaminants. The products of reactions catalyzed by low-molecular-weight catalysts, especially metal catalysts, are often contaminated by the catalysts. Catalyst removal can be difficult in such systems but necessary if the properties of the products are adversely affected by the presence of catalyst. Catalyst removal is much simpler with the use of a polymer catalyst. Further, the recovery and regeneration of an expensive catalyst is facilitated since the polymer catalyst can be separated from the reaction mixture by filtration.

Various polymer acids are used as polymer catalysts. Sulfonated polystyrene (Eq. 9-39) has been used to catalyze a variety of acid-catalyzed reactions, including acetal and ketal
formation, esterification, hydrolysis of amides and esters, aliphatic and aromatic alkylations, hydration of alkynes and alcohols, and the synthesis of bisphenol A from phenol and acetone [Delmas and Gaset, 1980; Hasegawa and Higashimura, 1981; Jerabek, 1980; Moxley and Gates, 1981]. A large-scale commercial application is the acid-catalyzed addition of methanol to isobutylene to form methyl t-butyl ether, which has been used as a gasoline additive. Poly (acrylic acid) and the hydrochloride of poly(4-vinylpyridine) have also been used as polymer acid catalysts [Yosida et al., 1981]. Various polymer superacids have been described. Sulfonated polystyrene complexed with AlCl₃ catalyzes the cracking and isomerization of n-hexane. Perfluorosulfonic acid copolymers (trade name: Nafion) (Sec. 6-8e) catalyze the addition of alcohols to ethylene oxide and the alkylation of aromatics [Olah et al., 1980, 1981; Waller, 1986]. Base-catalyzed reactions such as dehydrohalogenation, ester hydrolysis, and condensation of active methylene compounds with aldehydes and ketones have been carried out using polymer bases such as poly(4-vinylpyridine), poly-(2-dimethylaminoethyl acrylate), and poly(p-styrylmethyltrimethylammonium hydroxide) (XXXIX with A⁻ = OH⁻) [Bao and Pitt, 1990; Chiellini et al., 1981].

Various transition metal catalysts, including those based on Rh, Pt, Pd, Co, and Ti, have been bound to polymer supports—mainly through the phosphenation reaction described by Eq. 9-65 for polystyrene but also including other polymers, such as silica and cellulose, and also through other reactions (e.g., alkylation of titanocene by chloromethylated polystyrene). Transition-metal polymer catalysts have been studied in hydrogenation, hydroformylation, and hydrosilation reactions [Chauvin et al., 1977; Mathur et al., 1980].

The covalent bonding of photosensitizer moieties such as benzophenone, rose bengal, and eosin to polystyrene yields polymeric photosensitizers that can be used to bring about excitation and subsequent chemical reaction in low-molecular-weight substrates [Neckers, 1986; Nishikubo et al., 1989].

The esterolytic activity of poly[4(5)-vinylimidazole] and its copolymers has been studied in an attempt to understand and mimic the activity of the naturally occurring enzyme α-chymotrypsin [Imanishi, 1979; Kunitake, 1980; Overberger and Guterl, 1978, 1979]. The activity of α-chymotrypsin is generally ascribed to the imidazole and OH groups of the histidine and serine residues, respectively. Copolymers of 4(5)-vinylimidazole containing OH groups (from phenol moieties) were found to have increased esterolytic activity relative to poly[4(5)-vinylimidazole] or polymers containing only hydroxyl functions. The catalysis by the copolymers is ascribed to cooperative involvement of hydroxyl and imidazole groups. Among the proposed mechanisms are an acylation of the ester by the hydroxyl group followed by the imidazole moiety assisting the attack of water on the acylated intermediate (XXXXV):
A catalyst such as XXXXIV is referred to as a *bifunctional polymer catalyst*—two different catalyst moieties function simultaneously in the same reaction.

*Polymer phase-transfer catalysts* (also referred to as *triphase catalysts*) are useful in bringing about reaction between a water-soluble reactant and a water-insoluble reactant [Akelah and Sherrington, 1983; Ford and Tomoi, 1984; Regen, 1979; Tomoi and Ford, 1988]. Polymer phase transfer catalysts (usually insoluble) act as the meeting place for two immiscible reactants. For example, the reaction between sodium cyanide (aqueous phase) and 1-bromooctane (organic phase) proceeds at an accelerated rate in the presence of polymeric quaternary ammonium salts such as XXXIX [Regen, 1975, 1976]. Besides the ammonium salts, polymeric phosphonium salts, crown ethers and cryptates, polyethylene oxide, and quaternized polyethylenimine have been studied as phase-transfer catalysts [Hirao et al., 1978; Ishiwatari et al., 1980; Molinari et al., 1977; Tundo, 1978].

An *immobilized enzyme* is obtained by insolubilizing an enzyme on a polymer support [Chibata, 1978; Manecke and Vogt, 1978; Wingard et al., 1979]. (Enzymes are naturally occurring polypeptides that catalyze biochemical reactions.) The naturally occurring polysaccharide agarose, an alternating copolymer of D-galactose and 3,6-anhydro-L-galactose, is the most commonly used support. Cellulose, crosslinked dextran, polyacrylamide, and microporous glass are also used. For in vitro use, immobilized enzymes have the advantage of increased stability to temperature, pH, and other environmental conditions compared to the native enzymes. Immobilized enzymes are of interest for carrying out industrial biochemical and organic synthesis because of their generally high efficiency and specificity. An industrial application is the production of fructose corn syrup from corn by an immobilized form of the enzyme glucose isomerase [Keyes and Albert, 1986]. Immobilization can be achieved in many instances by covalent bonding of the enzyme to the polymer support. Enzymes containing amine groups can be immobilized by reaction with polymer supports containing hydroxyl groups (e.g., polysaccharide supports) through a coupling reaction with cyanogen bromide, carbonyldiimidazole, or p-nitrophenyl chloroformate. Immobilization by physical adsorption on the polymer support is also possible. Another approach is the polymerization of a mixture of a monomer and the enzyme. Polymerization of the monomer results in entrapment of the enzyme within the polymer matrix. The monomer used is often one that undergoes crosslinking during the process, such as by using a mixture of acrylamide and methylene bisacrylamide [Conlon and Walt, 1986]. This approach yields the equivalent of a semiinterpenetrating network (Secs. 2-13c-3 and 6-6c). Immobilization of whole cells has also received attention since it has the advantage of not requiring the separation and purification of the active enzyme from the rest of the cell in order to produce the immobilized enzyme. Also, in some instances the active enzyme is active only in the presence of other species (coenzymes, cofactors). The use of whole cells avoids the need to establish the identity of the other required species followed by their separation and incorporation in the immobilized enzyme.

*Affinity chromatography*, a chromatographic method of separation and purification, is an application of immobilized enzymes [Chaiken et al., 1984; Cuatrecasas and Anfinsen, 1971; Jakoby and Wilchek, 1974]. An immobilized enzyme constitutes the adsorbent in a chromatography column. When a mixture of biochemicals, such as a mixture of proteins, is passed through the column, a specific interaction (often through covalent bonding) between the immobilized enzyme and one of the components of the mixture separates that component from the mixture. Subsequent passage of the appropriate reagent through the column reverses the interaction and frees the desired component from the column. Immobilized enzymes in the form of affinity chromatography, electrodes, and other sensing devices are of interest for analytical purposes (including immunoassays).
The general scheme for utilizing a polymer substrate for synthetic purposes is shown in Fig. 9-2. A substrate $S$ is covalently bonded to an appropriate polymer support to yield the polymer substrate $P \rightarrow S$ (which is usually of the insoluble type). The polymer substrate

Fig. 9-2 Scheme for utilization of a polymer substrate. After Mathur and Williams [1976] (by permission of Marcel Dekker, New York).
is treated with a low-molecular-weight reagent (and/or catalyst) R to yield the polymer-bound product $S'$ and spent reagent $R'$. Filtration separates the polymer-bound product. An appropriate reaction is carried out to cleave the desired product $S'$ from the polymer. The spent polymer support is filtered off, leaving the crude product $S'$ in the filtrate. The purified product $S'$ is obtained from the filtrate after solvent evaporation and appropriate purification.

9-14a Solid-Phase Synthesis of Polypeptides

One of the most important applications of the polymer substrate technique is the solid-phase synthesis of polypeptides developed by Merrifield [Barany et al., 1988; Erickson and Merrifield, 1976; Kates and Abericio, 2000; Kent, 1988; Merrifield, 1978; 1985, 1988; Seward and Jakubke, 2002; Stewart, 1980]. Merrifield received the 1984 Nobel Prize in Chemistry for this achievement. Polypeptide synthesis is of interest for two reasons: (1) it is useful in confirming the structure of naturally occurring biological macromolecules and (2) it is a source of these substances as well as analogs that may show more desirable biological activity. Polypeptide synthesis involves the formation of an amide linkage between the amino and carboxyl groups of successive $\alpha$-amino acid monomers. In reacting two different amino acids with each other, it is necessary to protect the amino group of one amino acid and protect the carboxyl of the other amino acid. This prevents self-reaction of each amino acid with itself and directs the synthesis in the desired cross-reaction route. There are two copolymerization routes and only one of these is the desired route. For example, alanylglycine (Eq. 9-72) and glycylalanine (Eq. 9-73) are possible from the cross-reaction of alanine and glycine. Synthesis of alanylglycine requires that the amine end of alanine and the carboxyl end of glycine be protected prior to reaction. Synthesis of glycylalanine requires that the amine and carboxyl ends of glycine and alanine, respectively, be protected.

$$\begin{align*}
\text{H}_2\text{N} &- \text{CH} - \text{COOH} + \text{H}_2\text{N} - \text{CH}_2 - \text{COOH} \\
\text{CH}_3 & \quad \text{H}_2\text{N} - \text{CH} - \text{CONH} - \text{CH}_2 - \text{COOH} \\
\text{Alanylglycine} & \quad \text{Glycylalanine}
\end{align*}$$

The solid-phase synthesis of a polypeptide is described in Fig. 9-3. Chloromethylated polystyrene (usually based on 1% DVB) is commonly used as the polymer support. Reactions are carried out in nonaqueous media, usually methylene chloride, although DMF has also been used. The first amino acid monomer (often referred to as a unit or residue) is attached to the polymer support by nucleophilic displacement of the benzylic chloride by carboxylate anion. Reasonable reaction rates are achieved by having high concentrations of the carboxylate anion present by using either the cesium or trialkyl ammonium salt instead of the carboxylic acid. The attachment of the first amino acid to the polymer support also serves the purpose of protecting the carboxyl group. The amino group of the amino acid must be protected (often referred to as N-blocking or N-protecting) to prevent self-condensation of that monomer during attachment to the support. A variety of protecting groups were studied, including carbobenzoxy, $p$-toluene sulfonyl, triphenylmethyl, and $t$-butoxycarbonyl. The
The t-butoxycarbonyl group (referred to as Boc) is usually formed by reacting the amino acid with 2-(t-butoxycarbonyloxyimino)-2-phenylacetonitrile. Di-t-butyl dicarbonate and t-butoxy carbonyl azide have also been used for synthesizing Boc-protected amino acids. The Boc group is the most frequently used N-protecting group since it can be hydrolyzed, usually with 25–50% trifluoroacetic acid (TFA) in methylene chloride, without affecting the polymer support–polypeptide bond (i.e., the benzyl ester bond formed in the first step in Fig. 9-3).
After attachment of the first amino acid to the polymer support, the amino group must be deprotected (i.e., the Boc group removed) to allow a second amino acid residue to be added. The resulting ammonium salt is neutralized with a tertiary amine such as N,N-diisopropyl-ethylamine, and the free amino group of the bound amino acid is ready for coupling with a second amino acid. The second amino acid is also used in the form of the N-protected derivative. The reaction between the carboxyl group of the second amino acid and the amino group of the first amino acid residue is carried out under conditions that increase the reactivity of the carboxyl group since this reactivity is rather low at the ambient or moderate temperatures employed in solid-phase synthesis. A variety of more active derivatives of the carboxyl group (e.g., acid chloride, anhydride, ester) are possible. Dicyclohexylcarbodiimide (DCC) is commonly used as an activator for the condensation reaction since it results in high reaction rates and yields with a general absence of side reactions. DCC is added to the N-protected amino acid and the mixture reacted with the polymer substrate without isolation of the intermediate. The active intermediate is the O-acyl isourea (XXXVI), formed by reaction with the carboxyl group, which undergoes nucleophilic attack by the amino group of an amino acid.

\[
\text{RCOOH} + \text{C}_6\text{H}_{13} \text{CONHR} \rightarrow \text{C}_6\text{H}_{13} \text{NHCONH} - \text{C}_6\text{H}_{13} + \text{R'NH}_2
\]

The synthesis is continued in a similar manner until the desired sequence of amino acid residues is added. The addition of each amino acid involves amidation with an N-protected amino acid in the presence of DCC followed by deprotection by reaction with TFA. The final step in the overall process is to cleave the peptide from the polymer support. Treatment with HF accomplishes this cleavage simultaneously with deprotection of the last Boc protecting group, without cleavage of any of the amide linkages. The solid-phase method (also referred to as the Merrifield synthesis) has been successfully applied to various polypeptides such as bradykinin, oxytocin, insulin, and ribonuclease. The synthesis of ribonuclease is a formidable task since there are 124 amino acid residues in the ribonuclease molecule, which corresponds to a total of 369 chemical reactions (protection, coupling, deprotection). Such a synthesis involves an unreasonable length of time to accomplish in view of the much larger number (11,931) of procedural steps involved (the total of chemical reactions and separation steps) if carried out in the usual manner. The use of the polymer substrate approach brings this synthesis into the realm of possibility by allowing automation of the various chemical and separation steps.

Commercially available computer-automated peptide synthesizers allow synthesis of a polypeptide in a time of about one hour or less per amino acid unit. The ribonuclease synthesis takes about one week or less.

The Merrifield synthesis is not without limitations since anything less than quantitative conversion in each chemical step with the complete absence of side reactions and the complete removal of reagents prior to the next chemical step would yield an impure polypeptide compared to the naturally occurring biological macromolecule. Thus, for the synthesis of a
polypeptide containing 100 amino acid residues, an error of only 1% in adding each amino acid unit would lower the overall yield of the desired product to 36.6%. Even more significantly, the small errors lead to impurities (i.e., polypeptides that are missing one or more of the amino acid residues in the desired final product) that are carried along throughout the complete synthetic process and result in contamination of the final product. The ribonuclease originally synthesized by Merrifield was a relatively impure product with far less biological activity than the naturally occurring ribonuclease. At the present time, the Merrifield synthesis is most efficient for synthesizing polypeptides containing no more than 30–50 amino acid residues.

The major limitation in the solid-phase synthesis of polypeptides involves the deprotecting reactions. The polymer support–peptide bond (the bond between the polypeptide and the polymer support) and all amide linkages in the polypeptide chain must be completely stable during the successive deprotecting reactions. Also, side-chain protecting groups for those amino acid residues with a third functional group (e.g., lysine contains a second amino group and aspartic acid contains a second carboxyl group) must be stable to the normal deprotecting conditions but must be capable of being deprotected at the end of the synthesis without adversely affecting any of the amide bonds.

Considerable success has been achieved in overcoming the problems associated with the protecting and deprotecting steps by improvements in several areas—the blocking groups used, the type of chemical bond used for attaching the first amino acid residue to the support, and careful control of the deprotecting and final cleavage conditions. The bond between the peptide and the polymer support is less stable toward trifluoroacetic acid than desired. There is 1–2% loss of polypeptide from the support per cycle (i.e., per amino acid residue added) [Kent, 1988]. A much more stable means of anchoring the first amino acid residue to the support is accomplished by using a phenylacetamidomethyl (PAM) group:

\[
\begin{align*}
\text{PAM linker} & \quad \text{CH2NH2} + \text{HOOCCH2CH2OOC} - \text{CHR} - \text{NH} - \text{Boc} \\
\rightarrow & \quad \text{PAM} - \text{CH2NH} - \text{OCCH2CH2OOC} - \text{CHR} - \text{NH} - \text{Boc}
\end{align*}
\]

(9.77)

The PAM linker increases the acid stability of the anchored first amino acid residue by a factor of more than 100 compared to the simple benzyl ester. This approach uses an amino-methylated polystyrene support (usually referred to as PAM resin) instead of the chloromethylated polystyrene. Most solid-phase syntheses of polypeptides are now performed using the PAM resin.

Protecting groups for the side chain COOH or NH2 groups are chosen for high stability under conditions used for hydrolysis of Boc end groups. For example, p-toluenesulphonyl (arginine, histidine), 2-chlorobenzylxycarbonyl (lysine), 2,4-dinitrophenyl (histidine), cyclohexyl ester (aspartic and glutamic acids), 2-bromobenzoxycarbonyl (tyrosine), N-formyl (tryptophan), and 4-methylbenzyl (cysteine) are used. These protecting groups are quite stable to the conditions (25–50% anhydrous TFA) used for hydrolysis of Boc groups. Side reactions encountered during deprotection of the side groups and cleavage of the polypeptide from the polymer support are minimized by using a two-step hydrolytic sequence, referred to as the low–high HF procedure. The initial step involves 25% HF, 65% dimethylsulfide, and 5% each of p-cresol and p-thiocresol, conditions that foster S_N2 reaction over S_N1 and thus avoids undesirable acylation and alkylation side reactions. The subsequent hydrolytic step employs 90% HF and 5% each of p-cresol and p-thiocresol to remove the more resistant protecting groups (p-toluenesulphonyl, 4-methylbenzyl, and cyclohexyl ester).
An alternate strategy has developed to deprotect the amino group of each amino acid residue without affecting the side group protecting groups and the polymer support–polypeptide bond. This strategy involves the use of the 9-fluorenylmethoxycarbonyl (Fmoc) protecting group instead of the Boc group. The key to this strategy is that the Fmoc group can be cleaved with base instead of acid (piperidine in DMF or methylene chloride). The protecting groups used for amino acid side groups are mostly ether, ester, and urethane derivatives based on tert-butyl alcohol. The side-group protecting groups and the polymer support–polypeptide bond, which are stable toward base, are subsequently cleaved by TFA instead of HF. The strategy based on the Fmoc protecting group is second only to that based on the Boc group for solid-phase synthesis of polypeptides.

Another limitation to the solid phase of polypeptides is that the maximum yield of coupling and deprotection reactions is 99.5–99.8% instead of 100%. This has been ascribed to the less than complete compatibility of the polymer support with the reagents and/or growing polypeptide chain, although not all workers accept this explanation [Kent, 1988]. Efforts to overcome this problem have included the introduction of spacer groups on the benzene ring, for example, CH₂CH₂CH₂ instead of CH₂. This results in greater compatibility and flexibility of the reaction site for attachment of the first amino acid residue and of the growing polypeptide chain. Another solution, the use of polymers more polar than polystyrene, for example, poly[dimethylacrylamide], is being explored. This also includes soluble polymer supports such as PEG. However, polystyrene remains the polymer support of choice.

9-14b Other Applications

The success of solid-phase synthesis of polypeptides has stimulated efforts to use polymer substrates in other biochemical and organic syntheses:

1. The solid-phase approach has been extended to the synthesis of nucleic acids (polynucleotides) and oligosaccharides [Frechet, 1980a,b; Gait, 1980; Itakura et al., 1984; Narang, 1983; Seeberger, 2001]. The interest in synthesizing nucleic acids is usually coupled with recombinant DNA technology to synthesize polypeptides (both naturally occurring polypeptides and their analogs). The very large effort in this area at present makes this one of the most important applications of the polymer substrate method.

2. Conversion of one functional group in a molecule containing two (or more) functional groups can be achieved by covalently bonding the molecule to a polymer support through one (or more) of the functional groups. The latter group(s) is(are) protected while reactions are carried out on the unprotected group [Blossey and Ford, 1989; Hodge, 1988]. An example is the selective acylation of XXXXVII at the hydroxyl group on C-3 [Frechet, 1980a,b]. Treatment of XXXXVII with poly(p-styryl boronic acid) protects the hydroxyls at C-2 and C-4 and allows acylation at C-3. The polymer support is hydrolytically cleaved from the product with regeneration of the original protecting group. The same approach has been described for the monoderivitization of diacids, dialdehydes, diamines, and other difunctional compounds [Leznoff, 1978].

3. Undesirable intermolecular reactions can be avoided during certain synthetic conversions. Thus it is often useful to carry out C-alkylation and C-acylation of compounds that form enolate anions, for example, esters with α-hydrogens. Such reactions are often complicated by self-condensation since the enolate anion can attack the carbonyl group of a second ester molecule. Attachment of the enolizable ester to a polymer support at low loading levels allows the alkylation and acylation reactions (Eq. 9-79) to be performed under
the equivalent of high dilution conditions, where ester molecules are not sufficiently close to undergo intermolecular condensation [Kraus and Patchornik, 1971, 1974]. In a similar manner, one can favor various intramolecular cyclization reactions of supported diesters, cyanoesters, and dinitriles, as well as the cyclization reaction of a supported malonic ester with an α,ω-dihalide [Crowley et al., 1973; Mohanraj and Ford, 1985; Patchornik and Kraus, 1970].

4. Other applications of the polymer substrate technique include the synthesis of threaded macrocyclic systems (hooplanes, catenanes, knots), the retrieval of a minor component from a reaction system, and the trapping of reaction intermediates [Frechet, 1980a,b; Hodge, 1988; Hodge and Sherrington, 1980; Mathur et al., 1980].

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PROBLEMS

9-1  What reactions can be used to crosslink the following polymers?
   a. Polyester from ethylene glycol and maleic anhydride
   b. Polyester from ethylene glycol, phthalic acid, and oleic acid
   c. cis-1,4-Polyisoprene
   d. Polydimethylsiloxane
   e. Polyethylene
   f. Cellulose
   g. Chlorosulfonated polyethylene

Describe the crosslinking reactions by equations.

9-2  Show by equations the synthesis of each of the following:
   a. Cellulose acetate
   b. Cellulose nitrate
   c. Methyl cellulose
   d. Poly(vinyl formal)

9-3  Show by equations each of the following:
   a. Chlorination of polyethylene
   b. Chlorination of 1,4-polyisoprene
   c. Chlorosulfonation of polyethylene
   d. Synthesis of an anionic ion-exchange polymer from polystyrene
   e. Cyclization of 1,4-polyisoprene by HBr

9-4  Show the structure of each of the following:
   a. Poly(propene-b-styrene)
   b. Poly(styrene-g-methyl methacrylate)
c. Poly(methyl methacrylate-g-styrene)
d. Poly(methyl methacrylate-alt-styrene)
Describe by equations the methods of synthesizing each of these copolymers.

9-5 Explain each of the following observations.

a. The sulfonation of polystyrene can result in an insoluble (and brittle) product instead of the cation-exchange derivative shown in Eq. 9-39.

b. Poly(vinyl sulfonic acid) increases the rate of the reaction between Co(NH$_3$)$_3$Cl$_2^+$ and Hg$_2^{2+}$ (Eq. 9-5) to a greater extent than does poly(methacryloxy ethyl sulfonic acid).

\[
\text{CH}_2\text{CHSO}_3\text{H} \quad \text{CH}_2\text{COOCH}_2\text{CH}_2\text{SO}_3\text{H}
\]

Poly(vinyl sulfonic acid) \quad \text{Poly(methacryloxy ethyl sulfonic acid)}

c. It is difficult to synthesize homogeneous cellulose diacetate by the direct acetylation of cellulose.

9-6 \(\alpha\)-Chymotrypsin, which contains several NH$_2$ substituents, can be immobilized on an ethylene–maleic anhydride copolymer. Show by equations this synthesis of immobilized \(\alpha\)-chymotrypsin. The enzymatic activity of the immobilized enzyme shows a maximum at pH = 9.5 compared to pH = 8 for \(\alpha\)-chymotrypsin. Addition of sodium chloride to the immobilized enzyme causes the maximum activity to shift back to pH = 8. Explain.

9-7 Show by equations how the Merrifield method can be used to synthesize the tripeptide glycylvalylphenylalanine (Gly·Val·Phe)

\[
\text{NH}_2\text{CH}_2\text{C}^\text{O} \quad \text{NH}_3\text{CHC}^\text{O} \quad \text{CH}_2\text{N}^\text{H} \quad \text{CN}^\text{O}
\]

9-8 Synthesize HOOC–CH(CH$_3$)$_2$CH$_2$CH$_3$ using the polymer substrate technique. Your synthesis should include the preparation of the appropriate polymer support.

9-9 Show by equations how to synthesize each of the following polymer reagents:

a. Polyanamide support with \(-\text{CO--N(COCF$_3$)}\) functional group
b. Polystyrene support with \(-\phi\text{SnH}_2(n\text{-C}_4\text{H}_9)\) functional group
c. Polystyrene support with \(-\phi\text{CH}_2\text{N}^+(\text{CH}_3)_3(\text{CN}^-)\) functional group

9-10 Show by equations how to synthesize each of the following polymer catalysts:

a. Polystyrene support with \(-\text{P}^\text{d}_2\text{PtCl}_2\) catalyst group
b. Poly(4-vinyl pyridine) support with \(-\text{NCu(OH)}\text{Cl}\) catalyst group
A suggested route to the administration of small doses of a drug over relatively long periods of time is to place the desired drug as a side chain on a high-molecular-weight polymer. The polymer is expected to be only slowly cleared from the patient, and if the drug were attached by a hydrolyzable bond, it might be slowly released over an extended time. Consider the following candidates for such a polymeric drug

where X is the drug moiety. Which polymeric drug (I, II, or III) would be the best candidate for the stated objective? Explain and discuss your answer in terms of the relative rates of release of the drug X from I, II, and III.
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